

[ALGORITHMS & EFFICIENCY]

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GOALS

Build an event driven object-oriented Java program that takes as input an unsorted list of randomly generated integers, implements basic structures and uses algorithms to benchmark different sorting algorithms on the arrays. We will then proceed to compare their respective performances and provide evidence as to which of our tested sorting algorithm is best.

MY APPROACH

Firstly, I decided to compartmentalise individual sorting algorithms in to their own classes for future ease of use.

For the 'Quick Sort' algorithm I decided to use a stack-based approach, due to tests instantiating that this method drastically improves speeds and uses less memory.

For the 'Hybrid' sorting classes, I used subarray lists of the size of a given threshold. This means that the sub arrays are only the size of the threshold and can be sorted by themselves before parsing them back in to their primary arrays to be sorted again.

I used a combination of 'Quick Sort' mixed with either 'Selection Sort' or 'Insertion Sort' where 'Quick Sort' sorts the already sorted subarrays.

All of this was planned, and mapped using Kanban and Infinite Canvas to keep track of progress and write out algorithms in Pseudocode before programming them in (find below).

EXTRACTS

```
// Declares values for quick sort and reversed quick sort methods.
//
public int[] quickSort(List<Integer> Array, int elements) {
    int[] arr = new int[elements];
    for (int element = 0; element < elements; element++) {
        arr[element] = Array.get(element);
    }
    if(arr.length <= 0) return arr;
    Stack<Integer> stack = new Stack<>();

    stack.push(0);
    stack.push(arr.length - 1);
    while(!stack.isEmpty()){
        int high = stack.pop();
        int low = stack.pop();

        int pivotIdx = partition(arr, low, high);
        if(pivotIdx > low) {
            stack.push(low);
            stack.push(pivotIdx - 1);
        }
        if(pivotIdx < high && pivotIdx >= 0){
            stack.push(pivotIdx + 1);
            stack.push(high);
        }
    }
    return arr;
}
```

'Quicksort Algorithm'

```
private int partition(int[] arr, int low, int high){
    if(arr.length <= 0) return -1;
    if(low >= high) return -1;
    int l = low;
    int r = high;

    int pivot = arr[l];
    while(l < r){
        while(l < r && arr[r] >= pivot){
            r--;
        }
        arr[l] = arr[r];
        while(l < r && arr[l] <= pivot){
            l++;
        }
        arr[r] = arr[l];
    }
    arr[l] = pivot;
    return l;
}
```

'Quicksort Algorithm Partition'

```

public int[] insertionSort(List<Integer> Array, int elements){

    int[] arr = new int[elements];
    for (int element = 0; element < elements; element++) {
        arr[element] = Array.get(element);
    }
    if(arr.length <= 0) return arr;

    for( int i=0; i<arr.length-1; i++ ) {
        for( int j=i+1; j>0; j-- ) {
            if( arr[j-1] <= arr[j] )
                break;
            int temp = arr[j];
            arr[j] = arr[j-1];
            arr[j-1] = temp;
        }
    }
    return arr;
}

```

‘Insertion-Sort Algorithm’

```

public class sortSelection {
    public int[] selectionSort(List<Integer> Array, int elements){
        int[] arr = new int[elements];
        for (int element = 0; element < elements; element++) {
            arr[element] = Array.get(element);
        }
        if(arr.length <= 0) return arr;
        for(int i = 0; i < arr.length-1; i++){
            int min = i;
            for(int j = i+1; j < arr.length; j++){
                if(arr[j] < arr[min]){
                    min = j;
                }
            }
            if(min != i){
                int temp = arr[min];
                arr[min] = arr[i];
                arr[i] = temp;
            }
        }
        return arr;
    }
}

```

‘Selection-Sort Algorithm’

```

public int[] hybridSortQI(List<Integer> Array, int elements, int
threshold) {
    int[] arr = new int[elements];
    List<List<Integer>> subList = new ArrayList<>();
    List<Integer> ArrayCopy = new ArrayList<>(Array);
    for (int element = 0; element < elements; element++) {
        arr[element] = Array.get(element);
    }
    if(arr.length <= 0) return arr;

    for (int i = 0; i < elements; i += threshold) {
        subList.add(Array.subList(i, Math.min(i + threshold,
elements)));
    }

    int index = 0;
    for (int i = 0; i < subList.size(); i++) {
        List<Integer> cache = new ArrayList<>(subList.get(i));
        // Sort the subarrays using Insertion or Selection sort.
        int[] cacheSorted = sI.insertionSort(cache, cache.size());

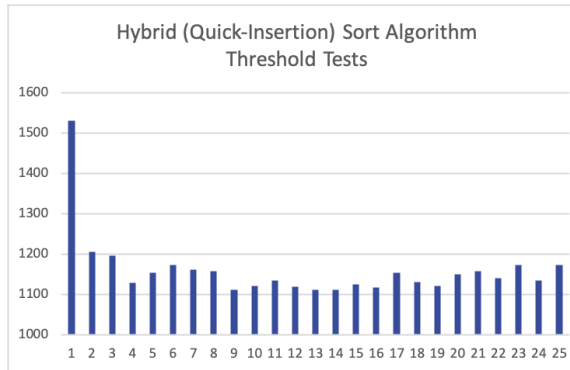
        for (int j = 0; j < cacheSorted.length; j++) {
            ArrayCopy.set(index++, cacheSorted[j]);
        }
    }
    // Sort the entire array using quicksort
    arr = sQ.quickSort(ArrayCopy, ArrayCopy.size());
    return arr;
}

```

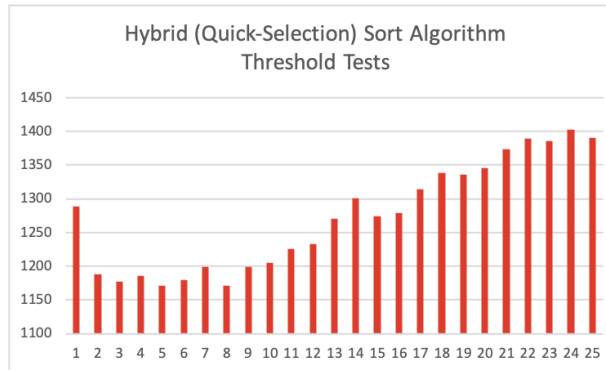
‘Hybrid-Sorting Algorithm’

BENCHMARKING

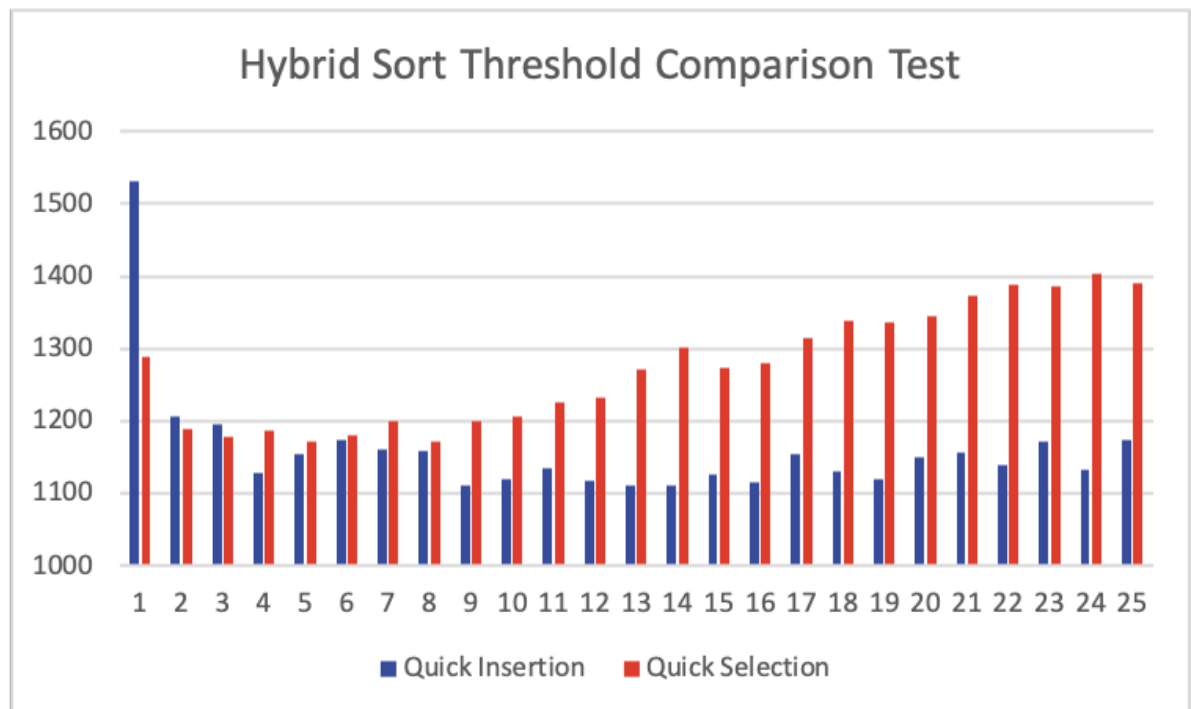
Firstly, to benchmark the hybrid sorting algorithms whilst at their peak efficiency, we needed to test which 'threshold' was best for each Hybrid Sort, so 'benchmarkComputerThreshold.java' was made, this file outputs a 'Comma Separated Values (CSV)' that is readable by Microsoft Excel. Once complete, benchmark performances can be graphed accordingly:



'Quick-Insertion' threshold tests
x: threshold value.
y: time in ms.



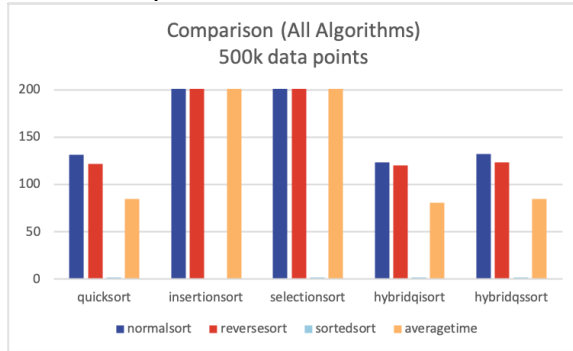
'Quick-Selection' threshold tests
x: threshold value.
y: time in ms.



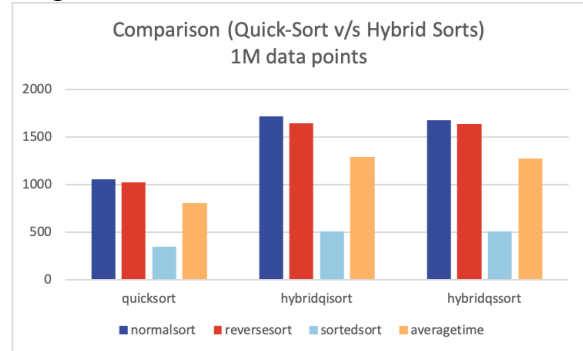
'Hybrid Sorts' compared
x: threshold value.
y: time in ms.

This shows that the 'Quick Insertion' sorting method has a better average performance at a threshold of 14 and that the most efficient 'Quick Selection' sorting can be is at a threshold of 8.

Now it's possible to benchmark the algorithms themselves as follows:



All algorithms: compared (500k random values).



Algorithms of interest: compared (1M random values).

(all random values are using same seed for more accurate testing)

This shows that the performance of quicksort is outweighed by that of both Hybrid Sorts by small margins for an array size of 500k values, but the opposite effect occurs once the array size is increased to 1M random values.

EVIDENCE

(loading a text file with over 500k lines was impossible for my machines, please find attached ZIP archive with file called 'sortedProof.txt' for full output of the Quicksort algorithm).

```
Sorted List: 2 3 4 4 7 7 8 8 8 9 10 13 14 15 16 19 20 20 21 21 21 23 23 24 24 25 25 26 26 27 27 27 28 28 28 29 29 30 32 32 32 33 34 34 36 36 36 39 39 41 42 43 45 46 46 47 47 48 50 51 52 52
53 54 55 57 57 58 58 62 62 65 66 66 66 66 66 67 69 69 69 69 71 72 72 73 76 76 77 79 80 81 82 84 85 86 86 88 88 89 90 91 91 92 93 94 94 94 96 98 98 99 100 100 100 102 103 105 109
109 110 112 113 114 115 115 117 117 120 120 123 123 123 124 125 125 126 128 128 129 130 130 131 132 132 132 132 133 134 135 135 135 137 137 139 141 141 141 142 143 145
145 149 150 151 151 151 153 154 156 156 157 157 159 159 162 162 162 163 165 167 167 170 170 171 172 173 173 175 177 178 180 180 181 181 181 184 184 185 186 186 186 186 186 188 189 190
499916 499916 499917 499917 499918 499919 499922 499923 499923 499925 499925 499926 499927 499930 499930 499932 499932 499933 499935 499935 499937 499938 499938 499938 499939
499939 499939 499940 499941 499941 499943 499944 499944 499947 499951 499952 499952 499954 499955 499955 499956 499959 499960 499962 499962 499963 499963 499964 499964 499965 499966
499968 499968 499969 499969 499970 499971 499971 499972 499972 499973 499974 499975 499975 499977 499978 499980 499980 499982 499982 499982 499983 499984 499984 499986 499989
499990 499991 499992 499993 499994 499996 499996 499996 499998 499999 499999 499999 499999 499999 499999 499999 499999 499999 499999 499999 499999 499999 499999 499999 499999
Sorted List (in reverse): 499998 499996 499996 499996 499999 499993 499992 499991 499990 499989 499988 499986 499984 499984 499984 499983 499982 499982 499982 499980 499980 499978 499977
499975 499975 499974 499973 499972 499972 499971 499971 499970 499969 499969 499968 499968 499966 499965 499964 499964 499963 499963 499962 499962 499960 499959 499956 499955
499954 499952 499952 499951 499947 499944 499944 499943 499941 499941 499940 499939 499939 499939 499938 499938 499937 499935 499935 499933 499932 499932 499930 499930 499927
499926 499925 499925 499923 499923 499922 499919 499918 499917 499917 499916 499916 499916 499915 499914 499912 499910 499910 499909 499908 499908 499906 499905 499902 499902
157 156 156 154 153 151 151 151 150 149 145 145 143 142 141 141 141 139 137 137 135 135 135 134 133 132 132 132 132 132 131 130 130 129 128 128 126 125 125 124 123 123 120 120
117 117 117 115 114 113 113 112 110 109 109 105 103 102 100 100 100 100 99 98 98 96 94 94 94 92 91 91 90 89 88 88 86 86 85 85 84 82 81 80 79 77 76 73 72 72 71 69 69 69 67
66 66 66 66 65 62 62 62 58 58 57 57 55 54 53 52 52 51 50 48 47 47 46 46 45 45 43 42 41 39 39 36 36 36 36 34 34 33 32 32 32 30 29 29 28 28 27 27 27 26 26 25 25 24 24 23 23 21 21 21 20 20 19 16
15 14 13 10 9 8 8 7 7 4 4 3 2
```

This proves the algorithm is indeed sorting all of the values as requested.

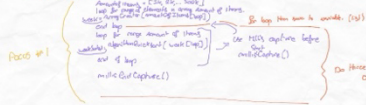
CONCLUSION

Overall, from what it seems thanks to the data the program provided, the Quick Sort function is much more efficient for larger datasets, although slower for the given data we were originally required to test.

Notes (mainly recursive) **Benchmarks?**

for 10, 100, 1000, 10000, 100000 and 1000000

Apply the quicksort algorithm to the array



Create Array

What's applied?

1. A recursive function takes a lot of time. 2. A recursive function takes a lot of time. 3. A recursive function takes a lot of time.

For Sort algorithm

1. Sort all elements 2. Sort all elements 3. Sort all elements

Recursion problem

1. Sort all elements 2. Sort all elements 3. Sort all elements

1. Sort all elements 2. Sort all elements 3. Sort all elements

1. Sort all elements 2. Sort all elements 3. Sort all elements

1. Sort all elements 2. Sort all elements 3. Sort all elements

THE RECURSION PROBLEM

1. Sort all elements 2. Sort all elements 3. Sort all elements

1. Sort all elements 2. Sort all elements 3. Sort all elements

1. Sort all elements 2. Sort all elements 3. Sort all elements

Next Sort: 1st pass in Recursion

1. Sort all elements 2. Sort all elements 3. Sort all elements

1. Sort all elements 2. Sort all elements 3. Sort all elements

Stop here: What are we doing?

Requirements: 1. Sort all elements 2. Sort all elements 3. Sort all elements

1. Sort all elements 2. Sort all elements 3. Sort all elements

1. Sort all elements 2. Sort all elements 3. Sort all elements

To Do:

1. Sort all elements 2. Sort all elements 3. Sort all elements

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1. Sort all elements 2. Sort all elements 3. Sort all elements

How Merge Sort works

1. Sort all elements 2. Sort all elements 3. Sort all elements

Sort Merge

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