## model.rmd

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### Modeller

#### Leser inn data

```
pm2 <- read_csv("data/pm2.csv", show_col_types = FALSE)</pre>
```

Vi er ute etter fylkesnummeret, for å lage en ny fylke faktorvariabel. (De to første siffrene i kommunenummeret). Vi bruker mutate() som funksjon for å hente ut deler av en tekststreng. Lager også en faktorvariabel fra årsvariabelen. Og skalerer variabelen Trade\_pc.

```
pm2 <- pm2 %>%
  mutate(
    fnr = (str sub(knr, 1,2))
  )
pm2 <- pm2 %>%
  mutate(
    fnr = parse_factor(fnr, levels = fnr),
    aar f = parse factor(as.character(aar))
  )
pm2 <- pm2 %>%mutate(Trade_pc_100K = trade_pc/100000)
head(pm2, n = 4)
## # A tibble: 4 x 19
##
     knr
           knavn
                          pm2 ya menn ya kvinner ya total inc k1 inc k5 uni k mf
                    aar
##
     <chr> <chr> <dbl> <dbl>
                                 <dbl>
                                            <dbl>
                                                      <dbl>
                                                             <dbl>
                                                                    <dbl>
                                                                             <dbl>
## 1 0101 Halden 2008 13427
                                  59.7
                                             56.8
                                                       58.3
                                                              24.5
                                                                     13.6
                                                                               17.8
## 2 0101 Halden 2009 13095
                                  59.8
                                             57.0
                                                       58.4
                                                              24.4
                                                                     14.1
                                                                              18.2
## 3 0101 Halden 2010 13832
                                  59.6
                                             57.1
                                                       58.3
                                                              23.9
                                                                     13.7
                                                                              18.6
## 4 0101 Halden 2011 14915
                                  59.8
                                             57.2
                                                       58.5
                                                              24
                                                                     14
                                                                               19
## # ... with 9 more variables: uni_k_m <dbl>, uni_k_f <dbl>, uni_l_mf <dbl>,
       uni l m <dbl>, uni l f <dbl>, trade pc <dbl>, fnr <fct>, aar f <fct>,
## #
       Trade pc 100K <dbl>
##Modell
```

```
mod1 <- 'pm2 ~ aar_f + ya_total + inc_k1 + inc_k5 + uni_k_mf + uni_l_mf + Trade_pc_100K'</pre>
```

#### i.Generer et lm objekt (lm1) utfra mod1 og datasettet pm2.

```
lm1 \leftarrow lm(mod1, data = pm2)
lm1 %>%
 summary()
##
## Call:
## lm(formula = mod1, data = pm2)
##
## Residuals:
##
      Min
                1Q
                   Median
                                3Q
                                       Max
## -9089.8 -1525.7
                      -0.9 1526.2 16322.2
##
## Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                 -23574.01
                              2293.29 -10.280 < 2e-16 ***
## aar f2009
                    235.79
                               237.53
                                        0.993 0.320967
## aar_f2010
                    856.73
                               236.16
                                       3.628 0.000291 ***
## aar_f2011
                   1573.77
                               233.50 6.740 1.94e-11 ***
## aar f2012
                               232.51
                                       9.234 < 2e-16 ***
                   2147.08
                               233.74 11.538 < 2e-16 ***
## aar f2013
                   2696.89
## aar f2014
                   2690.92
                               236.01 11.402 < 2e-16 ***
## aar_f2015
                   3273.99
                               236.74 13.830 < 2e-16 ***
## aar_f2016
                   3935.87
                               240.54
                                      16.363 < 2e-16 ***
## aar f2017
                   4750.67
                               241.87 19.641 < 2e-16 ***
## ya_total
                   640.19
                                33.87
                                      18.902 < 2e-16 ***
## inc k1
                                25.34 -15.030
                                              < 2e-16 ***
                   -380.90
## inc k5
                                19.24
                   198.36
                                      10.309 < 2e-16 ***
                                27.26
## uni k mf
                   -122.68
                                      -4.501 7.06e-06 ***
## uni l mf
                                40.27
                                       31.340 < 2e-16 ***
                  1262.10
## Trade_pc_100K
                 1184.06
                               205.44
                                        5.764 9.19e-09 ***
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 2611 on 2649 degrees of freedom
## Multiple R-squared: 0.8196, Adjusted R-squared: 0.8186
## F-statistic: 802.5 on 15 and 2649 DF, p-value: < 2.2e-16
```

#### ii. Legg residualene fra den lineære modellen til datasettet pm2.

```
pm2 <- pm2 %>%
  add_residuals(lm1)
```

#### Forklaring:

i.

Vi observerer at koeffisientene er signifikante på et 0.5%-nivå, og de fleste har solide t-verdier. Års-koeffisientene viser hvor mye prisene øker pr kvadratmeter fra år til år.

ii.

Fortegnene er som ventet. De illustrerer en økning fra år til år, som nevnt.

#### Test for heteroskedastisitet

i.

```
bptest(lm1)
```

```
##
## studentized Breusch-Pagan test
##
## data: lm1
## BP = 315.98, df = 15, p-value < 2.2e-16</pre>
```

ii.

Vi ser at p-verdien er under 0.5%. Dermed er det ikke grunnlag for heteroskedastisitet. Nullhypotesen forkastes ettersom p-verdien er under 0.5%.

```
library(gvlma)
gvlma(lm1)
```

```
##
## Call:
## lm(formula = mod1, data = pm2)
##
## Coefficients:
##
     (Intercept)
                       aar_f2009
                                       aar f2010
                                                       aar f2011
                                                                       aar_f2012
##
        -23574.0
                           235.8
                                           856.7
                                                          1573.8
                                                                          2147.1
       aar f2013
                       aar f2014
                                       aar f2015
                                                       aar f2016
                                                                       aar f2017
##
##
          2696.9
                          2690.9
                                          3274.0
                                                          3935.9
                                                                          4750.7
##
        ya_total
                          inc_k1
                                          inc_k5
                                                        uni_k_mf
                                                                        uni_l_mf
##
           640.2
                          -380.9
                                           198.4
                                                           -122.7
                                                                          1262.1
```

```
## Trade pc 100K
         1184.1
##
##
##
## ASSESSMENT OF THE LINEAR MODEL ASSUMPTIONS
## USING THE GLOBAL TEST ON 4 DEGREES-OF-FREEDOM:
## Level of Significance = 0.05
##
## Call:
##
   gvlma(x = lm1)
##
##
                      Value
                              p-value
                                                        Decision
## Global Stat
                     871.80 0.000e+00 Assumptions NOT satisfied!
                      65.91 4.441e-16 Assumptions NOT satisfied!
## Skewness
## Kurtosis
                     691.06 0.000e+00 Assumptions NOT satisfied!
                      84.17 0.000e+00 Assumptions NOT satisfied!
## Link Function
## Heteroscedasticity 30.66 3.077e-08 Assumptions NOT satisfied!
iii.
coeftest(lm1, vcov = vcovHC(lm1, type = "HC3"))
##
## t test of coefficients:
##
                   Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                -23574.015
                             2526.378 -9.3312 < 2.2e-16 ***
## aar f2009
                   235.786
                              203.381 1.1593 0.2464254
## aar f2010
                   856.728
                              194.239   4.4107   1.072e-05 ***
## aar f2011
                              198.548 7.9264 3.294e-15 ***
                   1573.772
## aar f2012
                  2147.080
                              212.046 10.1255 < 2.2e-16 ***
## aar f2013
                              207.517 12.9960 < 2.2e-16 ***
                  2696.888
## aar f2014
                              217.566 12.3683 < 2.2e-16 ***
                  2690.915
## aar f2015
                  3273.988
                              231.201 14.1608 < 2.2e-16 ***
## aar f2016
                  3935.865
                              249.553 15.7717 < 2.2e-16 ***
## aar f2017
                              265.244 17.9106 < 2.2e-16 ***
                  4750.672
## ya total
                   640.195
                              37.917 16.8841 < 2.2e-16 ***
## inc k1
                  -380.905
                               25.433 -14.9768 < 2.2e-16 ***
## inc k5
                               22.263 8.9099 < 2.2e-16 ***
                   198.359
                  -122.684
                               34.785 -3.5270 0.0004275 ***
## uni k mf
## uni l mf
                  1262.100
                               69.257 18.2233 < 2.2e-16 ***
                              218.171 5.4272 6.242e-08 ***
## Trade pc 100K
                 1184.061
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

```
iv.
```

```
pm2 <- pm2 %>%
  add_residuals(lm1)
```

 $\mathbf{v}.$ 

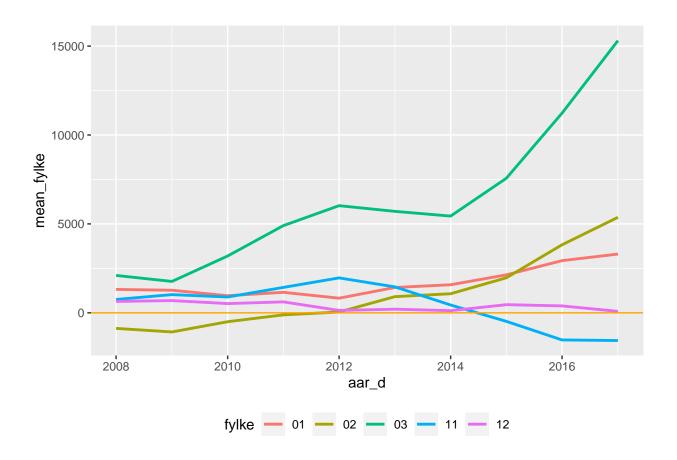
```
pm2 <- pm2 %>%
  mutate(aar_d =make_date(aar))
```

vi.

```
pm2 <- pm2 %>%
  mutate(fylke = substr(knr, start = 1, stop = 2))
```

```
vii + viii + ix + x
```

## 'summarise()' has grouped output by 'fylke'. You can override using the '.groups' arg



## Dummy fylke og år

#### i + ii.

## aar\_f2009

Her infører vi en dummy for hvert fylke hvert år. + Genererer lm2 fra modell 2 og datasettet pm2.

```
mod2 <- 'pm2 ~ aar_f*fnr + ya_total + inc_k1 + inc_k5 + uni_k_mf + uni_l_mf + Trade_pc_1</pre>
lm2 \leftarrow lm(mod2, data = pm2)
summary(1m2)
##
## Call:
## lm(formula = mod2, data = pm2)
##
## Residuals:
##
       Min
                 1Q
                     Median
                                  3Q
                       16.7
## -7923.8 -1315.5
                              1307.7 13524.6
##
## Coefficients:
##
                      Estimate Std. Error t value Pr(>|t|)
                    -21008.194
                                  2229.110 -9.424 < 2e-16 ***
## (Intercept)
```

0.150 0.880466

779.646

117.254

```
## aar f2010
                                             0.540 0.589252
                       427.365
                                   791.428
## aar f2011
                      1290.937
                                   791.696
                                             1.631 0.103103
## aar f2012
                                             1.862 0.062712 .
                      1475.509
                                   792.404
## aar_f2013
                                             3.176 0.001510 **
                      2518.738
                                   792.973
## aar f2014
                      2755.249
                                   782.555
                                             3.521 0.000438 ***
## aar f2015
                      3823.769
                                  782.737
                                             4.885 1.10e-06 ***
## aar f2016
                      5286.236
                                   795.176
                                             6.648 3.65e-11 ***
## aar f2017
                                             8.227 3.06e-16 ***
                      6448.890
                                   783.851
## fnr02
                     -1576.497
                                   745.081
                                            -2.116 0.034455 *
                                  2325.006
## fnr03
                                             1.229 0.219049
                      2858.301
## fnr04
                      -993.568
                                   822.150
                                            -1.208 0.226971
## fnr05
                     -1836.135
                                  792.893
                                            -2.316 0.020654 *
                                   770.483
                                            -2.681 0.007396 **
## fnr06
                     -2065.423
## fnr07
                      -647.551
                                  1148.302
                                            -0.564 0.572859
## fnr08
                     -3331.237
                                   878.035
                                            -3.794 0.000152 ***
                     -1665.045
                                   903.551
                                            -1.843 0.065481 .
## fnr09
## fnr10
                      -336.884
                                   879.838
                                            -0.383 0.701832
                                  772.929
## fnr11
                      -750.142
                                            -0.971 0.331883
## fnr12
                     -1106.505
                                   768.237
                                            -1.440 0.149905
                                  1019.569
## fnr14
                     -3038.500
                                            -2.980 0.002909 **
## fnr15
                     -3457.883
                                   758.964
                                            -4.556 5.47e-06 ***
## fnr16
                     -1190.346
                                   793.732
                                            -1.500 0.133825
                     -2715.149
                                            -3.161 0.001590 **
## fnr17
                                   858.902
## fnr18
                     -1485.901
                                   822.635
                                            -1.806 0.070998 .
## fnr19
                     -3255.562
                                  1253.077
                                            -2.598 0.009431 **
## fnr20
                     -2725.899
                                  1074.474
                                            -2.537 0.011243 *
## ya_total
                       527.285
                                    32.099
                                            16.427
                                                    < 2e-16 ***
                                                    < 2e-16 ***
## inc k1
                      -271.324
                                   23.167 -11.711
## inc k5
                       236.241
                                            11.745
                                                    < 2e-16 ***
                                    20.114
## uni_k_mf
                       131.552
                                    26.599
                                             4.946 8.09e-07 ***
                                                   < 2e-16 ***
## uni l mf
                       815.724
                                    40.991
                                            19.900
                      1376.572
## Trade pc 100K
                                   181.391
                                             7.589 4.54e-14 ***
## aar_f2009:fnr02
                       -71.931
                                  1031.037
                                            -0.070 0.944386
## aar_f2010:fnr02
                       774.604
                                  1039.933
                                             0.745 0.456427
## aar f2011:fnr02
                       976.443
                                             0.939 0.347869
                                  1039.975
## aar f2012:fnr02
                      1529.124
                                  1040.006
                                             1.470 0.141607
## aar f2013:fnr02
                      1893.317
                                  1040.167
                                             1.820 0.068849 .
## aar_f2014:fnr02
                      1996.251
                                  1031.509
                                             1.935 0.053071 .
## aar f2015:fnr02
                      2482.620
                                  1032.027
                                             2.406 0.016220 *
## aar f2016:fnr02
                      3546.831
                                  1040.857
                                             3.408 0.000666 ***
## aar_f2017:fnr02
                      4777.595
                                  1032.312
                                             4.628 3.88e-06 ***
## aar_f2009:fnr03
                        14.345
                                             0.004 0.996489
                                  3259.610
## aar f2010:fnr03
                      1913.904
                                  3262.569
                                             0.587 0.557509
                      3747.122
## aar f2011:fnr03
                                  3262.937
                                             1.148 0.250919
                                             1.677 0.093590 .
## aar f2012:fnr03
                      5474.015
                                  3263.386
```

```
## aar f2013:fnr03
                      4844.502
                                  3264.116
                                             1.484 0.137891
## aar f2014:fnr03
                      4686.445
                                  3261.996
                                             1.437 0.150936
## aar_f2015:fnr03
                      6763.321
                                  3264.005
                                             2.072 0.038360 *
## aar_f2016:fnr03
                                             3.004 0.002689 **
                      9816.586
                                  3267.606
## aar f2017:fnr03
                     13692.078
                                  3265.735
                                             4.193 2.85e-05 ***
## aar_f2009:fnr04
                      -444.565
                                  1130.748
                                            -0.393 0.694235
## aar f2010:fnr04
                      -136.985
                                  1138.855
                                            -0.120 0.904268
## aar f2011:fnr04
                      -814.258
                                  1138.925
                                            -0.715 0.474716
## aar f2012:fnr04
                      -883.900
                                  1138.982
                                            -0.776 0.437797
                                  1139.100
## aar f2013:fnr04
                     -1448.025
                                            -1.271 0.203777
## aar_f2014:fnr04
                     -1290.240
                                  1140.388
                                            -1.131 0.257995
## aar f2015:fnr04
                     -2018.714
                                  1108.852
                                            -1.821 0.068797 .
                                            -2.040 0.041416 *
## aar f2016:fnr04
                     -2342.956
                                  1148.279
## aar f2017:fnr04
                     -3652.695
                                  1122.818
                                            -3.253 0.001157 **
## aar_f2009:fnr05
                       308.104
                                  1102.501
                                             0.279 0.779916
## aar f2010:fnr05
                       570.141
                                             0.505 0.613395
                                  1128.329
## aar f2011:fnr05
                       397.338
                                  1103.369
                                             0.360 0.718793
## aar f2012:fnr05
                       682.055
                                  1096.902
                                             0.622 0.534130
## aar_f2013:fnr05
                      -515.624
                                  1103.659
                                            -0.467 0.640402
## aar f2014:fnr05
                                            -0.225 0.822069
                      -248.069
                                  1102.980
## aar f2015:fnr05
                     -1446.840
                                  1088.628
                                            -1.329 0.183955
## aar_f2016:fnr05
                     -2295.593
                                  1111.090
                                            -2.066 0.038926 *
## aar_f2017:fnr05
                     -2587.929
                                  1095.274
                                            -2.363 0.018214 *
## aar f2009:fnr06
                      -284.365
                                  1115.258
                                            -0.255 0.798762
## aar f2010:fnr06
                       199.040
                                  1095.054
                                             0.182 0.855784
## aar f2011:fnr06
                      -273.079
                                  1087.600
                                            -0.251 0.801770
## aar_f2012:fnr06
                       338.417
                                  1087.688
                                             0.311 0.755725
## aar f2013:fnr06
                       -30.035
                                  1095.053
                                            -0.027 0.978121
## aar f2014:fnr06
                       141.659
                                             0.130 0.896306
                                  1086.822
## aar_f2015:fnr06
                        50.755
                                  1095.323
                                             0.046 0.963044
## aar f2016:fnr06
                     -1265.800
                                  1095.330
                                            -1.156 0.247943
                                            -0.569 0.569332
## aar f2017:fnr06
                      -618.578
                                  1086.918
## aar f2009:fnr07
                       123.862
                                  1615.949
                                             0.077 0.938908
## aar_f2010:fnr07
                       742.421
                                  1621.634
                                             0.458 0.647120
## aar f2011:fnr07
                       290.257
                                             0.179 0.857969
                                  1621.737
## aar f2012:fnr07
                      1045.407
                                  1621.717
                                             0.645 0.519227
## aar f2013:fnr07
                       880.167
                                  1621.718
                                             0.543 0.587359
## aar_f2014:fnr07
                       620.068
                                  1616.312
                                             0.384 0.701285
## aar f2015:fnr07
                      1134.524
                                  1616.177
                                             0.702 0.482758
## aar f2016:fnr07
                       392.252
                                  1621.759
                                             0.242 0.808902
## aar_f2017:fnr07
                       970.177
                                  1563.951
                                             0.620 0.535093
## aar_f2009:fnr08
                                             0.373 0.709017
                       459.896
                                  1232.238
## aar f2010:fnr08
                      1394.612
                                  1239.740
                                             1.125 0.260731
## aar f2011:fnr08
                       653.046
                                  1239.741
                                             0.527 0.598408
## aar f2012:fnr08
                       613.058
                                  1224.304
                                             0.501 0.616599
```

```
## aar f2013:fnr08
                       435.360
                                 1224.295
                                             0.356 0.722170
## aar f2014:fnr08
                       723.664
                                 1232.312
                                             0.587 0.557096
## aar_f2015:fnr08
                                            -0.794 0.427096
                      -966.484
                                 1216.771
## aar_f2016:fnr08
                     -2335.970
                                 1211.230
                                            -1.929 0.053896
## aar f2017:fnr08
                     -2518.929
                                 1203.695
                                            -2.093 0.036481 *
## aar_f2009:fnr09
                       496.821
                                 1250.596
                                             0.397 0.691205
## aar f2010:fnr09
                       845.272
                                 1242.706
                                             0.680 0.496450
## aar f2011:fnr09
                       586.783
                                  1275.878
                                             0.460 0.645625
## aar f2012:fnr09
                      1078.728
                                 1275.855
                                             0.845 0.397917
## aar f2013:fnr09
                      -161.737
                                            -0.127 0.899151
                                  1276.067
## aar_f2014:fnr09
                      -572.407
                                 1269.304
                                            -0.451 0.652057
## aar f2015:fnr09
                      -775.032
                                  1268.702
                                            -0.611 0.541332
                     -1827.137
## aar f2016:fnr09
                                 1297.677
                                            -1.408 0.159255
## aar f2017:fnr09
                     -2917.203
                                  1290.742
                                            -2.260 0.023902 *
## aar_f2009:fnr10
                      -381.991
                                            -0.314 0.753591
                                 1216.757
## aar f2010:fnr10
                       430.096
                                  1224.244
                                             0.351 0.725382
## aar f2011:fnr10
                      -451.023
                                 1224.302
                                            -0.368 0.712612
## aar f2012:fnr10
                      -554.393
                                  1224.482
                                            -0.453 0.650764
## aar_f2013:fnr10
                      -793.190
                                 1240.041
                                            -0.640 0.522461
## aar f2014:fnr10
                      -848.570
                                 1233.045
                                            -0.688 0.491397
## aar f2015:fnr10
                     -1677.160
                                 1232.946
                                            -1.360 0.173864
## aar f2016:fnr10
                     -3029.946
                                 1258.763
                                            -2.407 0.016154 *
## aar_f2017:fnr10
                     -4488.173
                                            -3.687 0.000232 ***
                                  1217.432
## aar f2009:fnr11
                       356.831
                                 1059.170
                                             0.337 0.736223
## aar f2010:fnr11
                       542.002
                                  1074.015
                                             0.505 0.613850
## aar f2011:fnr11
                       952.291
                                  1062.307
                                             0.896 0.370107
                                  1057.622
## aar_f2012:fnr11
                      1895.127
                                             1.792 0.073275 .
## aar f2013:fnr11
                       891.229
                                 1057.851
                                             0.842 0.399595
## aar f2014:fnr11
                      -184.236
                                            -0.175 0.861363
                                  1054.843
## aar_f2015:fnr11
                     -1379.012
                                 1061.217
                                            -1.299 0.193907
## aar f2016:fnr11
                     -3293.368
                                  1064.259
                                            -3.095 0.001993 **
## aar f2017:fnr11
                     -3711.962
                                  1050.680
                                            -3.533 0.000419 ***
## aar f2009:fnr12
                       132.179
                                  1065.544
                                             0.124 0.901287
## aar_f2010:fnr12
                       250.201
                                  1062.208
                                             0.236 0.813803
## aar f2011:fnr12
                       183.677
                                  1062.212
                                             0.173 0.862729
## aar f2012:fnr12
                        33.874
                                 1052.540
                                             0.032 0.974329
## aar f2013:fnr12
                      -490.927
                                  1048.180
                                            -0.468 0.639568
## aar_f2014:fnr12
                      -603.292
                                 1044.182
                                            -0.578 0.563475
## aar f2015:fnr12
                      -725.510
                                 1044.000
                                            -0.695 0.487163
## aar f2016:fnr12
                     -1715.402
                                 1044.383
                                            -1.643 0.100613
## aar_f2017:fnr12
                     -2337.025
                                 1044.352
                                            -2.238 0.025325 *
## aar_f2009:fnr14
                      -426.236
                                 1525.949
                                            -0.279 0.780019
## aar f2010:fnr14
                      -644.540
                                 1434.484
                                            -0.449 0.653242
## aar f2011:fnr14
                       440.606
                                 1434.376
                                             0.307 0.758735
                                             0.337 0.735873
## aar f2012:fnr14
                       457.978
                                 1357.528
```

```
## aar f2013:fnr14
                      -384.308
                                 1378.066
                                            -0.279 0.780364
## aar f2014:fnr14
                      -936.722
                                 1371.465
                                            -0.683 0.494666
## aar_f2015:fnr14
                                            -1.165 0.244111
                     -1554.032
                                 1333.875
## aar_f2016:fnr14
                     -3120.327
                                 1403.357
                                            -2.223 0.026274 *
## aar f2017:fnr14
                     -2571.348
                                 1319.536
                                            -1.949 0.051447 .
## aar_f2009:fnr15
                       261.649
                                 1042.149
                                             0.251 0.801783
## aar f2010:fnr15
                       471.393
                                 1046.216
                                             0.451 0.652339
## aar f2011:fnr15
                                             0.274 0.784136
                       282.472
                                  1031.058
## aar f2012:fnr15
                       560.923
                                 1024.943
                                             0.547 0.584241
## aar f2013:fnr15
                                            -0.257 0.797212
                      -264.161
                                  1027.923
## aar_f2014:fnr15
                      -813.723
                                 1019.126
                                            -0.798 0.424685
## aar f2015:fnr15
                      -861.554
                                 1029.604
                                            -0.837 0.402796
                     -2262.057
## aar f2016:fnr15
                                 1027.905
                                            -2.201 0.027853 *
## aar f2017:fnr15
                     -2834.650
                                  1022.436
                                            -2.772 0.005605 **
## aar_f2009:fnr16
                      -246.995
                                            -0.221 0.825496
                                 1120.133
## aar f2010:fnr16
                      -166.038
                                  1119.104
                                            -0.148 0.882066
## aar f2011:fnr16
                      -340.432
                                 1103.490
                                            -0.309 0.757724
## aar f2012:fnr16
                       308.793
                                  1097.092
                                             0.281 0.778377
## aar_f2013:fnr16
                       -71.436
                                 1097.365
                                            -0.065 0.948102
## aar f2014:fnr16
                        -5.831
                                 1096.103
                                            -0.005 0.995756
## aar f2015:fnr16
                        96.743
                                 1095.855
                                             0.088 0.929661
## aar f2016:fnr16
                     -1427.167
                                 1091.278
                                            -1.308 0.191065
## aar_f2017:fnr16
                     -2135.764
                                  1089.054
                                            -1.961 0.049977 *
## aar f2009:fnr17
                       728.760
                                 1217.308
                                             0.599 0.549451
## aar f2010:fnr17
                        53.380
                                 1208.813
                                             0.044 0.964781
## aar f2011:fnr17
                       271.488
                                 1195.638
                                             0.227 0.820392
## aar_f2012:fnr17
                       558.253
                                             0.467 0.640669
                                  1195.861
## aar f2013:fnr17
                       163.080
                                 1184.640
                                             0.138 0.890519
                                            -0.018 0.985765
## aar f2014:fnr17
                       -21.005
                                  1177.212
## aar_f2015:fnr17
                      -966.679
                                 1166.258
                                            -0.829 0.407257
## aar f2016:fnr17
                     -1820.576
                                  1184.636
                                            -1.537 0.124465
## aar f2017:fnr17
                     -2008.188
                                 1188.256
                                            -1.690 0.091148 .
## aar f2009:fnr18
                      -264.823
                                  1140.066
                                            -0.232 0.816334
## aar_f2010:fnr18
                       240.262
                                 1138.884
                                             0.211 0.832934
## aar f2011:fnr18
                      -204.436
                                  1123.906
                                            -0.182 0.855678
## aar f2012:fnr18
                       539.456
                                 1124.472
                                             0.480 0.631453
## aar f2013:fnr18
                       128.551
                                  1123.848
                                             0.114 0.908942
## aar_f2014:fnr18
                      -555.694
                                 1109.804
                                            -0.501 0.616617
## aar f2015:fnr18
                      -948.114
                                 1076.882
                                            -0.880 0.378715
## aar f2016:fnr18
                     -1751.338
                                 1117.818
                                            -1.567 0.117302
## aar_f2017:fnr18
                     -2579.542
                                 1109.505
                                            -2.325 0.020155 *
## aar_f2009:fnr19
                      1114.445
                                             0.659 0.510186
                                 1692.031
## aar f2010:fnr19
                       136.839
                                 1769.674
                                             0.077 0.938372
## aar f2011:fnr19
                                  1647.754
                       153.142
                                             0.093 0.925959
## aar f2012:fnr19
                       807.952
                                 1611.002
                                             0.502 0.616049
```

```
## aar f2013:fnr19
                               1560.988 -0.397 0.691726
                    -619.025
## aar f2014:fnr19
                     827.923
                               1537.296 0.539 0.590240
## aar f2015:fnr19
                               1537.453 -0.529 0.596588
                    -813.901
## aar f2016:fnr19
                    -459.857
                               1543.410 -0.298 0.765767
## aar f2017:fnr19
                   -1726.045
                               1555.795 -1.109 0.267353
## aar f2009:fnr20
                   -1033.459
                               1564.091 -0.661 0.508840
## aar f2010:fnr20
                   -429.231
                               1569.873 -0.273 0.784555
## aar f2011:fnr20
                   -916.024
                               1570.019 -0.583 0.559645
## aar f2012:fnr20
                    -300.249
                               1648.151 -0.182 0.855462
## aar f2013:fnr20
                   -1072.631
                               1648.536 -0.651 0.515328
## aar_f2014:fnr20
                   -1324.069
                               1564.804 -0.846 0.397548
## aar f2015:fnr20
                   -2197.055
                               1564.890 -1.404 0.160454
## aar f2016:fnr20 -1780.031
                               1515.941 -1.174 0.240425
## aar f2017:fnr20 -3151.542
                               1564.756 -2.014 0.044109 *
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 2238 on 2469 degrees of freedom
## Multiple R-squared: 0.8765, Adjusted R-squared: 0.8667
## F-statistic: 89.86 on 195 and 2469 DF, p-value: < 2.2e-16
```

#### iii.

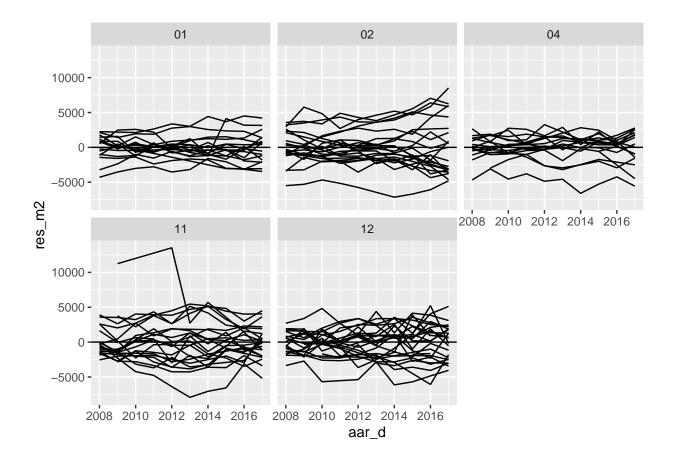
Legger residualene fra lm2 til pm2 og kaller dem res\_m2.

```
pm2 <- pm2 %>%
  mutate(res_m2 = resid(1m2))
```

#### iv.

Lager del-plott for hvert fylke.

```
pm2 %>% filter(fnr %in% c("01", "02", "04", "11", "12")) %>%
ggplot(mapping = aes(x = aar_d, y = res_m2)) +
geom_line(aes(group = knavn)) +
scale_size_manual(values = c(seq(2.0, 0.5, by = -0.1))) +
geom_hline(yintercept = 0) +
theme(legend.position = 'bottom') +
  facet_wrap(~fylke)
```



#### i.

Kvaliteten på modellen er ikke optimal, ettersom den har noen manglende variabler. Det er stor variasjon, noe som kan være forårsaket av heteroskedastisitet i modellen.

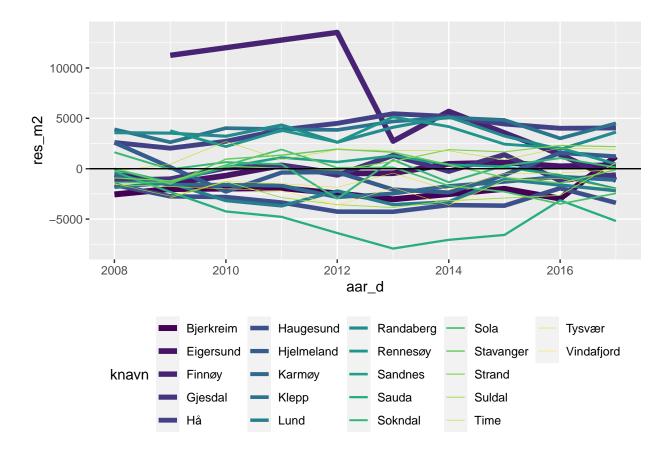
#### ii.

Ja, det er grunn til å mistenke at vi mangler viktige variabler i modell 2.

#### iii.

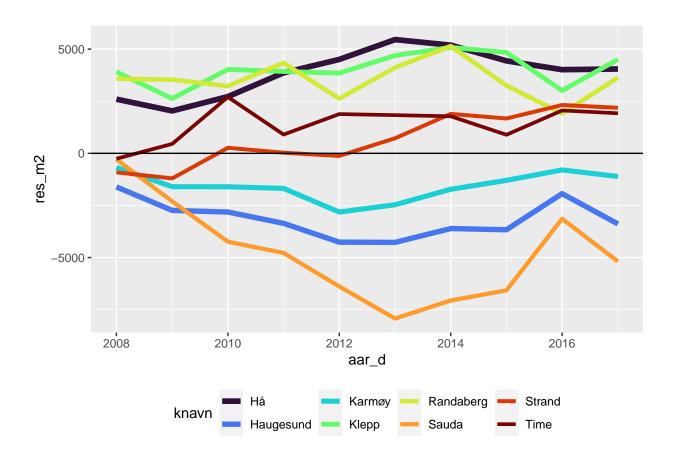
Filtrert med hensyn på fylke "11".

```
pm2 %>% filter(fnr %in% c("11")) %>%
ggplot(mapping = aes(x = aar_d, y = res_m2)) +
scale_color_viridis(discrete = TRUE, option = "D") +
geom_line(aes(group = knavn, colour = knavn, size = knavn)) +
scale_size_manual(values = c(seq(2.1, 0, by = -0.1))) +
geom_hline(yintercept = 0) +
theme(legend.position = 'bottom')
```



# i.Gjentar plottet ovenfor men med sortering for enkelte kommuner.

```
pm2 %>% filter(knr %in% c("1119", "1120", "1127", "1121", "1130", "1135", "1106", "1149"
ggplot(mapping = aes(x = aar_d, y = res_m2)) +
scale_color_viridis(discrete = TRUE, option = "H") +
geom_line(aes(group = knavn, colour = knavn, size = knavn)) +
scale_size_manual(values = c(seq(2.0, 0.5, by = -0.1))) +
geom_hline(yintercept = 0) +
theme(legend.position = 'bottom')
```



ii.

De kommunene som ligger nærme Stavanger overvuderes hva gjelder pris per kvadratmeter. Feil! Modelen undervurderer prisen derfor positiv residual.

## Modell for hvert år

i.

```
pm2 <- pm2 %>%
  mutate(
    aar_d = date(paste0(aar, "-01-01"))
)

pm2_n <- pm2 %>%
  select(pm2, fnr, knr, aar_d, aar, aar_f, ya_menn, ya_kvinner, ya_total, inc_k1, inc_k5
  group_by(aar_d) %>%
  nest()

pm2_n
```

## # A tibble: 10 x 2

```
## # Groups:
               aar d [10]
##
                 data
      aar d
##
      <date>
                 st>
## 1 2008-01-01 <tibble [241 x 13]>
## 2 2009-01-01 <tibble [243 x 13]>
## 3 2010-01-01 <tibble [250 x 13]>
## 4 2011-01-01 <tibble [265 x 13]>
## 5 2012-01-01 <tibble [276 x 13]>
## 6 2013-01-01 <tibble [275 x 13]>
## 7 2014-01-01 <tibble [273 x 13]>
## 8 2015-01-01 <tibble [285 x 13]>
## 9 2016-01-01 <tibble [276 x 13]>
## 10 2017-01-01 <tibble [281 x 13]>
pm2_n$data[[1]] %>%
head(n = 5)
## # A tibble: 5 x 13
                         aar aar_f ya_menn ya_kvinner ya_total inc_k1 inc_k5
##
       pm2 fnr
                 knr
     <dbl> <fct> <chr> <dbl> <fct>
                                                                  <dbl>
                                                                        <dbl>
##
                                      <dbl>
                                                 <dbl>
                                                           <dbl>
## 1 13427 01
                 0101
                        2008 2008
                                       59.7
                                                  56.8
                                                            58.3
                                                                   24.5
                                                                          13.6
## 2 18299 01
                 0104
                        2008 2008
                                       60.7
                                                  58.7
                                                            59.7
                                                                   22.8
                                                                          16.2
## 3 14981 01
                 0105
                        2008 2008
                                       60.9
                                                  58.1
                                                            59.5
                                                                   22.2
                                                                          13.6
                 0106
                        2008 2008
                                                  57.8
## 4 15671 01
                                       59.8
                                                            58.8
                                                                   21.8
                                                                          16.2
## 5 18844 01
                                       61.7
                                                  61.3
                 0111
                        2008 2008
                                                            61.5
                                                                   17.8
                                                                          19
## # ... with 3 more variables: uni k mf <dbl>, uni l mf <dbl>,
       Trade pc 100K <dbl>
i.
Funksjonen kom_model for å kjøre hvert enkelt år:
kom model <- function(a df) {</pre>
  lm(pm2 ~ fnr + ya_total + inc_k1 + inc_k5 + uni_k_mf + uni_l_mf + Trade_pc_100K, data
}
i.
pm2_n <- pm2_n %>%
  mutate(
    model = map(data, .f = kom model)
    )
# summary 2008
pm2_n$model[[1]] %>%
  summary()
```

```
##
## Call:
## lm(formula = pm2 ~ fnr + ya_total + inc_k1 + inc_k5 + uni_k_mf +
       uni_l_mf + Trade_pc_100K, data = a_df)
##
## Residuals:
##
       Min
                1Q
                   Median
                                3Q
                                       Max
## -4654.7 -1159.6
                     108.5
                            1074.2
                                    4907.5
##
## Coefficients:
##
                  Estimate Std. Error t value Pr(>|t|)
                                       -3.397 0.000812 ***
## (Intercept)
                 -19995.26
                              5886.89
## fnr02
                     94.71
                               661.30
                                       0.143 0.886251
## fnr03
                   4409.33
                              2011.32
                                       2.192 0.029429 *
## fnr04
                  -1846.50
                               670.37
                                       -2.754 0.006380 **
## fnr05
                  -2384.11
                               638.14
                                       -3.736 0.000239 ***
## fnr06
                  -1791.29
                               619.59
                                       -2.891 0.004231 **
## fnr07
                   -452.89
                               921.19
                                       -0.492 0.623476
## fnr08
                  -3705.14
                               705.30
                                       -5.253 3.57e-07 ***
## fnr09
                  -1867.00
                               726.18
                                       -2.571 0.010812 *
## fnr10
                   -422.80
                               723.49
                                       -0.584 0.559570
## fnr11
                    201.24
                               697.48
                                       0.289 0.773227
## fnr12
                   -562.95
                               668.02
                                       -0.843 0.400325
## fnr14
                  -2970.92
                               849.89
                                       -3.496 0.000574 ***
## fnr15
                  -3270.48
                               665.51
                                       -4.914 1.76e-06 ***
## fnr16
                  -1398.42
                               646.10
                                       -2.164 0.031531 *
## fnr17
                                       -4.570 8.21e-06 ***
                  -3260.93
                               713.61
## fnr18
                               681.74
                                       -2.988 0.003137 **
                  -2036.75
                                       -3.508 0.000549 ***
## fnr19
                  -3524.96
                              1004.86
## fnr20
                  -3077.48
                               873.75
                                       -3.522 0.000522 ***
## ya_total
                                85.56
                                        5.459 1.31e-07 ***
                    467.07
## inc k1
                   -116.06
                                65.47
                                       -1.773 0.077714 .
                                       3.614 0.000375 ***
## inc k5
                    191.86
                                53.09
## uni k mf
                    191.90
                                74.65
                                        2.571 0.010822 *
                                        4.774 3.32e-06 ***
## uni l mf
                    606.16
                               126.96
                                        2.610 0.009699 **
## Trade pc 100K
                   1338.87
                               513.05
## ---
                   0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Signif. codes:
##
## Residual standard error: 1768 on 216 degrees of freedom
## Multiple R-squared: 0.8652, Adjusted R-squared: 0.8502
## F-statistic: 57.76 on 24 and 216 DF, p-value: < 2.2e-16
```

#### i.

```
Funksjonen glance + mod_summary og unnest ()
```

```
pm2 n %>%
  filter(aar d == "2008-01-01") %>%
  .$model %>%
  map df(glance)
## # A tibble: 1 x 12
##
     r.squared adj.r.squared sigma statistic p.value
                                                           df logLik
                                                                       AIC
                                                                             BIC
##
                       <dbl> <dbl>
                                        <dbl>
                                                 <dbl> <dbl> <dbl> <dbl> <dbl> <
## 1
         0.865
                       0.850 1768.
                                         57.8 2.25e-80
                                                           24 -2131. 4314. 4404.
## # ... with 3 more variables: deviance <dbl>, df.residual <int>, nobs <int>
mod sum <- pm2 n %>%
  mutate(mod_summary = map(.x = model, .f = glance)) %>%
  unnest(mod summary) %>%
  print()
## # A tibble: 10 x 15
## # Groups:
               aar d [10]
##
                             model r.squared adj.r.squared sigma statistic
      aar d
                 data
                                                                              p.value
##
      <date>
                 t>
                             s>
                                       <dbl>
                                                     <dbl> <dbl>
                                                                      <dbl>
                                                                                <dbl>
  1 2008-01-01 <tibble [~ <lm>
                                       0.865
                                                     0.850 1768.
                                                                       57.8 2.25e- 80
## 2 2009-01-01 <tibble [~ <lm>
                                                     0.841 1867.
                                                                       54.2 2.66e- 78
                                       0.857
## 3 2010-01-01 <tibble [~ <lm>
                                       0.876
                                                     0.862 1842.
                                                                       66.0 5.80e- 88
## 4 2011-01-01 <tibble [~ <lm>
                                       0.873
                                                     0.861 2023.
                                                                       69.0 1.45e- 93
## 5 2012-01-01 <tibble [~ <lm>
                                                     0.834 2302.
                                                                       58.4 1.70e- 88
                                       0.848
## 6 2013-01-01 <tibble [~ <lm>
                                                     0.873 2095.
                                                                       79.7 9.97e-103
                                       0.884
## 7 2014-01-01 <tibble \lceil \sim < lm >
                                                     0.849 2308.
                                                                       64.5 2.02e- 92
                                       0.862
## 8 2015-01-01 <tibble [~ <lm>
                                       0.868
                                                     0.855 2438.
                                                                       70.9 1.20e- 99
## 9 2016-01-01 <tibble [~ <lm>
                                                     0.859 2535.
                                                                       70.5 3.01e- 97
                                       0.871
## 10 2017-01-01 <tibble [~ <lm>
                                       0.877
                                                     0.865 2703.
                                                                       75.7 7.97e-102
## # ... with 7 more variables: df <dbl>, logLik <dbl>, AIC <dbl>, BIC <dbl>,
       deviance <dbl>, df.residual <int>, nobs <int>
```

#### i.

Ny variabel av type date i *coef\_df* som angir år.

```
coef_df <- mod_sum$model %>%
  map_df(1) %>%
  tibble()

coef_df <- coef_df %>%
  mutate(
    aar = ymd(paste(2008:2017, "-01-01", sep = ""))
```

```
) %>%
select(aar, everything())
```

#### ii.

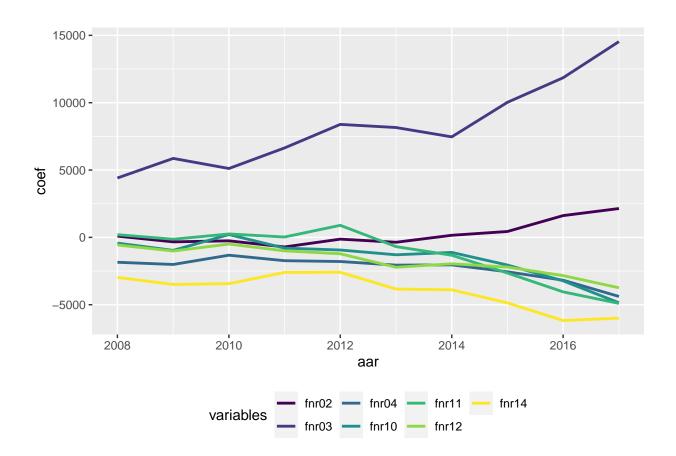
Bruk pivot\_longer på coef\_df for å gjøre om til coef\_df\_long

```
coef_df_long <- coef_df %>%
  pivot_longer(
    cols = `(Intercept)`:`Trade_pc_100K`,
    names_to = "variables",
    values_to = "coef")
```

#### iii.

Lager så et plot av fylke-faktorvariablenes koeffisienter ved bruk av coef\_df\_long.

```
coef_df_long %>%
  select(aar, variables, coef) %>%
  filter(
    variables %in% c("fnr02", "fnr03", "fnr04", "fnr10", "fnr11", "fnr12", "fnr14")
) %>%
  ggplot(mapping = aes(x = aar, y = coef, colour = variables)) +
  scale_color_viridis(discrete = TRUE, option = "D") +
  geom_line(aes(group = variables), lwd = 1) +
  theme(legend.position = 'bottom')
```



#### iv.

Plot-et sier oss at prisuktviklingen i fnr03 har økt kontinuerlig fra år 2008 til 2017, bortsett fra en liten nedgang fra 2012 til 2014.

Fnr02 skiller seg ut ved at den har så og si flat utvikling, har steget noe fra 2015 til 2017.

Resten av variablene har sunket over tidsrommet 2008 til 2017. Dette vil si at det har vært negativ prisutvikling i dette tidsrommet.

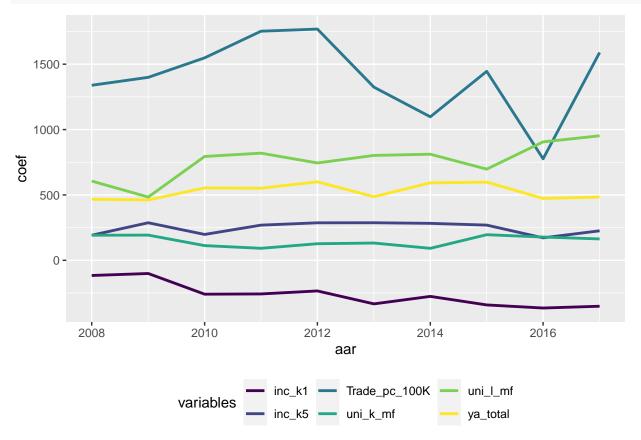
#### $\mathbf{v}.$

I 2014 gikk vi gjennom en oljekrise. Oljeprisen gikk fra 114 dollar fatet til under 30 usd på et halvt år. Norsk økonomi som er veldig avhengig av olje og norske kronen som er veldig avhengig av oljeprisen gikk dermed inn i en nedgangskonjuktur. Derav fikk vi mange oppsigelser direkte i oljerelaterte næringer men også økende arbeidsledighet generelt. Dette rammet særlig områder som har høy tetthet av oljerelatert næring, for eksempel Stavangerregionen. Noe som forårsaket en negativ boligpris utvikling og generelt lavere attraktivitet for hele området.

#### i.

Lage et tilsvarende plot, med nye variabler.

```
coef_df_long %>%
select(aar, variables, coef) %>%
filter(
variables %in% c("ya_total", "inc_k1", "inc_k5", "uni_k_mf", "uni_l_mf", "Trade_pc_100K"
) %>%
ggplot(mapping = aes(x = aar, y = coef, colour = variables)) +
scale_color_viridis(discrete = TRUE, option = "D") +
geom_line(aes(group = variables), lwd = 1) +
theme(legend.position = 'bottom')
```



#### ii.

3/4 av variablene ser ut til å være stabile over tid. Unntaket er <a href="trade\_pc\_100k">trade\_pc\_100k</a> og <a href="trade\_pc\_100k">inc\_k1</a>. uni\_I\_mf svinger godt et par ganger også, så den er ikke helt stabil på kort sikt, men relativt stabil over tid. <a href="trade\_pc\_100k">trade\_pc\_100k</a> er desidert mest ustabil over tidsrommet 2008-2017. <a href="trade\_nc\_k1">inc\_k1</a> har et par kraftige fall, og over tid er den ikke stabil, med tanke på at den har en nedadgående trend over tid.

#### #siste