

# COMP9020

## Term 3, 2019

### Course Review

# Course Review

Goal: for you to become a competent computer **scientist**.

Requires an understanding of fundamental concepts:

- Number Theory, Sets, Relations and Functions
- Recursion, Induction and Asymptotic Analysis
- Logic
- Graph Theory
- Combinatorics and Probability

In CS/CE these are used to:

- formalise problem specifications and requirements
- develop abstract solutions (algorithms)
- analyse and prove properties of your programs

# Assessment Summary

Quizzes: Best 10 out of 16 – (10 marks)

Assignments: 3 assignments worth 10 marks each – (30 marks)

Final exam – (60 marks)

## NB

*You must achieve 40% on the final exam AND 50% overall to pass the course.*

# Final Exam

Goal: to check whether you are a competent computer scientist.

Requires you to demonstrate:

- understanding of mathematical concepts
- ability to apply these concepts and explain how they work

Lectures, quizzes and assignments have built you up to this point.

# Final Exam

**Tuesday, 3 December, 8:45am**

Kensington Room, Randwick Racecourse

- 10 short-answer questions plus 5 long-answer questions
- Covers **all** of the contents of this course.
- Each short-answer question is worth 3 marks ( $10 \times 3 = 30$ )  
Each long-answer question is worth 18 marks ( $5 \times 18 = 90$ )  
Total exam marks = 120 (i.e. 1 mark/minute)
- Time allowed – 120 minutes + 10 minutes reading time
- *Closed book*. One handwritten or typed A4-sized sheet (double-sided is ok) of your own notes
- Three answer booklets – one for rough work and two for answers. Clearly label each booklet.

## Exam questions

Short answer questions (3 marks each)

- No justification necessary, but partial marks can be awarded for incorrect answers that demonstrate a level of understanding.
- No negative marking
- Don't have to answer each on its own page

Long answer questions (18 marks each)

- **Start each question on a new page**
- **List the questions attempted on the front of the booklet** in the order they were attempted
- Unless specified, *any* valid proof technique is acceptable

### NB

*Questions are culturally neutral – no concepts other than those taught in this course are assumed.*

# Revision Strategy

- Re-read lecture slides
- Read the corresponding chapters in the book (R & W)
- **Review/solve assignments and quizzes**
- Review/solve problem sets
- Solve more problems from the book
- Practice multiple choice questions

(Applying mathematical concepts to solve problems is a skill that improves with practice)

Additional consultation times:

- Tuesday November 26 (online) 9PM
- Wednesday November 27 (Rm 204, K17) 2-3PM

## Supplementary Exam

You can apply formally for special consideration

- a supplementary examination may or may not be granted
- a supplementary examination is typically more difficult than the original examination

If you attend an exam

- you are making a statement that you are “fit and healthy enough”
- it is your only chance to pass (i.e. no second chances)

If your overall result is  $\geq 47$  you can sit the supplementary exam, in which you must score 50 or higher to pass



# Assessment

Assessment is about determining how well you understand the syllabus of this course.

If you can't demonstrate your understanding, you don't pass.

In particular, I can't pass people just because ...

- please, please, ... my family/friends will be ashamed of me
- please, please, ... I tried really hard in this course
- please, please, ... I'll be excluded if I fail COMP9020
- please, please, ... this is my final course to graduate
- etc. etc. etc.

(Failure is a fact of life. For example, my scientific papers or project proposals get rejected sometimes too)

## Assessment (cont'd)

Of course, assessment isn't a "one-way street" ...

- I get to assess you in the final exam
- you get to assess me in UNSW's MyExperience Evaluation
  - go to <https://myexperience.unsw.edu.au/>
  - login using zID@ad.unsw.edu.au and your zPass

**Please fill it out ...**

- give me some feedback on how you might like the course to run in the future
- even if that is "Exactly the same. It was perfect this time."

# Content review

# Week 1: Proof techniques and Number Theory

- Proof strategies
- Number theory
  - Floor  $\lfloor \cdot \rfloor$  and ceiling  $\lceil \cdot \rceil$  functions
  - Interval  $[m, n]$ ,  $(m, n)$ , etc
  - Absolute value  $|\cdot|$  function
  - Divides relation  $m|n$
  - Greatest common divisor, least common multiple
  - div, %, mod

# Week 1: Need to know

- How to present proofs
- Number theory definitions and notation. Especially:
  - Interval notation
  - Divides relation
  - gcd, lcm
  - $a = b \pmod{n}$

## Week 2: Sets, Relations and Functions

Sets, languages, relations and functions:

- Set notation:  $\emptyset, \subseteq, \{\dots\}, [\dots]$
- Set operations:  $\cap, \cup, ^c, \setminus, \oplus, \times$
- Set theory laws
- Symbols, words, languages
- Language definitions:  $\Sigma^*$ ,  $\text{length}()$ , concatenation
- Relational image ( $R(A)$ ), converse relation ( $R^{\leftarrow}$ ), inverse image ( $R^{\leftarrow}(B)$ ), relation composition ( $R; S$ )
- Domain, co-domain, image, function composition
- Surjective, injective and bijective functions

## Week 2: Need to know

- Set operations
- Proofs using laws of set operations
- Definitions of languages, relations and functions
- Relational/functional image, relational/functional composition

## Week 3: Relations and Functions

- Binary relations:
  - Equivalence relations, equivalence classes
  - Partial orders, Hasse diagram, lub, glb
  - Total orders, topological sorting, lexicographic, lenlex
- Functions:
  - Injective, surjective, bijective
  - Inverse function
  - Matrices



## Week 3: Need to know

- Binary relations:
  - Equivalence relations, equivalence classes
  - Partial orders, Hasse diagram, lub, glb
  - Total orders, topological sorting, lexicographic, lenlex
- Functions:
  - Injective, surjective, bijective
  - Inverse function
  - Basic Matrix operations:  $A + B$ ,  $A \cdot B$ ,  $A^T$

# Weeks 4 & 5: Big-O, Recursion and Algorithmic Analysis

- Recursive definitions
- Solving recurrence equations
  - Unwinding
  - Simplifying using big-O
  - The Master Theorem
- Algorithmic analysis: Big-O,  $\Omega$  and  $\Theta$ 
  - Worst-case analysis
  - Running time (number of elementary operations)
  - Using big-O to simplify analysis
  - Aim to compare with “simple” functions, e.g.  $O(n)$ ,  $O(n \log n)$ ,  $O(2^n)$ , etc

## Weeks 4& 5: Need to know

- Big-O vs Big- $\Omega$  vs Big- $\Theta$
- How to define things recursively
- (At least) One method for solving recurrences
- Algorithmic analysis

# Weeks 5 & 6: Induction

- Basic Induction
- Induction variations
- Structural Induction

## Weeks 5 & 6: Need to know

How to do proofs using:

- Basic induction, from  $m$ , steps  $\geq 1$ .
- Structural induction

# Week 6: Propositional Logic I

- Propositions and connectives
- Syntax: Well-formed formulas
- Semantics: Boolean algebra  $\mathbb{B}$
- Logical equivalence
- Entailment and validity

## Week 6: Need to know

- Formal definitions of Propositional logic
- Evaluating functions on well-formed formulas

## Week 7: Propositional Logic II

- Boolean functions
- CNF and DNF
  - Converting formulas to CNF/DNF
  - Canonical DNF/CNF
  - Karnaugh maps
- Boolean algebras
- Beyond Propositional Logic



## Week 7: Need to know

- Definitions: Boolean function, CNF, DNF
- One method of creating an equivalent CNF and DNF
- Boolean Algebras:
  - Definitions
  - Giving proofs

## Week 8: Graphs

- Definitions and notation: vertices, edges, paths, cycles, connectedness
- Isomorphisms, Automorphisms
- Important graphs: Trees, Complete graphs, complete  $k$ -partite graphs
- Graph traversals: Eulerian path/circuit, Hamiltonian path/cycle
- Graph properties: Chromatic number, Clique number, Planarity

## Week 8: Need to know

- Definitions and notation: vertices, edges, paths, cycles, connectedness
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## Weeks 8 & 9: Combinatorics

- Disjoint sets, inclusion-exclusion rule
- Cartesian products, counting sequences
- Permutations and Combinations
- Sequences with/without replacement and with/without ordering, Balls in boxes

## Weeks 8 & 9: Need to know

- Counting based on basic set operations (union, intersection, etc)
- Four different types of sequences, their notation, and how to count them (i.e. formulas)

## Weeks 9 & 10: Probability

- Sample space
- Probability distribution, uniform probability
- Combining Events
  - Events from the same set of outcomes
  - Events involving different sets of outcomes
- Independent events
- Recursively defined scenarios
- Conditional probability
- Expectation
- Variance

## Weeks 9 & 10: Need to know

- Definitions and notation
- Probability computations:
  - Basic: First principles, examining sample space
  - Complex: Combining events: union, sequencing, conditional, recursive
- Expectation computations