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## Spectral modeling of scintillator for the NEMO-3 and SuperNEMO detectors

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### ABSTRACT

We have constructed a GEANT4-based detailed software model of photon transport in plastic scintillator blocks and have used it to study the NEMO-3 and SuperNEMO calorimeters employed in experiments designed to search for neutrinoless double beta decay. We compare our simulations to measurements using conversion electrons from a calibration source of <sup>207</sup>Pb and show that the agreement is improved if

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wavelength-dependent properties of the calorimeter are taken into account. In this article, we briefly describe our modeling approach and results of our studies.

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## 1. Introduction

Several dedicated efforts have recently been proposed to describe optical photon transport in scintillator detectors using various Monte Carlo packages [1–5]. Using the GEANT4 (version 4.9.1 patch 3) framework [6], we have constructed a comprehensive and detailed model of photon transport in plastic scintillator, then used the model to study the individual NEMO-3 calorimeter modules. In the model, we account for the wavelength dependence of optical properties of the scintillators, light guides, reflective wrappings, photodetectors and coupling materials. We use wavelength dependent self-absorption and re-emission in the scintillator and account for the fluorescent quantum yield of the wavelength shifter. Our results show that this detailed modeling exhibits better agreement with measurements compared to a monochromatic approach.

The NEMO-3 experiment, located at the Laboratoire Souterrain de Modane in the Fréjus tunnel, searches for neutrinoless double beta decay by employing tracking and calorimetry systems and has been taking data since 2003 [7–11]. The calorimeter modules consist of large polystyrene scintillator blocks with light guides coupled to either flat or hemispherical photomultiplier tubes (PMTs). Signals in an individual block are due to incident particles, mostly  $\beta$  and  $\gamma$  rays, and the response varies with the energy and the impact point on the entrance face. The response also depends on the size and geometry of the blocks. The energy resolution and background rejection improves if a correction for the non-uniformity due to the impact position is applied for each

type of employed blocks [7]. We have reproduced the spatial dependence of response of the NEMO-3 scintillators to  $^{207}\text{Bi}$  conversion electrons and have optimized the new scintillator block geometry for the next generation double beta decay experiment, SuperNEMO.

## 2. Modeling details

### 2.1. The detector

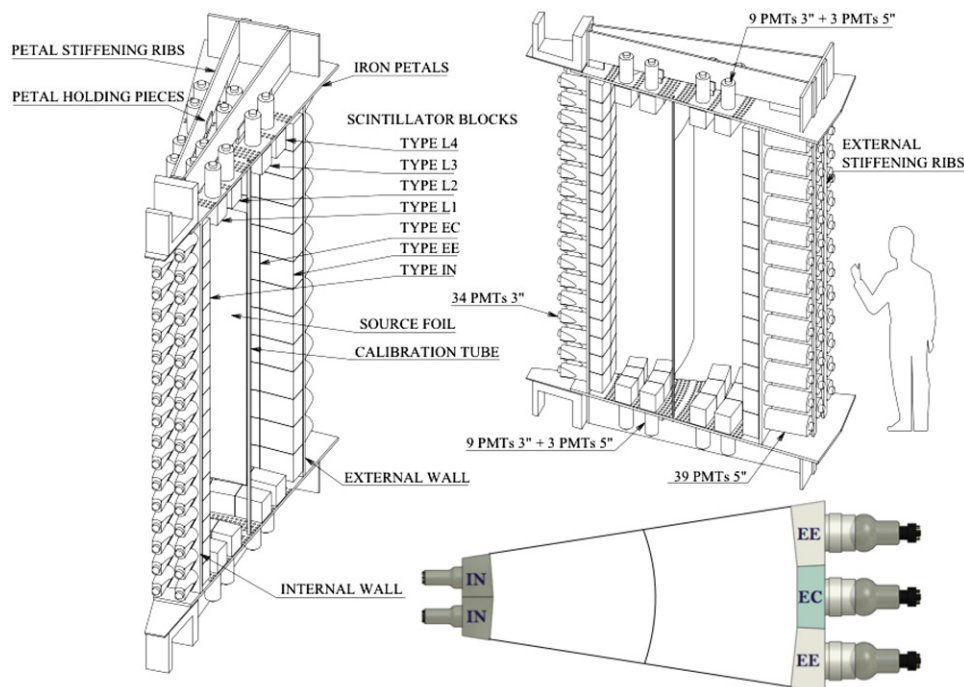
NEMO-3 calorimeter modules [7] were manufactured to conform to the overall cylindrical geometry of the detector. Each module faces the isotopic foil (a source of double beta transitions) and is composed of a scintillator block, a light guide, and a 3 in. or

**Table 1**

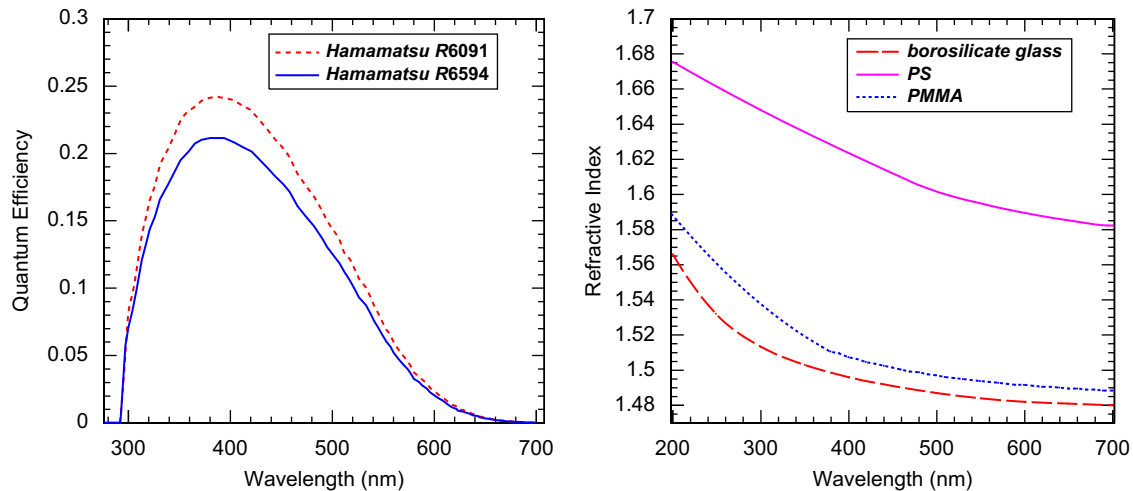
Types and dimensions of NEMO-3 inner and outer wall scintillator blocks.

| Block type          | IN            | EC            | EE            |
|---------------------|---------------|---------------|---------------|
| Thickness (mm)      | 98–110        | 99            | 99–123        |
| Height (mm)         | 153           | 200           | 200           |
| Width (mm)          | 138–154       | 218           | 218–230       |
| Associated PMT [12] | R6091 (3 in.) | R6594 (5 in.) | R6594 (5 in.) |
| Total number        | 680           | 260           | 520           |

The blocks were made at the Joint Institute for Nuclear Research (JINR) in Dubna, Russia [7].



**Fig. 1.** One of 20 sectors of the NEMO-3 detector with details showing the source foil, scintillator blocks, and photomultipliers. EE, EC, and IN identify blocks on the exterior and interior walls. L1–L4 identify blocks on the petals (not modeled in this work). The lower figure shows a 2-D rendering of the wall blocks.



**Fig. 2.** Input data used in the NEMO-3 simulations. Left: Typical quantum efficiency of Hamamatsu R6091 3 in. and Hamamatsu R6594 5 in. PMTs. Right: Refractive indices of borosilicate glass, polystyrene, and PMMA.

5 in. PMT. The detector is azimuthally divided into 20 identical wedge sectors, each assembled as a tracker and calorimeter with a source foil, as depicted in Fig. 1. The scintillators hermetically cover the two cylindrical walls which surround the foil and the tracking volume. There are three types of blocks comprising the walls and there is also partial scintillator coverage of the top and bottom end-caps. On the interior wall, there are two IN blocks which are mirror-symmetric. On the exterior wall, there are two types of blocks: center (EC) and edge (EE) type blocks, with EE blocks symmetrically placed on either side of an EC block. The dimensions of these scintillator blocks are given in Table 1. Simulations of the response of these three types of blocks was the primary objective of our work reported here.

The scintillator material is composed of polystyrene (PS) (98.49% by weight), a primary dopant *p*-terphenyl (pTP) (1.5% by weight) and a wavelength shifter 1,4-bis(5-phenyloxazol-2-yl) benzene (POPOP) (0.01% by weight). The light guides are made out of polymethylmethacrylate (PMMA) and serve as the interface between the PMTs and the scintillators. Five layers of 70  $\mu\text{m}$  thick Teflon ribbon are wrapped around the four side walls of each scintillator and two layers of single-sided 6  $\mu\text{m}$  thick aluminized Mylar foil are wrapped around the entrance face. One layer of double-sided 12  $\mu\text{m}$  thick aluminized Mylar foil is wrapped around the other five faces to protect against light produced by Geiger discharge in the tracking region. Bicon BC600 optical glue with a nominal thickness of 100  $\mu\text{m}$  is used to couple the light guides to the scintillator blocks.

## 2.2. Input components of the simulation model

We use spectral properties of all optical elements. The effective quantum efficiency spectra<sup>1</sup> for the PMTs are shown in Fig. 2, where data are taken from Refs. [12]. The refractive index data for borosilicate glass are given by the Cauchy dispersion law  $n_{\text{glass}} = 1.472 + 3760/\lambda^2$ , where  $\lambda$  is the photon wavelength [13]. Fig. 2 also shows the refractive index input data for the PMMA light guides and for scintillator polystyrene [14], which we have linearly extrapolated in the low wavelength (200–300 nm) region.

The measured reflection coefficients of Teflon and aluminized Mylar used in the simulations are shown in Fig. 3. We assume a 50  $\mu\text{m}$  air gap between the scintillator block and the Teflon/Mylar

wrappings whose reflectivities are modeled as 100% Lambertian for Teflon and 100% specular for aluminized Mylar. The scintillator blocks were treated under water with 1200 grit sandpaper to obtain diffusive reflection at the surfaces [7]. To address this, we incorporate the surface roughness parameter “sigma\_alpha” of GEANT4 with a value of 360°.

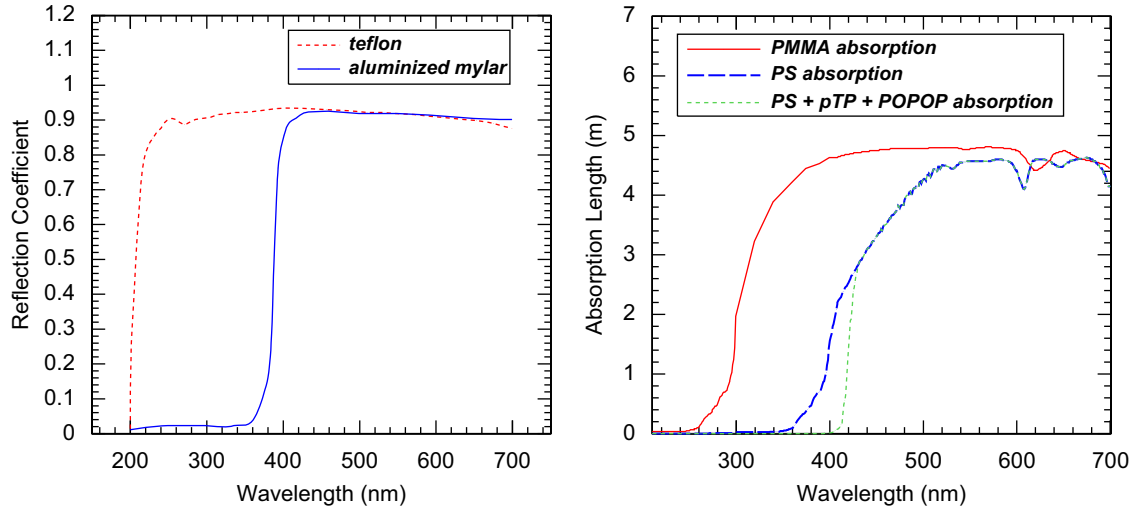
We treat the polystyrene and the primary dopant, pTP as a single entity and define the primary emission spectrum to be that of the pTP alone, since the number of emitted photons from the polystyrene is negligible compared to the number of photons generated by pTP. The pTP emission spectrum is shown in Fig. 4. Photons emitted from pTP can either propagate in the polystyrene according to the bulk absorption length (BAL) of the polystyrene and pTP mixture or interact with a POPOP wavelength-shifting molecule. Stokes shifting is determined by the combined absorption length of PS/pTP/POPOP with effective emission governed by the POPOP emission spectrum using data shown in Figs. 3 and 4. We account for the molecular quantum yield of POPOP by having absorbed photons re-emitted with 93% probability [15] and at a wavelength equal to or greater than the absorbing wavelength,<sup>2</sup> to obey energy conservation [16]. In GEANT4, two BALs must be specified: one for processes where the primary photon is absorbed in PS/pTP, and one for processes where the primary photon is absorbed by POPOP with the possibility of multiple wavelength shifts.

## 3. Energy calibration and impact corrections

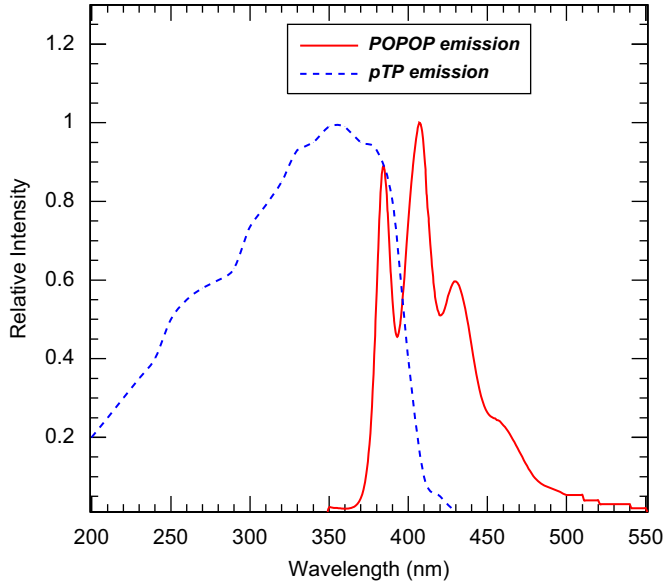
For energy calibration and alignment of blocks, the NEMO-3 experiment uses radioactive sources that are periodically inserted into the apparatus in well-defined positions. Measurements are taken using 60 <sup>207</sup>Bi sources with a mean activity of approximately 210 Bq. Three sources per sector are used and each 24 h run yields approximately two (three) thousand useful electron tracks for each IN (EE and EC) scintillator module. The bismuth decay provides conversion electrons with energies of 482, 976, and 1682 keV (K-lines). The electrons lose energy due to crossing several materials including the kapton window of the calibration tube [7], the helium gas, and the scintillator wrapping. The mean energy

<sup>1</sup> Effective quantum efficiency is the product of quantum efficiency and collection efficiency.

<sup>2</sup> A more precise treatment is possible for example, using Jablonsky diagrams for energy level spacing but would require an additional layer of complexity which we chose not to introduce at this time [16].



**Fig. 3.** Other input data used in the NEMO-3 simulations. Left: Reflection coefficients for the Teflon tape and aluminized Mylar. Right: Absorption lengths for PMMA, polystyrene, and the combined polystyrene/pTP/POPOP scintillator, where the absorption data were taken from Refs. [5,17]. The combination defines the scintillator absorption length after introduction of the fluors to the polystyrene.



**Fig. 4.** Primary emission spectrum for pTP and POPOP used in the simulations [15].

losses are estimated to be 45 and 40 keV for the 482 and 976 keV electrons, respectively. The relation between the PMT charge signal and the energy deposited in the scintillator block is linear from 150 keV to 4 MeV. We apply a linear formula to calculate the energy of each electron event:  $E = \alpha(C - P) + \beta$  where  $C$  is the ADC value of the scintillator,  $P$  is the pedestal and  $\alpha$  and  $\beta$  are fit parameters. The fit takes into account the energy loss calculated for each electron according to its energy and measured track length. The energy resolution,  $R_{FWHM}$  at 1 MeV, for each block, is obtained from the width of the 976 keV peak assuming

$$R_{FWHM}(E) = \frac{FWHM(E)}{E} = \sqrt{\frac{A}{E}} \quad (1)$$

where  $A$  (MeV) is a constant with a range from 0.014 to 0.032 for all blocks. The mean value of  $R_{FWHM}$  at 1 MeV for EC blocks is 13.8%, for EE blocks is 13.5%, and for IN blocks is 16.7%, as summarized in Table 2.

**Table 2**

Simulated and measured mean energy resolutions at 1 MeV for three different types of NEMO-3 scintillator modules.

| Block type | Simulated $R_{FWHM}$ | Measured $R_{FWHM}$ with impact corrections | Measured $R_{FWHM}$ without impact corrections |
|------------|----------------------|---|--|
| EC         | $14.4 \pm 1.1$       | $13.8 \pm 0.3$                              | $15.6 \pm 0.3$                                 |
| EE         | $14.0 \pm 1.1$       | $13.5 \pm 0.2$                              | $14.9 \pm 0.2$                                 |
| IN         | $14.9 \pm 1.1$       | $16.7 \pm 0.2$                              | $16.8 \pm 0.2$                                 |

Simulation uncertainty is taken from Table 3 for 10% input variations. Measurement uncertainty is calculated from the collective response variability between individual blocks.

The response of each scintillator block depends upon the entrance point of the electron. NEMO-3 data show a weak dependence of 1–2% for blocks equipped with 3 in. PMTs and a stronger dependence of up to 10% for larger blocks equipped with 5 in. PMTs. This effect has a non-negligible consequence on the energy resolution. The ADC value and energy loss were measured for each electron in each scintillator block to correct for this dependency. The front faces of the scintillator blocks were divided into 9 ( $3 \times 3$ ) rectangles of equal areas for modules equipped with 3 in. PMTs and 25 ( $5 \times 5$ ) rectangles of equal areas for modules equipped with 5 in. PMTs. ADC histograms were obtained for each impact region. Then the energy distribution around the 976 keV electron peak was refit to obtain the parameter  $A$  of the resolution function. The mean energy resolutions  $R_{FWHM}(E)$  at 1 MeV calculated using these corrections are given in Table 2.

#### 4. Results of simulations

The goal of our simulations was to understand the measured energy resolution and the response non-uniformity as a function of impact position. We investigated the light collection from electrons incident on the faces of three types of NEMO-3 scintillator blocks. In our model, 1 MeV electrons were generated 60 cm away from each type of scintillator block in vacuum, for direct comparison with the NEMO-3 geometry and the measured energy resolution. The angular distribution of simulated electrons matched the solid angle of the region of interest on the block surface. The block faces were divided in the same fashion as the measured data. We simulated

2500 electrons with energy of 1 MeV in each region of the grid. Following the literature, we assumed the light yield for the polystyrene-based NEMO-3 blocks to be 8000 photons per MeV for electrons [5]. This value is not well known for our scintillator and is a source of systematic uncertainty. The simulated energy resolutions in three types of blocks are compared to measured values shown in Table 2. The energy resolution  $R_{FWHM}$  is calculated as  $R_{FWHM} = 2.35 / \sqrt{N_{pe}}$ , where  $N_{pe}$  is the number of photoelectrons registered by the PMT per each simulated electron.

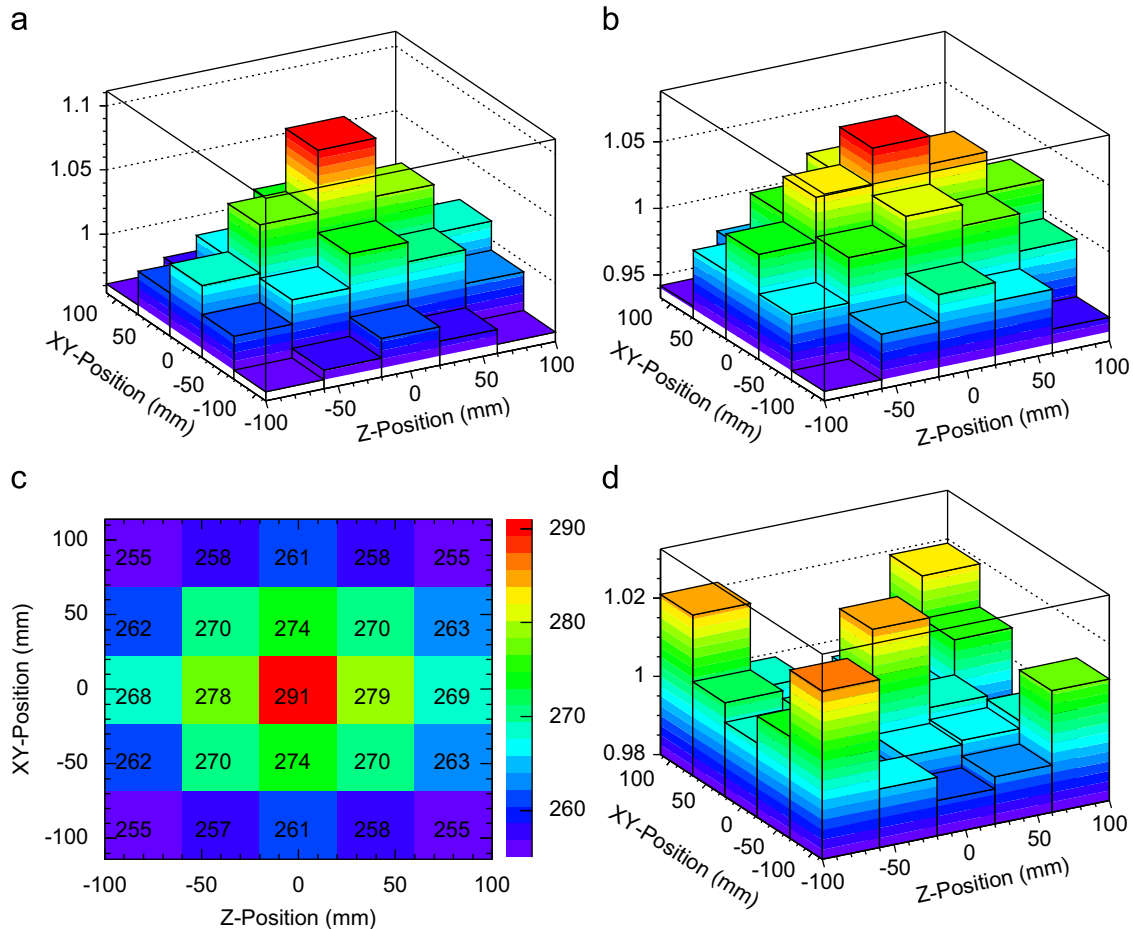
#### 4.1. Spatial non-uniformity of the response

We compared the simulated and measured spatial response non-uniformity by normalizing the number of simulated photoelectrons and the measured PMT charge from each region to the average over the entire block, shown in Table 2. The EC block response uniformity is shown in Fig. 5(a) and (b). The response reflects the symmetry of the block itself. For the EE block, one side is deeper than the other which results in a skewed response as is clearly seen in Fig. 6(a) and (b). The smaller IN block displays better uniformity although, one can still clearly identify the structural shape of the block in the results shown in Fig. 7(a) and (b). Our simulations reproduce the measured response non-uniformity of each NEMO-3 block type. The number of simulated photoelectrons collected by each type of module is shown in Figs. 5(c), 6(c), and 7(c). The ratio of the normalized simulation value to the normalized measured value show variations no greater than 2% for all block types, as shown in Figs. 5(d), 6(d), and 7(d). The ratio of the

minimum to maximum response in collected photoelectrons is 86% and 92% for EC and EE simulations, respectively, and 88% for measurement in both block types. The ratio of the minimum to maximum response is 97% for IN block simulations and 98% for measurement. The statistical uncertainty in the mean number of photoelectrons collected for each bin is 0.04%.

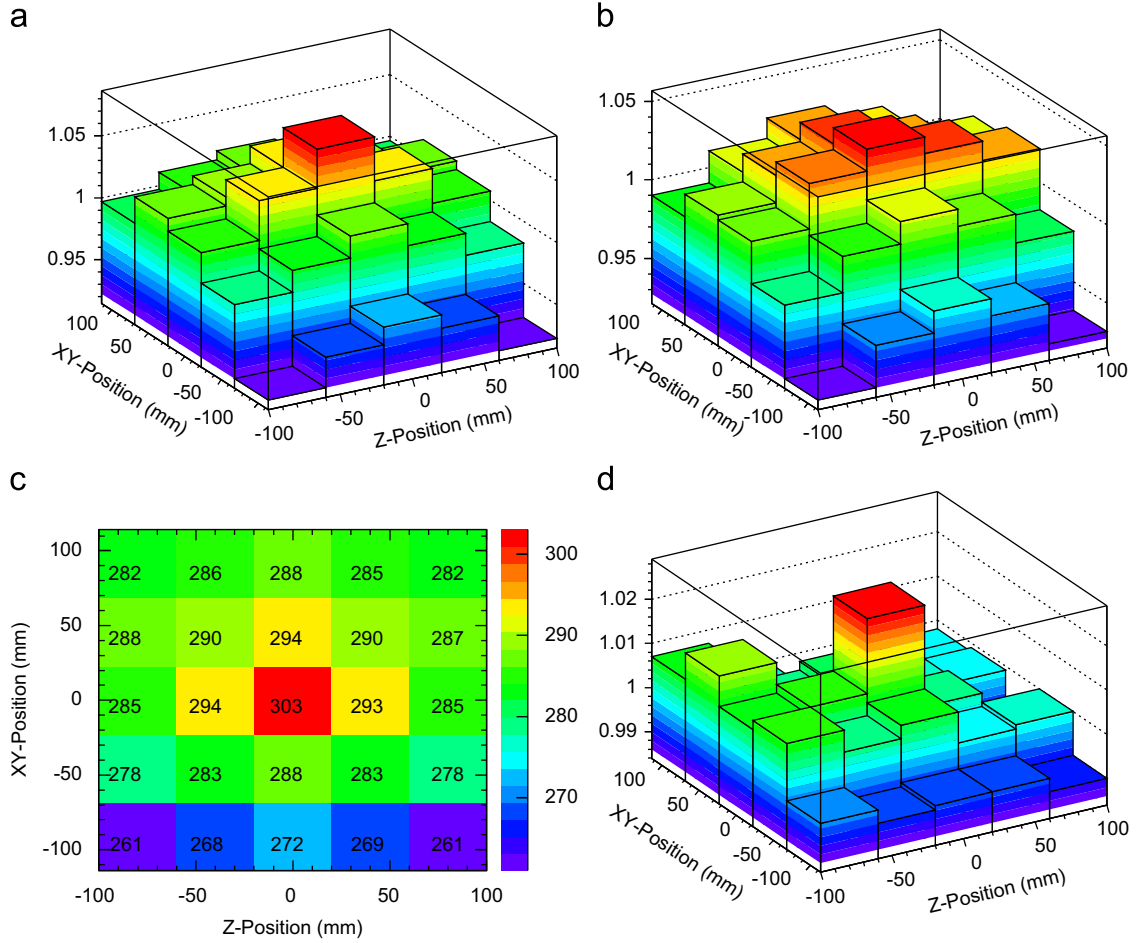
#### 4.2. Characteristics of simulated photons

Fig. 8 shows the incident angle of detected photons measured from the normal to the photocathode surface for the EC block. Fig. 8 also shows the initial and final wavelength profiles of the detected photons for the EC block. The distribution resembles that of the POPOP emission spectrum. Shorter wavelength photons are absorbed in the bulk scintillator material and on the surface of the wrappings resulting in a suppression below 400 nm. Longer wavelength photons are suppressed due to the low PMT quantum efficiency at longer wavelengths. Fig. 8 also shows the detection probability as a function of the number of wavelength shifts per photon, the number of reflections from the wrapping surfaces, and the number of total internal reflections. Each individual photon, for example, can undergo several wavelength shifts and several reflections (specular, diffuse, and total internal) before reaching the PMT. The distribution of wavelength shifting events suggests that a large fraction of the photons from pTP have been wavelength shifted. However, the probability for zero wavelength shifts is finite because pTP emission can take place above 400 nm, out of the range of large bulk attenuation.



**Fig. 5.** Results from 1 MeV electrons incident on the EC block. Simulated (a) and measured (b) response, normalized to the mean response. (c) The mean number of photoelectrons collected in each sub-region. (d) The ratio of simulation to measurement.





**Fig. 6.** Results from 1 MeV electrons incident on the EE block. Simulated (a) and measured (b) response, normalized to the mean response. (c) The mean number of photoelectrons collected in each sub-region. (d) The ratio of simulation to measurement.

#### 4.3. Dependence of simulations on input parameters

For the EC block, we have varied the simulation input parameters to evaluate the dependence of the energy resolution on these changes. The PMT quantum efficiency, the absorption length of the scintillator, the reflectivity of Teflon and Mylar wrappings, and the light yield were decreased and increased by 5% and 10%. These fractional changes reasonably reflect physical variations in production or manufacturing of most components. We then compared the result of each change to the central value of the energy resolution of 14.4%. Table 3 summarizes our studies.

#### 4.4. Dependence of energy resolution on spectral properties

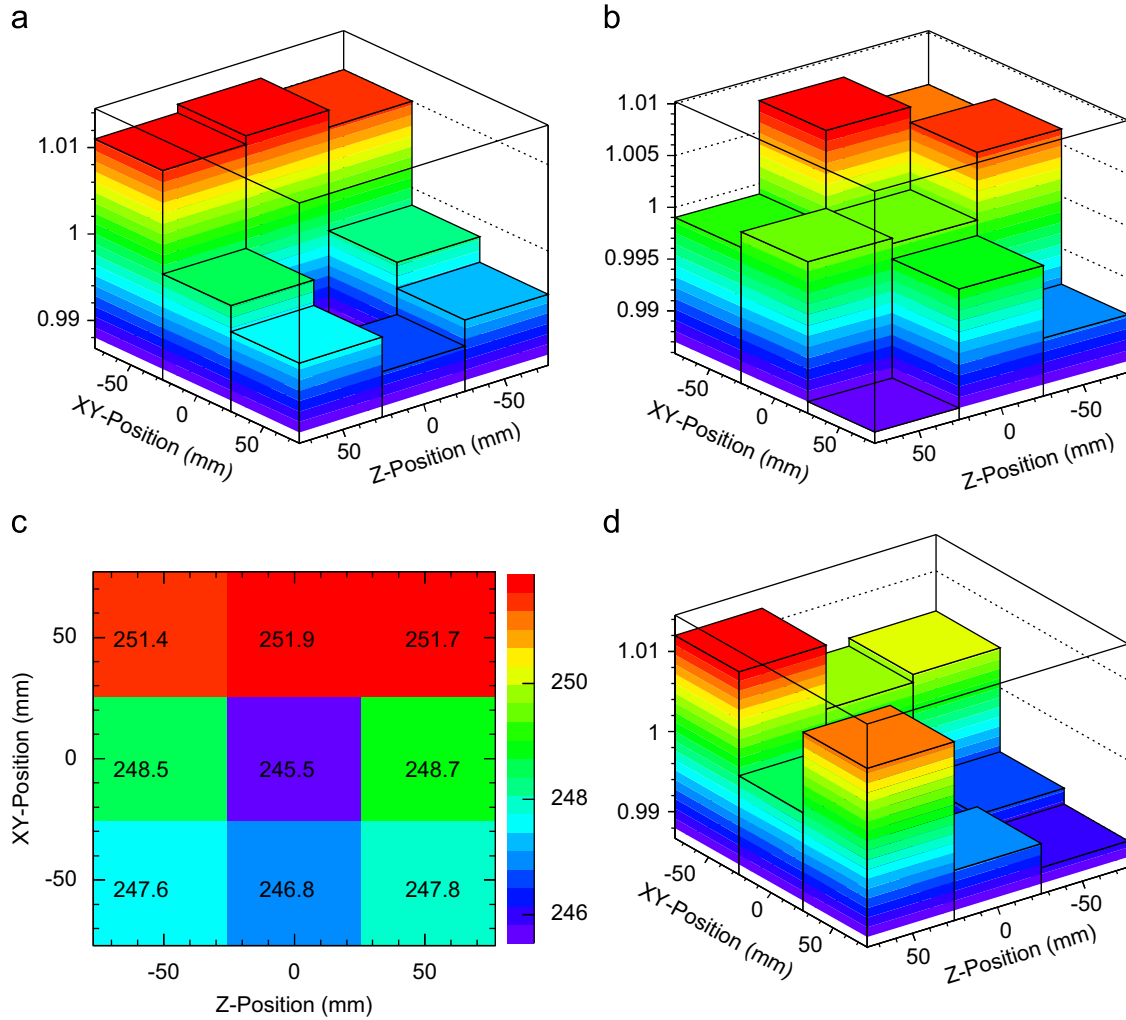
We evaluated the importance of using spectral properties of materials in our simulations of energy resolution of the EC block. We began with a simplified simulation of optical materials with wavelength-independent values and investigated the effect of systematically introducing the wavelength dependence into the simulation. Initially, we fixed the value for the quantum efficiency at 21%, the absorption length at 4.5 m, the reflectivity for the Teflon and Mylar at 93%, and the refractive indices at 1.5. The wavelength-dependent quantum efficiency of the PMT was introduced first. We then introduce a wavelength-dependent absorption length for the scintillator with no wavelength shifting and subsequently introduce wavelength-shifting dependence and molecular quantum efficiency. Finally, we introduced wavelength-dependence for the Teflon and Mylar reflection coefficients, and the scintillator and borosilicate glass

refractive indices. The values here were chosen as best-guess estimates at a peak wavelength of 420 nm that one may assume for a monochromatic simulation. The results for each step are shown in Table 4. The complete model reproduces the measured energy resolution within systematic uncertainty. It has been suggested that there is a variation in the PMT quantum efficiency as a function of the incident angle of the photon [13]. If we include this effect, assuming it is also relevant for NEMO-3 PMTs, the energy resolution for the complete model improves by about 0.3% while the spatial response distribution is left unchanged.

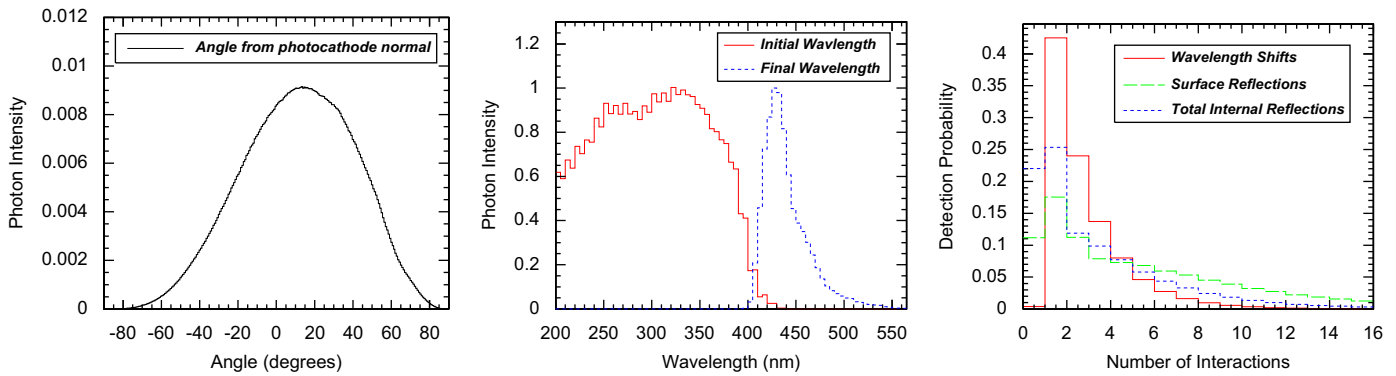
### 5. Modeling of SuperNEMO scintillator blocks

We have used our simulations to facilitate a scintillator choice for the SuperNEMO experiment [21]. SuperNEMO further plans to exploit the NEMO-3 technique of tracking and calorimetry. The new modular detector would incorporate about 100 kg of  $^{82}\text{Se}$ ,  $^{150}\text{Nd}$ , or  $^{48}\text{Ca}$ , to reach neutrinoless double beta decay half-life sensitivity of about  $1.5 \times 10^{26}$  years. This goal requires that the new experiment significantly improves its energy resolution with respect to NEMO-3. We have been conducting R&D and the developed simulation code is an important aid in our studies of the choice of materials, block shape and size, wrapping, and light collection.

A baseline provisional design for the SuperNEMO calorimeter calls for a hexagonal block with a proposed circumscribed radius of 22.5 cm made out of polyvinyltoluene (PVT) scintillator (e.g., Eljen EJ-200 [18]) coupled to a super-bialkali 8 in. hemispherical PMT (e.g., Hamamatsu R5912-MOD). Fig. 9 shows a drawing



**Fig. 7.** Results from 1 MeV electrons incident on the IN block. Simulated (a) and measured (b) response, normalized to the mean response. (c) The mean number of photoelectrons collected in each sub-region. (d) The ratio of simulation to measurement.



**Fig. 8.** Left: Incident angle of detected photons relative to the photocathode normal for the EC block. Center: Initial and final wavelengths of detected photons simulated for the EC block. The initial wavelength distribution is primarily that of the pTP emission. The final wavelength distribution is reminiscent of the POPOP emission spectrum with degradation due to absorption at short wavelengths and poor PMT quantum efficiency at long wavelengths. Right: The detection probability per photon as a function of the number of wavelength shifts, number of reflections off the wrapping surfaces, and number of total internal reflections.

of the proposed SuperNEMO scintillator module including the scintillator, PMT, and mounting brackets. The light yield of the PVT scintillator is taken to be 10,000 photons per MeV [18].<sup>3</sup>

<sup>3</sup> This is compared to a polystyrene scintillator with nominal light yield of 8000 photons per MeV.

The quantum efficiency of the PMT was taken to be approximately 33% at 420 nm [12].<sup>4</sup> We propose a high reflectivity aluminized Mylar from ReflecTech [19] around the

<sup>4</sup> This is compared to a 5 in. NEMO-3 PMT with a quantum efficiency of 25% at 420 nm.

**Table 3**

Changes of the EC block energy resolution at 1 MeV due to variations of input parameters.

| Optical parameter   | 5%    | 10%   |
|---------------------|-------|-------|
| Quantum efficiency  | 0.34% | 0.75% |
| Absorption length   | 0.12% | 0.31% |
| Teflon reflectivity | 0.92% | 2.50% |
| Mylar reflectivity  | 0.54% | 0.98% |
| Light yield         | 0.30% | 0.75% |
| Total change        | 1.17% | 2.90% |

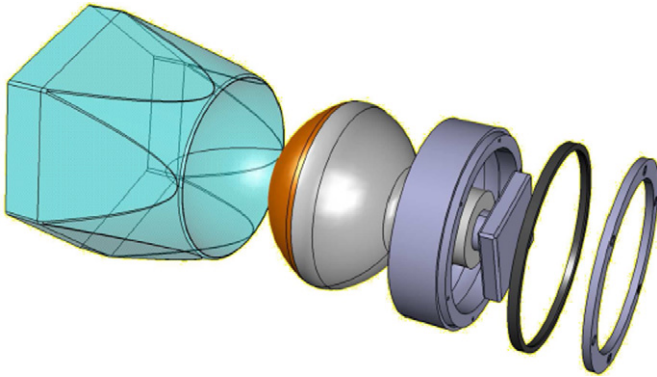
We increased and decreased the parameter values by 5% and 10% and quote the difference in the energy resolution between the central value of 14.4% and an average of the change. Total change is calculated by adding the individual changes in quadrature.

**Table 4**

Simulated FWHM of energy resolution at 1 MeV of EC scintillator blocks in NEMO-3 for increasingly comprehensive model parameters.

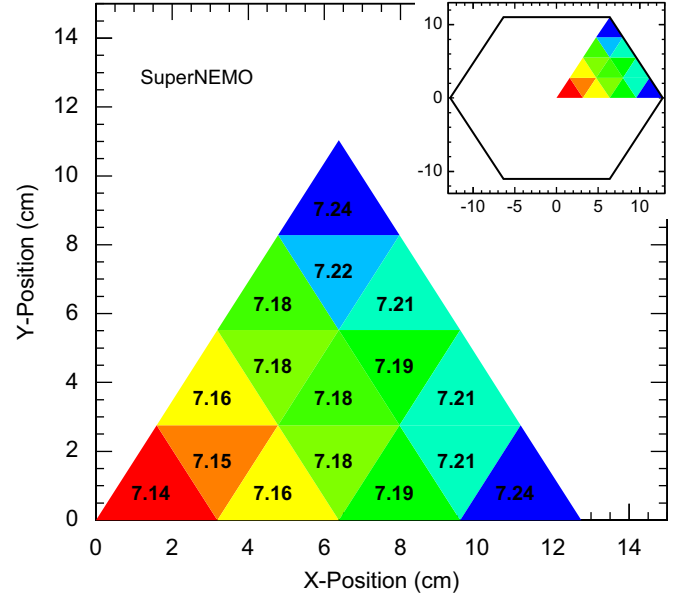
|  | $R_{FWHM}$ |
|--|------------|
| All quantities fixed                           |            |
| Quantum efficiency: 21%                        |            |
| Absorption length: 4.5 m                       |            |
| Teflon/Mylar reflectivity: 93%                 |            |
| Refractive indices: 1.5                        | 11.2       |
| After introduction of $\lambda$ dependence to: |            |
| Quantum efficiency (at constant abs. length)   | 11.6       |
| Absorption length                              | 13.8       |
| Absorption length with Stokes shifting         | 14.2       |
| Mylar reflection coefficient                   | 14.4       |
| Teflon reflection coefficient                  | 14.4       |
| All refractive indices                         | 14.4       |
| Complete model                                 | 14.4       |
| Measured                                       | 13.8       |

The initial values are best-guess estimates at a peak wavelength of 420 nm that one may assume for a simplified monochromatic simulation. Wavelength-dependence is introduced systematically to show the effect.



**Fig. 9.** A drawing of a provisional SuperNEMO scintillator module showing the scintillator, PMT, and mounting brackets.

sides and entrance face of the scintillator block and a Teflon wrapping on the top face near the PMT. Similar to NEMO-3, we assume an air gap of 50  $\mu\text{m}$  between all block faces and the Mylar wrapping. Our simulations show that with this configuration, assuming NEMO-3 scintillator absorption and emission, a resolution of  $7.5 \pm 0.5\%$  (FWHM) at 1 MeV [20] is expected. Using the symmetry of the block, each sixth of the hexagonal face is divided into 16 regions. As shown in Fig. 10, the energy resolution is fairly uniform across the face of the block. The mean energy resolution is 7.19% (FWHM) at 1 MeV and the minimum and maximum is 7.14% and 7.24%, respectively. Recently conducted preliminary measurements confirm our predictions [21].



**Fig. 10.** Spatial dependence of energy resolution (FWHM at 1 MeV) for one sixth of a SuperNEMO scintillator block.

## 6. Conclusions

We have constructed a GEANT4-based spectral model of NEMO-3 and SuperNEMO calorimeter blocks and compared the results of simulations with measurements of single electrons from  $^{207}\text{Bi}$  sources. The measured energy resolution and spatial dependence for the blocks were demonstrated to be in good agreement with simulations. The EC blocks show a doubly symmetric distribution of response about the center of the block while the EE blocks show a symmetric distribution about the z-axis, both in agreement with observations. For the SuperNEMO block, the main elements improving the resolution over the NEMO-3 blocks are the 25% increase in scintillator light yield, the 35% increase in the PMT quantum efficiency, the larger PMT size, and the incorporation of the high reflectivity aluminized Mylar. Additionally, by directly coupling the scintillator and PMT, we render light guides unnecessary which further improves the transparency and response uniformity.

As expected, including the spectral properties of all materials and incorporating wavelength-shifting absorption and emission with the effects of fluorescent quantum yield in the scintillator improves the agreement of modeling with measurements. Our approach is necessary for a detailed understanding of high resolution plastic calorimeters. The importance of these spectral simulations increases with distances travelled by photons so such models are necessary to study large-scale scintillator detectors.

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