# BEGINNER AND INTERMEDIATE LEVEL R COURSE

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# About the workshop

Materials can be accessed at https://github.com/Marcosjnez/R\_USF.

## 1. R as a Calculator

R can be used as a calculator:

3 + 2	# Sum
[1] 5	
5 - 2	# Subtraction
[1] 3	
3 * 4	# Multiplication
0 . 4	" Harorpiroactor
[1] 12	
15 / 5	# Division
[1] 3	
2^3	# Power
[1] 8	

```
10 + (2 + 3) * 3^2 # Preference order for computing

[1] 55
```

## 1.1. Assignments

R can store values using symbolic names. There are multiple ways to assign values:

```
a <- 3 # Best option
3 -> a # Less common...
a = 3 # Not recommended
a # Visualize the object
```

[1] 3

## 1.2. Reserved Words

Some names are reserved in R and cannot be used as variables:

```
# TRUE <- 4 # Error
?reserved # See reserved words</pre>
```

starting httpd help server ... done

```
?objects
```

## 1.3. Symbolic Operations

You can use variables in arithmetic operations:

```
a <- 3
b <- 2
c <- a + b
```

# 2. Data Types in R

R supports several basic data types.

## 2.1. Numeric

```
a <- 1
b <- 2
c <- 1 + 2
```

# 2.2. Character Strings

```
d <- "cat"
e <- "dog"</pre>
```

## 2.3. Factors

Factors are categorical variables:

```
d <- factor("cat")
e <- "dog"</pre>
```

# 2.4. Logical Data

Logical operations return TRUE or FALSE:

A == a # FALSE: R is case-sensitive

```
A <- 5
A == A # TRUE

[1] TRUE

B <- 5
A == B # TRUE

[1] TRUE
```

```
[1] FALSE
```

```
A > a # TRUE: A is greater than a
```

[1] TRUE

# 2.5. Complex Numbers

R supports complex numbers:

```
i <- 1i  # Square root of -1
exp(i*pi) + 1  # Euler's identity</pre>
```

[1] 0+1.224606e-16i

## 2.6. Constants

R has built-in constants like pi:

```
?Constants
pi
```

[1] 3.141593

## 2.1. Vectors

Vectors can hold elements of the same type:

## 2.2. Constructing Vectors

```
# Vector of numbers from 0 to 20 by steps of 2:
y <- seq(from = 0, to = 20, by = 2)
w <- 1:4 # Vector of integers from 1 to 4

# Concatenate the vectors:
z <- c(y, w)

# Take samples from random variables:
set.seed(2025)
rbinom(n = 10, size = 5, prob = 0.5)</pre>
```

#### [1] 3 2 3 2 3 3 4 1 3 3

```
rnorm(n = 10, mean = 0, sd = 1)
 [7] -1.75505405 -0.42096376 0.76490961 1.06616211
rt(n = 10, df = 5)
 [1] -0.2206268 -2.0056293 -0.2171123 2.5775456 -0.2399014 -1.4348883
 [7] 1.2676429 -0.6937007 -0.7065318 0.6663071
rchisq(n = 10, df = 5)
 [1] 4.792938 4.666413 2.102163 2.458308 1.923977 7.847497 2.850527 5.289288
 [9] 6.635302 2.455811
runif(n = 10, min = 0, max = 1)
 [1] 0.1097217 0.8087052 0.4355751 0.8042243 0.8617182 0.4337776 0.6402778
 [8] 0.9299222 0.8570572 0.1363258
# Random letters and categories:
sample(x = letters, size = 10, replace = TRUE)
 [1] "q" "o" "m" "d" "n" "n" "l" "t" "w" "i"
sample(c("dog", "cat"), size = 5, replace = TRUE)
[1] "dog" "dog" "cat" "dog"
# Automatic creation of long character vectors:
paste("Sujeto", 1:20, sep = "")
 [1] "Sujeto1" "Sujeto2" "Sujeto3" "Sujeto4" "Sujeto5" "Sujeto6"
 [7] "Sujeto7" "Sujeto8" "Sujeto9" "Sujeto10" "Sujeto11" "Sujeto12"
[13] "Sujeto13" "Sujeto14" "Sujeto15" "Sujeto16" "Sujeto17" "Sujeto18"
[19] "Sujeto19" "Sujeto20"
```

# 2.3. Vector Indexing

```
z <- 1:6
# Extract elements:
z[1]

[1] 1

z[c(2, 5)]

[1] 2 5
# Remove elements:
z[-1]

[1] 2 3 4 5 6

z[-c(2, 5)]

[1] 1 3 4 6</pre>
```

## 2.4. Numeric Vector Functions

```
x <- sample(x = 1:5, size = 6, replace = TRUE)
mean(x)
[1] 3.333333
median(x)</pre>
```

[1] 4

var(x)
[1] 2.266667
sd(x)
[1] 1.505545
min(x)
[1] 1
max(x)
[1] 5
sum(x)
[1] 20
prod(x)
[1] 640
log(x)
[1] 1.3862944 1.3862944 0.6931472 1.6094379 0.0000000 1.3862944
exp(x)
[1] 54.598150 54.598150 7.389056 148.413159 2.718282 54.598150
length(x)
[1] 6

```
head(x, n = 3)

[1] 4 4 2

tail(x, n = 3)

[1] 5 1 4

table(x)

x
1 2 4 5
1 1 3 1

?mean
x[1] <- NA
mean(x, na.rm = TRUE)

[1] 3.2
```

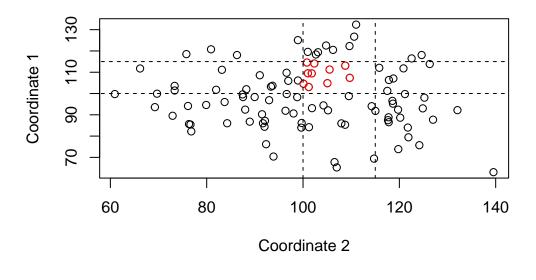
# 2.4.1. Plotting Two Numeric Vectors

```
x <- rnorm(n = 100, mean = 100, sd = 15)
y <- rnorm(n = 100, mean = 100, sd = 15)

plot(x, y, ylab = "Coordinate 1", xlab = "Coordinate 2")

# Highlight specific coordinates:
condition <- x > 100 & x < 115 & y > 100 & y < 115
indices <- which(condition)
points(x[indices], y[indices], col = "red")

# Draw segments:
segments(x0 = 100, x1 = 100, y0 = 0, y1 = 150, lty = "dashed")
segments(x0 = 115, x1 = 115, y0 = 0, y1 = 150, lty = "dashed")
segments(x0 = 0, x1 = 150, y0 = 100, y1 = 100, lty = "dashed")
segments(x0 = 0, x1 = 150, y0 = 115, y1 = 115, lty = "dashed")</pre>
```



## 2.5. Simulating Random Variables

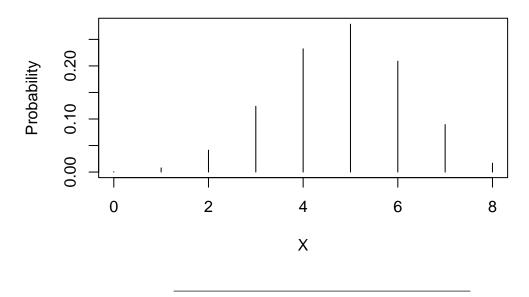
#### 2.5.1. Binomial Distribution

```
set.seed(123)
                                          # Random seed
N < -1000
                                          # Sample size
                                          # Number of trials
n <- 8
prob <- 0.60
                                          # Probability of success
b <- rbinom(N, size = n, prob = prob)</pre>
                                          # 1000 samples from Binomial
empirical <- table(b)/1000
                                          # Empirical proportions
factural <- dbinom(0:n, size = n,</pre>
                    prob = prob)
                                          # Theoretical proportions
cbind(empirical, factural)
                                          # Compare empirical and theoretical
```

```
empirical
              factural
0
      0.001 0.00065536
      0.007 0.00786432
1
2
      0.044 0.04128768
3
      0.112 0.12386304
      0.235 0.23224320
4
5
      0.287 0.27869184
      0.206 0.20901888
6
```

7 0.092 0.08957952 8 0.016 0.01679616

# $X \sim B(n=8, p=0.6)$



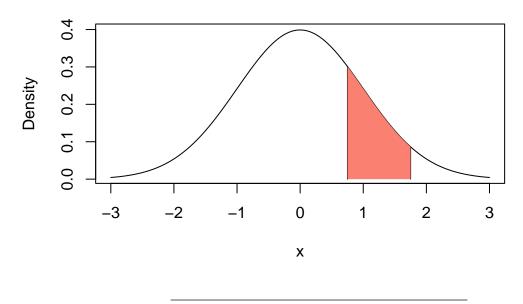
## 2.5.2. Normal Distribution

```
X \leftarrow rnorm(n = 100000, mean = 0, sd = 1)
x \leftarrow 1.25
delta \leftarrow 1
mean((X > x-delta/2 & X < x+delta/2)) / delta
```

[1] 0.18677

```
dnorm(x, mean = 0, sd = 1)
```

[1] 0.1826491



## 2.5.3. Chi-Square Distribution

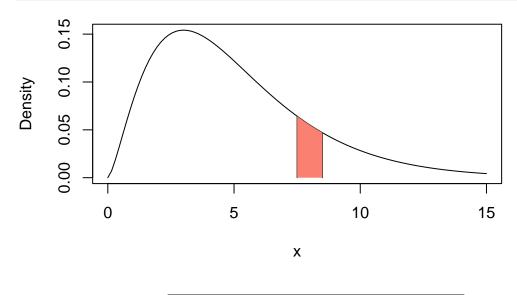
```
df <- 5
X <- rchisq(n = 100000, df = df)

x <- 8
delta <- 1
mean((X > x-delta/2 & X < x+delta/2)) / delta</pre>
```

[1] 0.05497

```
dchisq(x, df = df)
```

## [1] 0.05511196



#### 3.1. Creation of Matrices

```
# Create a matrix with a number of rows and columns:
N <- matrix(1:4, nrow = 2, ncol = 2)
N</pre>
```

```
# Create a matrix by binding vectors:
x1 \leftarrow rnorm(n = 5, mean = 0, sd = 1)
x2 \leftarrow runif(n = 5, min = 0, max = 1)
rbind(x1, x2)
                     [,2]
         [,1]
                             [,3]
                                             [,4]
                                                       [,5]
x1 -1.0016347 -1.17737291 -0.3945986 0.07629852 1.1837093
x2 0.4718714 0.03208153 0.5716739 0.45549370 0.6932237
X \leftarrow cbind(x1, x2)
                          x2
              x1
[1,] -1.00163467 0.47187144
[2,] -1.17737291 0.03208153
[3,] -0.39459859 0.57167386
[4,] 0.07629852 0.45549370
[5,] 1.18370929 0.69322374
# Set names:
colnames(X) <- paste("Score", 1:2, sep = "_")</pre>
rownames(X) <- paste("Suject", 1:5, sep = " ")</pre>
X
                       Score_2
             Score_1
Suject 1 -1.00163467 0.47187144
Suject 2 -1.17737291 0.03208153
Suject 3 -0.39459859 0.57167386
Suject 4 0.07629852 0.45549370
Suject 5 1.18370929 0.69322374
```

## 3.2. Matrix Indexing

```
X <- matrix(rnorm(2*4), nrow = 2, ncol = 4)
X</pre>
```

```
[,1] [,2] [,3] [,4]
[1,] -0.62904648 -0.4053884 -0.04479366 -0.9214312
[2,] -0.03305434  0.4058965 -0.66945112 -0.1832950

X[2, 4] # Element in row 2, column 4

[1] -0.183295

X[2, ] # All elements in row 2

[1] -0.03305434  0.40589648 -0.66945112 -0.18329500

X[, 4] # All elements in column 4

[1] -0.9214312 -0.1832950
```

## 3.3. Matrix Operations

```
# Matrix by vector multiplication:
set.seed(123)
N <- 20
p <- 4
b <- rnorm(n = p, mean = 0.5, sd = 2)
X <- matrix(rnorm(N*p), nrow = N, ncol = p-1)</pre>
```

Warning in matrix(rnorm(N \* p), nrow = N, ncol = p - 1): data length [80] is not a sub-multiple or multiple of the number of columns [3]

```
X <- cbind(1, X)
e <- rnorm(N, mean = 0, sd = 1.5)
y <- X %*% b + e

fit <- lm(y ~ 0 + X)
summary(fit)</pre>
```

```
Call:
```

 $lm(formula = y \sim 0 + X)$ 

#### Residuals:

Min 1Q Median 3Q Max -2.3744 -0.5936 -0.2121 0.7138 2.3042

#### Coefficients:

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 1.201 on 16 degrees of freedom Multiple R-squared: 0.9193, Adjusted R-squared: 0.8991

F-statistic: 45.58 on 4 and 16 DF, p-value: 1.5e-08

#### fit\$coefficients

X1 X2 X3 X4 -0.19338130 0.02804353 3.91971708 -0.10644232

## solve(t(X) %\*% X) %\*% t(X) %\*% y

[,1]

- [1,] -0.19338130
- [2,] 0.02804353
- [3,] 3.91971708
- [4,] -0.10644232

## 3.3. Matrix by Matrix Multiplication

```
Z <- matrix(rnorm(6), nrow = 3, ncol = 2)</pre>
Y <- matrix(rnorm(6), nrow = 2, ncol = 3)
ZY <- Z %*% Y
ZY
           [,1]
                      [,2]
                                  [,3]
[1,] -0.4665383 1.63228136 -0.9965839
[2,] -0.2052576 0.09397571 -0.1378942
[3,] 1.0103096 1.21882211 -0.1309261
Z[, 1, drop = FALSE] %*% Y[1, , drop = FALSE] +
  Z[, 2, drop = FALSE] %*% Y[2, , drop = FALSE]
           [,1]
                      [,2]
                                  [,3]
[1,] -0.4665383 1.63228136 -0.9965839
[2,] -0.2052576 0.09397571 -0.1378942
[3,] 1.0103096 1.21882211 -0.1309261
```

#### 3.3. Matrix Utilities

```
ncol(ZY)
```

[1] 3

nrow(ZY)

[1] 3

```
rowSums(ZY)
```

[1] 0.1691592 -0.2491761 2.0982055

#### colMeans(ZY)

[1] 0.1128379 0.9816931 -0.4218014

```
# Apply a custom function to each column
X <- matrix(runif(16), nrow = 4, ncol = 4)

geomean <- function(x) {
    n <- length(x)
    result <- prod(x)^(1/n)
    return(result)
}

apply(X, MARGIN = 2, FUN = geomean)</pre>
```

[1] 0.2393893 0.3770300 0.4454315 0.5436993

3.4. Arrays

```
A <- array(rnorm(2*3*4), dim = c(2, 3, 4))
```

```
[,1] [,2] [,3]
[1,] 1.8438620 0.23538657 -0.96185663
[2,] -0.6519499 0.07796085 -0.07130809

, , 2

[,1] [,2] [,3]
[1,] 1.4445509 0.04123292 -2.053247
[2,] 0.4515041 -0.42249683 1.131337

, , 3
```

```
[,1]
                     [,2]
                                [,3]
[1,] -1.4606401 1.909104 0.7017843
[2,] 0.7399475 -1.443893 -0.2621975
, , 4
          [,1]
                     [,2]
                                [,3]
[1,] -1.572144 -1.6015362 -1.4617556
[2,] -1.514668 -0.5309065 0.6879168
apply(A, MARGIN = 2, FUN = mean)
                                      # Across dimensions 1 and 3
[1] -0.08994217 -0.21689360 -0.28616584
apply(A, MARGIN = c(1, 2), FUN = sum) # Across slices
           [,1]
                      [,2]
                                [,3]
[1,] 0.2556286 0.5841869 -3.775075
[2,] -0.9751660 -2.3193357 1.485748
```

## 3.5. Data Frames

```
N <- 100
x1 <- sample(c("dog", "cat"), size = N, replace = TRUE)
x2 <- sample(1:4, size = N, replace = TRUE)

df <- data.frame(pet = x1, score = x2)
df$pet</pre>
```

```
[1] "cat" "cat" "dog" "dog" "cat" "cat" "dog" "cat" "dog" "cat" "dog" "dog" "cat" "dog" [13] "dog" "dog" "cat" "dog" "cat" "dog" "cat" "cat" "cat" "cat" "cat" "dog" "dog" [25] "dog" "cat" "dog" "dog" "cat" "dog" "dog" "cat" "dog" "dog" "cat" "cat" "cat" "cat" [37] "dog" "dog" "dog" "dog" "cat" "dog" "dog" "dog" "dog" "cat" "dog" [49] "cat" "dog" "dog" "cat" "dog" "dog" "dog" "cat" "dog" "cat" "dog" "cat" [61] "dog" "dog" "dog" "cat" "cat" "dog" "dog" "cat" "dog" "cat" "dog" [73] "cat" "dog" "dog" "cat" "cat" "cat" "cat" "cat" "cat" "dog" "dog" "cat" "dog" "dog" "cat" "dog" "dog" "cat" "dog" "cat" "dog" "dog" "dog" "dog" "dog" "cat" "dog" "d
```

#### df\$score

```
[1] 3 3 4 2 3 3 3 1 1 3 2 3 2 1 4 2 2 2 4 1 4 1 1 3 3 1 1 3 1 3 4 2 1 1 3 4 2 [38] 3 2 1 2 3 2 3 3 1 2 4 1 2 2 4 2 4 2 4 2 1 4 2 4 1 4 2 1 4 4 3 2 1 3 2 4 3 2 3 [75] 3 1 4 2 3 1 1 3 2 3 2 2 2 4 1 4 2 1 4 2 1 4 1 4 2 2
```

```
fit <- lm(score ~ pet, data = df)
summary(fit)</pre>
```

```
Call:
```

lm(formula = score ~ pet, data = df)

#### Residuals:

Min 1Q Median 3Q Max -1.4386 -0.6836 -0.4186 0.5814 1.5814

#### Coefficients:

Estimate Std. Error t value Pr(>|t|)

(Intercept) 2.41860 0.16769 14.42 <2e-16 \*\*\*

petdog 0.01999 0.22211 0.09 0.928
---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 1.1 on 98 degrees of freedom
Multiple R-squared: 8.266e-05, Adjusted R-squared: -0.01012

F-statistic: 0.008101 on 1 and 98 DF, p-value: 0.9285

#### 3.6. Lists

```
L <- list(1, 1:5, matrix(1:16, nrow = 4, ncol = 4))
L
```

[[1]]

[1] 1

```
[[2]]
[1] 1 2 3 4 5
[[3]]
     [,1] [,2] [,3] [,4]
[1,]
       1
                 9
            5
[2,]
        2
             6
                 10
                      14
[3,]
        3
             7
                 11
                      15
[4,]
        4
           8
                 12
                      16
# Multiply and sum rank-1 matrices using lapply
f <- function(i) {</pre>
 x \leftarrow Z[, i, drop = FALSE] %*% Y[i, , drop = FALSE]
return(x)
ZY \leftarrow lapply(1:ncol(Z), FUN = f)
[[1]]
                                  [,3]
           [,1]
                     [,2]
[1,] 0.54751085 1.53960722 -0.49427754
[2,] 0.02590656 0.07284958 -0.02338772
[3,] 0.45159240 1.26988337 -0.40768504
[[2]]
                       [,2]
           [,1]
                                   [,3]
[1,] -1.0140492 0.09267413 -0.5023063
[2,] -0.2311642 0.02112613 -0.1145065
[3,] 0.5587172 -0.05106126 0.2767589
ZY[[1]] + ZY[[2]]
                                  [,3]
           [,1]
                      [,2]
[1,] -0.4665383 1.63228136 -0.9965839
[2,] -0.2052576 0.09397571 -0.1378942
[3,] 1.0103096 1.21882211 -0.1309261
```

## 3.7. Objects in the Environment

```
objects()
                  " A "
                               "b"
                                            "B"
                                                          "c"
 [1] "a"
                                                                       "condition"
                               "df"
                                            "e"
                                                          "empirical" "f"
 [7] "d"
                  "delta"
[13] "factural" "fit"
                               "geomean"
                                            "i"
                                                          "indices"
                  "L"
                                                          "p"
[19] "1"
                               "n"
                                            "N"
                                                                       "prob"
[25] "w"
                  "x"
                               יי ע יי
                                                          "x1"
                                                                       "x2"
                                            "x_fill"
                  "Y"
                                            "z"
                                                          "Z"
                                                                       "ZY"
[31] "y"
                               "y_fill"
ls()
 [1] "a"
                  " A "
                               "b"
                                            "B"
                                                          "c"
                                                                       "condition"
                                                          "empirical" "f"
 [7] "d"
                               "df"
                                            "e"
                  "delta"
                                            "i"
[13] "factural" "fit"
                               "geomean"
                                                          "indices"
[19] "1"
                  "L"
                                            "N"
                               "n"
                                                          "p"
                                                                       "prob"
                  "x"
                               "X"
[25] "w"
                                            "x fill"
                                                          "x1"
                                                                       "x2"
                  "Y"
                                                          "Z"
                                            "z"
                                                                       "ZY"
[31] "y"
                               "y_fill"
```

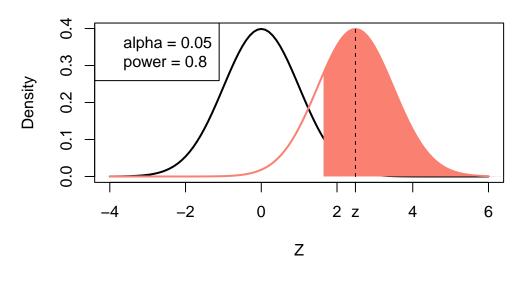
## 4.1. Simulation Setup for the Linear Model

```
set.seed(123) # Fix the seed to get the same random numbers
# Setup:
N <- 10
                                        # Sample size
x \leftarrow rnorm(N, mean = 0, sd = 1)
                                       # Predictor / Independent variable
                                       # Standard deviation of the errors
sigma <- 1.5
true\_se \leftarrow sigma / sqrt(var(x)*(N-1)) # True standard error of b
                                        # Statistical power
power <- 0.80
alpha <- 0.05
                                       # Type-I error
threshold <- qnorm(1-alpha)
                                      # One-sided point for rejection
# Get the b that gives the desired statistical power:
b <- qnorm(power, mean = threshold, sd = 1) * true_se</pre>
```

## 4.2. Simulating Power

## 4.3. Visual Insight into Statistical Power

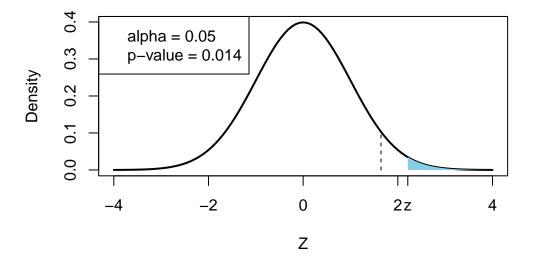
# **Null vs. Alternative hypothesis**



# 4.4. Visual Insight into the P-value

```
# Generate a random z-statistic under the alternative hypothesis:
z_statistic <- rnorm(1, mean = b / true_se, sd = 1)</pre>
pval <- round(1 - pnorm(z_statistic), 3)</pre>
curve(dnorm(x, mean = 0, sd = 1), xlim = c(-4, 4), lwd = 2,
      xlab = "Z", ylab = "Density", main = "Null hypothesis")
# Shade the p-value region:
x_fill <- seq(z_statistic, 10, length.out = 100)</pre>
y_{fill} \leftarrow dnorm(x_{fill}, mean = 0, sd = 1)
polygon(c(z_statistic, x_fill, 10),
        c(0, y_fill, 0),
        col = "skyblue", border = NA)
segments(x0 = threshold,
         x1 = threshold,
         y0 = 0,
         y1 = dnorm(threshold, mean = 0, sd = 1),
         lty = "dashed")
axis(1, at = z_statistic, label = "z")
legend(x = "topleft", legend = c(paste("alpha =", alpha),
                                   paste("p-value =", pval)))
```

# **Null hypothesis**



## 5.1. Linear Model with Multiple Predictors

```
set.seed(123)
N <- 20
p <- 4
b <- rnorm(n = p, mean = 0.5, sd = 2)
X <- matrix(rnorm(N*p), nrow = N, ncol = p-1)</pre>
```

Warning in matrix(rnorm(N \* p), nrow = N, ncol = p - 1): data length [80] is not a sub-multiple or multiple of the number of columns [3]

```
X <- cbind(1, X)</pre>
nsim <- 1000
sigma <- 1.5
true_se <- sqrt(diag(sigma^2 * solve(t(X) %*% X)))</pre>
power \leftarrow c(0.80, 0.60, 0.40, 0.05)
alpha <- 0.05
threshold \leftarrow qt(1 - alpha, df = N - p)
f <- function(power, threshold) {</pre>
  suppressWarnings(uniroot(\(x) (1 - pt(threshold, df = N - p, ncp = x)) - power,
                               interval = c(-6, 6))$root)
}
t_stat <- sapply(power, FUN = f, threshold = threshold)</pre>
b <- t_stat * true_se</pre>
# Initialize result storage:
coefs <- matrix(NA, nsim, p)</pre>
se <- matrix(NA, nsim, p)</pre>
ts <- matrix(NA, nsim, p)</pre>
pval <- matrix(NA, nsim, p)</pre>
upper <- matrix(NA, nsim, p)</pre>
lower <- matrix(NA, nsim, p)</pre>
error <- vector(length = nsim)</pre>
for (i in 1:nsim) {
  e <- rnorm(N, mean = 0, sd = sigma)
```

```
y <- X %*% b + e
fit <- lm(y ~ 0 + X)
coefs[i, ] <- coefficients(fit)
error[i] <- sum(resid(fit)^2) / (N - p)
se[i, ] <- sqrt(diag(error[i] * solve(t(X) %*% X)))
ts[i, ] <- coefs[i, ] / se[i, ]
upper[i, ] <- coefficients(fit) + qnorm(1 - alpha/2) * se[i, ]
lower[i, ] <- coefficients(fit) + qnorm(alpha/2) * se[i, ]
pval[i, ] <- (1 - pt(ts[i, ], df = N - p))
}</pre>
```

## 5.1. Checking Simulation Accuracy

```
cbind(colMeans(coefs), b) # Linear coefficients
                            b
[1,] 0.87159473 8.793200e-01
[2,] 0.69604900 6.956320e-01
[3,] 0.52666068 5.304025e-01
[4,] -0.02259479 -7.209672e-08
cbind(colMeans(se), true_se) # Standard errors
                true_se
[1,] 0.3328807 0.3383593
[2,] 0.3451118 0.3507917
[3,] 0.3590934 0.3650034
[4,] 0.4216360 0.4285753
cbind(colMeans(ts), t_stat) # t statistics
                       t_stat
[1,] 2.69519451 2.598776e+00
[2,] 2.08044868 1.983035e+00
[3,] 1.51452823 1.453144e+00
[4,] -0.05401576 -1.682241e-07
```

```
apply(pval, MARGIN = 2, FUN = (x) mean(x < alpha)) # Empirical power
```

[1] 0.799 0.585 0.398 0.045

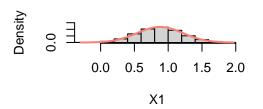
power

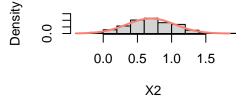
[1] 0.80 0.60 0.40 0.05

## 5.2. Distribution of Coefficients

## **Distribution of coefficients**

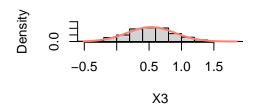
## **Distribution of coefficients**

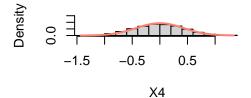




## **Distribution of coefficients**

## **Distribution of coefficients**

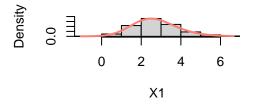


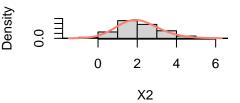


## 5.3. Distribution of t Statistics

## Distribution of the t statistic

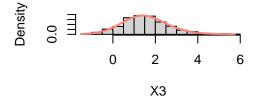
## Distribution of the t statistic

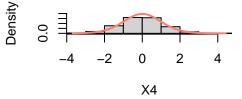




#### Distribution of the t statistic

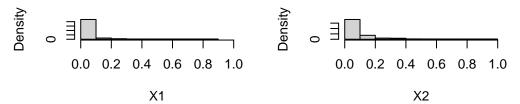
#### Distribution of the t statistic



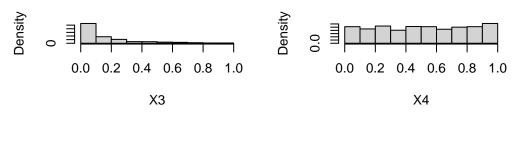


#### 5.4. P-curve

## istribution of the p-value for poweristribution of the p-value for power



## istribution of the p-value for powerstribution of the p-value for power



## 5.5. The Dance of Confidence Intervals

```
par(mfrow = c(1, 1))
success \leftarrow rep(0, p)
failure <- rep(0, p)
nsim <- 20
for (i in 1:nsim) {
  plot(b, 1:p, xlab = "Value", ylab = "Coefficient",
       ylim = c(-1, 4.5), xlim = c(-2, 5),
       main = "The Dance of confidence intervals",
       yaxt = "n")
  axis(2, labels = paste(1:p), at = 1:p)
  for (j in 1:p) {
    segments(x0 = upper[i, j], x1 = lower[i, j], y0 = j, y1 = j)
    if (b[j] > lower[i, j] & b[j] < upper[i, j]) {</pre>
      points(b[j], j, bg = "skyblue", pch = 21)
      success[j] <- success[j] + 1</pre>
    } else {
```

```
points(b[j], j, bg = "red", pch = 21)
    failure[j] <- failure[j] + 1
}

text(x = 4.5, y = j, labels = paste(success[j], failure[j], sep = "/"))
}

text(x = 1, y = 0, paste("Iteration", i, sep = "="))
Sys.sleep(2)
}</pre>
```