

Prob and Stat Hmwk ch4

Marcus Hall

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Pg 212: 1,2,8,10

2) Let $X \sim \text{Bin}(9, 0.4)$. $P(X > 6)$

```
pbinom(6,9,0.4,lower.tail = FALSE)
```

```
## [1] 0.02503475
```

$P(X \geq 2)$

```
1-pbinom(1,9,0.4)
```

```
## [1] 0.9294561
```

$\Pr(X > 1) = \Pr(X \geq 2)$

$P(2 \leq X < 5) \Rightarrow P(x < 5) - P(x \leq 2) \Rightarrow P(x \leq 4) - P(x \leq 2)$

```
pbinom(4,9,0.4)-pbinom(2,9,0.4)
```

```
## [1] 0.5016453
```

$P(2 \leq X \leq 5) - P(x < 2) \Rightarrow P(x \leq 5) - P(x \leq 1)$

```
pbinom(5,9,0.4)-pbinom(1,9,0.4)
```

```
## [1] 0.8301036
```

$P(X = 0)$

```
pbinom(0,9,0.4)
```

```
## [1] 0.0100777
```

$P(X = 7)$

```
dbinom(7,9,0.4)
```

```
## [1] 0.02123366
```

$\mu(x) = 3.6$ $\text{Sigma}^2(x) = 2.16$

8) A general contracting firm experiences cost overruns on 20% of its contracts. In a company audit, 20 contracts are sampled at random.

$P(X = 4)$

```
dbinom(4,20,0.2)
```

```
## [1] 0.2181994
```

$P(X < 3)$

```
pbinom(2,20,0.2)
```

```
## [1] 0.2060847
```

$P(X = 0)$

```
dbinom(0,20,.2)
```

```
## [1] 0.01152922
```

$\mu(x)$ [Mean] = 4 $\sigma^2(x)$ (Standard Deviation) = 1.78

- 10) A quality engineer takes a random sample of 100 steel rods from a day's production and finds that 92 of them meet specifications.

Estimate the proportion of that day's production that meets specifications and find the uncertainty in the estimate. a) 0.3119 Estimate the number of rods that must be sampled to reduce the uncertainty to 1%. b) 0.17679

Pg 227: 1,4,6,16 4) Geologists estimate the time since the most recent cooling of a mineral by counting the number of uranium fission tracks on the surface of the mineral. A certain mineral specimen is of such an age that there should be an average of 6 tracks per cm^2 of surface area. Assume the number of tracks in an area follows a poisson distribution. Let X represent the number of tracks counted in 1 cm^2 of surface area. Find... $\lambda = 6$ A) $P(X=7)$

```
dpois(7,6)
```

```
## [1] 0.137677
```

- b) $P(X \geq 3)$

```
ppois(2,6,lower.tail = FALSE)
```

```
## [1] 0.9380312
```

$P(x \geq 3) = P(X > 2)$

- c) $P(2 < X < 7)$

```
ppois(6,6)-ppois(1,6)
```

```
## [1] 0.5889515
```

d) $\mu(x)$ $\mu = \lambda = 6$ e) $\sigma^2(x) = 6$

- 6) one out of every 5000 individuals in a population carries a certain defective gene. A random sample of 1000 individuals is studied. $\lambda = 1/5000$

- a) What is the probability that exactly one one of the sample individuals carries the gene?

```
dpois(1,1/5000*1000)
```

```
## [1] 0.1637462
```

- b) That none are carries the gene?

```
dpois(0,1/5000*1000)
```

```
## [1] 0.8187308
```

- C) that more than 2 carry the gene?

```
ppois(2,1/5000*1000,lower.tail = FALSE)
```

```
## [1] 0.001148481
```

- d) Mean = $\lambda = 1/5000 \cdot 1000$

```
1/5000*1000
```

```
## [1] 0.2
```

e) $SD = \lambda = .2 = \text{mean}$

16) Grandma is trying out a new recipe for raisin bread. Each batch of bread dough makes 3 loaves and each loaf contains 20 slices of bread.

a) 100 raisins into a batch of dough, what is the probability that a randomly chosen slice of bread contains no raisins? average = $100/(3*20) = 1.666$ raisins per slice.

```
dpois(0,100/60)
```

```
## [1] 0.1888756
```

b) 200 raisins into a batch of dough, what is the probability that a randomly chosen slice of bread contains 5 raisins? average = $200/(3*20) = 3.33$ raisins per slice.

```
dpois(5,200/60)
```

```
## [1] 0.1223388
```

c) how many raisins must be put in a batch so the probability that a randomly selected slice will have no raisins is 0.01? $\lambda = -\ln(P(X=0))$ $P(X=0)=0.01$

```
-log(0.01)
```

```
## [1] 4.60517
```

```
N=Lambda*20
```

```
(-log(0.01)*3*20)
```

```
## [1] 276.3102
```

Pg 240: 1, 2, 12 2) There are 30 restaurants in a certain town. Assume that four of them have health code violations. A health inspector chooses 10 restaurants at random to visit. a) what is the probability that two of the restaurants with health code violations will be visited. $X \sim \text{Hyper}(30,4,10)$... $P(X=2)$ $m = 4$, $n = 26$, $k = 10$ $\text{dhyper}(X,m,n,k) = \text{dhyper}(X_value, \text{of success}, \text{failures}, \text{Sample size})$

```
dhyper(2,4,26,10)
```

```
## [1] 0.3119869
```

B) What is the probability that none of the restaurants that are visited will have health code violations?

```
dhyper(0,4,26,10)
```

```
## [1] 0.1767926
```

12) A lot of parts contains 500 items, 100 of which are defective. Suppose that 20 are selected at random. Let X be the number of selected items that are defective. $m = 100$ $n = 400$ $k = 20$

a) express the quantity $P(X=5)$ using factorials. $P(X=5) = \frac{(m|x)(n|(k-x))}{(N|k)}$; $\frac{(100|5)(400|20-5)}{(500|20)}$ $(A|W) = \frac{A!}{(W!(A-W)!)}$

b) $\frac{100!400!20!480!}{5!95!15!385!*500!}$

c) Use the binomial approximations to compute an approximation to $P(X=5)$

```
dbinom(5,20,100/500)
```

```
## [1] 0.1745595
```

Pg 252: 1,4,8,9,12,15,22

4) If $X \sim N(2,9)$, compute

a) $P(X \geq 2)$

```
pnorm(1,2,9)
```

```
## [1] 0.4557641
```

b) $P(1 \leq X < 7) = P(X \leq 6) - P(X \leq 1)$

```
pnorm(6,2,9)-pnorm(1,2,9)
```

```
## [1] 0.2158752
```

C) $P(-2.5 \leq X < -1)$

```
pnorm(-2,2,9)-pnorm(-2.5,2,9)
```

```
## [1] 0.0198231
```

d) $P(-3 \leq X < 3)$

8) weights of female cats of a certain breed are normally distributed with mean 4.1kg and a SD of 0.6kg

A) What proportion of female cats have weights between 3.7 and 4.4kg? $P(3.7 < X < 4.4)$

```
pnorm(4.4,4.1,0.6)-pnorm(3.7,4.1,0.6)
```

```
## [1] 0.4389699
```

b) $P(X > 4.1 + 0.6 * 0.5)$

```
pnorm(4.1+0.6*0.5,4.1,0.6)
```

```
## [1] 0.6914625
```

c) $Z = (x - \mu) / \sigma$

```
pnorm(0.8416215)
```

```
## [1] 0.8000001
```

$Z = 0.84163 = (x - 4.1) / 0.6$

```
0.8416215*0.6+4.1
```

```
## [1] 4.604973
```

answer for c is 4.6kg

d) a female cat is chosen at random. what is the probability that she weighs more than 4.5kg?

```
pnorm(4.5,4.1,0.6,lower.tail = FALSE)
```

```
## [1] 0.2524925
```

e) Six female cats are chosen at random, what is the probability that exactly one of them weighs more than 4.5kg? -not sure-

12) Specifications for an aircraft bolt require that the ultimate tensile strength be at least 18kN. It is known that 10% of the bolts have strengths less than 18.3 and that 5% of the bolts have strengths greater than 19.76kN. It is also that the strengths of these bolts are normally distributed.

a) Find the mean and standard deviation of the strengths.

b) Mean = 18.9 and Sd = 0.5

c) what proportion of the bolts meet the strength specification?

d) 0.97

22) Two resistors with resistances R1 and R2, are connected in series. R1 is normally distributed with mean 100ohm and sd of 5 ohm. R2 is normally distributed with mean 120ohm and sd 10ohm.

- a) what is the probability that $R2 > R1$? 0.475
- b) what is the probability that $R2$ exceeds $R1$ by more than 30ohm? 0.238

pg 270: 2,4,9,10

2)

A) $\lambda = 1/0.5$

```
1/0.5
```

```
## [1] 2
```

B)

```
0.5
```

```
## [1] 0.5
```

c) $sd = 1/\lambda^2$

```
1/2^2
```

```
## [1] 0.25
```

Pg 300 4)

a) 0.841 b) 0.606

6)

a) 0.238

b) 1.295

c) 1076

16)

a) 0

b) Yes

c) 0

d) 0.344

e) No

f) 0.344