

---

## Table of Contents

.....	1
Annexe .....	1
Nombre de photons theorique detecte .....	1
Simulation numerique .....	3
Differences relatives .....	7

```
clear all;  
clc;  
close all;
```

## Annexe

```
Q = 10000; %Taux emission photon en photons/s  
hs = 40; %Hauteur source en cm  
he = 40; %Hauteur ecran en cm  
le = 40; %Largeur ecran en cm  
ld = 4; %Arete du detecteur  
hd = 4; %Hauteur du detecteur  
sigma = 0.5; %Section efficace ecran en cm^-1  
time = 5*60;
```

```
r_e = [0 -10 0;  
       0 0 0;  
       0 10 0];
```

## Nombre de photons theorique detecte

```
Q_l = Q/hs;  
Det_Area = ld*ld;  
l1 = -20;  
l2 = 20;  
  
% Experience 1  
x_d = 50;  
x = [sqrt(x_d^2 + 10^2); x_d; sqrt(x_d^2 + 10^2)];  
for i = 1:length(x)  
    theta1(i) = atan(l1/x(i));  
    theta2(i) = atan(l2/x(i));  
    I1_th(i) = (Q_l/(4*pi*x(i)))*(theta2(i) - theta1(i));  
    C1_th(i) = I1_th(i)*time*Det_Area;  
end  
C1_th = C1_th';  
  
% Experience 2  
x_d = 100;  
x = [sqrt(x_d^2 + 10^2); x_d; sqrt(x_d^2 + 10^2)];  
for i = 1:length(x)  
    theta1(i) = atan(l1/x(i));
```

---

```

        theta2(i) = atan(l2/x(i));
        I2_th(i) = (Q_l/(4*pi*x(i)))*(theta2(i) - theta1(i));
        C2_th(i) = I2_th(i)*time*Det_Area;
    end
    C2_th = C2_th';

    % Experience 3
    x_d = 50;
    x_e = 20;
    e = 2;
    x = [sqrt(x_d^2 + 10^2); x_d; sqrt(x_d^2 + 10^2)];
    theta1 = atan(l1./x);
    theta2 = atan(l2./x);
    y = x.*sigma*(e/x_d);

    for i = 1:3
        F = @(theta) exp(-y(i)*sec(theta));
        I3_th(i) = (Q_l/(4*pi*x(i)))*(quad(F,0,theta2(i)) -
            quad(F,0,theta1(i)));
        C3_th(i) = I3_th(i)*time*Det_Area;
    end
    C3_th = C3_th';

    % Experience 4
    x_d = 50;
    x_e = 40;
    e = 2;
    x = [sqrt(x_d^2 + 10^2); x_d; sqrt(x_d^2 + 10^2)];
    theta1 = atan(l1./x);
    theta2 = atan(l2./x);
    y = x.*sigma*(e/x_d);

    for i = 1:3
        F = @(theta) exp(-y(i)*sec(theta));
        I4_th(i) = (Q_l/(4*pi*x(i)))*(quad(F,0,theta2(i)) -
            quad(F,0,theta1(i)));
        C4_th(i) = I4_th(i)*time*Det_Area;
    end
    C4_th = C4_th';

    % Experience 5
    x_d = 50;
    x_e = 40;
    e = 4;
    x = [sqrt(x_d^2 + 10^2); x_d; sqrt(x_d^2 + 10^2)];
    theta1 = atan(l1./x);
    theta2 = atan(l2./x);
    y = x.*sigma*(e/x_d);

    for i = 1:3
        F = @(theta) exp(-y(i)*sec(theta));
        I5_th(i) = (Q_l/(4*pi*x(i)))*(quad(F,0,theta2(i)) -
            quad(F,0,theta1(i)));

```

---

---

```

        C5_th(i) = I5_th(i)*time*Det_Area;
    end
    C5_th = C5_th';

    % Nombre de photons detectes
    Nph_th = [C1_th C2_th C3_th C4_th C5_th]; % Pour chaque source
    Nph_th_total = [sum(C1_th); sum(C2_th); sum(C3_th); sum(C4_th);
        sum(C5_th)]; % Nb photon total provenant des 3 sources pour chaque
        experience

    fprintf ('Nombre de photons detecte theoriquement par le detecteur:
    \n');
    fprintf ('                                %d\n', round(Nph_th_total));
    fprintf ('\n \n');

    Nombre de photons detecte theoriquement par le detecteur:
                                4254
                                1124
                                1507
                                1507
                                534

```

## Simulation numerique

```

N = 10;
NbPhotonsIni = Q*time;

for rko = 1:N
    % Experience 1
    x_d = 50;
    NbPhotons_Exp1 = 0;

    for i = 1:size(r_e,2)
        for j = 1:NbPhotonsIni
            photon = r_e(i,:) + [0, 0, (hs*(rand() - 0.5))]; %
            Generation du photon
            phi = 2*pi*rand();
            mu = (2*rand()) - 1;

            omega_S = [cos(phi)*sqrt(1-mu^2), sin(phi)*sqrt(1-mu^2),
            mu];

            photonDir = omega_S; % Direction du photon
            t = (x_d - photon(1))/photonDir(1);
            photonProp = photon + t*photonDir; % Propagation photon
            if ((t > 0) && (photonProp(2)<=(ld/2)) &&
            (photonProp(2)>=(-ld/2)) && (photonProp(3)<=(hd/2)) &&
            (photonProp(3)>=(-hd/2)))
                NbPhotons_Exp1 = NbPhotons_Exp1 + 1;
            end
        end
    end
end

```

---

```

% Experience 2
x_d = 100;
NbPhotons_Exp2 = 0;

for i = 1:size(r_e,2)
    for j = 1:NbPhotonsIni
        photon = r_e(i,:) + [0, 0, (hs*(rand() - 0.5))]; %
Generation du photon
        phi = 2*pi*rand();
        mu = (2*rand()) - 1;

        omega_S = [cos(phi)*sqrt(1-mu^2), sin(phi)*sqrt(1-mu^2),
mu];

        photonDir = omega_S; % Direction du photon
        t = (x_d - photon(1))/photonDir(1);
        photonProp = photon + t*photonDir; % Propagation photon
        if ((t > 0) && (photonProp(2)<=(ld/2)) &&
(photonProp(2)>=(-ld/2)) && (photonProp(3)<=(hd/2)) &&
(photonProp(3)>=(-hd/2)))
            NbPhotons_Exp2 = NbPhotons_Exp2 + 1;
        end
    end
end

% Experience 3
x_d = 50;
e = 2;
x_e = 20;
NbPhotons_Exp3 = 0;

for i = 1:size(r_e,2)
    for j = 1:NbPhotonsIni
        photon = r_e(i,:) + [0, 0, (hs*(rand() - 0.5))]; %
Generation du photon
        phi = 2*pi*rand();
        mu = (2*rand()) - 1;
        omega_S = [cos(phi)*sqrt(1-mu^2), sin(phi)*sqrt(1-mu^2),
mu];

        photonDir = omega_S; % Direction du photon
        t = (x_d - photon(1))/photonDir(1);
        photonProp = photon + t*photonDir; % Propagation photon
        if ((t > 0) && (photonProp(2)<=(ld/2)) &&
(photonProp(2)>=(-ld/2)) && (photonProp(3)<=(hd/2)) &&
(photonProp(3)>=(-hd/2)))
            t_entre = (x_e - photon(1))/photonDir(1);
            photon_entreEcran = photon + t_entre*photonDir;
            t_ecran = (x_e + e - photon(1))/photonDir(1);
            photon_exitEcran = photon + t_ecran*photonDir;
            l_ecran = sqrt((photon_exitEcran(1)
- photon_entreEcran(1))^2 + (photon_exitEcran(2)
- photon_entreEcran(2))^2 + (photon_exitEcran(3) -
photon_entreEcran(3))^2);

```

---

---

```

        if (rand() < exp(-0.5*l_ecran))
            NbPhotons_Exp3 = NbPhotons_Exp3 + 1;
        end
    end
end

% Experience 4
x_d = 50;
e = 2;
x_e = 40;
NbPhotons_Exp4 = 0;

for i = 1:size(r_e,2)
    for j = 1:NbPhotonsIni
        photon = r_e(i,:) + [0, 0, (hs*(rand() - 0.5))]; %
Generation du photon
        phi = 2*pi*rand();
        mu = (2*rand()) - 1;
        omega_S = [cos(phi)*sqrt(1-mu^2), sin(phi)*sqrt(1-mu^2),
mu];

        photonDir = omega_S; % Direction du photon
        t = (x_d - photon(1))/photonDir(1);
        photonProp = photon + t*photonDir; % Propagation photon
        if ((t > 0) && (photonProp(2)<=(ld/2)) &&
(photonProp(2)>=(-ld/2)) && (photonProp(3)<=(hd/2)) &&
(photonProp(3)>=(-hd/2)))
            t_entre = (x_e - photon(1))/photonDir(1);
            photon_entreEcran = photon + t_entre*photonDir;
            t_ecran = (x_e + e - photon(1))/photonDir(1);
            photon_exitEcran = photon + t_ecran*photonDir;
            l_ecran = sqrt((photon_exitEcran(1)
- photon_entreEcran(1))^2 + (photon_exitEcran(2)
- photon_entreEcran(2))^2 + (photon_exitEcran(3) -
photon_entreEcran(3))^2);

            if (rand() < exp(-0.5*l_ecran))
                NbPhotons_Exp4 = NbPhotons_Exp4 + 1;
            end
        end
    end
end

% Experience 5
x_d = 50;
e = 4;
x_e = 40;
NbPhotons_Exp5 = 0;

for i = 1:size(r_e,2)
    for j = 1:NbPhotonsIni
        photon = r_e(i,:) + [0, 0, (hs*(rand() - 0.5))]; %
Generation du photon
        phi = 2*pi*rand();

```

---

---

```

        mu = (2*rand()) - 1;
        omega_S = [cos(phi)*sqrt(1-mu^2), sin(phi)*sqrt(1-mu^2),
mu];

        photonDir = omega_S; % Direction du photon
        t = (x_d - photon(1))/photonDir(1);
        photonProp = photon + t*photonDir; % Propagation photon
        if ((t > 0) && (photonProp(2)<=(ld/2)) &&
(photonProp(2)>=(-ld/2)) && (photonProp(3)<=(hd/2)) &&
(photonProp(3)>=(-hd/2)))
            t_entre = (x_e - photon(1))/photonDir(1);
            photon_entreEcran = photon + t_entre*photonDir;
            t_ecran = (x_e + e - photon(1))/photonDir(1);
            photon_exitEcran = photon + t_ecran*photonDir;
            l_ecran = sqrt((photon_exitEcran(1)
- photon_entreEcran(1))^2 + (photon_exitEcran(2)
- photon_entreEcran(2))^2 + (photon_exitEcran(3) -
photon_entreEcran(3))^2);

            if (rand() < exp(-0.5*l_ecran))
                NbPhotons_Exp5 = NbPhotons_Exp5 + 1;
            end
        end
    end
end

Nph_Exp1(rko) = NbPhotons_Exp1;
Nph_Exp2(rko) = NbPhotons_Exp2;
Nph_Exp3(rko) = NbPhotons_Exp3;
Nph_Exp4(rko) = NbPhotons_Exp4;
Nph_Exp5(rko) = NbPhotons_Exp5;
end

% Nombre de photons obtenus numeriquement pour chaque experience pour
10 iterations
Nph_numeric = [Nph_Exp1; Nph_Exp2; Nph_Exp3; Nph_Exp4; Nph_Exp5];

% Nombre de photons moyenne obtenu numeriquement pour chaque
experience
Nph = [sum(Nph_Exp1); sum(Nph_Exp2); sum(Nph_Exp3); sum(Nph_Exp4);
sum(Nph_Exp5)]./N;

% Ecart-type provenant de la simulation numerique
for wwe = 1:length(Nph)
    Std(wwe) = (100/Nph(wwe))*sqrt((1/N)*sum((Nph_numeric(wwe,:) -
Nph(wwe)).^2));
end

% Ecart-type theorique
for jjj = 1:length(Nph_th_total)
    Std_t(jjj) = 100/(sqrt(N*Nph_th_total(jjj)));
end

```

---

---

```

fprintf ('Nombre de photons moyen detecte numeriquement par le
detecteur:\n');
fprintf ('                                %d\n', round(Nph));
fprintf ('\n \n');
fprintf ('Ecart-type provenant de la simulation numerique: \n');
fprintf ('                %.3f %% \n', Std);
fprintf ('\n \n');
fprintf ('Ecart-type theorique: \n');
fprintf ('                %.3f %% \n', Std_t);
fprintf ('\n \n');

```

*Nombre de photons moyen detecte numeriquement par le detecteur:*

```

4084
1100
1451
1466
515

```

*Ecart-type provenant de la simulation numerique:*

```

2.005 %
2.767 %
2.297 %
3.032 %
4.332 %

```

*Ecart-type theorique:*

```

0.485 %
0.943 %
0.815 %
0.815 %
1.368 %

```

*Differences relatives:*

```

-3.995 %
-2.076 %
-3.761 %
-2.766 %
-3.624 %

```

## Differences relatives

```

for jj = 1:length(Nph)
    D(jj) = 100*((Nph(jj) - Nph_th_total(jj))/Nph_th_total(jj));
end

fprintf ('Differences relatives: \n');
fprintf ('                %.3f %% \n', D);
fprintf ('\n \n');

```

---

*Published with MATLAB® R2018b*