

Data Structures and Algorithms (DSA)

I claim that the difference between a bad programmer and a good one is whether he considers his code or his data structures more important.

Bad programmers worry about the code.

Good programmers worry about data structures and their relationships.

Linus Torvalds, 2006

Literature

- **10 Best books in DSA:** <https://medium.com/javarevisited/10-best-books-for-data-structure-and-algorithms-for-beginners-in-java-c-c-and-python-5e3d9b478eb1>
- **Algorithms:** <https://algs4.cs.princeton.edu/home/>
- **Princeton Videos:** <https://algs4.cs.princeton.edu/lectures/>
- **TutorialsPoint:**
https://www.tutorialspoint.com/data_structures_algorithms/index.htm
- **Geeksforgeeks:** <https://www.geeksforgeeks.org/learn-data-structures-and-algorithms-dsa-tutorial/>
- **Progamiz:** <https://www.programiz.com/dsa>
- **W3schools:** <https://www.w3schools.blog/data-structure-algorithm>

Some main DSAs

Data Structures	Algorithms
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Linked lists	Search
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Stacks	Sorting
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Queues	Graph/tree traversing
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Sets	Dynamic programming
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Maps	Regex
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Hash tables	Hashing
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Search trees	AI
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The Big O

$O()$ is the asymptotic notation of the worst case scenario.

$O()$ is also called time complexity.

Definition:

$$f(x) = O(g(x))$$

for $x \rightarrow \infty$

It is equivalent with the following postulat:

There is a $M \in \mathbb{R}$ and a $x_0 \in \mathbb{R}$

such for all $x \geq x_0 \in \mathbb{R}$

we have, $|f(x)| \leq Mg(x)$

Example

$$f(x) = 6x^4 - 2x^3 + 5$$

and,

$$g(x) = x^4$$

For $M \in \mathbb{R} \sup +$

$$f(x) = O(g(x)) \rightarrow |f(x)| \leq Mg(x)$$

$$|6x^4 - 2x^3 + 5| < |6x^4| + |2x^3| + |5|$$

$$|6x^4 - 2x^3 + 5| < 6x^4 + 2x^4 + 5^4$$

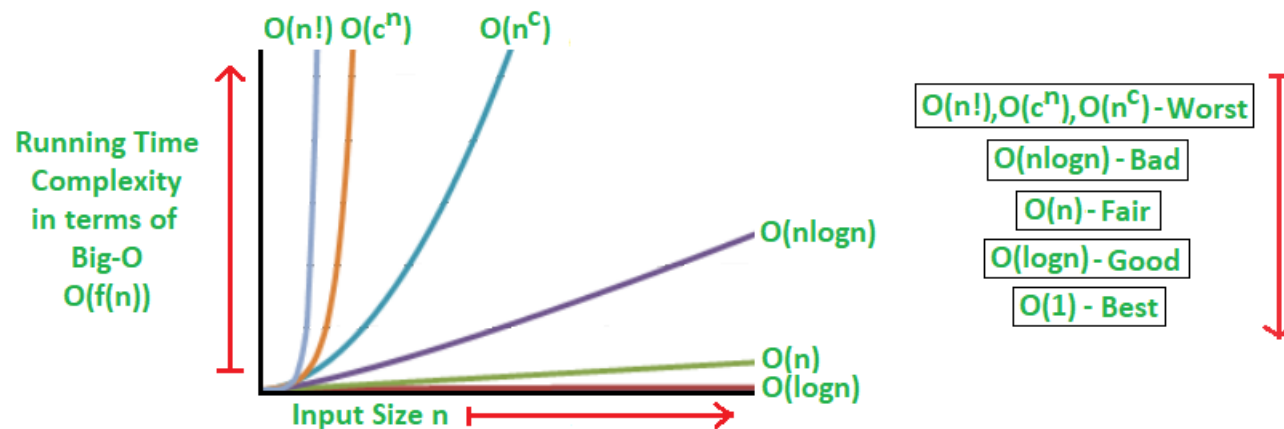
for all, $x \geq x_0 = 1$

$$|6x^4 - 2x^3 + 5| < 13x^4 \rightarrow M = 13$$

Implies that

$$f(x) = O(x^4)$$

constant	$O(1)$	Best
logarithmic	$O(\log n)$	Good
linear	$O(n)$	Fair
$n \log(n)$	$O(n \log n)$	Bad
potential	$O(n^c)$	Worst
exponential	$O(c^n)$	Worst
factorial	$O(n!)$	Worst



Time complexity of single and nexted loops

The time complexity of a loop is $O(N)$

A code containing two single loops

Loop1: M times

$O(1)$ operation

Loop2: N times

$O(1)$ operation

The teoretical time complexity is $O(M+N+1) = O(M+N)$

Time complexity of two nested loops

Outside loop M times

Inner loop N times

$O(1)$ operation

The time complexity is $O(M*N)$

Example i C

```
for(i=0;i<M;i++)  
    for(j=0;j<N;j++)  
        k=i+j;
```

Time complexity of nexted loops with same iterator

Outer Loop for $i=1$ to N
Inner Loop for $j=1$ to i
 $O(1)$ operation

=> The time complexity is $O(N \log N)$

The time complexity of a loop when the iterator is divided by k is:
 $O(\log_k N)$

```
int N=8,k=0;
for(i=N/2;i<=N;i++){
    for(j=2;j<=N;j=j*2)
        j=2*j;
    printf("%d ",k);
    k=k+N/2;
```

The inner loop is $O(\log N)$ and the outer loop goes $N/2$ times $\Rightarrow O(N/2)$

\Rightarrow The entire algorithm is $O(\log^2 N)$

'Hands on' laborationer

- Using clock() benchmark a function containing loops
- Using Gnuplot plot all results in loglog scales

