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EVOLUTIONARY ANALOG AMPLIFIER OPTIMISATION

EVOLUČNÍ OPTIMALIZACE ANALOGOVÝCH ZESILOVAČŮ

BACHELOR'S THESIS

BAKALÁŘSKÁ PRÁCE

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Abstract

The standard way to design an amplifier is to calculate the values of its components by mathematical equations. The goal of this thesis is to use artificial intelligence and make the computer determine the values without the equations.

Abstrakt

Do tohoto odstavce bude zapsán výtah (abstrakt) práce v českém (slovenském) jazyce.

Keywords

artificial intelligence, evolutionary computation, evolution strategies, ngSPICE, analog amplifiers, fitness function

Klíčová slova

Sem budou zapsána jednotlivá klíčová slova v českém (slovenském) jazyce, oddělená čárkami.

Reference

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Evolutionary Analog Amplifier Optimisation

Declaration

Hereby I declare that this bachelor's thesis was prepared as an original author's work under the supervision of Ing. Michal Bidlo, Ph.D. All the relevant information sources, which were used during preparation of this thesis, are properly cited and included in the list of references.

> Marek Bielik April 12, 2017

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Chapter 1

Preface

The standard way to design an amplifier is to calculate the values of its components by mathematical equations. The goal of this thesis is to use artificial intelligence and make the computer determine the values without the equations.

Chapter 2

Evolutionary algorithms

'Owing to this struggle for life, variations, however slight and from whatever cause proceeding, if they be in any degree profitable to the individuals of a species, in their infinitely complex relations to other organic beings and to their physical conditions of life, will tend to the preservation of such individuals, and will generally be inherited by the offspring. The offspring, also, will thus have a better chance of surviving, for, of the many individuals of any species which are periodically born, but a small number can survive. I have called this principle, by which each slight variation, if useful, is preserved, by the term Natural Selection'. [1, p. 115]

In biological evolution, species are selected depending on their relative success in surviving and reproducing in the environment and mutations play a crucial role in this process as they are the key to the adaptation of the species. This concept has been used as a metaphor in computer science and it inspired the formation of a whole new area of artificial intelligence called Evolutionary Computation. This area mainly deals with an *optimization problem* which we discuss in the following section.

2.1 Optimization problem

Consider the function $f: A \to \mathbb{R}$ from a set A to the real numbers and we are looking for an element x_0 in A such that $f(x_0) \leq f(x)$ or $f(x_0) \geq f(x)$ for all x in A (we are looking for either the global minimum or maximum of the function f). The domain A of f is called the search space and the elements of A are called candidate solutions. The function f can be called variously (an objective function, a loss function), in this text we will call the function f a fitness function. A candidate solution that gives us the global maximum or minimum of the fitness function is called an optimal solution. The search space A is usually in the form of \mathbb{R}^n n-dimensional Euclidean space and the function f is also n-dimensional.

A simple approach to find the optimal solution would be to scour the whole search space and try every candidate solution. This approach will always give us the optimal solution, but the search space can be so vast, that we are not able to try every candidate solution in reasonable time.

A more sophisticated approach would be to use the technique presented in algorithm 1. The population $P \subseteq A$ would be a subset of the search space A and every individual of the population would represent one element of A. The individuals can be also called *chromosomes* in certain types of evolutionary algorithms. Every loop in the algorithm represents

one *generation* of individuals. This approach helps us to avoid those elements in the search space which wouldn't provide any good solution but the finding of the optimal solution is not guaranteed.

From the biological point of view, this algorithm can be seen as the driving force behind evolution and from the mathematical point of view it can be seen as a stochastic, derivative-free numerical method for finding global extrema of functions that are too hard or impossible to find analytically. Biology uses this approach to create well adapted beings and humans can use this method to find optimal solutions to problems that are difficult to solve analytically.

Algorithm 1 Evolutionary algorithm

- 1: Create a population P of randomly selected candidate solutions;
- 2: while terminating condition do
- 3: (Selection) Select the appropriate individuals (parents) for breeding from P;
- 4: (Mutation) Generate new individuals (offspring) from the parents;
- 5: (Reproduction) Replace some or all individuals in P with the new individuals;
- 6: end while

2.2 Evolution Strategies

Evolution strategies (ES) is a family of stochastic optimization algorithms which belongs to the general class of evolutionary algorithms. It was created by Rechenberg and Schwefel in the early 60s and attracted a lot of attention due to its strong capability to solve real-valued engineering problems. ES typically uses a real-valued representation of chromosomes and it relies primarily on selection and mutation to drive the evolutionary process. ES also often implements self-adaptation of the parameters used for mutating the parents in the population during the evolution, which means that these parameters coevolve with the individuals. This feature is natural in evolution strategies and other evolutionary algorithms have adopted it as well over the last years.

Algorithm 2 is a basic non-self-adaptive form of ES. Chromosomes in this algorithm are in the form of vectors of real numbers $x = (x_1, ..., x_n) \in \mathbb{R}^n$. Every vector represents one solution of the search space in our problem domain and the goal of the algorithm is to find such vector that produces global extremum of our fitness function.

The terminating condition of the algorithm can have various forms which can be combined together:

- Wait until the algorithm finds a chromosome with a fitness function value that meets our requirements.
- Limit the total number of generations.
- Track the best chromosome in every generation and stop the evolution if the fitness doesn't change anymore.

The last two approaches are suitable when the algorithm gets stuck in a local optimum and doesn't leave it after a significant amount of time.

This form of the algorithm is also implemented in this thesis with various extensions in order to produce better results. These extensions are described and discussed in the rest of this chapter.

Algorithm 2 Non-self-adaptive Evolution Strategies $(\mu + \lambda)$

```
1: Randomly create an initial population \{x^1,...,x^\mu\} of parent vectors, where each \vec{x}^i is of the form x^i=(x^i_1,...,x^i_n), i=1,...,\mu;
```

2: Evaluate the fitness function of each chromosome;

```
3: while terminating condition do
```

4: repeat

5: Randomly select a parent from $\{x^i : i = 1, ... \mu\}$;

6: Create a child vector by applying a mutation operator to the parent;

7: **until** λ children are generated

8: Rank the $\mu + \lambda$ chromosomes (children and parents) from the best to worst;

9: Select the best μ of these chromosomes to continue into the next generation;

10: end while

2.3 Selection

There are two main parameters in evolutionary strategies that are used to describe the type of the selection process:

- 1. Parameter μ specifies the number of chromosomes (parents) that are selected for reproduction
- 2. Parameter λ specifies the number of children that are produced in every generation.

There are also two types of selection:

```
1. (\mu + \lambda)-ES selection scheme
```

2.
$$(\mu, \lambda)$$
-ES selection scheme

In the first scheme, denoted by $(\mu+\lambda)$ -ES, both parents from the previous generation and newly produced children are mixed together and compete for survival in every generation where only the best μ chromosomes (parents for the next generation) are selected and get the chance to be reproduced. This scheme implements so called *elitizm*, because if there is a chromosome with a very good fitness function, it can survive for many generations and it can be replaced only if a better individual occurs. This approach has a higher natural tendency to get stuck in a local optima than the second scheme.

In the second type of selection, denoted (μ, λ) -ES, the parents are selected only from the set of children λ , so every chromosome lives only in one generation. Even a chromosome with a very good fitness function is discarted and replaced by a child with potencially worse fitness, so the convergence is not as strict as in the previous scheme, but it is easier to move away from a local optimum for this method.

Both schemes are implemented in this thesis with various values of μ and λ parameters ($\mu \ll \lambda$). Schemes such as (1 + 1)-ES and (1, λ)-ES are also possible ((1 + 1)-ES was mainly studied when evolution strategies was invented), but they show a slower convergency properties.

2.4 Mutation

Chromosomes in evolution strategies are represented as vectors of real values, formula 2.1.

$$\vec{x} = (x_1, ..., x_n) \tag{2.1}$$

These values correspond to the solution variables. Mutations can be performed in various ways, the simplest form is shown in formula 2.3 where m is a real number drawn from a normal (Gaussian) distribution with the mean in 0 and the stadard deviation σ is chosen by the user. The parameter σ represents the mutation step size and its value is crucial since it determines the effect of the mutation operator. The value should be kept relatively small to the problem domain in order not to perform large mutations too often. The parent chromosome is denoted by $\vec{x}(t)$ and $\vec{x}(t+1)$ denotes a child. It is also important to keep the values of the candidate solution $(x_1,...,x_n)$ in their domain interval and return it back every time the mutation shifts it out of the interval.

$$m = N(0, \sigma) \tag{2.2}$$

$$\vec{x}(t+1) = \vec{x}(t) + m$$
 (2.3)

This approach ignores two important facts:

- 1. When the search is close to the global optimum, it is appropriate to perform only subtle changes to the chromosomes so that the algorithm will not leave the good region.
- 2. Every dimension in the solution space can require different scaling, so that one dimension can require large mutation steps while another only small ones.

Both these facts became crucial to the ability of the algorithm to find an optimal solution during the implementation, so they are discussed and examined in the following sections.

2.4.1 Mutation with One Step Size

In this version of mutation, we change the the vector x, formula 2.4.

$$\vec{x} = ((x_1, ..., x_n), \sigma)$$
 (2.4)

 $(x_1,...,x_n)$ is the original vector and σ is a real-valued strategy parameter which controls the mutation process for every chromosome separately. The mutation process is described in formulas 2.6 and 2.7. The constant τ is set by the user and it is inversely proportional to the square root of the problem size. It represents the learning rate of the algorithm. The σ parameter is then mutated by multiplying with a variable with log-normal distribution, which ensures that σ is always positive. The reasons for this form of mutation of σ by a log-normal distribution are stated in [?]. The newly mutated σ is then used to mutate the solution values for the child where i=1,...,n are the n elements making up one chromosome. It is important to keep the right order of the mutation - to mutate the value of σ first and then mutate the vector's elements itself.

$$\tau \propto \frac{1}{\sqrt{n}} \tag{2.5}$$

$$\sigma(t+1) = \sigma(t) \cdot e^{\tau \cdot N(0,1)} \tag{2.6}$$

$$x_i(t+1) = x_i(t) + \sigma(t+1) \cdot N_i(0,1), \quad i = 1, ..., n$$
 (2.7)

This approach allows the mutation step size to coevolve with the chromosomes, since the fitness function indirectly evaluates the suitability of the mutation. It is important to vary the step size during the evolution run as we want the algorithm to prefer longer steps when it is far away from the optima and small steps when it is close to the optima.

2.4.2 Mutation with n step sizes

The fitness function surface can have different inclination in every dimension, so while one dimension requires large mutation steps another one might require only subtle ones. We can solve this problem by adding a strategy parameter σ to every element of the chromosome's solution vector, formula 2.8.

$$\vec{x} = ((x_1, ..., x_n), \sigma_1, ..., \sigma_n)$$
 (2.8)

The mutation process is then described in formulas 2.10 and 2.11.

$$\tau' \propto \frac{1}{\sqrt{2\sqrt{n}}} \tag{2.9}$$

$$\sigma_i(t+1) = \sigma_i(t) \cdot e^{\tau' \cdot N(0,1)' + \tau \cdot N_i(0,1)}$$
(2.10)

$$x_i(t+1) = x_i(t) + \sigma_i(t+1) \cdot N(0,1)_i, \quad i = 1, ..., n$$
 (2.11)

Equation 2.6 differs from 2.10. A simple modification of 2.6 which we could do is shown in formula 2.12. The reason why we add one more normally distributed variable in the actual algorithm (equation 2.10) is because we want keep the overall change of the mutability but we also want a finer granularity on the coordinate level.

$$\sigma_i(t+1) = \sigma_i(t) \cdot e^{\tau \cdot N_i(0,1)} \tag{2.12}$$

Chapter 3

Analog amplifiers

One of the goals of the thesis is to automate the design of analog amplifiers which are electronic circuits that are used to increase the input signal with the minimum amount of distortion to the output signal. There are two types of amplifiers used in this thesis which are discussed below.

3.1 Single stage common emitter amplifier

The single stage common emitter amplifier was chosen because it belongs to the most commonly used examples of analog amplifiers in class A. We can see the circuit diagram in figure 3.1.

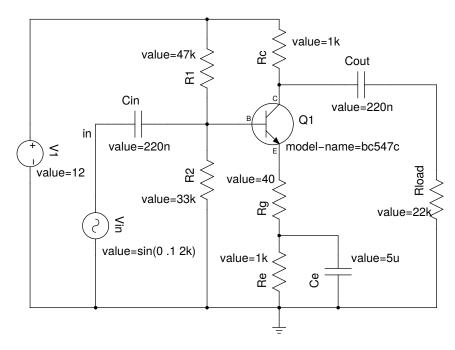


Figure 3.1: Circuit diagram for the common emitter amplifier

Resistors R1 and R2 are used to bias the transistor Q1 in order to set the quiescent point of the transistor to the middle of its DC load line, so that the collector of Q1 is put at 1/2 of the voltage V1. This allows the maximum symmetrical swings of the output

signal without clipping (flattening of the top or the bottom of the waveform). The collector voltage depends on the collector current (quiescent current), equation 3.1. This current depends on the applied base bias and the values of Rc and Re.

$$V_c = V1 - I_c \cdot Rc \tag{3.1}$$

Instead of using a voltage divider for biasing, it is possible to use only resistor R1, but this approach would make the quiescent point highly dependent on the current gain β of the transistor. This parameter varies considerably in every transistor and the manufacturer usually speciefies only a certain range of β . For this reason, we use a voltage divider constituted by R1 and R2 which impedance should be small compared with the impedance looking into the transistor base, formula 3.2. This will give us a divider which is stiff enough so that the quiescent point is insensitive to variations in transistor β . However, the current flowing in the divider should not be unnecessarily large as it affects the overall consumption of the amplifier.

$$R1||R2 \ll \beta Re \tag{3.2}$$

Capacitors *Cin* and *Cout* form high pass filters and they are used as coupling capacitors to separate the AC signals from the DC voltage used to set up the amplifier. Their values are chosen so that the capacitors have low impedance for the desired input and output signal frequencies. This ensures that the signal's average is zero, as the capacitors pass only AC signals and block any DC component.

The input voltage Vin causes a wiggle in the base voltage. The emitter voltage follows the base voltage which causes a wiggle in the emitter and also collector current. The output voltage which is the collector voltage depends on the current flowing through Rc, equation 3.1. When this current rises, the collector voltage drops and vice versa. That means that the amplifier also inverts the input signal, figure 3.3. The output AC signal is then superimposed on the collector DC voltage and the DC component is subsequently filtered out by the capacitor Cout (high pass filter).

Capacitor Ce is used to reach the amplifier's maximum gain. The values of Re and Rg set the emitter voltage which affects the amplifier's gain and we usually want these values to be as low as possible since this gives us the highest gain. However, if the emitter voltage is too low, it will vary significantly as the base-emitter drop varies with temperature. The solution is to bypass the Re resistor so that the impedance for the emitter will vary according to the signal's frequency. The bypass capacitor Ce is an open circuit component for DC bias and the emitter voltage depends on both Re and Rg which allows stable biasing. For higher frequency signals, the bypass capacitor short circuits Re and the emitter voltage now depends mostly on Re which value sets the maximum gain.

The analytical calculation for this circuit is beyond the scope of this thesis and it is left up to the evolutionary algorithms. The subject of the optimization are elements R1, R2, Rc, Rg, Rc, Cin, Ce. These elements represent the solution variables in the evolution and make up the vector \vec{x} which is thoroughly discussed in section 2.4.

3.2 Two stage amplifier

Two stage amplifier.

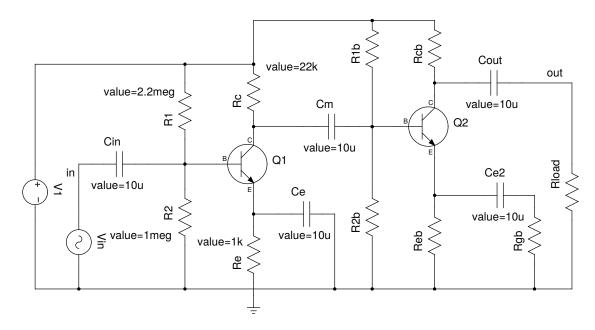


Figure 3.2: Circuit diagram for the two stage common emitter amplifier

3.3 ngSPICE

ngSPICE is an open-source circuit simulator based on SPICE (Simulation Program with Integrated Circuit Emphasis). It uses a language which syntax has been inherited from SPICE for describing circuits.

An example of such description of the circuit from section 3.1 is shown in listing 3.1. The first line contains the name of the circuit and on the next four lines, there is a description of the transistor used in the circuit. On the next lines, there is a list of the circuit's elements. The name of the element is on the first position followed by the numbers or names of the nodes which the element is connected to. The last position contains the properties of the element. The second last line contains the description of the simulation. In this case, we do a transient analysis of the circuit for 1.22 ms with the sampling period 20 µs. This netlist can be generated by using the gEDA (*Electronic Design Automation*) toolkit which is also an open-source project oriented towards electronic design.

```
1
     amplifier
2
    .model bc547c NPN (BF=730 NE=1.4 ISE=29.5F IKF=80M IS=60F
3
           + VAF=25 ikr=12m BR=10 NC=2 VAR=10 RB=280 RE=1 RC=40
4
           + VJE = .48 tr = .3u tf = .5n cje = 12p vje = .48 mje = .5
           + cjc = 6p \ vjc = .7 \ mjc = .33 \ isc = 47.6p \ kf = 2f
5
6
   Vin in 0 \sin(0.1.2k)
 7
   V1 \quad 4 \quad 0
   Ce 0 5 5u
8
9
   Cout 1 out 220n
   Cin in 3 220n
10
   Rc 1 4 1k
11
   Rload 0 out 22k
   Re 0 5 1k
14 Rg 5 2 40
```

```
15 R2 0 3 33k
```

- 16 R1 3 4 47k
- 17 Q1 1 3 2 bc547c
- 18 .TRAN 20u 1.22m
- 19 . end

Listing 3.1: description of an amplifier using the SPICE syntax

The last version of ngSPICE contains a C API which makes the simulator the ideal choice for utilizing it with the evolutionary algorithms. Every chromosome (candidate solution) in the evolution represents one amplifier and the simulator is used to determine the quality of it. In figure 3.3 we can see the simulation output of the circuit from listing 3.1 which is the same circuit as in section 3.1. This circuit was also built using real electronic components in order to verify the simulation results. The measurement results of the real circuit proved that the simulation works correctly for this circuit as the values corresponded to each other.

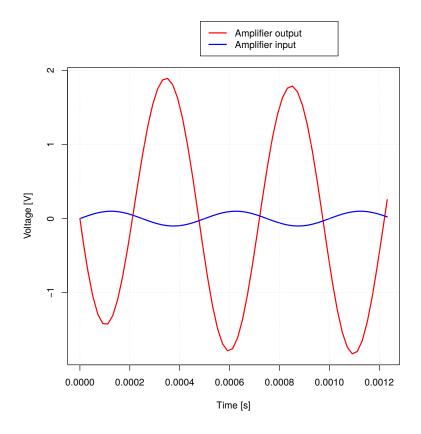


Figure 3.3: Simulation of the common emitter amplifier

The API is used to pass the description of the amplifier to the simulator, run the simulation and obtain the simulation results. The results are in the form of arrays in C which represent time and the corresponding voltage values. These arrays have equal length which depends on the simulation duration and the sampling period. The default input frequency for the amplifier is 2 kHz. The duration of the simulation is set to 1.22 ms and it contains approximately two and a half period of the output signal. The duration does not need to be longer because the shape of the waveform does not change afterwards. The

sampling period is 20 µs so that the waveform is smooth enough on one hand and the simulation does not take too long on the other hand. The array containing the output voltage is used for the evaluation of the chromosomes which is thouroughly discussed in section 4.1.

The simulator is launched several thousand times during a typical evolution and it takes most of the computation time. During the implementation of the algorithms discussed in section 2 and the integration of the simulator, it emerged that there are memory leaks on several places in the source code of the simulator. This was a problem as the simulator leaked memory in every iteration. A significant amount of time was spent on fixing these bugs and the result is that the memory leaks have been removed. These improvements were proposed to the development team and they are currently waiting for their approval, so that they can be incorporated into the new version of ngSPICE.

Chapter 4

Experiments

The evolutionary algorithms described in section 2 were implemented in C++. This language was chosen due to it's flexibility, performance and the possibility to make use of the ngSPICE simulator. The implementation also utilises the RInside library which integrates R into C++. The R language is used to plot graphs dynamically during the evolution either to the screen or to a file so the user can see and record how the solution evolves.

The program is written as a console application and the user can specify the properties of the evolution via command-line arguments. This approach also allows the user to easily run the application multiple times and collect the results of the evolution.

4.1 Chromosomes evaluation

A fitness function provides us means by which we can determine how good the evolved solution is, so that we can distinguish the more appropriate candidates from the less appropriate ones. It is important to mention that the quality of this function is essential, because the ability of the algorithm to find the most suitable solution is highly dependent on the ability of the fitness function to distinguish between the individuals. The value of the function is a positive real number in our case and the algorithm uses it only for comparing the individuals between each other. We consider those individuals with the lower value as the better ones.

The implementation required some methods of trial and error and in the end, there are three fitness functions implemented in this thesis. All of them use the ngSPICE simulator in order to obtain the output of the amplifier and assess it afterwards. The simulation is done for every candidate solution and it takes most of the computation time of the overall evolutionary algorithm.

4.1.1 Best match with the reference solution

This fitness function has been implemented as the first one in order to find out if the evolution has at least the ability to get close to the analytical solution. It is based on the method of least squares which is used in regression analysis.

The fitness function uses the output voltage vector from the simulator for assessing the chromosomes. The vector represents the waveform of the output signal from the circuit and the shape of the waveform gets similar to an inverted sine wave as the solution evolves. The length of the vector is set to 69 (the sampling period is approximately $20\,\mu s$) elements during the whole evolution and the vector contains approximately 2.5 periods of the signal

(the signal's frequency is 20 kHz). The fitness function uses two types of these vectors, one serves as the reference vector (the output of the amplifier which elements' values were calculated analytically) and all the candidate vectors are compared to it. As we can see in figure 3.3, the first period of the signal is unstable, so the fitness function skips it and picks only the second period for comparison with the reference signal. It is sufficient to compare only the second period because the shape of the signal doesn't change anymore after the circuit gets to a stable state.

The functions in algorithm 3 are used to extract the second period from the waveform. Since the vector has a constant length and the values represent an inverted sine wave, we can walk through the first two and the last half-period to get to the desired part of the signal. When the evolution starts, the waveform of some candidate solutions is not in the shape of an inverted sine wave and therefore it crosses zero sooner than the desired waveform. In this case, the algorithm ends with indexes close to the starting and ending index and such candidate solution is assessed with a high fitness value.

Algorithm 3 Find the first and last index of the second period

```
1: function GETSTART(vector)
2:
        start \leftarrow 0;
        while start < 0 do
3:
4:
           start \leftarrow start + 1:
        end while
5:
        while start > 0 do
6:
           start \leftarrow start + 1;
7:
        end while
8:
9:
        return start:
10: end function
    function GETEND(vector)
        end \leftarrow vector.length();
12:
        while end < 0 do
13:
           end \leftarrow end - 1;
14:
        end while
15:
        return end:
16:
17: end function
```

The function in algorithm 4 is used to evaluate the candidate solutions. It iterates over the second period in both reference and candidate vectors and it calculates the sum of squares which sides are defined by the difference between the values in the reference vector and the candidate vector. The overall sum is returned as the result of the fitness function and the lower the value, the better the candidate solution is. The reason why we add up squares and not only the absolute values of the differences is important. Consider two imaginary vectors of two values which differ from the reference vector by (1,5) and by (3,3). The sum of the absolute values is 6 in both cases, so this method doesn't distinguish between these vectors. However, the sum of the squares is 26 for the first vector and 18 for the second one. This difference is important as we want all the values to be close to the reference and not only some of them and therefore the second vector is assessed as a better one.

We can see the result of the evolution using this fitness function in figure 4.1.

Algorithm 4 Fitness evaluation using the analytical solution

```
1: function RATECHROMOSOME(candidateVector, referenceVector)
2:
       fitness \leftarrow 0;
       start \leftarrow \text{GETSTART}(candidateVector);
3:
4:
       end \leftarrow \text{GETEND}(candidateVector);
       for i \leftarrow start : end do
5:
           fitness \leftarrow fitness + (referenceVector[i] - candidateVector[i])^2;
6:
       end for
7:
       return fitness;
8:
9: end function
```

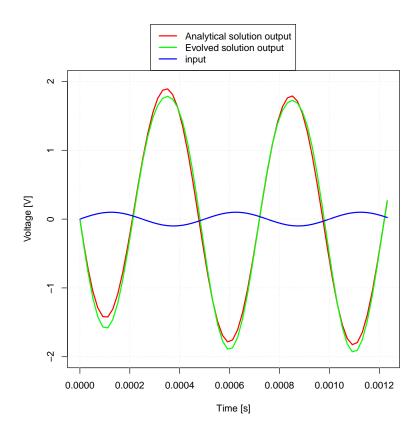


Figure 4.1: The result of evolution towards the analytical solution

4.1.2 Ideal sine wave

This method is similar to the previous one but instead of using pre-simulated output as a reference, it uses an analytically calculated sine wave. An analytical sine wave is used in order to force the evolution towards such solution that won't produce a distorted output signal since the input is in the form of a sine wave as well. The function also uses the method of least squares explained in the previous section and it iterates over the second period of the signal which is represented by the *candidateVector*.

We can see the technique in algorithm 5. In every iteration, it calculates the value of the sine wave and compares it with the simulated signal. The sum of the comparisons is then returned as the fitness value and the lower the result is, the closer the candidate solution is

to the reference. The amplitude of the sine wave is set by the user, so this method allows users to design amplifiers with an arbitrary amplification which doesn't exceed the circuit's capabilities.

Algorithm 5 Fitness evaluation using the ideal sine wave

```
1: function RATECHROMOSOME(candidateVector, amplitude)
2:
        fitness \leftarrow 0:
3:
        start \leftarrow GETSTART(candidateVector);
        end \leftarrow \text{GETEND}(candidateVector);
4:
        refSineSize \leftarrow end - start;
5:
        for i \leftarrow 0 : refSineSize do
6:
            refSine \leftarrow -amplitude \cdot \sin(\frac{2\pi i}{refSineSize-1});
7:
            fitness \leftarrow fitness + (refSine - candidateVector[start + i])^2;
8:
        end for
9:
        return fitness;
10:
11: end function
```

4.1.3 Maximal amplitude

This fitness function is designed to rate the candidate solutions only according to the amplitude of the output regardless of the waveform's shape. It can be used for finding the highest amplification capabilities of the circuit. The function finds the trough and the peak in the second amplitude and returns the multiplacive inverse of their difference.

Algorithm 6 Rating the chromosomes according to the amplitude

```
1: function RATECHROMOSOME(candidateVector)
2: start \leftarrow \text{GETSTART}(candidateVector);
3: end \leftarrow \text{GETEND}(candidateVector);
4: trough \leftarrow \min(candidateVector[start], candidateVector[end]);
5: peak \leftarrow \max(candidateVector[start], candidateVector[end]);
6: \mathbf{return} \ \frac{1}{peak - trough};
7: end function
```

4.1.4 Waveform symmetry

All of the fitness functions discussed above have difficulties in finding symmetrical waveforms. An example is shown in figure 4.2.

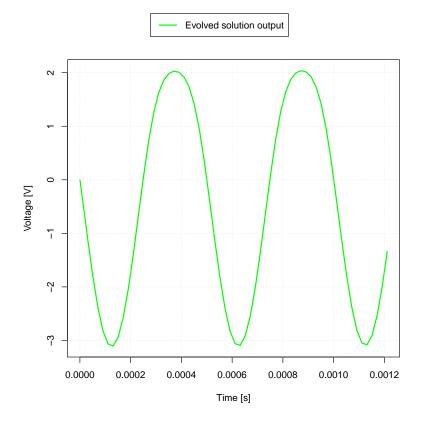


Figure 4.2: An asymmetrical result of the evolution using the 'ideal sine wave' evaluation

The problem is that at the start, the output signal has zero power and as the evolution continues, only one half of the signal rises and the fitness function value decreases even though the evolution doesn't go in the right direction. At the end, the evolution ends up in the state shown in figure 4.2. The first solution to this problem is described in formula 4.1.

$$result = (|peak + trough| + 1) \cdot fitness \tag{4.1}$$

The peak and trough values are obtained in the same way as in algorithm 6. If the signal is symmetrical, the absolute value of the sum of these values is close to zero and therefore the result will also be lower. We add 1 to the sum because we need to distinguish between perfectly symmetrical signals with different fitness. However, it emerged that this approach is too restrictive as it promotes only signals which are perfectly symmetrical, but often distorted. The result is shown in figure 4.3.

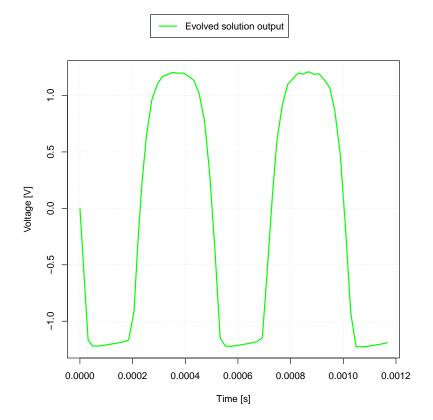


Figure 4.3: A distorted result using the 'ideal sine wave' evaluation

The ability of the evolution to find the desired solution was also decreased because some asymmetrical candidate solutions head towards a good solution. These consequences led to another solution to this problem.

```
Algorithm 7 Rating the chromosomes with regard to the symmetry of the signal
```

```
1: function RATECHROMOSOME(candidateVector, maxDifference)
2: min \leftarrow min(|trough|, peak);
3: max \leftarrow max(|trough|, peak);
4: if \frac{min}{max} < (1 - \frac{maxDifference}{100}) then
5: return DOUBLE\_MAX;
6: end if
7: \triangleright continue evaluating the chromosome
8: end function
```

Condition on line 4 in algorithm 7 is used to separate the symmetrical and asymmetrical chromosomes. The values of the variables trough and peak are obtained in the same way as in algorithm 6. The value of maxDifference is in the interval [0,100] and it is set by the user. It represents the maximal percentage difference between the peak and trough in the second period of the signal. The algorithm calculates the ratio between the peak and trough and if the result is less than the threshold value, the chromosome is evaluated with the maximal fitness and the function is terminated. Othervise the evaluation continues. This allows the user to control the results of the evolution with respect to the symmetry of the output signal.

4.2 Results

4.2.1 Initial stages

The first experiments were performed only in order to optimize the value of resistor R1 in the single stage amplifier. We used the 'best match' evaluation method and mutations with one step size. The evolution always found a value close to $50 \,\mathrm{k}\Omega$ which was the desired solution. These experiments were always successful as this was a very simple task for the evolution.

In the next stage, the task was to optimize the voltage divider constituted by R1 and R2. We again used the 'best match' method and mutations with one step size and it emerged, that the evolution was able to find the solution even faster than in the previous case. This was because we were looking only for the right ratio between the resistors and not for specific values so the set of the desired solutions was larger in this case.

The next task for the evolution was to find the right values for resistors R1, R2 and Rq. The evolution parameters were set in the same way as in the previous experiments. This task showed the weak spot of mutations with one step size as the evolution was able to find an acceptable solution very rarely. The reason was that the desired value of Rq is ver close to the lower bound of the search space (the analytical value is only $40\,\Omega$). Since mutations with one step size use the same mutation value in every dimension, it was not possible to mutate Rg only by a few ohms (not to move away from the lower bound of this dimension) and at the same time look for the right values in other dimensions which required steps in kiloohms. The value of Rg heavily influences the overall fitness of the chromosome because high values significantly decrease the gain of the amplifier. The usual course of the evolution was that the value of Rg converged quickly to the lower boundary and since this parameter has a great influence on the fitness, the evolution preferred chromosomes with this property. This led to a quick decrease of the mutation step size σ (the fitness function also indirectly evaluates the value of σ) and the algorithm got stuck in a local optimum since other dimensions (values of other resistors) in the search space could not be searched properly. The solution to this problem was to implement mutations with n step sizes discussed in section 2.4.2. This approach allows us to treat every dimension separately and therefore search the search space more effectively. After the implementation, the evolution was able to find a satisfactory solution in most of its runs.

The previous experiments proved that the evolutionary algorithms are able to provide acceptable solutions in the domain of analog amplifiers. The next section describes the process of determining the ideal parameters for the evolution.

4.2.2 Evolution paramters

In order to make the evolution strategies work efficiently, we need to find and set the correct parameters for the evolution.

The size of the search space is defined by the number of dimensions and by the size of every dimension. The number of dimensions depends on the number of electronic components that we want to optimize and the sizes of the dimensions depends on the range the of values that every component can have. These ranges were set to $0-200000~\Omega$ for resistors and 0-500000~nF for capacitors. The upper bounds are based on the values of real electronic components so for example we do not expect to have higher resistance than $200~k\Omega$ in the circuit. The values of some particular components could have a smaller range, for example resistor Rg which value does not need to be higher than a few kiloohms, but the assumption

is that we have no knowledge about the circuit at all.

The initial mutation step size σ is set to 100. This value is not very important because this parameter is adapted during the evolution. Experiments showed that there is no difference between setting the initial σ to 10 or 500 for example. However, if we set the initial value too high, it is more likely that the evolution will get stuck in a local optimum. The experiments also showed that the values of the learning parameters τ and τ' have a significant impact on the speed at which the evolution converges to the optimum. The higher the values were, the faster the evolution converged, nevertheless this also means that the probability of finding only a local optimum was rapidly increased. For this reason, the values were set according to formulas 4.2 and 4.3 to their lowest possible values.

$$\tau = \frac{1}{\sqrt{n}} \tag{4.2}$$

$$\tau' = \frac{1}{\sqrt{2\sqrt{n}}}\tag{4.3}$$

The maximum difference between the peak and trough of the amplifier's output waveform was empirically set to 25. This means that the values of the peak and trough of the waveform can differ at most by 25 %.

Chapter 5

Conclusion

Bibliography

[1] Knuth, D. E.: *The T_EXbook*. Addison-Wesley Publishing Company. 1996. ISBN 0-201-13447-0.

Appendices

Appendix A

Jak pracovat s touto šablonou

V této kapitole je uveden popis jednotlivých částí šablony, po kterém následuje stručný návod, jak s touto šablonou pracovat.

Jedná se o přechodnou verzi šablony. Nová verze bude zveřejněna do konce roku 2016 a bude navíc obsahovat nové pokyny ke správnému využití šablony, závazné pokyny k vypracování bakalářských a diplomových prací (rekapitulace pokynů, které jsou dostupné na webu) a nezávazná doporučení od vybraných vedoucích. Jediné soubory, které se v nové verzi změní, budou projekt-01-kapitoly-chapters.tex a projekt-30-prilohy-appendices.tex, jejichž obsah každý student vymaže a nahradí vlastním. Šablonu lze tedy bez problémů využít i v současné verzi.

Popis částí šablony

Po rozbalení šablony naleznete následující soubory a adresáře:

bib-styles Styly literatury (viz níže).

obrazky-figures Adresář pro Vaše obrázky. Nyní obsahuje placeholder.pdf (tzv. TODO obrázek, který lze použít jako pomůcku při tvorbě technické zprávy), který se s prací neodevzdává. Název adresáře je vhodné zkrátit, aby byl jen ve zvoleném jazyce.

template-fig Obrázky šablony (znak VUT).

fitthesis.cls Šablona (definice vzhledu).

Makefile Makefile pro překlad, počítání normostran, sbalení apod. (viz níže).

projekt-01-kapitoly-chapters.tex Soubor pro Váš text (obsah nahraďte).

projekt-20-literatura-bibliography.bib Seznam literatury (viz níže).

projekt-30-prilohy-appendices.tex Soubor pro přílohy (obsah nahraďte).

projekt.tex Hlavní soubor práce – definice formálních částí.

Výchozí styl literatury (czechiso) je od Ing. Martínka, přičemž anglická verze (englishiso) je jeho překladem s drobnými modifikacemi. Oproti normě jsou v něm určité odlišnosti, ale na FIT je dlouhodobě akceptován. Alternativně můžete využít styl od

Ing. Radima Loskota nebo od Ing. Radka Pyšného¹. Alternativní styly obsahují určitá vylepšení, ale zatím nebyly řádně otestovány větším množstvím uživatelů. Lze je považovat za beta verze pro zájemce, kteří svoji práci chtějí mít dokonalou do detailů a neváhají si nastudovat detaily správného formátování citací, aby si mohli ověřit, že je vysázený výsledek v pořádku.

Makefile kromě překladu do PDF nabízí i další funkce:

- přejmenování souborů (viz níže),
- počítání normostran,
- spuštění vlny pro doplnění nezlomitelných mezer,
- sbalení výsledku pro odeslání vedoucímu ke kontrole (zkontrolujte, zda sbalí všechny Vámi přidané soubory, a případně doplňte).

Nezapomeňte, že vlna neřeší všechny nezlomitelné mezery. Vždy je třeba manuální kontrola, zda na konci řádku nezůstalo něco nevhodného – viz Internetová jazyková příručka².

Pozor na číslování stránek! Pokud má obsah 2 strany a na 2. jsou jen "Přílohy" a "Seznam příloh" (ale žádná příloha tam není), z nějakého důvodu se posune číslování stránek o 1 (obsah "nesedí"). Stejný efekt má, když je na 2. či 3. stránce obsahu jen "Literatura" a je možné, že tohoto problému lze dosáhnout i jinak. Řešení je několik (od úpravy obsahu, přes nastavení počítadla až po sofistikovanější metody). Před odevzdáním proto vždy překontrolujte číslování stran!

Doporučený postup práce se šablonou

- 1. **Zkontrolujte, zda máte aktuální verzi šablony.** Máte-li šablonu z předchozího roku, na stránkách fakulty již může být novější verze šablony s aktualizovanými informacemi, opravenými chybami apod.
- 2. **Zvolte si jazyk**, ve kterém budete psát svoji technickou zprávu (česky, slovensky nebo anglicky) a svoji volbu konzultujte s vedoucím práce (nebyla-li dohodnuta předem). Pokud Vámi zvoleným jazykem technické zprávy není čeština, nastavte příslušný parametr šablony v souboru projekt.tex (např.: documentclass[english]{fitthesis} a přeložte prohlášení a poděkování do angličtiny či slovenštiny.
- 3. **Přejmenujte soubory.** Po rozbalení je v šabloně soubor projekt.tex. Pokud jej přeložíte, vznikne PDF s technickou zprávou pojmenované projekt.pdf. Když vedoucímu více studentů pošle projekt.pdf ke kontrole, musí je pracně přejmenovávat. Proto je vždy vhodné tento soubor přejmenovat tak, aby obsahoval Váš login a (případně zkrácené) téma práce. Vyhněte se však použití mezer, diakritiky a speciálních znaků. Vhodný název tedy může být např.: "xlogin00-Cisteni-a-extrakce-textu.tex". K přejmenování můžete využít i přiložený Makefile:

make rename NAME=xlogin00-Cisteni-a-extrakce-textu

¹BP Ing. Radka Pyšného http://www.fit.vutbr.cz/study/DP/BP.php?id=7848

²Internetová jazyková příručka http://prirucka.ujc.cas.cz/?id=880

- 4. Vyplňte požadované položky v souboru, který byl původně pojmenován projekt.tex, tedy typ, rok (odevzdání), název práce, svoje jméno, ústav (dle zadání), tituly a jméno vedoucího, abstrakt, klíčová slova a další formální náležitosti.
- 5. Nahraďte obsah souborů s kapitolami práce, literaturou a přílohami obsahem svojí technické zprávy. Jednotlivé přílohy či kapitoly práce může být výhodné uložit do samostatných souborů rozhodnete-li se pro toto řešení, je doporučeno zachovat konvenci pro názvy souborů, přičemž za číslem bude následovat název kapitoly.
- 6. Nepotřebujete-li přílohy, zakomentujte příslušnou část v projekt.tex a příslušný soubor vyprázdněte či smažte. Nesnažte se prosím vymyslet nějakou neúčelnou přílohu jen proto, aby daný soubor bylo čím naplnit. Vhodnou přílohou může být obsah přiloženého paměťového média.
- 7. Nascanované zadání uložte do souboru zadani.pdf a povolte jeho vložení do práce parametrem šablony v projekt.tex (documentclass[zadani]{fitthesis}).
- 8. Nechcete-li odkazy tisknout barevně (tedy červený obsah bez konzultace s vedoucím nedoporučuji), budete pro tisk vytvářet druhé PDF s tím, že nastavíte parametr šablony pro tisk: (documentclass[zadani,print]{fitthesis}). Barevné logo se nesmí tisknout černobíle!
- 9. Vzor desek, do kterých bude práce vyvázána, si vygenerujte v informačním systému fakulty u zadání. Pro disertační práci lze zapnout parametrem v šabloně (více naleznete v souboru fitthesis.cls).
- 10. Nezapomeňte, že zdrojové soubory i (obě verze) PDF musíte odevzdat na CD či jiném médiu přiloženém k technické zprávě.

Pokyny pro oboustranný tisk

- Zapíná se parametrem šablony: \documentclass[twoside] {fitthesis}
- Po vytištění oboustranného listu zkontrolujte, zda je při prosvícení sazební obrazec na obou stranách na stejné pozici. Méně kvalitní tiskárny s duplexní jednotkou mají často posun o 1–3 mm. Toto může být u některých tiskáren řešitelné tak, že vytisknete nejprve liché stránky, pak je dáte do stejného zásobníku a vytisknete sudé.
- Za titulním listem, obsahem, literaturou, úvodním listem příloh, seznamem příloh a případnými dalšími seznamy je třeba nechat volnou stránku, aby následující část začínala na liché stránce (\cleardoublepage).
- Konečný výsledek je nutné pečlivě překontrolovat.

Užitečné nástroje

Následující seznam není výčtem všech využitelných nástrojů. Máte-li vyzkoušený osvědčený nástroj, neváhejte jej využít. Pokud však nevíte, který nástroj si zvolit, můžete zvážit některý z následujících:

MikTeX LATEX pro Windows – distribuce s jednoduchou instalací a vynikající automatizací stahování balíčků.

- **TeXstudio** Přenositelné opensource GUI pro I₄TEX. Ctrl+klik umožňuje přepínat mezi zdrojovým textem a PDF. Má integrovanou kontrolu pravopisu, zvýraznění syntaxe apod. Pro jeho využití je nejprve potřeba nainstalovat MikTeX.
- JabRef Pěkný a jednoduchý program v Javě pro správu souborů s bibliografií (literaturou). Není potřeba se nic učit – poskytuje jednoduché okno a formulář pro editaci položek.
- **InkScape** Přenositelný opensource editor vektorové grafiky (SVG i PDF). Vynikající nástroj pro tvorbu obrázků do odborného textu. Jeho ovládnutí je obtížnější, ale výsledky stojí za to.
- GIT Vynikající pro týmovou spolupráci na projektech, ale může výrazně pomoci i jednomu autorovi. Umožňuje jednoduché verzování, zálohování a přenášení mezi více počítači.
- Overleaf Online nástroj pro IATEX. Přímo zobrazuje náhled a umožňuje jednoduchou spolupráci (vedoucí může průběžně sledovat psaní práce), vyhledávání ve zdrojovém textu kliknutím do PDF, kontrolu pravopisu apod. Zdarma jej však lze využít pouze s určitými omezeními (někomu stačí na disertaci, jiný na ně může narazit i při psaní bakalářské práce) a pro dlouhé texty je pomalejší.

Užitečné balíčky pro LATEX

Studenti při sazbě textu často řeší stejné problémy. Některé z nich lze vyřešit následujícími balíčky pro LATEX:

- amsmath rozšířené možnosti sazby rovnic,
- float, afterpage, placeins úprava umístění obrázků,
- fancyvrb, alltt úpravy vlastností prostředí Verbatim,
- makecell rozšíření možností tabulek,
- pdflscape, rotating natočení stránky o 90 stupňů (pro obrázek či tabulku),
- hyphenat úpravy dělení slov,
- picture, epic, eepic přímé kreslení obrázků.

Některé balíčky jsou využity přímo v šabloně (v dolní části souboru fitthesis.cls). Nahlédnutí do jejich dokumentace může být rovněž užitečné.

Sloupec tabulky zarovnaný vlevo s pevnou šířkou je v šabloně definovaný "L" (používá se jako "p").