

BELIEFS, AGGREGATE RISK, AND THE U.S. HOUSING BOOM*

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Abstract

This paper presents a one-step solution method to endogenize beliefs about future prices in general equilibrium models with incomplete markets and aggregate risk. In an application to the U.S. housing boom of the 2000s, beliefs about future house prices are formed via adaptive learning when fundamentals like credit conditions loosen. Adaptive learning induces partial updating which is key for 1) matching both the time-path and volatility of house prices throughout the boom and 2) generating beliefs that are increasingly optimistic and co-move with house prices, as observed in existing and novel empirical evidence. Because model-generated beliefs are sensitive to policy interventions, how beliefs are formed has direct implications for prudential policy.

Keywords: housing boom; aggregate risk; heterogeneous agents; adaptive learning

JEL Codes: E20, E3, C68, R21

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1 Introduction

Record house prices in the 2000s preceded one of the worst recessions in modern U.S. history. Understanding what drove this housing boom has been a central question for researchers and policymakers as they seek to safeguard against a repeat of the economic damage. The two most commonly proposed drivers are looser credit conditions and optimistic beliefs about future house prices.¹ Looser credit conditions allow households to overcome mortgage financing constraints and purchase homes that would otherwise be unattainable, which can increase house prices. Because the number of constrained households determines the size of the house price response, household heterogeneity becomes a key channel through which credit conditions affect house prices. Likewise, the effect of beliefs on house prices depends on how beliefs are formed and those that depart from full-information rational expectations have been shown to capture key features of empirical evidence like correlation with past price changes and partial updating.²

Existing models of the U.S. housing boom typically focus on either heterogeneity from incomplete markets or beliefs that depart from full-information rational expectations, but not both because of their computational intensity. This paper’s solution method can incorporate both in a general equilibrium model with aggregate risk by solving for a Krusell and Smith (1998) approximate equilibrium in one step, bypassing the multiple steps involved in the standard fixed-point solution method. The one-step is achieved by forecasting house prices directly with a rule that is updated via adaptive learning and disciplined with survey evidence—as advocated by Moll (2024). While applicable to many settings with rich heterogeneity and endogenous beliefs, this paper demonstrates the usefulness of the one-step solution method by addressing 1) why beliefs became more optimistic and 2) how belief formation matters for the effectiveness of prudential policies.

To address the first, this paper accounts for optimistic beliefs and house prices via limited knowledge about the evolution of house prices in an economic expansion with looser credit conditions. Given today’s ongoing debate about the degree to which credit conditions affect house prices, it is unlikely that everyone in the early 2000s had a clear understanding. And how could they have known if expectations about future house prices were in line with

¹See Favilukis et al. (2017), Greenwald (2018), Arslan et al. (2022), Lind (2021), Johnson (2019), Landvoigt (2016), Kermani (2012), Justiniano et al. (2019), Mian and Sufi (2017) and Di Maggio and Kermani (2017) for the role of loose credit conditions in the housing boom. See Kaplan et al. (2020), Burnside et al. (2016), Piazzesi and Schneider (2009), Gelain and Lansing (2014), Adelino et al. (2018), Nathanson and Zwick (2018), Glaeser and Nathanson (2017), Albanesi et al. (2022), and Foote et al. (2012, 2018) for the role of optimistic beliefs. See Duca et al. (2021) for an overview of the drivers of housing cycles in the U.S. and other countries.

²See Kuchler et al. (2023) for an overview and work by Glaeser and Nathanson (2017), Adam et al. (2024), Kindermann et al. (2024), Armona et al. (2019), Granziera and Kozicki (2015), and others.

fundamentals when innovations in mortgage finance that allowed for looser credit conditions had never before been experienced on a nation-wide scale? For these reasons, this paper’s new method models loose credit conditions as an aggregate state where the exact effect of fundamentals on house prices is unknown.

When credit conditions loosen, agents must form beliefs to forecast future house prices and do so via adaptive learning—for which this paper is one of the first to embed in a framework with incomplete markets and aggregate risk.³ Under adaptive learning, the partial updating of beliefs prevents agents from fully internalizing the increase in demand for housing services as credit conditions loosen, which results in house prices rising by more than expected. Agents interpret this forecast error as a signal that their beliefs were not optimistic enough, revise their beliefs upward, and will continue to do so absent a new signal suggesting that their beliefs are too optimistic. Because agents pull forward demand for housing services when they expect house prices to rise in the future, optimistic beliefs bring to fruition higher house prices.

The model’s key mechanism for generating optimistic beliefs—and hence higher house prices—is persistently positive house price forecast errors. To corroborate this mechanism with external empirical evidence, this paper develops a novel proxy for house price beliefs in the 2000s from the University of Michigan Survey of Consumers. Although Kuchler et al. (2023, Table 2) document limited availability of empirical house price expectations prior to 2007, this paper exploits the tight correlation of a question on house price beliefs that is only available starting in 2007 with a question on selling conditions going back to 1992 to construct the empirical proxy. In applications of learning to housing in later periods when expectations data is available, Adam et al. (2024) and Kindermann et al. (2024) relatedly find evidence of forecast error persistence like that I detect using my novel proxy.

In addition to matching external empirical evidence on forecast errors, model-generated house prices under endogenously optimistic beliefs formed via adaptive learning match many features of aggregate house price data. While the model matches 75 percent of the empirical increase in aggregate house prices from 1997 to 2007—similar to the framework of Kaplan et al. (2020)—it also replicates the time path, 96 percent of the autocorrelation, and 89 percent of the volatility observed in the data. As noted by Piazzesi and Schneider (2016), existing models can struggle to generate any house price volatility, let alone match that in the data.

In the model, looser credit conditions unaccompanied by optimistic beliefs have only a slight direct effect on house prices, but are key for matching the housing boom dynamics of

³Giusto (2014) and Hoffman (2016) embed adaptive learning with incomplete markets and aggregate risk, the former in the canonical Krusell and Smith (1998) model and the latter to study the interactions of beliefs and income fluctuations. Broer et al. (2022, 2023), Porapakkrum and Young (2007), and Kübler and Scheidegger (2021) explore aggregate risk under information frictions more generally.

homeownership, mortgage leverage, and foreclosures. The small effect of credit conditions on house prices is the result of 1) only a fraction of heterogeneous households—those who are younger and have lower income—being constrained from homeownership and 2) these households buying similar sized properties as those they were renting.⁴ None-the-less, in the framework of this paper, any increase in demand for housing services—like the slight increase from constrained households—can generate persistently positive house price forecast errors and hence endogenously optimistic beliefs.

This paper’s contribution of endogenous beliefs in a model with incomplete markets and aggregate risk positions it to contribute one of the first studies of how belief formation affects the management of housing booms. The prudential policies studied are similar to those of Allen and Greenwald (2022) and Graham and Sharma (2024) who assess the effects of borrowing limits and higher interest rates on housing dynamics, respectively, under full information rational expectations. When optimistic beliefs are endogenously formed under adaptive learning, these prudential policies dampen or eliminate an outsized increase in house prices. By contrast, the same prudential policies have little effect on house prices when optimistic beliefs are instead exogenous.

House prices are sensitive to prudential policy under endogenous beliefs because these beliefs are 1) time-varying and 2) depend on recent house price forecast errors. Changes in fundamentals like higher interest rates or lower borrowing limits can dampen demand for housing services which, in turn, pushes down forecast errors resulting in relatively less optimistic beliefs in current and subsequent periods. By contrast, these same changes in fundamentals cannot offset the expectation of higher future house prices when beliefs are instead formed exogenously. Chodorow-Reich et al. (2023) similarly find that housing boom dynamics are sensitive to interest rates when knowledge is limited. Both Igan and Kang (2011) and Kuang et al. (2024) relatedly document that house price expectations respond to changes in borrowing constraints.

2 Related Literature

This paper’s first question of why beliefs about future house prices became optimistic in the 2000s is addressed via regional heterogeneity by Howard and Liebersohn (2023) and

⁴Constrained households are thus the closest parallel to subprime borrowers who have been shown by Mian and Sufi (2009, 2017), Griffin et al. (2021), and others to account for the dynamics of the housing boom. Additional channels could result in credit conditions having a larger effect on house prices, but may still fall short of matching house price statistics other than the level increase as is in this paper. Favilukis et al. (2017) also include aggregate risk and incomplete markets, but instead link credit conditions to house prices via a potentially counterfactually high risk aversion, a less simplified financial sector, and influx of foreign borrowers. Subsequent work explores the role of market segmentation of renters and homeowners [Greenwald and Guren (2024)], the type of credit conditions [Greenwald (2018) and Justiniano et al. (2019)], and the feedback between households and the financial sector [Arslan et al. (2022)].

Chodorow-Reich et al. (2023) who propose regional divergence and relocation to downtown neighborhoods, respectively, as fundamentals-based explanations. Although regional heterogeneity is beyond the scope of this paper, it is complementary to household heterogeneity and belief formation, the latter of which is also a key feature of Landvoigt (2016).

By allowing for endogenous belief formation in a model with incomplete markets and aggregate risk, this paper contributes a new innovation of the Krusell and Smith (1998) solution method and applies it to the U.S. housing boom of the 2000s. In particular, this paper builds off of the state-of-the art quantitative frameworks of Favilukis et al. (2017) and Kaplan et al. (2020) which rely on time-invariant and fully-known beliefs about future house prices. Relatedly, work by Hoffman (2016) also forms endogenous beliefs via adaptive learning to study the interactions of beliefs and income fluctuations across several economic cycles. The interactions between beliefs and fundamentals in other frameworks is also featured in Johnson (2019), Cox and Ludvigson (2021), and Dong et al. (2022).

More specifically, this paper’s tractable one-step solution method incorporates adaptive learning into a rich quantitative model to allow for both heterogeneity from incomplete markets and beliefs that depart from full-information rational expectations. Other structural models with adaptive learning have successfully accounted for housing market dynamics via limited knowledge about the supply of credit and demand for assets [Caines (2020)], house prices [Adam et al. (2012), Kuang (2014)], or the permanence of financial innovations [Boz and Mendoza (2014)]. In contrast to this paper’s rich household heterogeneity, these studies typically rely on representative agents which may overstate the direct effect of looser credit conditions on higher house prices. Chodorow-Reich et al. (2023) and Kindermann et al. (2024) are an exception by allowing for regional heterogeneity and learning about local fundamentals. While they, and most other adaptive learning applications, assume limited knowledge about model quantities, Adam and Marcet (2011) provide microfoundations for learning about market clearing prices, as is the case in this paper. Relatedly, Bastianello and Fontanier (2024, 2025) provide comparisons of learning about fundamentals versus prices.

Because this paper’s contribution of endogenous belief formation adds several additional dimensions to already computationally intensive frameworks, assuming homogeneous beliefs allows for tractability and clean interpretation of mechanisms. In structural models with heterogeneous beliefs, Piazzesi and Schneider (2009), Burnside et al. (2016), Glaeser and Nathanson (2017), Mian and Sufi (2022) and Dong et al. (2022) show that optimists push up house prices to generate the housing boom, which is also consistent with the survey evidence of Kindermann et al. (2024). This paper’s homogeneous beliefs can thus be interpreted as a first step towards incorporating these richer forms of beliefs into computationally intensive quantitative models, as advocated by Moll (2024).

Even though explicit measures of house price expectations are only available starting in 2007, this paper’s novel empirical proxy and other evidence supports optimistic beliefs during the 2000s. Surveys by Case and Shiller (1988, 2004), Case et al. (2012), and Shiller and Thompson (2022) document high expectations for house price growth during local booms. For the 2000s boom specifically, Piazzesi and Schneider (2009), Ben-David et al. (2024), and Soo (2018) all document optimism rising with house prices.

By assuming that shifts in aggregate credit conditions along with fluctuations in aggregate income trigger adaptive learning about house price forecasts, this paper takes the stance that beliefs respond to credit conditions. Although some evidence suggests the opposite direction of causality, identification remains debated and difficult to disentangle.⁵ For example, Diamond and Landvoigt (2022) find an important role for the endogenous expansion of credit conditions in explaining housing boom dynamics.

Loose credit conditions and optimistic beliefs are not the only explanations of the U.S. housing boom of the 2000s. Low interest rates have also been studied with mixed success. Even though Adam et al. (2017), Garriga et al. (2019), Jordà et al. (2015), Chodorow-Reich et al. (2023) and Diamond and Landvoigt (2022) successfully link low interest rates to high house prices, Dokko et al. (2011) and Glaeser et al. (2013) do not find a similar connection.

To that end, the counterfactual prudential policy simulations in this paper are in line with previous studies of interest rate policy under learning and macroprudential policies under behavioral biases more generally. Adam and Woodford (2021), Adam et al. (2024), and Caines and Winkler (2021) show that it may be optimal for monetary policy to lean against house prices and other assets under adaptive learning. Fontanier (2025) shows that optimal policy prescriptions can depend on the source of behavioral biases with learning. While this paper abstracts away from the rich general equilibrium feedback from other sectors of the economy, like those also shown to be important by Kinnerud (2024), the prudential policy counterfactual simulations none-the-less provide a clean mechanism for showing how belief formation can matter in housing boom management.

3 Model

3.1 Environment

The model allows for endogenous beliefs about future house prices in a state-of-the art macro-housing model designed to nest that of Kaplan et al. (2020).⁶ Time is discrete and

⁵While Mian and Sufi (2009, 2017) find that changes in credit conditions increased expected future house prices, Adelino et al. (2018) and Foote et al. (2012) suggest the opposite direction of causality. Cox and Ludvigson (2021) find contemporaneous correlation between beliefs and credit conditions.

⁶See Appendix E for more details including some small differences in implementation of this paper’s nested model relative to that of Kaplan et al. (2020).

the economy is populated by a continuum of measure one finitely lived households who are heterogeneous in ages and idiosyncratic income endowments. These households trade goods and services with a lending sector, a rental housing sector, housing construction firms, and final goods firms. Lowercase letters denote individual household quantities and uppercase letters denote aggregates.

Preferences: Households are active in economic life for $j = 1, \dots, J$ periods where they work from $j = 1$ to J^{ret-1} and retire at J^{ret} until they exit the economy with certainty at J . Households have preferences over final goods consumption and housing expenditures $\{c_j, s_j\}_{j=1}^J$ with final goods consumption as the numeraire. All j subscripts have been dropped unless needed. The utility function is given as:

$$u_j(c_j, s_j) = e_j \frac{[(1 - \phi)c_j^{1-\gamma} + \phi s_j^{1-\gamma}]^{\frac{1-\sigma}{1-\gamma}} - 1}{1 - \sigma}$$

Where ϕ is the taste for housing relative to goods consumption, $1/\gamma$ is the elasticity of substitution between housing expenditures and goods consumption, and σ is the intertemporal elasticity of substitution. A deterministic equivalence scale $\{e_j\}_{j=1}^J$ adjusts consumption for changes in household size over the life-cycle. Expected life-time utility at time t for $0 < \beta < 1$ is given as:

$$\mathbb{E}_t \left[\sum_{j=1}^J \beta^{j-1} u_j(c_j, s_j) + \beta^J v(b) \right]$$

Where the warm-glow bequest motive at the end of life J follows the functional form of De Nardi (2004) which modifies that of Carroll (2002):

$$v(b) = \psi \frac{(b + \underline{b})^{1-\sigma} - 1}{1 - \sigma} \quad (1)$$

The bequest motive prevents households from counterfactually ramping up debt and drawing down housing when they exit the economy. The strength of the bequest motive is regulated by $\psi \geq 0$ and the extent to which bequests are luxuries is given by $\underline{b} \geq 0$.

Income endowments: While working, households receive an income endowment comprised of an aggregate stochastic endowment $\Theta(Z)$, a deterministic life-cycle profile that varies by age χ_j , and an idiosyncratic stochastic endowment $\epsilon_j(z)$ that follows a Markov process.

$$\log y = \log \Theta(Z) + \chi_j + \epsilon_j(z), \quad \text{when } j < J^{ret}$$

The transition matrix for earnings $\epsilon_{j+1}(z') \sim \Upsilon_{j+1|j}(\epsilon_j(z))$ is age-dependent which helps

account for rising income volatility throughout working life.

In retirement, households receive a fraction ρ_{SS} of their last working period income with aggregate income averaged across states $\bar{\Theta}$. Heterogeneity in retirement income helps preserve the wealth distribution of retired agents.

$$y = \rho_{SS}(\log \bar{\Theta} + \chi_{J^{ret}-1} + \epsilon_{J^{ret}-1}), \quad \text{when } J^{ret} \leq j \leq J \quad (2)$$

Income tax follows the functional form of Heathcote et al. (2017) where τ_y^0 sets the average level of taxation and τ_y^1 sets the degree of tax progressivity. To capture the tax benefits of homeownership, households can deduct ϱ fraction of the interest paid on their mortgage $r_m m$ for the first \$1,000,000 of mortgage debt, \bar{m} .

$$\mathcal{T}(y, m) = y - \tau_y^0(y - \varrho r_m \min\{m, \bar{m}\})^{1-\tau_y^1} \quad (3)$$

If a household does not have a mortgage, the expression simplifies to, $\mathcal{T}(y) = y - \tau_y^0(y)^{1-\tau_y^1}$.

Housing: Households can either rent or own houses. To capture the lumpy dynamics of housing over the life-cycle—as described by Chambers et al. (2009)—housing units are indivisible and available in discrete fixed sizes $\mathcal{H} \in \{h^0, \dots, h^N\}$ for homeowners and $\tilde{\mathcal{H}} \in \{\tilde{h}^0, \dots, \tilde{h}^N\}$ for renters. If housing units were instead a continuum of sizes households would make a counterfactually large number of adjustments to square footage over the life-cycle as they could upsize or downsize by a fraction of a room.

Markets for rental and owner-occupied housing are both frictionless and competitive where the law of one price holds and selling is instantaneous.⁷ Rental units cost $\rho(\mu, Z)$ and owner-occupied units cost $p(\mu, Z)$. Renting generates housing services equal to the size of the housing unit, $s = \tilde{h}$ while homeownership offers additional utility $s = \omega h$ for $\omega \geq 1$. Homeowners pay per-period taxes and maintenance costs $(\delta_h + \tau_h)p(\mu, Z)h$ where maintenance offsets the depreciation of the housing unit. When selling, homeowners pay a transaction cost $\kappa p(\mu, Z)h$ that is linear in housing value. Renters do not pay these costs and can adjust the size of their housing unit without transaction costs.

Liquid savings: Households can save in one-period bonds b at the price $q_b = 1/(1+r_b)$, the reciprocal of the exogenous risk-free rate. Unsecured borrowing is prohibited and households cannot trade among themselves. Households transact bonds with risk-neutral non-modeled foreign agents with deep pockets.

Assuming an exogenous financial sector implies that the model is essentially a small

⁷See Hedlund (2016) for the role of search frictions such as time delays in housing market dynamics.

open economy which is a fairly standard assumption in the literature [Arslan et al. (2022), Kaplan et al. (2020), Greenwald and Guren (2024), Chodorow-Reich et al. (2023)]. Arslan et al. (2022) explain that at the onset of the housing boom in the late 1990s, net exports decline and stay negative, which in turn implies that there is a net capital inflow to the U.S. consistent with the data. Although allowing for endogenous determination of the risk-free rate r_b would lend to more rigorous counterfactual simulations, it would also require zero net supply of financial instruments or capital rented to final goods firms. Not only would the dynamics and mechanisms be complicated by an additional endogenous price, but r_b would also need to be approximated via a Krusell and Smith (1998) equilibrium such that the coefficients on the evolution of $r_b(\mu, Z_0)$ would need to be solved for in addition to house prices $p(\mu, Z)$.

Mortgages: Homeowners finance housing purchases with multi-period defaultable mortgages subject to a fixed origination cost $\kappa^m(Z)$. These mortgages are amortized over the life of the household at interest rate $r^m = (1 + \iota)r_b$ which is equal to the risk-free rate scaled by an intermediation wedge.⁸ Default risk is thus priced by the mortgage pricing function $q_j(\mathbf{x}', y; Z, \mu)$ rather than the interest rate. This function depends on variables that predict future repayment which include the age j of borrowing households, individual state variables $\mathbf{x}' = \{b', h', m'\}$, individual income y , and aggregate states Z and μ .

When a household aged j obtains a mortgage with principal balance m' they receive $q_j(\mathbf{x}', y; Z, \mu)m'$ from the lender where $q_j(\mathbf{x}', y; Z, \mu) < 1$. The down payment at origination is thus $p(\mu, Z)h' - q_j(\mathbf{x}', y; Z, \mu)m'$. Households make $J - j$ mortgage payments until the mortgage is fully repaid, $\pi_j^{min}(m) \leq m(1 + r_m) - m'$. The minimum payment is determined by constant amortization:

$$\pi_j^{min}(m) = \left[\frac{r_m(1 + r_m)^{J-j+1}}{(1 + r_m)^{(J-j+1)} - 1} \right] m \quad (4)$$

A loan-to-value (LTV) constraint limits mortgage size to a fraction of the value of housing collateral $m' \leq \theta^{LTV}(Z)p(\mu, Z)h'$ and the payment-to-income constraint (PTI) caps the minimum mortgage payment at a fraction of household income $\pi_j^{min}(m') \leq \theta^{PTI}(Z)y$. Because mortgages are multi-period debt, households are only subject to these constraints in the period when mortgages are originated.

HELOCs: Home equity lines of credit (HELOCs) allow homeowners to borrow one-period,

⁸Allowing homeowners to choose the length of mortgages with borrower-specific interest rates would add more realism at the cost of more state variables. Tractability is assured by 1) mortgages being due at the deterministic end of economic life and by 2) amortization at the common mortgage interest rate r^m .

non-defaultable debt up to a fraction of the value of housing collateral $-b' \leq \theta^{HELOC} p(\mu, Z)h$ with an interest rate equal to that on mortgages r_m . Although only a small fraction of homeowners have HELOCs, including these debt instruments is important for matching targeted net worth moments in the calibration of the cross-sectional distribution of households. Evidence is mixed as to whether or not HELOCs account for mortgage debt dynamics in the U.S. housing boom. Chen et al. (2020) find an important role while Kim (2021) argue that it is more negligible.

Shocks: Z indexes an aggregate state where income $\Theta(Z)$ fluctuates via a two state Markov chain with transition matrix $Z' \sim \Gamma_Z(Z)$ and credit conditions $\mathcal{C}(Z) = \{\theta^{LTV}(Z), \theta^{PTI}(Z), \kappa^m(Z), \zeta^m(Z)\}$ loosen via a one-time unanticipated shock as in Favilukis et al. (2017). Because agents expect permanently looser credit conditions in the housing boom, the tightening of credit conditions in the housing bust is also a one-time unanticipated shock. Allowing for a two-state Markov chain for credit conditions is richer than assuming a one-time loosening, but less computationally tractable in the new solution method with endogenous beliefs. However, because existing calibrations assume the probability of a shift in credit conditions is 1 percent, simulations of the housing boom with Markov credit conditions will be little different than simulations with a one-time shift as shown in Appendix E.

The two aggregate states of the economy are a high and low state $Z \in \{high, low\}$. In the housing boom, income and credit conditions simultaneously attain their high state values while the subsequent bust is thus a contraction back to their low state values.

Individual income $\epsilon_j(z)$ follows an AR(1) process with persistence ρ and an age-dependent standard deviation σ_{ϵ_j} resulting in an age-dependent transition matrix $\epsilon_{j+1}(z') \sim \Upsilon_{j+1|j}(\epsilon_j(z))$

$$\epsilon_j(z) = \rho \epsilon_{j-1}(z_{-1}) + \varepsilon_j(z), \quad \varepsilon_j(z) \sim \mathcal{N}(0, \sigma_{\epsilon_j}^2) \quad (5)$$

Aggregate state space: The distribution of individual household states μ is a necessary state variable for agents to correctly forecast next period prices under incomplete markets and aggregate risk. $\Gamma_\mu(\mu; Z, Z')$ is the equilibrium law of motion of the measure of agents such that $\mu' = \Gamma_\mu(\mu; Z, Z')$. The aggregate state space of the economy is thus the distribution over individual states and the aggregate shock $\{\mu, Z\}$. Let $\mathcal{X}^h = \mathcal{B} \times \mathcal{H} \times \mathcal{M} \times \mathcal{E} \times \mathcal{J}$ denote the set of individual states for homeowners and $\mathcal{X}^r = \mathcal{B} \times \mathcal{E} \times \mathcal{J}$ that of renters with measure $\int_{\mathcal{X}^h} \mu^h d\mu^h + \int_{\mathcal{X}^r} \mu^r d\mu^r = 1$.

Beliefs: This paper introduces a solution method where agents form boundedly rational expectations with respect to fully known shocks $\{Z, \epsilon_j(z)\}$ and only form beliefs about house

prices $p(\mu, Z)$, which are a subset of endogenous prices that are not pinned down by modeling assumptions like the other prices. This paper solves for a Krusell and Smith (1998) equilibrium by approximating the potentially infinitely dimensional distribution μ and its law of motion $\mu' = \Gamma_\mu(\mu; Z, Z')$ with a forecasting rule for house prices. Under this paper's one-step solution method, agents know the form of the forecasting rule for house prices but do not know its parameter values. As discussed by Moll (2024), this approximate equilibrium does not require any additional moments such as means or variances and allows for tractable computation with aggregate non-linearities, which is a key feature of booming house prices.⁹ Section 3.7 discusses in more detail the equilibrium properties of the model and Appendix B discusses the solution method with endogenous beliefs.

3.2 Households' Problem

See Appendix A.1 for the full recursive households' problems.

Renters are endowed with savings $b > 0$ and income y . They must choose to stay a renter or purchase a house and become a homeowner solving the problem:

$$V_j^r(b, y; \mu, Z) = \max\{V_j^{rent}(b, y; \mu, Z), V_j^{own}(b, y; \mu, Z)\} \quad (6)$$

Newly originated mortgages are subject to loan-to-value and payment to income constraints:

$$m' \leq \theta^{LTV}(Z) p_h(\mu, Z) h' \quad (7)$$

$$\pi_j^{min}(m') \leq \theta^{PTI}(Z) y \quad (8)$$

Relative to renting, homeownership offers households the benefits of extra utility, tax deductible mortgage interest payments, and collateral for borrowing liquid assets in the form of HELOCs. Renting has the advantage of shielding households from capital gains fluctuations due to movements in house prices. When model simulated house prices match the empirical standard deviation as is the case under endogenous beliefs, renting becomes relatively more advantageous due to more volatile house prices.

Homeowners have four options: sell their house to purchase a new house or become a renter, default and become a renter, stay in their house and pay their existing mortgage, or stay in their house and refinance a new mortgage.

$$V_j^h(\mathbf{x}, y; \mu, Z) = \max\{V_j^r(b^n, y; \mu, Z), V_j^{default}(b, y; \mu, Z), V_j^{stay, pay}(\mathbf{x}, y; \mu, Z), V_j^{stay, refi}(\mathbf{x}, y; \mu, Z)\} \quad (9)$$

⁹Although additional statistics, lags, or forms of a forecasting rule may be used, Krusell and Smith (1998) find that more complexity only incrementally improves accuracy. Moreover, Pancrazia and Pietrunti (2019) find that simple forecasting rules are best at fitting the path house prices throughout the 2000s.

3.3 Lending Sector

The lending sector originates mortgages m' to households aged j at price $q_j(\mathbf{x}', y; \mu, Z) \leq 1$. Although lenders are competitive, uninsurable aggregate risk may induce profits and losses along the equilibrium path. Lenders are owned by non-modeled foreign agents with deep pockets who receive these profits and losses as net exports. The mortgage market clears loan-by-loan with the pricing of mortgage points depending on individual future default probabilities and collateral of foreclosed homes.

$$q_j(\mathbf{x}', y; \mu, Z) = -\zeta(Z) + \mathbb{E}_{Z', \epsilon'} \left\{ \begin{array}{ll} 1 & \text{sell/refi} \\ \frac{(1 - \delta_h^d - \tau_h - \kappa_h)p'(\mu', Z')h'}{(1 + r_m)m'} & \text{default} \\ \frac{(1 + r_m)m' - m'' + q_{j+1}(\mathbf{x}'', y'; \mu', Z')m''}{(1 + r_m)m'} & \text{pay} \end{array} \right. \quad (10)$$

If a homeowner sells or refinances, they repay the full balance of their mortgage so that the lender receives the principal plus interest less the intermediation cost $\zeta(Z)$. If the household defaults, the lender forecloses and sells the house to recover the market value of the house as a fraction of the original mortgage. If the homeowner pays their existing mortgage, the lender values the contract as the next period mortgage payment $(1 + r_m)m' - m''$ plus the continuation value of the contract $q_{j+1}(\mathbf{x}'', y'; \mu', Z')m''$.

3.4 Final Goods and Construction Firms

See Appendix A.2 for the full recursive problems of final goods and housing construction firms. The competitive final goods sector has a linear constant returns to scale technology $Y = \Theta(Z)N_c$ with inelastic labor supply N_c . Profit maximization delivers an aggregate wage equal to aggregate productivity:

$$w(\mu, Z) = \Theta(Z) \quad (11)$$

A competitive construction sector produces houses with technology $H_h = (\Theta N_h)^\alpha \bar{L}^{1-\alpha}$ where N_h is labor services and \bar{L} is the amount of newly available buildable land. Using the equilibrium wage in equation (11) housing supply is:

$$H_h = [\alpha p(\mu, Z)]^{\frac{\alpha}{1-\alpha}} \bar{L} \quad (12)$$

The profit maximization of the construction sector thus pins down a single price for housing $p(\mu, Z)$ via aggregate housing supply H_h and the aggregate productivity shock $\Theta(Z)$.

3.5 Rental Sector

The rental rate is pinned down by a user-cost formula that is a function of current and future house prices along with a per-period operating cost Ξ as shown in Appendix A.2. The competitive rental sector frictionlessly buys and sells housing units to convert them into rental housing which incurs the same depreciation and taxes as owner-occupied housing.

$$\rho(\mu, Z) = \Xi + p(\mu, Z) - (1 - \delta_h - \tau_h) \mathbb{E}_{Z', \epsilon' | Z, \epsilon} [q_b p'(\mu', Z')] \quad (13)$$

Greenwald and Guren (2024) show that looser credit conditions can quantitatively account for the drop in the rent-price ratio observed throughout the housing boom when landlords are heterogeneous with disperse ownership costs. Although Kaplan et al. (2020, Appendix D) and Arslan et al. (2022) introduce these important frictions in their frameworks, doing so in this paper is complicated by aggregate risk. With costs on the conversion of newly purchased housing units into rentals, the aggregate stock of rental housing \tilde{H}' becomes an additional state variable with an unknown evolution that must be approximated via a forecasting rule like that for house prices $p(\mu, Z)$. Although frictions on the stock of rental housing would give credit conditions a more important direct role and beliefs potentially less, this does not conflict with the goal of this paper to unify these two explanations of the housing boom and relate the shift in beliefs to fundamentals.

3.6 Government

The sum of income tax revenues $\mathcal{T}(y, m)$ less mortgage interest rate deductions, property tax revenues $p(\mu, Z) \tau_h \int_{\mathcal{X}^h} h d\mu^h$, and land permit revenues $p(\mu, Z) H_h - w(\mu, Z) N_h$ net of pension outlays $\int_{\mathcal{X}} y_{ret} d\mu^{\mathcal{J}^{ret}}$ are always positive and spent on government services G that are not valued by households and thus discarded.

3.7 Computation of Equilibrium

See Appendix A.3 for the definition of the recursive competitive equilibrium and Appendix B for the one-step computational algorithm and its goodness of fit. In the Krusell and Smith (1998) algorithm, aggregate risk and incomplete markets rule out an equilibrium distribution over individual states μ corresponding to a steady state. To determine prices, agents must keep track of a potentially infinitely dimensional object to compute the distribution's equilibrium law of motion $\mu' = \Gamma_\mu(\mu; Z, Z')$.¹⁰ An approximate equilibrium thus achieves

¹⁰Ahn et al.'s (2018) alternative to the Krusell and Smith (1998) method first solves for a stationary equilibrium with only idiosyncratic shocks and then linearizes around the steady state of aggregate shocks. Linearization may only be suitable if the wealth distribution remains close to the aggregate steady state and this may not be the case when allowing for endogenous beliefs, and hence booming house prices. The Krusell and Smith (1998) method may thus be more robust than linearization in the setting of this paper.

computational tractability by tracking house prices directly and updating them with a forecasting rule for each combination of current and future aggregate states, $\mathcal{Z} \in \{Z, Z'\}$.¹¹

$$\log p'(p(Z); \mathcal{Z}) = a_{\mathcal{Z}}^0 + a_{\mathcal{Z}}^1 \log p(Z) \iff \mu' = \Gamma_{\mu}(\mu; \mathcal{Z}) \quad (14)$$

The log-linear AR(1) forecasting rule for house prices in equation (14) is standard in macro housing applications and assumes that the conditional sample log means of house prices $\mu_{\mathcal{Z}}^p = a_{\mathcal{Z}}^0 / (1 - a_{\mathcal{Z}}^1)$ are sufficient statistics to accurately predict future prices.

The standard Krusell and Smith (1998) solution method assumes that agents have full knowledge of the forecasting coefficients in equation (14) and solves for these coefficients as fixed point. Computing an approximate equilibrium requires multiple steps: one first guesses values for these coefficients $\mathbf{a}_{\mathcal{Z}} = (a_{\mathcal{Z}}^0, a_{\mathcal{Z}}^1)'$ and then solves and simulates the model. Using the time series of simulated market clearing prices p_t , one estimates new coefficients via an ordinary least squares regression shown in equation (15). These steps are repeated until the new coefficients are close to the originals, $\mathbf{a}_{\mathcal{Z}} \approx \mathbf{a}_{\mathcal{Z}}^{new}$. Let $\mathcal{Z}, t \in \{Z, Z'\}$ index the partition of current and future aggregate states at time t .

$$\log p_{\mathcal{Z}, t+1} = \underbrace{a_{\mathcal{Z}}^0 + a_{\mathcal{Z}}^1 \log p_{\mathcal{Z}, t}}_{\mathbf{x}'_{\mathcal{Z}, t} \mathbf{a}_{\mathcal{Z}}} + e_{\mathcal{Z}, t+1}, \quad \mathbf{a}_{\mathcal{Z}}^{new} = \left(\sum_{t=1}^T \mathbf{x}_{\mathcal{Z}, t} \mathbf{x}'_{\mathcal{Z}, t} \right)^{-1} \sum_{t=1}^T \mathbf{x}_{\mathcal{Z}, t} \log p_{\mathcal{Z}, t+1} \quad (15)$$

This paper's contribution of a one-step solution method embeds adaptive learning into the forecasting rule for house prices shown in equation (14). Rather than solving for converged forecasting coefficients in multiple steps a fixed point, agents instead update the coefficients in each simulation period $\mathbf{a}_{\mathcal{Z}, t}$ with a combination of past coefficients and weighted lagged forecast errors e_{t-1} as shown by the recursive stochastic gradient mechanism for adaptive learning in equation (16).¹² Let $\mathbf{x}_{t-2} = (1, \log p_{t-2})'$.

$$\mathbf{a}_{\mathcal{Z}, t} = \mathbf{a}_{\mathcal{Z}, t-1} + g_t \mathbf{x}_{t-2} \underbrace{(\log p_{t-1} - \mathbf{x}'_{t-2} \mathbf{a}_{\mathcal{Z}, t-1})}_{e_{t-1}} \quad (16)$$

¹¹A single housing price $p(\mu, Z)$ is the only price determined via market clearing. The lending sector, rental sector, final goods firms, and construction firms are all perfectly competitive with linear objective functions. The number of prices is thus reduced from four to one.

¹²Evans et al. (2010) show that stochastic gradient learning does not weight the forecast error by the inverse of the matrix of second moments, $\mathbf{R}_{\mathcal{Z}, t} = \mathbf{R}_{\mathcal{Z}, t-1} - g_t (\mathbf{x}'_{t-2} \mathbf{x}_{t-2} - \mathbf{R}_{\mathcal{Z}, t-1})$. Stochastic gradient learning has the advantages of simplicity and ease of interpretation when embedding in a general equilibrium framework. Furthermore, Mele et al. (2020) argue that stochastic gradient learning keeps the state space small by abstracting from the evolution of the estimated second moments. However, stochastic gradient learning has different convergence criteria than least squares learning as shown by Barucci and Landi (1997).

Following the convention of Evans and Honkapohja (1999), agents form beliefs at time t using information available at $t-1$.¹³ Because the next period aggregate state Z' is unknown at time t , agents will need to calculate as many vectors of coefficients as there are next period aggregate states Z' . With four possible aggregate states, agents will compute four different coefficients each period and the time t expected future house prices is $\mathbb{E}_t[\log p_{t+1}] = \sum_{Z'} \pi_{Z,Z'} \exp \{a_{Z,t}^0 + a_{Z,t}^1 \log p_t\}$.¹⁴ The functional form of g_t is the mixed learning gain of Marcet and Nicolini (2003) where the learning gain is constant, $g_t = g$, if the economy is in an aggregate state with loose credit conditions and is decreasing, $g_t = g_{t-1}/(1 + g_{t-1})$, if credit conditions are instead tight. As discussed in detail in section 4.1, the mixed learning gain has the benefit of rapid adjustments in the booms states and dampened oscillations in the non-boom states. Appendix F.4 shows that housing boom simulations are similar if the learning gain is not mixed and is instead either constant or decreasing.

$$g_t = \begin{cases} g & \text{if } Z_t \in \{Z_{high}^{loose}, Z_{low}^{loose}\} \\ \frac{g_{t-1}}{1 + g_{t-1}} & \text{otherwise} \end{cases}$$

As agents learn the true values of the forecasting coefficients, beliefs about future house prices may not yet correspond to the actual evolution of prices. The resulting temporary equilibria may be self-referential where optimism leads to relatively higher market clearing realizations or pessimism leads to relatively lower. How the values of time-varying coefficients $\mathbf{a}_{Z,t}$ differ from their near-rational known counterparts \mathbf{a}_Z depends on the evolution of the house price forecast error, which, in turn, depends on three key parameters: the gain parameter g_t governing the speed of updating and the vector of initial coefficients $\mathbf{a}_{Z,0}$.

As shown in figure (1), under either the standard fix-point coefficients \mathbf{a}_Z or the time-varying adaptive learning coefficients $\mathbf{a}_{Z,t}$, equilibrium selection relies on the convergence of coefficients to an ergodic distribution. How coefficients converge differs between the two solution methods—the standard coefficients converge via a fixed point while the time-varying coefficients converge sequentially. Even though the fixed-point solution method solves and simulates the model many times at many different coefficient values, coefficient remain fixed throughout each version of the simulation and are updated at each iteration until the original guess is close to the simulated value as shown by the dashed lines in figure (1). By contrast, under adaptive learning, the model is solved in one-time on a grid of future prices so that

¹³A forecasting rule like that in Malmendier and Nagel (2016) where time t information is included in time t beliefs via the forecast error, $e_t = \log p_t - \mathbf{x}'_{t-1} \mathbf{a}_{Z,t-1}$, would induce a simultaneity problem in this general equilibrium setting as agents would be determining house prices p_t while also using them to form beliefs.

¹⁴There are several alternative forms of equation (16) and Appendix F.2 shows that these have little material difference on the main housing boom simulations.

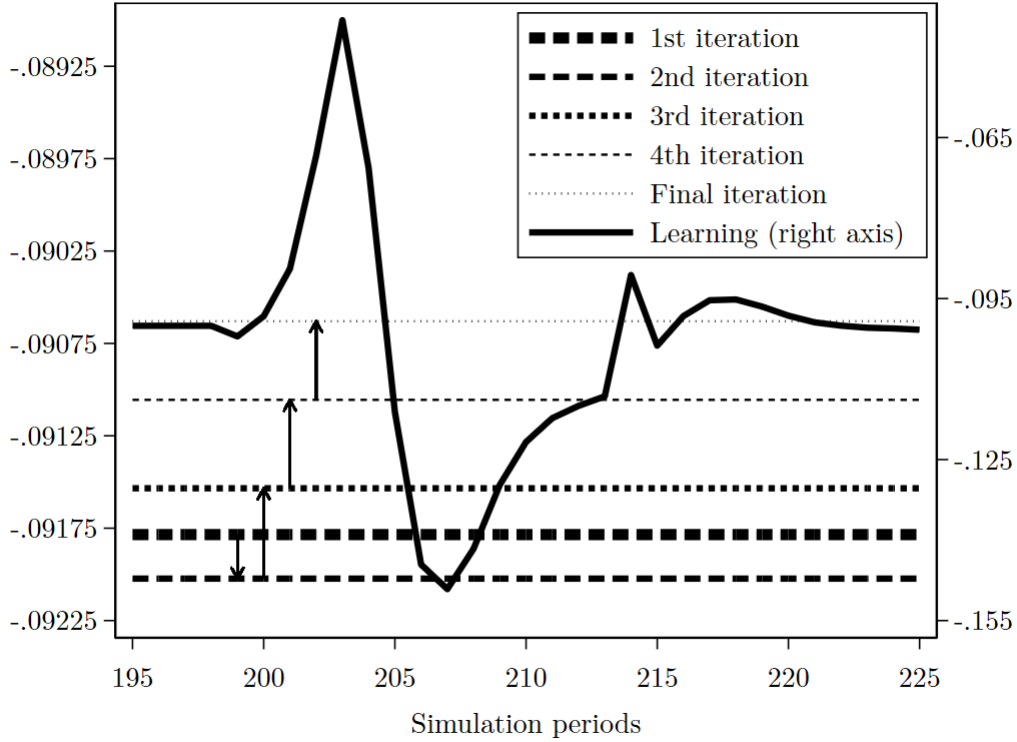


Figure 1: House price forecast coefficient $a_{Z_{low_t}, Z'_{low}}^0$ solved for as a fixed point or sequentially or under learning, which starts in period 200. The spikes in the coefficients under learning (solid thick line) are periods where the economy changes aggregate states. The coefficients eventually return to near their ergodic distribution (pre 200 values) by about period 220.

coefficients can vary throughout simulation. Although the resulting sequence of coefficients may diverge from the near-rational fixed-point counterparts temporarily—as shown by the solid line in Figure (1)—the sequence of coefficients does eventually converge to a nearby ergodic distribution.

Given that there are the many forms of expectations that allow for limited knowledge, this paper does not claim that the adaptive learning rule given by equation (16) is uniquely suitable for endogenizing beliefs about future prices. In fact, the one-step solution method in Appendix B is generalizable to many models with rich heterogeneity and endogenous beliefs. In this paper's application to the U.S. housing boom of the 2000s, adaptive learning has the advantages of 1) a backwards looking house price forecast component found to best fit the data by Gelain et al. (2016), Glaeser and Nathanson (2017), Case and Shiller (1989), Pancrazia and Pietrunti (2019), and Granziera and Kozicki (2015) and 2) tractability when embedded in a detailed quantitative model, and 3) well-studied equilibrium convergence properties.¹⁵ Alternatives forms of endogenous beliefs such as extrapolative, diagnostic, or

¹⁵See Evans and Honkapohja (2001) for adaptive learning convergence to rational expectations equilibria.

natural expectations may be equally suitable for the application to the U.S. housing boom as these beliefs can all generate key empirical features of house price beliefs such as correlation with past price changes and extrapolation of recent pricing trends.

4 Parameterization and Calibration

4.1 Parameters

The model’s parameters are discussed in detail in Appendix C.1 and are set to resemble the U.S. economy in the late 1990s with the cross-sectional moments from the 1998 Survey of Consumer Finances via Kaplan et al. (2020). Table (1) lists targeted moments from the model’s stochastic steady state which is characterized by tight credit conditions and fluctuations in income. Parameters that differ from Kaplan et al. (2020) are discussed below along with this paper’s contribution of a proxy for external empirical evidence on belief formation constructed from the University of Michigan Survey of Consumers.

Housing Preferences: The preference for housing relative to goods consumption $\phi = 0.13$ pins down housing demand so that the average share of housing expenditure to total expenditures from the model is 0.16, as in the data. In Kaplan et al. (2020) this parameter is not fixed and instead follows a stochastic process where it can take on a low value $\phi_{low} = 0.12$ and a high value $\phi_{high} = 0.20$.

Moment	Parameter	Empirical Value	Model Value
Agg. net worth/annual agg. labor income	β	5.5	4.9
Median ratio of net worth to labor income	β	1.2	1.2
Median net worth: age 75/age 50	ψ	1.55	1.48
% of bequests in bottom 1/2 of wealth dist.	\underline{b}	0	0
Housing/total cons. expenditures	ϕ	0.16	0.16
Aggregate home-ownership rate	ω	0.66	0.68
Foreclosure rate	ξ	0.005	0.0002
P10 housing/total net worth of owners	$\min \mathcal{H}$	0.11	0.13
P50 housing/total net worth of owners	$\# \mathcal{H}$	0.5	0.33
P90 housing/total net worth of owners	$\text{gap } \mathcal{H}$	0.95	0.74
Average sized owned house/rented house	$\min \tilde{\mathcal{H}}$	1.5	2
Average earnings of owners to renters	$\# \tilde{\mathcal{H}}$	2.1	2.8
Annual fraction of houses sold	κ_h	0.1	0.09
Homeownership rate of < 35 y.o.	Ξ	0.39	0.34
Employment in construction sector	\bar{L}	0.05	0.04

Table 1: Targeted moments in calibration corresponding to model parameters.

Aggregate shocks: The economy has aggregate shocks to income $\Theta(Z)$ and credit con-

ditions $\mathcal{C}(Z) = \{\theta^{LTV}(Z), \theta^{PTI}(Z), \kappa^m(Z), \zeta^m(Z)\}$. Aggregate income follows a two-state Markov chain with values $\{\Theta(Z_{low}), \Theta(Z_{high})\}$ following a discrete approximation of an AR(1) process estimated from a linearly de-trended series of total U.S. labor productivity. The accompanying transition probabilities $\pi_{Z,Z'}^\Theta$ are similarly obtained from the Markov chain approximation.

Aggregate credit conditions loosen via a one-time unanticipated shift to characterize the onset of the housing boom in the 1990s. They are represented by perfectly correlated movements in the loan-to-value constraint $\theta^{LTV}(Z)$, payment-to-income-constraint $\theta^{PTI}(Z)$, the fixed mortgage origination cost $\kappa^m(Z)$, and the mortgage intermediation wedge $\zeta(Z)$. Although higher loan-to-value constraints are the most common representation of looser credit conditions in macro housing models, other innovations in mortgage finance also played a role in extending relatively more credit to households and are hence included.¹⁶ Dokko et al. (2019) find that 60 percent of all mortgages contained at least one non-traditional feature by 2005 and Greenwald (2018) and Ma and Zubairy (2020) show that payment-to-income constraints $\theta^{PTI}(Z)$ are quantitatively more important than loan-to-value constraints $\theta^{LTV}(Z)$ in accounting for mortgage debt throughout the 2000s.

The loan-to-value constraint is equal to 0.95 in the low state which is slightly higher than Duca et al.’s (2011) estimates for cumulative loan-to-value ratios of first-time home buyers in the 1990s. Following Kaplan et al. (2020), the value 0.95 replicates the 90th percentile of the loan-to-value distribution observed in the pre-boom data. The high state value of 1.1 targets a 15 percentage point rise in combined loan-to-value ratios from the late 1990s to 2006. The payment-to-income constraint values are $\theta^{PTI}(Z_{high}) = 0.5$ and $\theta^{PTI}(Z_{low}) = 0.25$, which are slightly lower than the values of Greenwald (2018) to account for the life-time amortization of mortgages being longer than the typical 30 years. Falling financial intermediation and funding costs are represented by a decrease in the fixed mortgage origination costs $\kappa^m(Z)$ from \$2,000 to \$1,200 as described by Favara and Imbs (2015) and a decrease in the mortgage intermediation wedge $\zeta^m(Z)$ from 100 basis points to 60 basis points capture as described by Arslan et al. (2022).

Beliefs: This paper’s contribution of endogenous beliefs via adaptive learning introduces three parameters that affect the formation of house price expectations.

First, the learning gain g_t assigns the speed at which agents update their beliefs with

¹⁶Loan-to-value constraints also make the households’ problems well defined as explained by Engelhardt (1996). Along with Kiyotaki et al. (2011), Engelhardt (1996) notes that loan-to-value constraints are a reduced-form representation of contract enforcement frictions in credit markets. Because lenders fear that borrowers might not repay mortgages, they can distribute some of the downside risk by requiring the house to be pledged as collateral and forcing borrowers to hold equity via loan-to-value constraints.

Interpretation	Parameter	Value
Aggregate income $\Theta(\mathbf{Z})$		
Aggregate income	$\{\Theta(high), \Theta(low)\}$	$\{1.035, 0.965\}$
Transition probability	$\pi_{h,h}^\Theta = \pi_{l,l}^\Theta$	0.9
Aggregate credit conditions $\mathcal{C}(Z)$		
Loan-to-value ratio	$\{\theta^{LTV}(loose), \theta^{LTV}(tight)\}$	$\{1.1, 0.95\}$
Payment-to-income ratio	$\{\theta^{PTI}(loose), \theta^{PTI}(tight)\}$	$\{0.5, 0.25\}$
Fixed origination cost	$\{\kappa^m(loose), \kappa^m(tight)\}$	$\{\$1,200, \$2,000\}$
Proportional origination cost	$\{\zeta(loose), \zeta(tight)\}$	$\{0.006, 0.010\}$
Beliefs/learning		
Constant gain	$g_t = g$	0.508
Initial learning coefficients	$\mathbf{a}_0 = \mathbf{a}_{Z_{high}, Z'_{high}}^{tight}$	$\{-0.102, 0.838\}$

Table 2: Parameters for aggregate shocks to income and credit conditions along with those for endogenous beliefs characterized via adaptive learning. The model period is two years and values are not annualized.

incoming information. Following Marcet and Nicolini (2003) and Milani (2014), a mixed gain specifies a constant gain $g_t = g$ in boom states so that beliefs are updated more aggressively to more recent house price observations and a decreasing gain $g_t = g_{t-1}/(g_{t-1} + 1)$ in non-boom states so that beliefs more closely track the sample mean of house price observations. The aggregate states characterized by loose credit conditions (with either high or low income) are the boom states with constant gain and all other states are the non-boom states with a decreasing gain.

A mixed gain has the benefit of rapid adjustments in boom states and dampened oscillations in non-boom states. Updating beliefs about future house prices $\mathbf{a}_{\mathcal{Z},t}$ aggressively with incoming information under a constant gain is useful in the boom states when agents have limited knowledge about the true values of beliefs $\mathbf{a}_{\mathcal{Z}}$ and thus the sample mean of house prices, $\mu_{\mathcal{Z}}^p = a_{\mathcal{Z}}^0/(1 - a_{\mathcal{Z}}^1)$. If agents interpret large forecast errors as a signal that their beliefs are far from the sample mean of house prices, it may be advantageous to adjust their beliefs as quickly as possible in the direction of the forecast error, as prescribed by the constant gain. By contrast, aggressive belief updating in non-boom states may assign too much signal to noisy observations that are far from the sample mean. Consequently, because the decreasing gain puts successively less weight on recent observations, beliefs are less likely to assign much signal to new information. Although decreasing gain learning can potentially guarantee convergence to a rational expectations equilibrium, the Krusell and Smith (1998) approximate equilibrium solved for in this paper may not necessarily be a true rational expectations equilibrium, and convergence may only be to an ergodic distribution.

Following Caines (2020), this paper calibrates the housing boom’s constant gain $g_t = g$ for the boom states by minimizing the difference between mean squared house price forecast errors from the model and an empirical proxy constructed from the University of Michigan Survey of Consumers detailed in Appendix D and shown in Figure (2). Even though series of expected house prices are only available at the end of the housing boom in 2007, the “next 12 months” expectations series has a 0.92 correlation with a series on selling conditions that dates back to 1992. As a result, backcasting the shorter expectations series from the longer selling conditions series can deliver a proxy of house price expectations throughout the 2000s.

Besides the high correlation, why can one intuitively think of selling conditions as a proxy for expectations? The link between the two series comes from a housing asset valuation equation like that in Famiglietti et al. (2023) shown in equation (17) where the price of housing $p(\mu, Z)$ is equal to the cashflow of rents $\rho(\mu, Z)$ and the discounted expected capital gain from selling next period $p'(\mu'; \mathcal{Z})$.¹⁷ Suppose $p'(\mu; \mathcal{Z}) = \exp(a_{\mathcal{Z},t}^0 + a_{\mathcal{Z},t}^1 \log p_{\mathcal{Z},t})$ as in equations (15)-(16), then as beliefs $(a_{\mathcal{Z},t}^0, a_{\mathcal{Z},t}^1)$ become more optimistic, expected future capital gains from selling housing necessarily rise as well.

$$p(\mu, Z) = \rho(\mu, Z) + \mathbb{E}_{Z', \epsilon' | Z, \epsilon} \left[\frac{p'(\mu'; \mathcal{Z})}{1 + r_b} \right] \quad (17)$$

The proxy for house price expectations constructed from the backcast of selling conditions and its counterpart of expected house price growth for the next 5 years were both elevated in the 2000s housing boom, as shown in Panel (2a). As a result, the forecast errors used to calibrate the constant learning gain $g_t = g$ are large and have a steady upward path following that of house prices as shown in Panel (2b).¹⁸ Mian and Sufi (2022) show somewhat contradictory evidence that all but optimistic marginal home buyers thought it was a bad time to buy a house in the later part of the boom using 1) disaggregated data from the University of Michigan Survey of Consumers and 2) survey data from Case et al. (2012). However, Appendix F.5 confirms their evidence and shows that model-generated endogenous beliefs would have eventually become endogenously pessimistic had credit conditions stayed looser for longer.

With an annualized value of about $g = 0.3$ (0.508 non-annualized), this paper’s constant gain is on the larger end of values typically found elsewhere in the literature. Milani (2014) notes that when forecast errors are large, agents may be concerned that the economy is experiencing a structural break and assign a large weight to incoming information and hence

¹⁷This valuation equation is a simpler version of the housing demand equation for an unconstrained household who buys a house in this period and sells it next period as in equation (6).b in Appendix A.1.

¹⁸Appendix F.4 shows that housing boom simulations are similar with a decreasing learning gain that does not rely on this calibration.

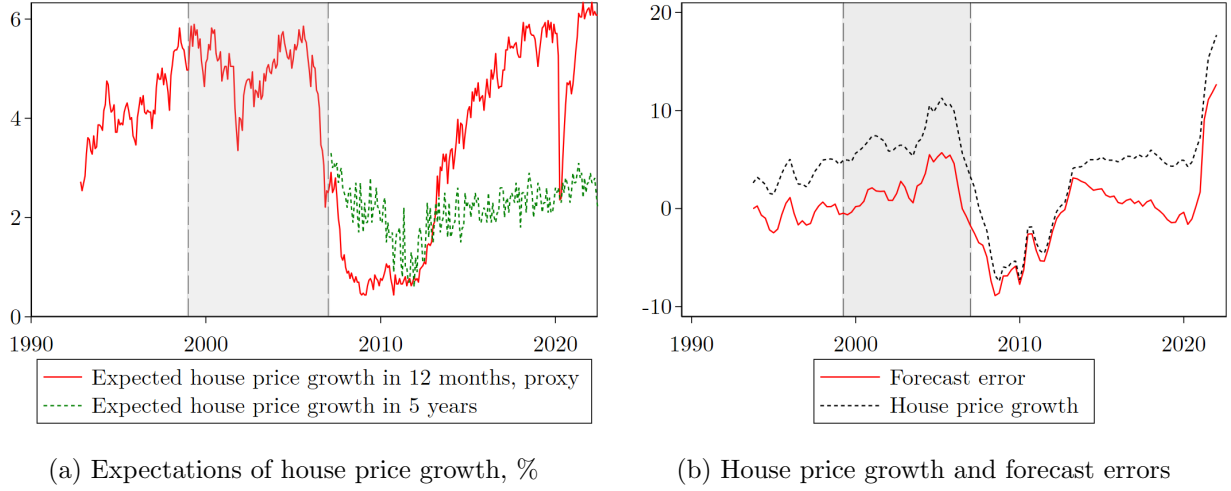


Figure 2: 12-month percent change in expected house price growth and 4-quarter percent change in house price growth with forecast errors calculated as house price growth less the proxy. Shaded bar between the dashed vertical lines marks the U.S. housing boom (1999 to 2007).

a high value for the constant gain. Caines (2020), Adam et al. (2012), Adam et al. (2024) use annualized gains of about 0.03 to 0.06 in their applications of adaptive learning to housing. These smaller values may arise from 1) agents learning about house price growth instead of house price forecasting coefficients and 2) differences in house price expectations used in calibration. For example, both Caines (2020) and Adam et al. (2024) use post-boom house price expectations from the Case-Shiller house price futures or the Michigan Survey. On the other hand, Marcet and Nicolini (2003) estimate an annualized constant gain ranging from 0 to 0.5 in boom-like settings, Milani (2014) estimates constant gains ranging from 0.21 to 0.32, and Carvalho et al. (2023) close to 0.45 at an annualized frequency. Taken together, this evidence suggests that an annualized constant gain of about 0.3 is high but still within an established range of values.

The decreasing gain $g_t = g_{t-1}/(g_{t-1} + 1)$ only affects the non-boom states and is initialized at $g_t = g/(1 + t \times g)$ which follows the convention of Marcet and Nicolini (2003) and Milani (2014) plus a decay parameter $t = 5$ that takes into account the number of periods since the start of the housing boom and thus limited knowledge about the evolution of house prices. Appendix F.5 discusses simulations without the decay parameter.

The second and third learning parameters are contained in the vector of initial learning coefficients \mathbf{a}_0 . These parameters determine the initial forecast error and there is no definitive convention, as noted by Lubik and Matthes (2016). Using the known pre-boom coefficients for tight aggregate credit conditions and the high income state $\mathbf{a}_{Z_{high}, Z'_{high}}^{tight}$ as initial beliefs for the boom state leads to an initial forecast error of 1 percent which is close to its empirical value of 1.36 percent. Appendix F.3 shows that the results are similar if the constant

coefficient a_0^0 is adjusted so that the initial forecast error attains a value of 1.36, while leaving the slope coefficient unchanged at $a_0^1 = a_{Z_{high}, Z'_{high}}^{1, tight}$. Furthermore, results are similar if the slope coefficient is adjusted and the constant coefficient is unchanged. As a sensitivity check, Appendix F.3 also shows that the housing boom dynamics are broadly similar if either coefficient is adjusted so that the initial forecast error is 1.5 times its empirical value.

4.2 Calibration

See Appendix C.2 for an in depth discussion of the cross-sectional distribution of households in the model’s stochastic steady state which assumes known forecasting coefficients, tight aggregate credit conditions, and fluctuations in aggregate income.

Parameter	Empirical Value	Model Value
Fraction of homeowners with a mortgage	0.66	0.65
Fraction of homeowners with a HELOC	0.06	0.02
Aggregate mortgage debt/housing value	0.42	0.48
P10 LTV ratio for mortgages	0.15	0.02
P50 LTV ratio for mortgages	0.57	0.5
P90 LTV ratio for mortgages	0.92	0.85
Share of NW held by bottom quintile	0	0
Share of NW held by middle quintile	0.05	0.09
Share of NW held by top quintile	0.81	0.66
Share of NW held by top 10 percent	0.7	0.43
Share of NW held by top 1 percent	0.46	0.06
P10 house value/earnings	0.9	0.94
P50 house value/earnings	2.1	1.8
P90 house value/earnings	5.5	4.1

Table 3: Untargeted moments in calibration.

Table (3) shows a comparison of untargeted moments from the model to their empirical counterparts. The model matches the distributions of homeownership and mortgage debt shown in the top panel and the bottom 90th percentile of the wealth distribution shown in the bottom panel. As is common in models with heterogeneous households, the top 10th percentile of the model’s wealth distribution is far below that of the data because wealthy households can only hold housing or liquid financial instruments and thus accumulate a counterfactually high share.¹⁹ Appendix C.3 discusses the assumption on the partial segmentation of housing unit sizes by renters and homeowners.

¹⁹Although allowing for risky assets with heterogeneous returns is a solution proposed by Cioffi (2021) and Xavier (2021), it is beyond the scope of this paper as it would complicate how a shift in beliefs affects house prices. Relatedly, adding two types of discount factors could better capture the right tail of the wealth distribution, solving a Krusell and Smith (1998) with two discount factors could lead to multiple equilibria, convergence issues, or numerical accuracy where an AR(1) forecasting rule for house prices may not be enough moments to pin down the evolution of house prices.

5 Housing Boom Simulations

The housing boom is initiated by a sequence of aggregate shocks to income and credit conditions, as shown in panel (3a). In 1999, aggregate income (solid blue lines) transitions from the low state to the high state and aggregate credit conditions (dotted red lines) unexpectedly loosen in 2001 which is when adaptive learning about house price forecasting coefficients begins.²⁰ After remaining in this boom state with high income and loose credit conditions for 4 periods (8 years), aggregate income transitions back to the low state and aggregate credit conditions unexpectedly tighten back to their pre-boom values. The housing boom is thus a period where agents do not anticipate looser credit conditions, but then expect them to stay in place permanently.²¹

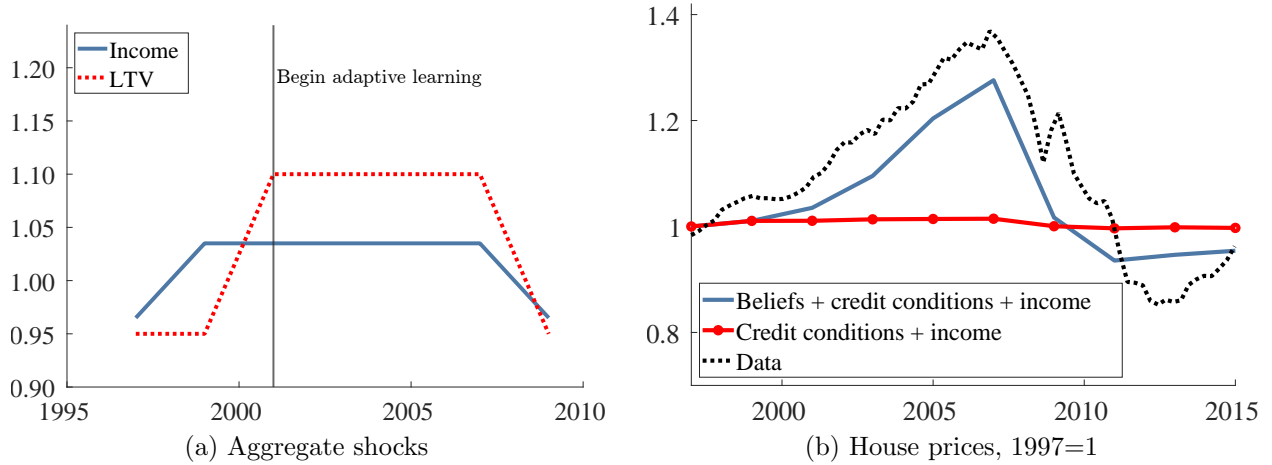


Figure 3: Aggregate shocks and house prices. Aggregate shocks correspond to values in table (2) for 1997-2009. House prices from the data and the model solved under endogenous beliefs. See Appendix G for sources and definitions of the data series.

Panel (3b) shows that optimistic beliefs along with shocks to income and credit conditions (solid blue lines) can match the boom in U.S. house prices in the 2000s. Aggregate house prices peak 35 percent and 28 percent above their pre-boom values in the data and the model, respectively. The path of house prices generated by the model closely tracks that of the data, which results in the model matching additional features of aggregate house price data such as 96 percent of the autocorrelation and 89 percent of the standard deviation. Key to the model generating any volatility in house prices—let alone matching successfully matching the data—is partial updating of endogenous beliefs via adaptive learning. Given that agents can

²⁰Appendix F.5 shows that the results are similar if adaptive learning instead begins at the start of the model simulation instead of in 2001.

²¹Appendix E shows credit conditions evolving via a one-time shock or a Markov process has little effect on the housing boom simulations under exogenous beliefs. A one-time shock is therefore assumed under both exogenous and endogenous beliefs.

only partially internalize the increase in aggregate demand when credit conditions loosen, house prices come in higher than expected, which results in a positive forecast error that is interpreted as signal that beliefs were too low and results in even more optimistic beliefs.

By contrast, panel (3b) shows that shocks to income and credit conditions without endogenous beliefs (red lines with circles) results in only an incremental increase house prices and almost no volatility. Because demand for housing services—and hence house prices—is generally determined by income, the 7 percentage point increase in aggregate income shown in panel (3a) is not large enough to generate the nearly 35 percentage point increase in house prices shown in panel (5a). Relatedly, the increase in housing demand from looser credit conditions is limited to only a fraction of households due to heterogeneous incomes and ages. Because these constrained households tend to be younger and buy the same size of house they were renting when credit conditions loosen in this framework, overall demand for housing services only increases slightly, which results in almost no increase in house prices.²² As will be discussed and is shown by Ma and Zubairy (2020), looser credit conditions are important for accounting for homeownership dynamics across the age distribution. Appendix F.1 shows additional simulations such as those with just beliefs and no shift in credit conditions.

If the economy did not revert back to the non-boom state in 2009 agents would become pessimistic about future house prices leading to an endogenous housing bust, as shown in Appendix F.5. When the boom states persist beyond 2009, beliefs eventually turn pessimistic as agents realize that they were too optimistic given that aggregate demand for housing services only increased slightly in response to looser credit conditions. However, in the simulations shown in figure (3) the bust in house prices is attributed to the contraction of aggregate states instead of an endogenous self-correction of over optimism. Additionally, Appendix F.6 shows that beliefs do eventually converge to an ergodic distribution in a longer simulation with a counterfactual recurrence of the housing boom state.

How closely model generated house prices match the data depends on the constant gain parameter g as shown in Panel (4a). Although house prices steadily rise under all values of the constant gain g shown, a smaller constant gain results in a more muted housing boom while a larger constant gain results in one that is more pronounced. There is a positive correlation between the constant gain and house price growth because the constant gain determines the speed at which agents incorporate new information into their beliefs—a larger value of the constant gain g thus updates beliefs more aggressively.

Empirical house price forecast errors constructed from the proxy of the University of

²²Greenwald and Guren (2024) show that this is not a general result and frameworks that incorporate endogenous investment in the housing stock along with landlord heterogeneity can generate higher house prices from looser credit conditions.

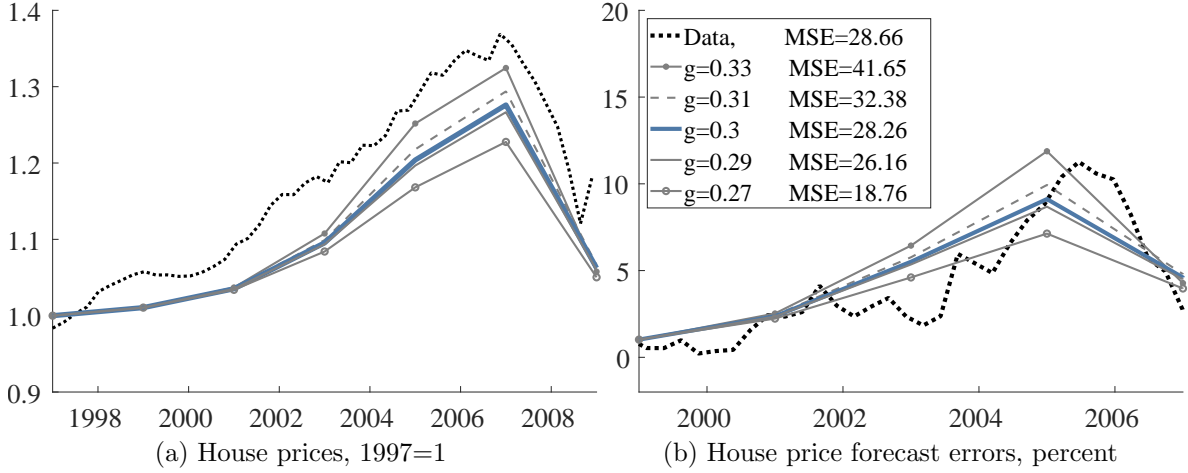


Figure 4: House prices and forecast errors from the data and model solved under endogenous beliefs. The model’s forecast error is $\log p_t - \mathbb{E}_{t-1}[a_{Z,t-1}^0 + a_{Z,t-1}^1 \log p_{t-1}]$. The parameter g is the learning gain and is annualized in the legend. See Appendix G for sources and definitions of the data series and Appendix D for details on the construction of the proxy for empirical forecast errors from University of Michigan Survey of Consumers.

Michigan Survey of Consumers are persistently positive throughout the 2001 to 2007 period, as shown in panel (4b) via the dotted black line. Under all values of the constant gain g shown, forecast errors are positive and match the upward path observed in the data, but with less volatility due to their observation at a lower two year frequency.²³ Agents underpredict house prices because their initial beliefs do not fully internalize the increase in housing demand from looser credit conditions. Since beliefs are combination of past values and recent forecast errors, partial updates of large positive forecast errors can result in persistently underpredicted house prices and positive forecast errors. At 28.66, the mean squared error for the annualized constant gain $g = 0.2986$ ($g=0.508$ at a two-year frequency) is the closest fit to the data and hence used in the main results.²⁴

This paper’s finding that beliefs can account for the 2000s housing boom has also been shown by Kaplan et al. (2020), but under exogenous instead of endogenous beliefs. I next compare how model prices, forecast errors, and quantities evolve under different types of belief formation and finds many similarities. Despite these similarities, section 5.1 shows that belief formation matters for the effectiveness of policy interventions.

Under either the endogenous beliefs of this paper or the exogenous beliefs of Kaplan et al. (2020), the housing boom is initiated by the same sequence of aggregate shocks to

²³Because it is unclear if it is better to aggregate via end of period observations or averages, I do not transform the quarterly data to a 2-year frequency.

²⁴Because the data used to calibrate the constant gain g is only an empirical proxy there could be concerns about measurement noise that biases results. However, Appendix F.4 shows that the housing boom simulation results are similar if a decreasing learning gain that does not rely on data constructed from an empirical proxy is used instead.

income and credit conditions shown in panel (3a). Under exogenous beliefs, there is no adaptive learning but a third shock to housing preferences that occurs in 2003 in the period following the shift in credit conditions in 2001. While the housing preference parameter ϕ is fixed under endogenous beliefs it evolves according to a three state Markov process under exogenous beliefs. In the first state, it is at its low value and has zero probability of shifting to its high value. In the second state, it also has its low value but has a probability of 0.85 to shift to its high value. This second state where a shift to the high value is likely is the exogenous shift in beliefs that accounts for higher house prices observed in panel (5a).

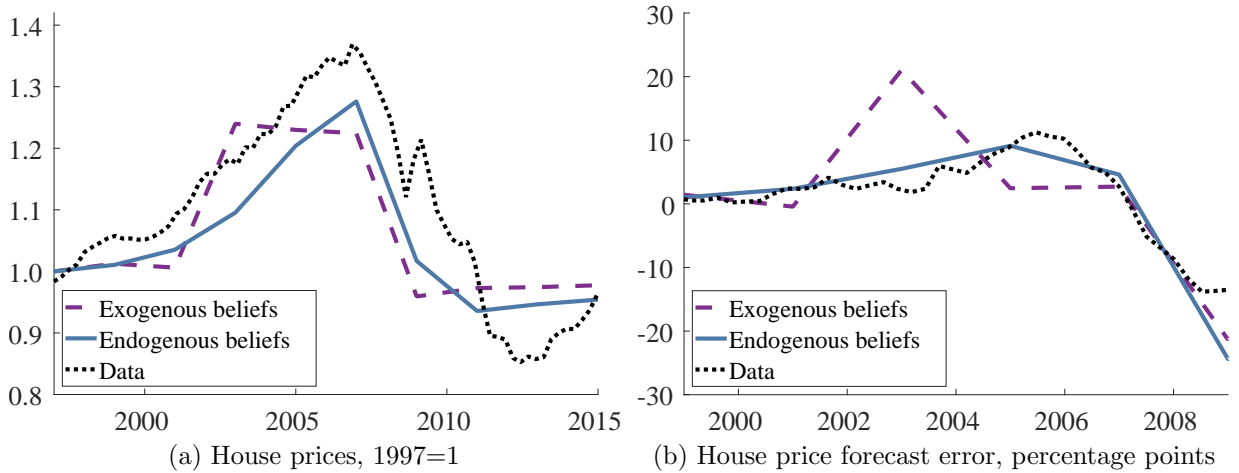


Figure 5: House prices and forecast errors from the data and the model solved under endogenous beliefs and exogenous beliefs. The model's forecast error is $\log p_t - \mathbb{E}_{t-1}[a_{Z,t-1}^0 + a_{Z,t-1}^1 \log p_{t-1}]$. See Appendix G for sources and definitions of the data series and Appendix D for details on the construction of the proxy for empirical forecast errors from University of Michigan Survey of Consumers.

	St. dev., σ_{p_t}	$\frac{\sigma_{p_t}}{\sigma_{data}}$	Autocorr., $\rho(p_t, p_{t-1})$	$\frac{\rho(p_t, p_{t-1})}{\rho_{data}}$
Exogenous beliefs, 2003-2007	0.020	16%	0.325	71%
Exogenous beliefs, 1999-2007	0.152	115%	0.225	39%
Endogenous beliefs, 1999-2007	0.113	89%	0.440	96%
Data, 1999-2007	0.127	100%	0.458	100%

Table 4: Biannual house prices statistics from the data and model for the U.S. housing boom.

Model generated house prices under exogenous beliefs (dashed purple lines) peak just under the 28 percent peak of their counterparts generated under endogenous beliefs (solid blue lines), as shown in panel (5a). However, instead of steadily rising path like that under endogenous beliefs, exogenous beliefs generate a counterfactual jump in a single period. As a result, table (4) shows that exogenous beliefs severely undershoot or overshoot the auto-

correlation and standard deviation of aggregate house prices, while the fit under endogenous beliefs is 96 percent and 89 percent, respectively. The house price forecast errors shown in panel (5b) provide external empirical validation: while forecast errors are positive and persistent under endogenous beliefs as in the data, they display a counterfactual sign change and are negative in all periods except for 2003 under exogenous beliefs.

Given that endogenous beliefs generate house prices that match the path, autocorrelation, and standard deviation of the house price data while also matching empirical forecast errors, this paper next investigates how endogenous beliefs affect the homeownership rate which is a key determinant of housing demand and hence house prices.

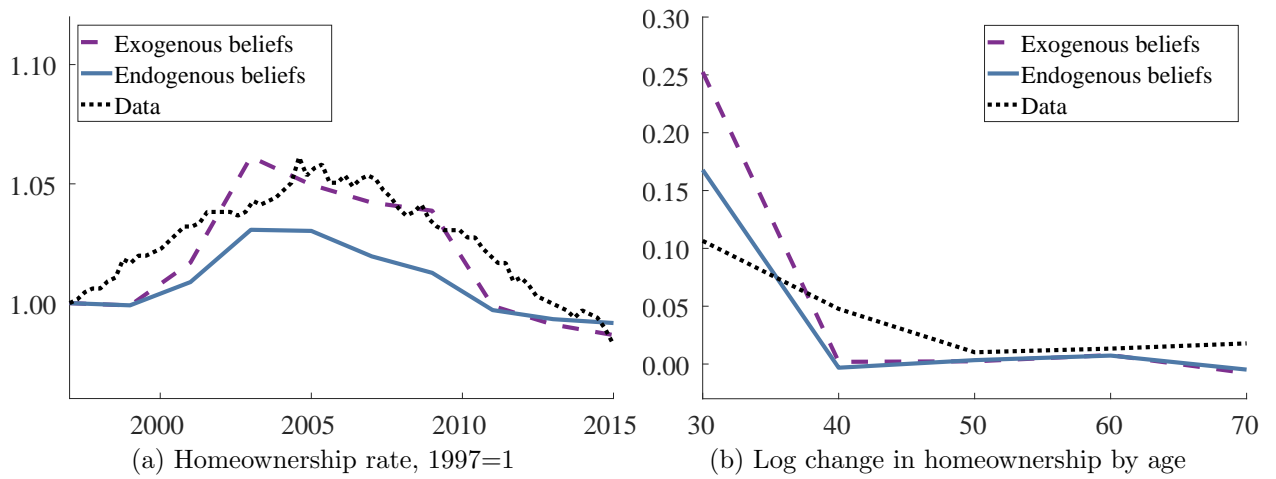


Figure 6: The homeownership rate from the data and the model solved under endogenous and exogenous beliefs. See Appendix G for sources and definitions of the data series.

Figure (6) shows that the homeownership rate largely matches its empirical counterpart over time and in the cross section. Panel (6a) shows that the aggregate homeownership rate under endogenous beliefs captures the gradual rise and decline of the path and about half of the peak observed in the data throughout the boom. Although there is a more pronounced initial jump in the homeownership rate under exogenous beliefs, the simulations are quite similar with either type of belief formation. The increase in the homeownership rate in both the model and the data is mostly driven by households under the age of 40 purchasing homes as shown in panel (6b). The size of this increase in homeownership among these young households in panel (6b) is reflected in the aggregate homeownership in panel (6a). Looser credit conditions allow a larger fraction of young households to overcome payment-to-income and loan-to-value constraints earlier in life than under tighter credit conditions. New homeowners tend to purchase the same sized housing unit they were previously renting, which results in slightly more aggregate demand for housing services and only accounts for a small fraction of the increase in house prices. Higher house prices can mostly be attributed

to unconstrained household upsizing their housing units in response to wealth effects from higher expected future house prices.

Figure (7) shows that other prices and quantities also match the data under either exogenous or endogenous beliefs. Matching the volatility of house prices under endogenous beliefs leads to the rent-price ratio and aggregate consumption better matching the path observed in the data which is useful for understanding the consumption response to house prices.

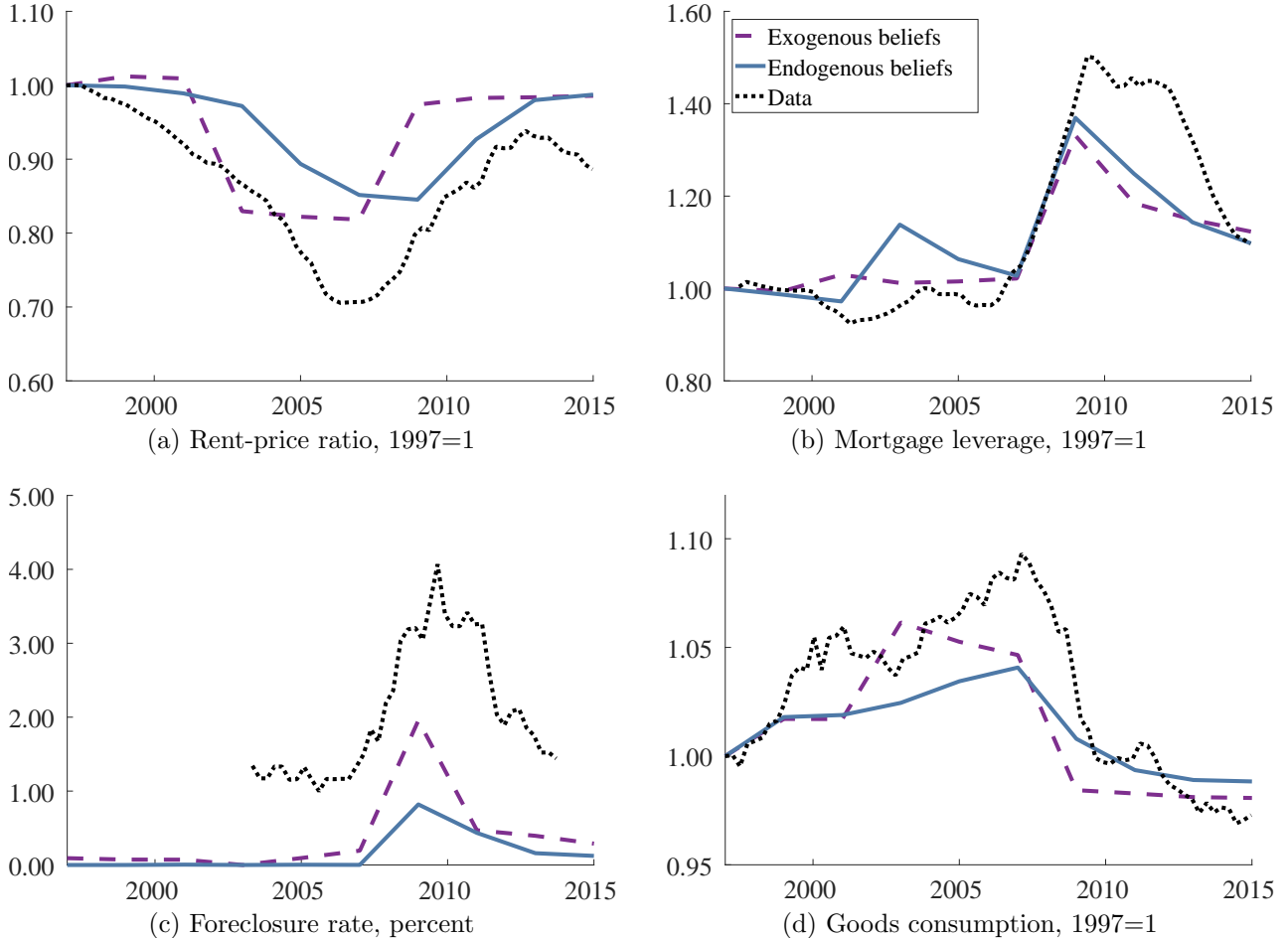


Figure 7: Housing boom prices and quantities from the data and the model solved under endogenous and exogenous beliefs. See Appendix G for sources and definitions of the data series.

Panel (7a) shows that the decline in the rent-price ratio under either exogenous or endogenous beliefs matches about half of the decline observed in the data. Although most models of housing succeed at generating an increase in prices and homeownership, it is often at the expense of counterfactually rising rents. The rental rate in equation (13) shows that high expected future house prices—like those from optimistic beliefs—are key to rents decreasing and thus a drop in the rent-price ratio. When model generated house prices more closely track their counterparts in the data, as under endogenous beliefs, the model

generated rent-price ratio also better tracks its empirical counterpart.

Greenwald and Guren (2024) show that the tenure supply elasticity—the elasticity of house prices to credit supply shocks divided by the elasticity of homeownership to credit supply shocks—is an empirically important moment for understanding the effects of credit conditions on house prices. Dividing the peak percentage point increase in the price-rent ratio (27 p.p.) by that of the homeownership rate (3.1 p.p.) under the endogenous beliefs proposed by this paper delivers a ratio 8.9 which is close to that observed in the data of 11 (70 p.p. peak in the price-rent ratio divided by a 6 p.p. peak in the homeownership rate). While the ratio under endogenous beliefs is closer to the no segmentation case of Greenwald and Guren (2024), it is in line with their empirical estimates of at least 3.8

Panel (7b) shows that modeled generated mortgage leverage remains near its pre-boom values throughout most of the boom and then rises in the bust, similar to what is observed in the data. The only shortcoming of endogenous beliefs is a counterfactual one-time jump during the boom that is not present in their exogenous beliefs counterparts.

The model’s foreclosure rate shown in Panel (7c) rises in 2009 when income contracts and credit conditions tighten in the bust. The rise in the foreclosure rate is smoother under endogenous beliefs relative to exogenous beliefs reflecting a smoother path of house prices rather than a one-time jump under exogenous beliefs.

Finally, panel (7d) shows that optimistic beliefs and higher house prices generate a path of consumption that matches about half of the peak in the data with a path that gradually rises throughout the boom, as observed empirically. In line with a housing wealth effect, the paths of consumption under either exogenous or endogenous beliefs show a strong correlation with the respective paths of house prices.²⁵ The model under endogenous beliefs can thus better match the data’s steady rise in the path of goods consumption due to its corresponding steady rise in house prices.

5.1 Policy counterfactuals

Although model generated house prices under endogenous beliefs are validated by external empirical evidence and match many features of house prices beyond the level increase, other prices and quantities from the model are quite similar under either type of belief formation. This section addresses the implications of belief formation by showing that endogenous beliefs are more sensitive to prudential policy interventions than their exogenous counterparts. These findings stem from two counterfactual scenarios during the house boom, one where interest rates increase and another where credit conditions tighten during the housing.

²⁵The size of the housing wealth effect remains debated. While Berger et al. (2018) find large consumption responses to house price movements, Guren et al. (2020) note that responses in the 2000s are smaller than those of the 1980s.

Using monetary policy to “lean against” rising house prices has been studied as a prudential policy for housing boom management because higher policy rates push up mortgage rates, thereby dampening demand for housing services. However, because higher interest rates also 1) dampen output along with house prices and 2) may make homeownership less affordable, researchers have cautioned that lowering house prices may be too costly [Benati (2021), Lambertini et al. (2013), Ehrenbergerova et al. (2021), Svensson (2017)]. On the other hand, researchers have also shown that leaning against house prices maybe optimal when knowledge is limited [Caines and Winkler (2021) and Adam and Woodford (2021)].

The higher interest rate scenario relies on the same aggregate shocks as the main housing boom simulation shown in panel (3a), along with an additional unexpected shock to the risk-free rate that occurs in 2001 when credit conditions loosen. More specifically, the risk-free rate r_b rises 50 basis points from 3 percent to 3.5 percent on an annual basis resulting in the mortgage rate $r^m = (1 + \iota)r_b$ rising from 4 percent to 4.5 percent on an annual basis.

Figure (8) shows that house prices under endogenous beliefs are much more sensitive to a 50 basis point increase in the risk-free rate than their exogenous counterparts. In fact, the thin solid blue line in panel (8a) shows a bust instead of a boom. House prices drop because of pessimistic beliefs—the decrease in demand for housing services from higher interest rates leads to a negative forecast error that persists due to the slow updating of beliefs under adaptive learning, as shown in panel (8b). By contrast, under exogenous beliefs house prices and forecast errors are little different in the scenario with higher interest rates (thin dashed purple lines) relative to the main simulation (thick dashed purple lines). Because exogenous beliefs rely on households pulling forward higher expected demand for housing services that never materializes, house prices will only be substantially lower if the dampening effects of higher interest rates can offset these amplifying effects of beliefs. The counterfactual shows that this unlikely with only a 50 basis point increase in interest rates.

Raising interest rates to lean against high house prices is one of many prudential policies in housing boom management. Statutory borrowing limits on loan-to-value ratios and payment-to-income ratios are more widely studied as these policies directly limit leverage, thereby reducing demand for housing services and decreasing house prices [Kelly et al. (2018), Fuster and Zafar (2016), and Bolliger et al. (2025)]. However statutory borrowing limits may be costly for younger and less well-off borrowers who remain renters for longer [Gete and Reher (2016), Carozzi (2019), and others].

The statutory tighter credit conditions scenario is the same as the main housing boom simulation shown previously, but with credit conditions tightening in 2005 instead of 2009. This scenario can be interpreted as one where innovations in mortgage finance allow for looser credit conditions, but the government reacts by imposing statutory limits at pre-boom values.

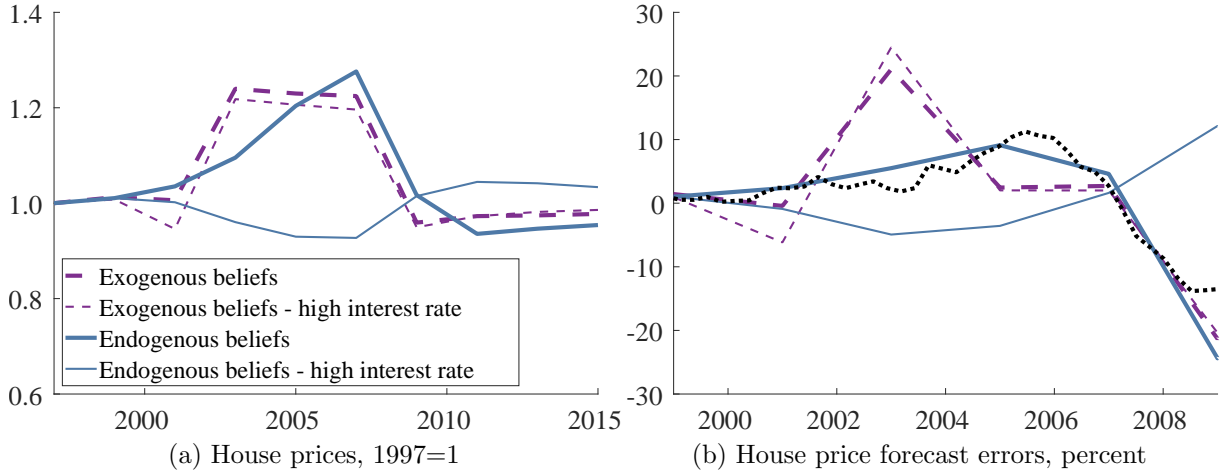


Figure 8: House prices and forecast errors with counterfactually higher interest rates. The model's forecast error is $\log p_t - \mathbb{E}_{t-1}[a_{Z,t-1}^0 + a_{Z,t-1}^1 \log p_{t-1}]$.

Figure (9), like figure (8), shows that house prices are more sensitive to macroprudential policy under endogenous belief than under exogenous beliefs. Under endogenous beliefs, house prices begin to contract as credit conditions tighten, as shown via the thin solid blue line in panel (9a). When house prices are high and credit conditions tighten, households that are younger and with relatively lower income can no longer afford to become homeowners thereby dampening demand for housing services. The decrease in house prices pushes down the house price forecast error, as shown in panel (9b), which then dampens house prices. By contrast, under exogenous beliefs there is little difference between the simulations when credit conditions contract earlier in the boom (thin and thick dashed purple lines).

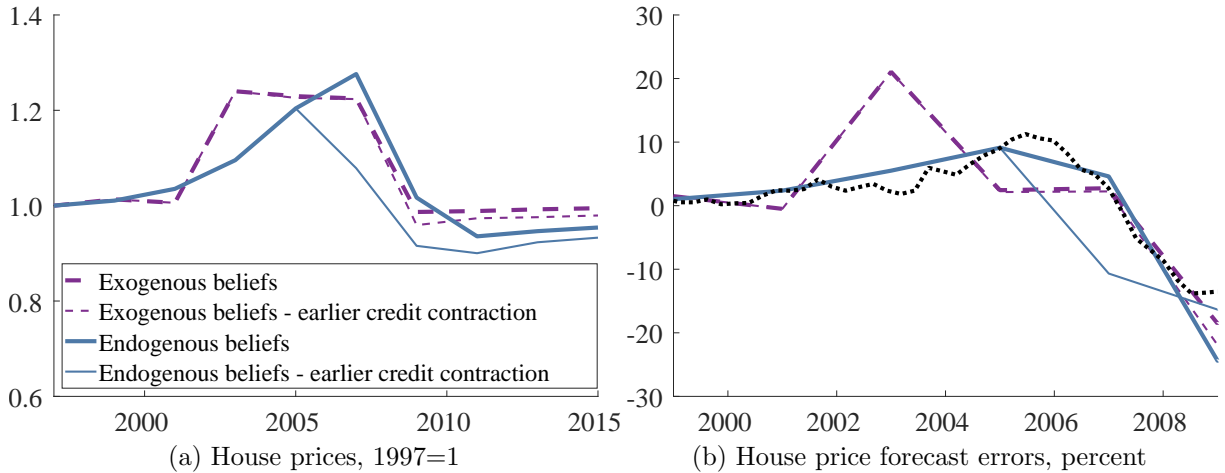


Figure 9: House prices and forecast errors with counterfactually tighter credit conditions midway through the boom. The model's forecast error is $\log p_t - \mathbb{E}_{t-1}[a_{Z,t-1}^0 + a_{Z,t-1}^1 \log p_{t-1}]$.

The two counterfactual scenarios studied have several caveats. First, the model is assumed to be a small open economy where interest rates are taken as given and fixed rather

than endogenously responding to macroeconomic conditions as they would in other settings. Second, the rich household heterogeneity along with incomplete markets and aggregate risk necessitates simplifying some of the general equilibrium feedback from other sectors of the economy. Nonetheless, these counterfactual scenarios show that belief formation affects the sensitivity of house prices to macroprudential policy, which is important for the management of housing booms.

6 Conclusion

This paper presents a one-step solution method to endogenize beliefs about future prices in general equilibrium models with incomplete markets and aggregate risk. In an application to the U.S. housing boom of the 2000s, this method allows me to address 1) *why* beliefs about future house prices shifted in the early 2000s to push up house prices and 2) how belief formation affects prudential policy.

First, this paper shows that limited knowledge of the evolution of house prices in an economic expansion with loose credit conditions can account for optimistic beliefs. When agents underpredict future house prices and update their beliefs via adaptive learning, the model generates persistently positive forecast errors that are externally validated with empirical evidence obtained via a novel proxy developed from the University of Michigan Survey of Consumers. The resulting model-generated house prices match the time path, autocorrelation, and standard deviation of empirical aggregate house prices in addition to the level increase. As noted by Piazzesi and Schneider (2016), existing models typically struggle to generate any volatility in house prices, let alone match the high volatility of house price data.

Next, this paper shows that the effectiveness of prudential policies can depend on belief formation. Prudential policies like higher interest rates or tighter credit conditions can dampen endogenously formed optimistic beliefs such that the boom in house prices is shorter or non-existent. By contrast, these policies have little material effect on house prices under exogenously optimistic beliefs. Because raising interest rates may lower output, and tightening credit conditions decrease homeownership, studying the effectiveness of these policies is important for understanding when benefits outweigh costs.

Finally, this paper’s contribution of a one-step solution method to endogenize beliefs in a model with incomplete markets and aggregate risk can generalize to settings beyond adaptive learning and the 2000s housing boom. For example, an unexpected shift to an economic state without precedent could describe events such as the onset of the COVID-19 pandemic in 2020 where house prices also boomed.²⁶

²⁶Loewenstein and Willen (2024) find that beliefs explain the 2000s boom, but a combination of beliefs and preference for larger house account for that of the 2020s.

A Appendix: Recursive Problems

A.1 Recursive Households' Problem

Households are renters r or homeowners h with distribution $\mu^r + \mu^h = \mu = 1$. In the final period, ($j = J$), all solve the bequest problem. Let $\Upsilon_{j+1|j}(y)$ denote the distribution of $y'|y$ which embeds the Markov transition for the individual shocks $\epsilon_j(z)$ and deterministic χ_j .

Renters' Problem ($j < J$)

Renters have two choices: stay renters or purchase a house and become homeowners.

$$V_j^r(b, y; \mu, Z) = \max\{V_j^{rent}(b, y; \mu, Z), V_j^{own}(b, y; \mu, Z)\} \quad (6)$$

Rent to rent: if renters choose to stay renters, they solve

$$\begin{aligned} V_j^{rent}(b, y; \mu, Z) &= \max_{\{b', \tilde{h}', c\}} \{u_j(c, s) + \beta \mathbb{E}_{Z', \epsilon' | Z, \epsilon} [V_{j+1}^r(b', y'; \mu', Z')]\} \quad (6.a) \\ s.to. \quad c + q_b b' + \rho(\mu, Z) \tilde{h}' &= y - \mathcal{T}(y) + b \\ 0 &\leq b' \\ s &= \tilde{h}' \in \tilde{\mathcal{H}} \\ \mu' &= \Gamma_\mu(\mu; Z, Z') \\ Z' &\sim \Gamma_Z(Z) \\ y' &\sim \Upsilon_{j+1|j}(y) \end{aligned}$$

Liquid financial instruments b , income y , and age j are individual state variables. Rental housing \tilde{h}' costs $\rho(\mu, Z)$ and enters the budget constraint as a cost of foregone consumption.

Rent to own: if renters choose to purchase a house and become homeowners, they solve

$$\begin{aligned} V_j^{own}(b, y; \mu, Z) &= \max_{\{b', h', c\}} \{u_j(c, s) + \beta \mathbb{E}_{Z', \epsilon' | Z, \epsilon} [V_{j+1}^h(b', h', m', y'; \mu', Z')]\} \quad (6.b) \\ s.to. \quad c + p(\mu, Z) h' + q_b b' &= y - \mathcal{T}(y) + b + q_j(b', h', m', y; \mu, Z) m' - \kappa^m(Z) \\ 0 &\leq b' \\ 0 &\leq m' \leq \theta^{LTV}(Z) p_h(\mu, Z) h' \\ \pi_j^{min}(m') &\leq \theta^{PTI}(Z) y \\ s &= \omega h', \quad h' \in \mathcal{H} \\ \mu' &= \Gamma_\mu(\mu; Z, Z') \\ Z' &\sim \Gamma_Z(Z) \\ y' &\sim \Upsilon_{j+1|j}(y) \end{aligned}$$

Where the minimum mortgage payment is defined in equation (4) as:

$$\pi_j^{min}(m) = \left[\frac{r_m(1 + r_m)^{J-j+1}}{(1 + r_m)^{(J-j+1)} - 1} \right] m \quad (4)$$

Renters who purchase a house have the homeowners' continuation value $V_{j+1}^h(b', h', m', y'; \mu, Z)$ which has a state space that also includes the newly originated mortgage m' and the purchased house h' .

Homeowners' Problem ($j < J$)

Homeowners have five options: sell their house and purchase a new house, sell their house and become a renter, default and become a renter, stay in their house and pay their existing mortgage, or stay in their house and refinance a new mortgage. Let $\mathbf{x} \equiv \{b, h, m\}$.

$$V_j^h(\mathbf{x}, y; \mu, Z) = \max \begin{cases} V_j^{sell, buy}(b^n, y; \mu, Z) \\ V_j^{sell, rent}(b^n, y; \mu, Z) \\ V_j^{default}(b, y; \mu, Z) \\ V_j^{stay, pay}(\mathbf{x}, y; \mu, Z) \\ V_j^{stay, refi}(\mathbf{x}, y; \mu, Z) \end{cases} \quad (9)$$

Sell to rent or buy: homeowners who sell their house solve the renters' problem (6) with financial assets b^n equal to one-period liquid financial instruments b plus the equity from the sale of the house—the sale price less housing costs and the outstanding mortgage balance.

$$b^n = b + (1 - \delta_h - \tau_h - \kappa_h)p(\mu, Z)h - (1 + r_m)m$$

Default: homeowners who default become renters, incur a utility penalty ξ , and live in the smallest rental housing unit \tilde{h}^0 . Their property is foreclosed and the lender receives the proceeds from the sale of the housing unit less property taxes and depreciation. In default, depreciation is higher $\delta_h^\delta > \delta_h$.²⁷ Defaulters are not subject to recourse meaning that the lender cannot lay claim to other assets should the housing collateral not cover all of the defaulted mortgage balance.

²⁷As studied by Gabriel et al. (2021), not all defaults lead to foreclosure and there is sometimes a time lag between the two events. A default is failure to meet the terms of mortgage contract and a defaulted mortgage is foreclosed when the homeowner's rights to the property are eliminated. See Fannie Mae's glossary: <https://www.knowyouroptions.com/find-resources/information-and-tools/glossary>.

$$\begin{aligned}
V_j^{default}(b, y; \mu, Z) &= \max_{\{b', c\}} \left\{ u_j(c, \tilde{h}^0) - \xi + \beta \mathbb{E}_{Z', \epsilon' | Z, \epsilon} [V_{j+1}^r(b', y'; \mu', Z')] \right\} \\
s.to. \quad c + q_b b' + \rho(\mu, Z) \tilde{h}^0 &= y - \mathcal{T}(y) + b \\
0 &\leq b' \\
\tilde{h}^0 &= \min \tilde{\mathcal{H}} \\
\mu' &= \Gamma_\mu(\mu; Z, Z') \\
Z' &\sim \Gamma_Z(Z) \\
y' &\sim \Upsilon_{j+1|j}(y)
\end{aligned} \tag{9.a}$$

Stay and pay: homeowners who stay in their house and pay their existing mortgage solve

$$\begin{aligned}
V_j^{stay, pay}(\mathbf{x}, y; \mu, Z) &= \max_{\{b', m', c\}} \left\{ u_j(c, s) + \beta \mathbb{E}_{Z', \epsilon' | Z, \epsilon} [V_{j+1}^h(\mathbf{x}', y'; \mu', Z')] \right\} \\
s.to. \quad c + q_b b' + (\delta_h + \tau_h) p(\mu, Z) h + m(1 + r_m) &= y - \mathcal{T}(y, m) + b + m' \\
\pi_j^{min}(m) &\leq (1 + r_m) m - m' \\
0 &\leq m' \\
-b' &\leq \theta^{HELOC} p(\mu, Z) h \\
s &= \omega h, \quad h' = h \\
\mu' &= \Gamma_\mu(\mu; Z, Z') \\
Z' &\sim \Gamma_Z(Z) \\
y' &\sim \Upsilon_{j+1|j}(y)
\end{aligned} \tag{9.b}$$

Because these homeowners stay in the same house $h' = h$, there is no housing choice. Instead, these homeowners pay the housing depreciation costs and tax $(\delta_h + \tau_h) p(\mu, Z) h$ and a mortgage payment greater than the minimum payment $\pi_j^{min}(m)$ described in equation (4). These homeowners can also borrow against the value of their house in the form of HELOCs.

Stay and refi: homeowners who stay in their house and refinance a new mortgage solve:

$$\begin{aligned}
V_j^{stay,refi}(\mathbf{x}, y; \mu, Z) &= \max_{\{b', m', c\}} \{u_j(c, s) + \beta \mathbb{E}_{Z', \epsilon' | Z, \epsilon} [V_{j+1}^h(\mathbf{x}', y'; \mu', Z')]\} \quad (9.c) \\
s.to. \quad c + q_b b' + (\delta_h + \tau_h) p(\mu, Z) h + m(1 + r_m) &= y - \mathcal{T}(y, m) + q_j(\mathbf{x}', y; \mu, Z) m' - \kappa^m(Z) \\
0 \leq m' &\leq \theta^{LTV}(Z) p_h(\mu, Z) h' \\
\pi_j^{min}(m') &\leq \theta^{PTI}(Z) y \\
-b' &\leq \theta^{HELOC} p(\mu, Z) h \\
s &= \omega h, \quad h' = h \\
\mu' &= \Gamma_\mu(\mu; Z, Z') \\
Z' &\sim \Gamma_Z(Z) \\
y' &\sim \Upsilon_{j+1|j}(y)
\end{aligned}$$

These homeowners stay in their house h and pay housing maintenance costs $(\delta_h + \tau_h)p(\mu, Z)$. They pay off their existing mortgage m with the proceeds of a new mortgage m' that is subject to points $q_j(\mathbf{x}', y; \mu, Z) \leq 1$, the fixed mortgage origination cost $\kappa^m(Z)$, and loan-to-value and payment-to-income constraints described in equations (7)-(8).

Homeowners can thus extract equity from HELOCS or mortgage refinancing which is essentially a cash-out equity extraction because all mortgages amortize at the same rate r_m .²⁸ Because mortgage refinancing requires the payment of fixed origination cost $\kappa^m(Z)$ and mortgage points $q_j(\mathbf{x}', y; \mu, Z)$, it is preferred to HELOCS when homeowners are extracting relatively large amounts of equity or have a higher income such that $q_j(\mathbf{x}', y; \mu, Z)$ is closer to 1. Otherwise, HELOCs may be preferred.

Bequest Problems ($j = J$)

When households exit economic life, they solve the following problems with the bequest motive $V_{J+1} = v(b + \underline{b})$ described in equation (1).

Renters' Bequest Problem

Renters must stay renters and cannot become homeowners in the final period of economic life. Their value function is thus $V_J^r(b, y; \mu, Z) = V_J^{rent}(b, y; \mu, Z)$.

²⁸Wong (2019) relaxes the fixed interest rate assumption when modeling mortgage refinancing and finds that younger households or those with larger mortgages are more likely to refinance.

$$\begin{aligned}
V_J^{rent}(b, y; \mu, Z) &= \max_{\{b', \tilde{h}', c\}} \{u_j(c, s) + \beta v(\mathfrak{b} + \mathfrak{b})\} \\
s.to. \quad c + q_b b' + \rho(\mu, Z) \tilde{h}' &= y - \mathcal{T}(y) + b \\
\mathfrak{b} &= b' \\
0 &\leq b' \\
s = \tilde{h}' &\in \tilde{\mathcal{H}}
\end{aligned} \tag{18}$$

Homeowners' Bequest Problem

Homeowners have three choices in the final period of economic life. They can sell their houses and become renters, default and become renters, or stay in their house and leave it as a bequest after paying off the residual mortgage.²⁹ Homeowners can neither purchase a new house nor refinance a new mortgage in the final period of economic life.

$$V_J^h(\mathbf{x}, y; \mu, Z) = \max \begin{cases} V_J^{sell, rent}(b^n, y; \mu, Z) \\ V_J^{default}(b, y; \mu, Z) \\ V_J^{stay, pay}(\mathbf{x}, y; \mu, Z) \end{cases} \tag{19}$$

Sell to rent: when homeowners sell their house and choose to become renters, they solve the renters bequest problem (18) with liquid financial instruments b^n .

$$b^n = b + (1 - \delta_h - \tau_h - \kappa_h)p(\mu, Z)h - (1 + r_m)m$$

Default: homeowners who default in the last period of economic life solve:

$$\begin{aligned}
V_J^{rent}(b, y; \mu, Z) &= \max_{\{b', c\}} \left\{ u_j(c, \tilde{h}^0) - \xi + \beta v(\mathfrak{b} + \mathfrak{b}) \right\} \\
s.to. \quad c + q_b b' + \rho(\mu, Z) \tilde{h}^0 &= y - \mathcal{T}(y) + b \\
0 &\leq b' \\
\mathfrak{b} &= b'
\end{aligned} \tag{19.a}$$

²⁹Strategic bequests and dynasties are beyond the scope of this paper, see Brandsaas (2024) for a study.

Stay and pay: homeowners who pay off their mortgage and leave their house in bequest solve:

$$\begin{aligned}
V_J^{pay,stay}(\mathbf{x}, y; \mu, Z) &= \max_{\{b', c\}} \{u_j(c, s) + \beta \mathbb{E}_{Z'|Z}[v(b + \underline{b})]\} \\
s.to. \quad c + q_b b' + (\delta_h + \tau_h)p(\mu, Z)h + (1 + r_m)m' &= y - \mathcal{T}(y, m) + b \\
0 &\leq b' \\
b &= b' + (1 - \kappa_h)p'(\mu'; Z, Z')h \\
s &= h\omega, \quad h \in \mathcal{H} \\
\mu' &= \Gamma_\mu(\mu; Z, Z') \\
Z' &\sim \Gamma_Z(Z)
\end{aligned} \tag{19.b}$$

A.2 Final Goods, Construction, and Rental Firms' Problems

Final goods firms: V_c denotes the value function of final goods producing firms.

$$\begin{aligned}
V_c(N_c; \mu, Z) &= \max_{N_c} \{Y - w(\mu, Z)N_c\} \\
s.to. \quad Y &= \Theta(Z)N_c \\
0 &\leq N_c \\
\mu' &= \Gamma_\mu(\mu; Z, Z')
\end{aligned}$$

Because final goods consumption C is the numeraire, the price for final goods has been normalized to one. Taking the first order condition with respect to labor N_c pins down the aggregate equilibrium wage:

$$w(\mu, Z) = \Theta(Z) \tag{11}$$

Housing construction firms: V_h denotes the value function of housing construction firms.

$$\begin{aligned}
V_h(N_h; \mu, Z) &= \max_{N_h} \{p(\mu, Z)H_h - w(\mu, Z)N_h\} \\
s.to. \quad H_h &= [\Theta(Z)N_h]^\alpha \bar{L}^{1-\alpha} \\
0 &\leq N_h \\
\mu' &= \Gamma_\mu(\mu; Z, Z')
\end{aligned}$$

Taking the first order condition with respect to labor N_h and using the above equilibrium expression for aggregate wage $w(\mu, Z)$ yields:

$$\alpha \Theta(Z)p(\mu, Z)[\Theta(Z)N_h]^{\alpha-1} \bar{L}^{1-\alpha} = \Theta(Z)$$

Re-arranging delivers the expression for housing supply:

$$\underbrace{[\Theta(Z)N_h]^\alpha \bar{L}^{1-\alpha}}_{\equiv H_h} = [\alpha p(\mu, Z)]^{\frac{\alpha}{1-\alpha}} \bar{L} \quad (12)$$

Rental housing sector: V_r denotes the value function of the rental housing sector with the stock of housing units owned by the rental company given as \tilde{H}' and the rental ready housing units given as X' .

$$\begin{aligned} V_r(\tilde{H}, X; \mu, Z) = & \max_{\tilde{H}', X'} \{ [\rho(\mu, Z) - \Xi] X' - p(\mu, Z) [\tilde{H}' - (1 - \delta_h - \tau_h) \tilde{H}] \dots \\ & \dots + q_b \mathbb{E}_{Z', \epsilon' | Z, \epsilon} [V_r(\tilde{H}', X'; \mu', Z')] \} \\ \text{s.to.} \quad & X' \leq \tilde{H}' \\ & 0 \leq \tilde{H}', X' \\ & \mu' = \Gamma_\mu(\mu; Z, Z') \end{aligned}$$

First order and envelope conditions yield the rental housing pricing equation:

$$\rho(\mu, Z) = \Xi + p_h(\mu, Z) - (1 - \delta_h - \tau_h) q_b \mathbb{E}_{Z', \epsilon' | Z, \epsilon} [p'(\mu', Z')] \quad (13)$$

See Appendix D of Kaplan et al. (2020) for a more general version that allows for financial and convertibility frictions.

A.3 Recursive Competitive Equilibrium

A *recursive competitive equilibrium* consists of:

- A sequence of income endowments y to households.
- Prices for owner-occupied housing $p(\mu, Z)$, rental housing $\rho(\mu, Z)$, wages $w(\mu, Z)$, and mortgages $q_j(\mathbf{x}', y; \mu, Z)$ where $\mathbf{x} = \{b, h, m\}$.
- Government parameters for constraints on loan-to-value $\theta^{LTV}(Z)$ and payment-to-income $\theta^{PTI}(Z)$, land permits \bar{L} , taxes $\mathcal{T}(y, m)$, and social security payments ρ_{SS} .
- Perceived laws of motion for the state space $\mu = \Gamma_\mu(\mu; Z, Z')$ where $\mu = \mu^r + \mu^h$ is the measure over the set of individual states for renters r and homeowners h . Let $\mu = 1$ and the respective state spaces be defined as $\mathcal{X}^h = (\mathcal{B} \times \mathcal{H} \times \mathcal{M} \times \mathcal{E} \times \mathcal{J})$ and $\mathcal{X}^r = (\mathcal{B} \times \mathcal{E} \times \mathcal{J})$.
- Value functions for renters $V_j^r(b, y; \mu, Z)$ with policy functions for consumption, liquid financial instruments, owner-occupied housing, and rental housing $\{c, b', h', \tilde{h}'\}$ solve the renters' problem. Value functions for homeowners $V_j^h(\mathbf{x}, y; \mu, Z)$ with policy functions for consumption, liquid financial instruments, owner-occupied housing, rental housing, and mortgages $\{c, b', h', \tilde{h}', m'\}$ solve the homeowners' problem.

Markets clear:

- The lending sector maximizes profits and the mortgage market clears loan-by-loan with homeowner specific pricing functions $q_j(\mathbf{x}', y; \mu, Z)$.

$$\int_{\mathcal{X}^h} m' d\mu^h = M'$$

- The rental sector maximizes profits with policy function \tilde{H}' at price $\rho(\mu, Z)$ to supply rental housing.

$$\underbrace{\int_{\mathcal{X}^r} \tilde{h}' d\mu^r}_{\text{renters}} + \underbrace{\int_{\mathcal{X}^h} \tilde{h}' d\mu^h}_{\substack{\text{sellors} \\ \& \\ \text{defaulters}}} = \tilde{H}'$$

- Housing construction firms maximize profits with policy functions for labor demand N_h and the supply of new housing units H_h . There is a single housing price $p(\mu, Z)$ that clears the housing market so that housing outflows (LHS) equal inflows (RHS).

$$\begin{aligned} & \underbrace{\tilde{H}' - (1 - \delta_h)\tilde{H}}_{\substack{\text{rental sector} \\ \text{housing purchases}}} + \underbrace{\int_{\mathcal{X}^r} h' d\mu_r}_{\substack{\text{purchases} \\ \text{by renters}}} + \underbrace{\int_{\mathcal{X}^h} h' d\mu_h}_{\substack{\text{purchases} \\ \text{by owners}}} \\ &= \underbrace{H_h - \delta_h \int_{\mathcal{X}^h} h d\mu^h}_{\substack{\text{new construction} \\ \text{less depreciation}}} + \underbrace{\int_{\mathcal{X}^h} h [\mathbb{1}_{\text{sell}} + \mathbb{1}_{\text{default}} (1 - \delta_h^d + \delta_h)] d\mu^h}_{\text{sales by owners \& sales of foreclosures}} + \underbrace{\int_{\mathcal{X}^h} \mathbb{1}_{\text{bequest}} h' d\mu^h}_{\text{estate sales}} \end{aligned}$$

- Final goods firms maximize profits so that the labor market clears at $\Theta(Z) = w(\mu, Z)$ with the total labor supply from housing construction and final goods firms $N_h + N_c$ normalized to 1.

$$\int_{\mathcal{X}} \exp(\chi_j + \epsilon_j(z)) d\mu_{\mathcal{J}_{work}} = \underbrace{N_h + N_c}_1$$

- The government collects revenue from income taxes $\mathcal{T}(y, m)$, property taxes τ_h , and the sale of land permits $[p(\mu, Z)H_h - w(\mu, Z)N_h]$ to finance expenditures on social security income for retirees y_{ret} and non-valued government spending G :

$$\mathcal{T}(y, m) + \tau_h p(\mu, Z) \int_{\mathcal{X}^h} h d\mu^h + [p(\mu, Z)H_h - w(\mu, Z)N_h] = \rho_{ss} \int_{\mathcal{X}} y_{ret} d\mu_{\mathcal{J}_{ret}} + G$$

- Profits or losses from the financial and rental sectors are expressed as net exports:

$$\begin{aligned} NX = & \underbrace{\int_{\mathcal{X}^r} [b - q_b b'] d\mu^r + \int_{\mathcal{X}^h} [b - q_b b' \mathbb{1}_{[b' > 0]} - (r_b(1 + \iota))^{-1} b' \mathbb{1}_{[b' < 0]}] d\mu^h}_{\text{lenders' net expenses from liquid financial instruments}} \\ & \dots + \underbrace{\int_{\mathcal{X}^h} [(1 + r_m)m + q_j(\mathbf{x}', y; \mu, Z)m'] d\mu^h}_{\text{lenders' net revenue from mortgages}} \\ & \dots + \underbrace{(\rho(\mu, Z) - \Xi)\tilde{H}'}_{\text{rental sector revenue less operating costs}} - \underbrace{p(\mu, Z)[\tilde{H}' - (1 - \delta_h - \tau_h)\tilde{H}]}_{\text{rental sector housing purchases}} \end{aligned}$$

- The aggregate resource constraint is satisfied where household consumption C , government spending G , net exports NX equal output Y less housing and mortgage adjustment costs.

$$\begin{aligned} & \int_{\mathcal{X}^h} c d\mu^h + \int_{\mathcal{X}^r} c d\mu^r + G + NX + \Xi \tilde{H}' \\ = & Y - \kappa p(\mu, Z) \int_{\mathcal{X}^h} h(\mathbb{1}_{sell} + \mathbb{1}_{default}) d\mu^h - \iota r_b \int_{\mathcal{X}^h} (m + b \mathbb{1}_{\{b < 0\}}) d\mu^h \\ & - (\zeta + \kappa^m) \int_{\mathcal{X}^h} m'(\mathbb{1}_{buy} + \mathbb{1}_{refi}) d\mu^h \end{aligned}$$

- Consistency is satisfied and perceived laws of motion of the state space $\mu' = \Gamma_\mu(\mu, Z, Z')$ is consistent with individual behavior

B Appendix: Computational Algorithm

Both the multi- and one-step algorithms with either fixed or time-varying forecasting coefficients, respectively, rely on the assumption that agents keep track of house prices via a log-linear forecasting rule for each combination of current and future aggregate states $\mathcal{Z} \in \{Z, Z'\}$ as an approximation of the entire distribution over individual states μ and its law of motion $\Gamma_\mu(\mu; \mathcal{Z})$. While the aggregate capital stock in Krusell and Smith (1998) is predetermined, aggregate housing is not and requires explicit market clearing, which makes the computational algorithm in this paper closer to that of Krusell and Smith (2006).

$$\log p'(p(Z); \mathcal{Z}) = a_{\mathcal{Z}}^0 + a_{\mathcal{Z}}^1 \log p(Z) \iff \mu' = \Gamma_\mu(\mu; \mathcal{Z})$$

The model is first solved with the multi-step fixed-point method to obtain fixed coefficients. Next, the model is solved with the one-step method that endogenizes beliefs by tracking time-varying coefficients throughout the simulation. Because the one-step method with endogenous beliefs requires as many additional grids as there are aggregate states in the one-step method, the households' problem must be solved $3^2 = 9$ times for two belief grids with 3 points each.³⁰ Fortunately, the increase in dimensionality is not too much of a computational burden because the belief grids can be parallelized.³¹ The model has been solved on the high-throughput computing clusters at Indiana University (Karst and Carbonate), the University of Texas at Dallas (BigTex), and the Federal Reserve Board.

1. Define grids over ages $j = 1, \dots, J$, liquid financial instruments b , liquid financial instrument choices b' , rental housing choices \tilde{h}' , owner-occupied housing h , owner-occupied housing choices h' , mortgage balances m , mortgage choices m' , aggregate income $\Theta(Z) \in \{\Theta(Z_{high}), \Theta(Z_{low})\}$, aggregate credit conditions $\mathcal{C}(Z) \in \{\mathcal{C}(Z_{high}), \mathcal{C}(Z_{low})\}$, and house prices p .

2. Define coefficients:

- Fixed: to pin down next period house prices, guess coefficients $\mathbf{a}_{\mathcal{Z}}$ for each \mathcal{Z} for a total of $\#Z^2 = 4$ vectors of coefficients.³²

$$\log p'(p(Z); \mathcal{Z}) = a_{\mathcal{Z}}^0 + a_{\mathcal{Z}}^1 \log p(Z)$$

³⁰Experiments with 5 grid points instead of 3 show that although individual aggregate housing demand may vary, the demand schedule for housing is roughly similar.

³¹Allowing independent aggregate shocks to credit conditions and income would require defining four belief grids instead of two. With 3 points for each grid, the households' problem would then need to be solved $3^4 = 81$ times instead of $3^2 = 9$ times. Computation times increase drastically as a result of increasing the dimensions of the arrays and interpolation in two additional dimensions.

³²The forecasting equation is $\log p_{\mathcal{Z}, t+1} = \mathbb{1}_{\mathcal{Z}} a_{\mathcal{Z}}^0 + a_{\mathcal{Z}}^1 \log p_{\mathcal{Z}, t}$ for $\mathcal{Z} \in \{Z, Z'\}$ which is slightly different, but practically equivalent to equation (14), $\log p_{\mathcal{Z}, t+1} = a_{\mathcal{Z}}^0 + a_{\mathcal{Z}}^1 \log p_{\mathcal{Z}, t}$.

- Beliefs: define additional grids over future house prices in each future state $\{p'(Z'_{low}), p'(Z'_{high})\}$ for a total of $\#Z' = 2$ additional grids.

With a risk-neutral lending sector, the mortgage price $q_j(\mathbf{x}', y; p(Z), Z)$ is pinned down by the lenders' mortgage pricing function in equation (10). The price for financial assets q_b is taken as given. The price of rental housing $\rho(\mu, Z)$ is pinned down by the rental sector's maximization problem (13) and aggregate wages $w(\mu, Z)$ are pinned down by the final goods firms' maximization problem (11).

3. Solve the households' problem at each point on the house price grid p (and at each point on the belief grids if endogenizing beliefs). I use value function iteration with grid search for housing and mortgages and a golden section solver for liquid financial instruments.
4. Simulate a long time series of aggregate states Z_t for $t = 1, \dots, T$ where $T = 5000$ with a burn in period of 100.
5. Fix an initial distribution of liquid financial instruments, idiosyncratic incomes, and ages assuming that all households are initially renters $\mu_t \in \mathcal{B} \times \mathcal{E} \times \mathcal{J}$ for $t = 1$. Beginning realizations of $\{b, \epsilon, j\}$ denote liquid financial instruments, income realizations, and ages, respectively. There are $N = 125000$ households.

Some notes on initialization:

- endowments of liquid financial instruments equal zero for all households at $t = 1$.
- because all agents are renters at $t = 1$, there is no initial housing endowment
- initial household ages are drawn from a uniform distribution³³ $j \sim [1, \dots, J]$
- when household i reaches the final period of economic life, $j_{i,t} = J$, a new household replaces them with $j_{i,t+1} = 1$ as renters with no mortgage debt $m_{i,t} = 0$. These new households inherit a random draw of liquid financial instruments $b_{i,t}$ that are correlated with individual income so that household with a higher income are more likely to inherit larger quantities.
- if solving with beliefs, set calibrated initial coefficients \mathbf{a}_0 .

6. Simulate

- Fixed: coefficients are already set at \mathbf{a}_Z at the beginning of the problem.
- Beliefs: compute period t coefficients to pin down $p'(p(Z); \mathcal{Z})$. Coefficients for each future aggregate state $\mathbf{a}_{Z_t, Z'_{low}}$ and $\mathbf{a}_{Z_t, Z'_{high}}$ are necessary because the value of Z' is not yet known. For this reason, endogenous beliefs require as many additional grids as there are aggregate states.

³³This assumption follows Kaplan and Violante (2014). Matching the distribution of ages would introduce generational demographic changes into equilibrium dynamics which is beyond the scope of this paper.

7. Compute the aggregate demand schedule for housing at each point on the house price grid p from the housing policy functions for renters \tilde{h}' and homeowners h' . Interpolate over $b_{i,t}$ for renters and $\{b_{i,t}, h_{i,t}, m_{i,t}\}$ for homeowners. Average by housing type:

$$\begin{aligned} \text{Renters: } \tilde{H}_{t+1}(p, \mathbf{X}_t) &= \frac{1}{N} \sum_{i=1}^{N^r} \tilde{h}'(b_{i,t}, y_{i,t}, j_{i,t}; p, \mathbf{X}_t) \\ \text{Homeowners: } H_{t+1}(p, \mathbf{X}_t) &= \frac{1}{N} \sum_{i=1}^{N^h} h'(b_{i,t}, h_{i,t}, m_{i,t}, y_{i,t}, j_{i,t}; p, \mathbf{X}_t) \end{aligned}$$

The number of aggregate states in the vector \mathbf{X}_t depends on the algorithm:

- Fixed: $\mathbf{X}_t = \{Z_t\}$
- Beliefs: $\mathbf{X}_t = \{Z_t, p'(Z'_{low}), p'(Z'_{high})\}$ which requires additional interpolation over $p'(Z'_{low})$ and $p'(Z'_{high})$.

8. Compute excess demand for aggregate housing at each point on the house price grid p and recover the equilibrium house price $p_t^*(Z_t)$ from the market clearing condition:

$$H_{t+1}(p_t^*(Z_t), \mathbf{X}_t) + \tilde{H}_{t+1}(p_t^*(Z_t), \mathbf{X}_t) = H_h + (1 - \delta_h)[H_t + \tilde{H}_t]$$

9. Interpolate the individual policy functions b' , h' , \tilde{h}' , and m' at the equilibrium house price $p_t^*(Z_t)$ and then average to calculate the aggregate equilibrium quantities.

$$\begin{aligned} B_{t+1}^*(p_t^*(Z_t), \mathbf{X}_t) &= \frac{1}{N} \sum_{i=1}^N b'(b_{i,t}, h_{i,t}, m_{i,t}, y_{i,t}, j_{i,t}; p_t^*(Z_t), \mathbf{X}_t) \\ \tilde{H}_{t+1}^*(p_t^*(Z_t), \mathbf{X}_t) &= \frac{1}{N} \sum_{i=1}^{N^r} \tilde{h}'(b_{i,t}, y_{i,t}, j_{i,t}; p_t^*(Z_t), \mathbf{X}_t) \\ H_{t+1}^*(p_t^*(Z_t), \mathbf{X}_t) &= \frac{1}{N} \sum_{i=1}^{N^h} h'(b_{i,t}, h_{i,t}, m_{i,t}, y_{i,t}, j_{i,t}; p_t^*(Z_t), \mathbf{X}_t) \\ M_{t+1}^*(p_t^*(Z_t), \mathbf{X}_t) &= \frac{1}{N} \sum_{i=1}^N m'(b_{i,t}, h_{i,t}, m_{i,t}, y_{i,t}, j_{i,t}; p_t^*(Z_t), \mathbf{X}_t) \end{aligned}$$

Again, the number of aggregate states \mathbf{X}_t depends on the algorithm:

- Fixed: $\mathbf{X}_t = \{Z_t\}$
- Beliefs: $\mathbf{X}_t = \{Z_t, p'(Z'_{low}), p'(Z'_{high})\}$

$$\mathbf{p}'(p_t^*(Z_t)) = \begin{pmatrix} \exp\{a_{Z_t, Z'_{low}}^0 + a_{Z_t, Z'_{low}}^1 \log(p_t^*(Z_t))\} \\ \exp\{a_{Z_t, Z'_{high}}^0 + a_{Z_t, Z'_{high}}^1 \log(p_t^*(Z_t))\} \end{pmatrix}$$

10. Simulate for $t = 1, \dots, T$ periods by repeating steps (6)-(9).

11. Compare coefficients:

- Fixed: partition the time series of market clearing house prices $\{p_t^*(Z_t)\}_{t=burn}^T$ by $\mathcal{Z} \in \{Z, Z'\}$ to generate $\#Z^2 = 4$ sub-samples. Estimate new forecasting

coefficients for each sub-sample \mathcal{Z} via ordinary least squares regression:

$$\mathbf{a}_{\mathcal{Z}}^{new} = \left(\sum_{t=burn}^T \mathbf{x}_{\mathcal{Z},t} \mathbf{x}_{\mathcal{Z},t}' \right)^{-1} \sum_{t=burn}^T \mathbf{x}_{\mathcal{Z},t} \log p_{\mathcal{Z},t+1}$$

Repeat steps (2) - (11) until coefficients converge, $\mathbf{a}_{\mathcal{Z}}^{new} \approx \mathbf{a}_{\mathcal{Z}}$

- Beliefs: verify that the time-varying coefficients $\{\mathbf{a}_{\mathcal{Z},t}\}_{t=burn}^T$ from step (9) converge to their near-rational counterparts $\mathbf{a}_{\mathcal{Z}}$.

Chipeniuk et al. (2022) propose a solution check called auctioneer iteration to avoid relying on potentially misleading R^2 statistics as measures of accuracy. Their method adds the following steps after coefficients are obtained via a fixed point:

12. Use converged $\mathbf{a}_{\mathcal{Z}}$ and a price grid that is a subset of simulated prices, $p = \subset \{p_t^*(Z_t)\}_{t=1}^T$.
13. Repeat steps (1)-(11) to obtain new converged coefficients and new prices $\{p_t^{new}(Z_t)\}_{t=1}^T$.
14. Stop if $\{p_t^{new}(Z_t)\}_{t=1}^T \approx \{p_t^*(Z_t)\}_{t=1}^T$, otherwise go to step (1).

B.1 Computational Details

The known forecasting coefficients $\mathbf{a}_{\mathcal{Z}}$ shown in Table (5) are solved as a fixed point in the model's stochastic steady state characterized by tight aggregate credit conditions and fluctuations in aggregate income. The coefficients have similar values in all combinations of current and future income states which is consistent with Kaplan et al. (2020) and suggests that shocks to aggregate income do not have much effect on house price forecasts. Approximating the sample mean of house prices $\bar{p}_{\mathcal{Z}}$ via the coefficients points to slightly more variation in the highest and lowest values attained in the transitions between income states.

Income states	$a_{\mathcal{Z}}^0$	$a_{\mathcal{Z}}^1$	$\bar{p}_{\mathcal{Z}} \approx \frac{a_{\mathcal{Z}}^0}{1-a_{\mathcal{Z}}^1}$	R^2	Den Haan	Chipeniuk et. al
High, High	-0.102	0.838	0.53	0.9999	0.01	0.01
High, Low	-0.111	0.838	0.50			
Low, High	-0.091	0.847	0.55			
Low, Low	-0.100	0.847	0.52			

Table 5: Converged forecasting coefficients under tight aggregate credit conditions.

Like Kaplan et al. (2020) and Favilukis et al. (2017), the model's R^2 statistic is close to 1 which suggests adequate goodness of fit standards. Because R^2 statistics can be misleading gauges of accuracy, Den Haan (2010) and Chipeniuk et al. (2022) propose alternative tests which both come in sufficiently low at 0.01.

C Appendix: Calibration

C.1 Parameter Values

The model’s parameters are set to resemble the U.S. economy in the late 1990s with the cross-sectional moments from the 1998 Survey of Consumer Finances to nest Kaplan et al. (2020).

Demographics: Each model period is equal to two years. Households begin economic life at age 21 ($j = 1$), retire at age 65 ($J^{ret} = 23$), and exit economic life at age 79 ($J = 30$).³⁴

Preferences: The elasticity of substitution between goods consumption and housing expenditures $1/\gamma$ is set to 1.25 based on the estimates of Piazzesi et al. (2007). The elasticity of intertemporal substitution equals 0.5 by setting $\sigma = 2$. A McClements (1977) scale sets the consumption equivalence scale $\{e_j\}$ to match the OECD average number of children across different age groups. The discount factor β is set to replicate the 1998 ratio of aggregate net worth to annual labor income of 5.5 for which the model comes in slightly below at 4.9.

Two parameters, the strength of the bequest motive ψ and the extent to which bequests are luxuries \underline{b} , pin down the warm-glow bequest motive given in equation (1). The strength of bequests ψ is chosen to replicate the ratio of net worth at age 75 to age 50 of 1.55 which indicates the importance of bequests as a saving motive. The model comes in slightly below at 1.48. The luxuriousness of bequests \underline{b} is chosen so that households in the bottom half of the model’s wealth distribution do not leave bequests, as observed in the data.

Homeowners’ additional utility ω sets the average homeownership rate which was 66 percent in the late 1990s and is slightly higher at 68 percent in the model. Defaulters’ disutility ξ is set to match the average foreclosure rate in the late 1990s of 0.5 percent and is slightly lower at 0.02 percent in the model.

Income endowments: The deterministic life-cycle component of earning $\{\chi_j\}$ is from Kaplan and Violante (2014). Stochastic individual earnings $\epsilon_j(z)$ in equation (5) follow an AR(1) process in logs with an annual persistence of 0.97, annual standard deviation of 0.2, and an initial standard deviation of 0.42. The variance of log earnings rises by 2.5 between ages 21 and 64 which follows Heathcote et al. (2010). Bequested inheritances are correlated with individual income so that higher income households are more likely to inherit more.

³⁴Krueger and Kübler (2004) find that computational accuracy decays rapidly if the length of economic life extends beyond 30 periods when using aggregate risk in a life-cycle economy.

Housing: The following three parameters discipline the size of owner-occupied housing units \mathcal{H} : the size of the smallest unit h^0 , the number of house sizes available $\#\mathcal{H}$, and the gap between housing sizes. The values of these parameters are obtained from targeting the 10th, 50th, and 90th percentiles of the distribution of the ratio of housing net worth to total net worth. The model matches the 10th percentile but comes in a bit below the 50th and 90th percentiles, as is common this class of model. The size of rental housing units $\tilde{\mathcal{H}}$ is chosen to target a ratio of median owner-occupied to rental housing of 1.5 square feet per person as detailed in Chatterjee and Eyigungor (2015) and a ratio of the average earnings of homeowners to renters equal to 2.1. The model generates moments that are mostly in line with these empirical targets.

The maintenance cost of housing that offsets depreciation δ_h equals 0.015 and replicates the empirical depreciation rate of the housing stock of 1.5 percent per year.³⁵ Defaulted housing has a higher depreciation rate δ_h^d equal to 0.22 to account for the loss of value from foreclosure. The linear transaction cost of housing adjustments κ_h equals 7 percent which falls within the 6 to 12 percent range estimated by Quigley (2002).³⁶ In line with the data, 9 percent of homeowners in the model buy or sell houses each year. The relative cost of renting versus owning is determined in part by the operating cost of the rental company Ξ and is particularly salient for young households. Ξ is chosen to match the 39 percent homeownership rate of households younger than 35 and comes in slightly lower at 34 percent.

Housing construction technology α is set so that the price elasticity of housing supply $\alpha/(1 - \alpha)$ equals 1.5, the median among MSAs in Saiz (2010). Land permits \bar{L} pin down employment in the construction sector at 5% of total employment which is consistent with the 1998 employment share of construction measured by the Bureau of Labor Statistics.

Financial instruments: The risk-free rate r is 2.5 percent per year and the lending wedge ι is 0.33 so that the interest rate on loans r_b is equal to 3 percent per year to replicate the gap between the average rate on 30-year fixed-term mortgage and the 10-year Treasury rate in the late 1990s. The maximum HELOC value θ^{HELOC} is 0.2.

Government: The property tax τ_h is set to 1% per year which is the median tax rate across U.S. states according to the Tax Policy Center. The income tax function in equation (3) follows the functional form of Heathcote et al. (2017). The parameter τ_y^0 indicates the average level of taxation and is set so that aggregate income tax revenues are 20% of income.

³⁵Kaplan et al. (2020, p. 18) use the Bureau of Economic Analysis' Table 7.4.5 which details the consumption of fixed capital of the housing sector divided by the stock of residential housing at market value.

³⁶Ghent (2012) finds a value of 13 percent and Ngai and Sheedy (2020) settle on 10 percent suggesting that 7 percent may be on the lower end of the established range.

The parameter τ_y^1 measures the degree of progressivity of the tax and transfer system and is set at 0.15 based on the estimates of Heathcote et al. (2017). The share of mortgage interest deducted ϱ is set at 0.75 to so that only the first \$1,000,000 of mortgage debt is deductible. Social security payments in equation (2) maintain income heterogeneity by scaling the last realization of earnings y_{jret-1}^w by the replacement rate ρ_{ss} . Kaplan et al. (2020) compute the ratio of average benefits to average lifetime earnings and find a replacement rate equal to 0.4.

Interpretation	Parameter	Value	Annualized
Demographics			
Maximum age	J	30	N
Retirement age	J^{ret}	23	N
Preferences			
Inverse elasticity of substitution	γ	0.8	N
Risk aversion	σ	2	N
Discount factor	β	0.97	Y
Strength of bequest motive	ψ	100	N
Extent of bequests as a luxuries	\underline{b}	7.7	N
Taste for housing	ϕ	0.13	N
Additional utility from owning	ω	1.015	N
Utility cost of foreclosure	ξ	0.8	N
Individual income			
Deterministic income	$\{\chi_j\}$	Kaplan & Violante (2014)	N
Annual persistence, ind. income	ρ_ϵ	0.97	Y
Annual st. dev., ind. income	σ_ϵ	0.20	Y
Initial st. dev., ind. income	σ_{ϵ_0}	0.42	Y
Distribution of bequest to new hhs	$b_{j=1} = b'_{j=J}$	Kaplan & Violante (2014)	N
Housing			
Owner-occupied housing unit sizes	\mathcal{H}	$\{1.5, 1.92, 2.46, \dots$ $\dots 3.15, 4.03, 5.15\}$	N
Rental housing unit sizes	$\tilde{\mathcal{H}}$	$\{1.125, 1.5, 1.92\}$	N
Depreciation rate of housing	δ_h	0.015	Y
Housing loss in foreclosure	δ_h^d	0.22	Y
Housing transaction cost	κ_h	0.07	N
Operating cost of rental company	Ξ	0.002	N
Housing supply elasticity	$\alpha/(1 - \alpha)$	1.5	N
New land permits	\bar{L}	0.311	N
Financial instruments			
Risk-free interest rate	r	0.025	Y
Interest rate wedge on borrowing	ι	0.33	N
Maximum HELOC	θ^{HELOC}	0.2	N
Government			
Property tax on housing	τ_h	0.01	Y
Income tax function	τ_y^0, τ_y^1	0.75, 0.151	N
Mortgage interest deduction fraction	ϱ	0.75	N
Mortgage interest deduction limit	\bar{m}	\$1 mil.	N
Social Security replacement rate	ρ_{SS}	0.42	N

Table 6: Parameter values. A period is two years and annualized values are noted in the final column with a Y. 1=\$52,000 which is the average value of income in the 1998 SCF.

C.2 Cross-sectional Distribution across the Life-Cycle

Before simulating the U.S. housing boom under this paper's contribution of endogenously optimistic beliefs, it is important to first discuss the cross-sectional distribution of households in the model's stochastic steady state which assumes known forecasting coefficients, tight aggregate credit conditions, and fluctuations in aggregate income.³⁷ Figure (10) shows that the life-cycle profiles of the means and variances of model quantities are largely consistent with a typical incomplete markets model where households succeed at some smoothing of goods consumption and housing expenditures by accumulating a buffer stock of liquid financial instruments.

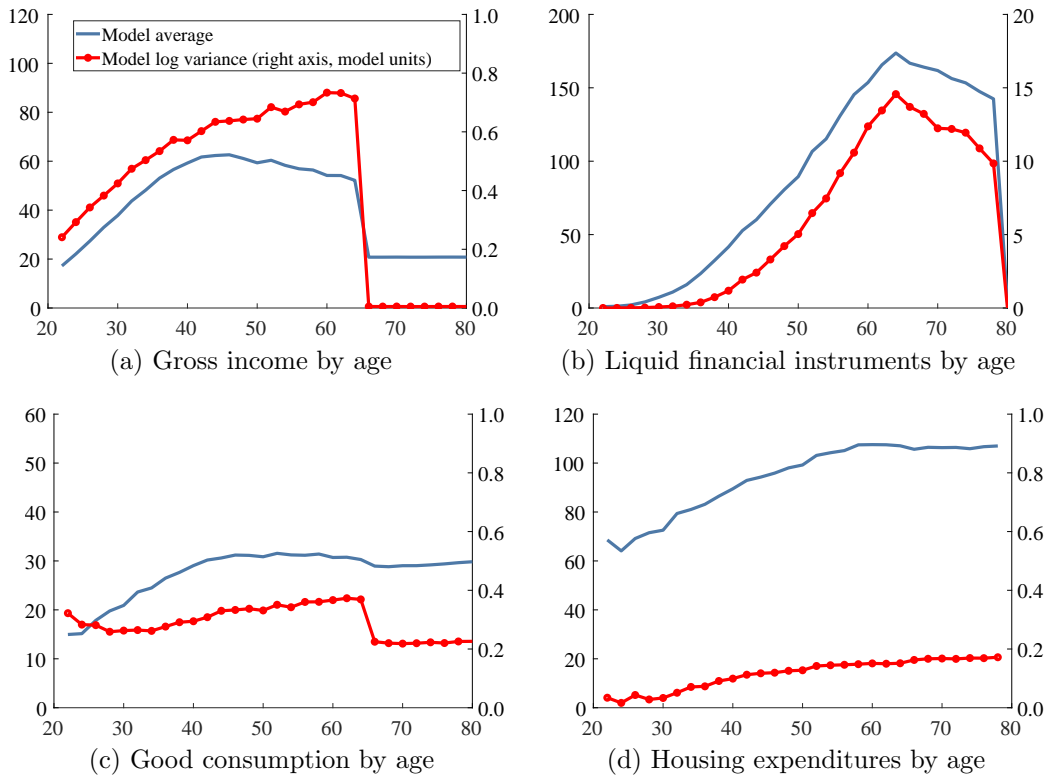


Figure 10: Life-cycle statistics from the model in thousands of 1998 dollars.

Panel (10a) shows that the average and log variance of income rise over the life-cycle consistent with the data from the 1998 Survey of Consumer Finances. The non-stationary age-dependent variance for idiosyncratic income helps match the more volatile earnings in the pre-retirement phase as is observed in the data.

Panel (10b) shows that households accumulate liquid financial instruments, on average, as a buffer against both idiosyncratic shocks and the decrease in earnings at retirement.

³⁷Appendix C.4 shows that the calibration is similar assuming the credit conditions can fluctuate between their loose and tight values via a Markov chain. Appendices E and F.1 confirm for impulse response functions are similar under credit conditions that shift one time or are Markov.

The pronounced hump-shape profile in both the average and variance (in levels, not logs) arises from a desire to smooth both consumption and housing expenditures in retirement. Average liquid financial instruments drop at the end of economic life because of bequest heterogeneity—only households in the top half of the wealth distribution leave inheritances.

The relatively flat profiles of both goods consumption and housing expenditures over the life-cycle shown in Panels (10c)-(10d) suggest that households partially self-insure against idiosyncratic shocks and retirement. Housing illiquidity and the availability of liquid financial assets are also both key for generating the flat profile of average housing expenditures, which is, in turn, key for matching the data and solving for a Krusell and Smith (1998) approximate equilibrium. Iacoviello and Pavan (2007) explain that illiquid housing results in households accumulating a buffer stock of wealth in liquid financial instruments instead of housing since households cannot adjust housing without paying additional transaction costs. If liquid financial instruments were not available, the average housing expenditure profile would look like that of liquid financial instruments with the hump-shape indicating more variation in marginal propensities to consume within and across households. The simple AR(1) forecast given by equation (14) would then be insufficient to approximate the evolution of house prices and would generate worse goodness of fit measures than those in Appendix B.

An empirically consistent distribution of housing is key for pinning down aggregate house prices throughout the housing boom and Figure (11) shows the model also matches the homeownership rate and mortgage leverage ratio over the life-cycle. Young households are particularly important because they are less likely to own homes and more likely to have maximum leverage which makes them the most sensitive to looser credit conditions.

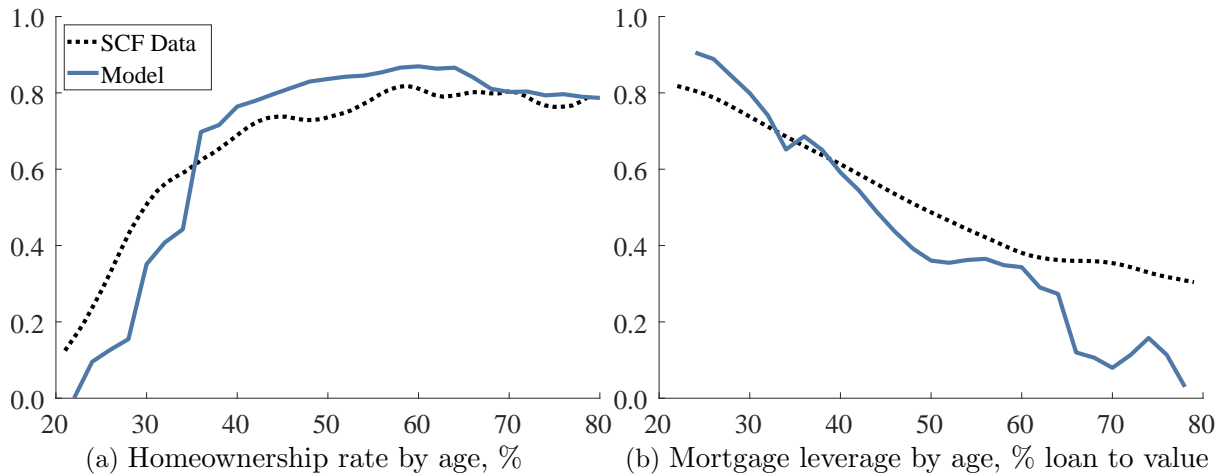


Figure 11: Housing statistics over the life-cycle, 1998 dollars.

Panel (11a) shows that households remain renters, on average, in the first part of economic life in order to accumulate enough wealth and earnings to overcome the loan-to-value and

payment-to-income constraints. The size of inheritances and initial income endowments determine the age in which households can afford to purchase housing.³⁸ Consistent with the data, the worse off households can never afford housing and remain life-long renters.

Panel (11b) shows that mortgage leverage—homeowners’ ratio of mortgage debt to housing value—is highest at age 22 and declines thereafter as households amortize mortgage balances. Model simulated leverage is slightly below but mostly in line with its empirical counterpart until age 65. Thereafter, it takes on counterfactual oscillations and low values due to assumptions on mortgages. In the model, homeowners can take out a mortgage that lasts for only a few years while in practice mortgages may only be available longer tenures.

³⁸See Brandsaas (2024) for an overview of how parental transfers help young households overcome mortgage constraints. Including inter vivos transfers is beyond the scope of this paper.

C.3 Segmentation of Housing Unit Sizes

This Appendix evaluates the assumptions on the partial segmentation of housing unit sizes and shows that the model’s distributions match those of the data minus a few discrepancies. Because housing size enters the households’ utility function, empirically consistent partial segmentation can be represented by certain sizes of housing units only being available to a subset of households.³⁹ To best fit the pre-boom homeownership rate of 66 percent, I follow Kaplan et al. (2020) and assume that the smallest housing unit cannot be owned and the larger housing units cannot be rented. Table (7) shows that in the data only 9 percent of homeowners occupy the smallest sized unit and only 10 percent of renters occupy the largest sized unit which suggests that the partial segmentation assumption only restricts the model from matching a fraction of the overall size distribution. The model’s distributions of owner-occupied and rental units overstate the demand for the smallest available units but match the rest of the distributions relatively well. Alternative segmentation assumptions shown in Table (7) provide small fixes to these shortcomings at the expense of distorting other targeted moments such as the homeownership rate or the housing expenditure share as shown in Table (8).

House Size	Data Owners	Benchmark Model	No seg.	Full seg.	Partial seg.	Smaller size 1	Larger size 1
1	9		19		19		
2	24	55	23		22	46	49
3	25	9	23		24	17	14
4	18	13	13	89	12	13	13
5	10	17	16	2	16	18	18
6	9	4	5	9	5	5	4
7	6	2	1	0	1	1	1
House Size	Data Renters	Benchmark Model	No seg.	Full seg.	Partial seg.	Smaller size 1	Larger size 1
1	51	79	76	75	76	73	77
2	28	14	14	12	14	18	14
3	11	7	6	13	10	9	9
4	5		2				
5	2		2				
6	1		1				
7	2		0				

Table 7: Distribution of housing unit sizes in percentage points by segmentation assumptions. Source: American Housing Survey, Kaplan et al. (2020).

³⁹Landvoigt et al.’s (2015) empirical evidence points to partial segmentation of housing markets by quality of units rather than size which is beyond the scope of most macro housing models. Absent a standard segmentation convention, Arslan et al. (2022) rely on rental sector convertibility frictions and Greenwald and Guren (2024) assume separate housing stocks similar to the full segmentation shown in Table (7).

Moment	Empirical Value	Benchmark Model	No seg.	Full seg.	Smaller size 1	Larger size 1
Housing/total cons. expenditures	0.16	0.16	0.15	0.18	0.15	0.16
Aggregate home-ownership rate	0.66	0.68	0.7	0.54	0.71	0.68
Av. sized owned/rented house	1.5	2	1.6	2	1.6	1.7
Av. earnings of owners/renters	2.1	2.8	2.6	2.6	2.6	2.7
Homeownership rate of < 35 y.o.	0.39	0.34	0.38	0.26	0.38	0.36

Table 8: Moments by segmentation assumptions. Source: American Housing Survey, Kaplan et al. (2020).

The segmentation assumptions are:

- **Benchmark:** renters can only choose the smallest three housing unit sizes and owners cannot choose the smallest size.
- **No segmentation:** renters and owners can choose all available housing unit sizes.
- **Full segmentation:** homeowners can only choose the largest four housing unit sizes so that there is no overlap between the units available to renters and homeowners.
- **Smaller unit 1:** size 1 is decreased to 1.07 (1.125 in the benchmark).
- **Larger unit 1:** size 1 is increased to 1.17 (1.125 in the benchmark).

Table (9) shows that the model matches the data in terms of the change in housing size as households change dwellings.

Data	Rent-to-own	Rent-to-rent	Own-to-rent	Own-to-own
Data	0.25 (0.01)	0.04 (0.01)	-0.29 (0.01)	0.04 (0.01)
Model	0.29	0.15	-0.34	0.03

Table 9: Average log-changes in house size by type of transition. House size is the number of rooms of a house in the data which is the PSID form 1968 to 1996 via Kaplan et al. (2020). Standard errors are in parentheses.

C.4 Cross-sectional Calibration under Markov Credit Conditions

Moment	Parameter	Empirical Value	Model Value
Agg. net worth/annual agg. labor income	β	5.5	4.9
Median ratio of net worth to labor income	β	1.2	1.2
Median net worth: age 75/age 50	ψ	1.55	1.47
% of bequests in bottom 1/2 of wealth dist.	\underline{b}	0	0
Housing/total cons. expenditures	ϕ	0.16	0.16
Aggregate home-ownership rate	ω	0.66	0.7
Foreclosure rate	ξ	0.005	0.0014
P10 housing/total net worth of owners	$\min \mathcal{H}$	0.11	0.08
P50 housing/total net worth of owners	$\# \mathcal{H}$	0.5	0.29
P90 housing/total net worth of owners	$\text{gap } \mathcal{H}$	0.95	0.76
Average sized owned house/rented house	$\min \tilde{\mathcal{H}}$	1.5	2
Average earnings of owners to renters	$\# \tilde{\mathcal{H}}$	2.1	2.7
Annual fraction of houses sold	κ_h	0.1	0.1
Homeownership rate of < 35 y.o.	Ξ	0.39	0.42
Employment in construction sector	\bar{L}	0.05	0.04

Table 10: Targeted moments in calibration corresponding to model parameters. The table is similar to table (1) in the main text but with credit conditions that evolve according to a Markov process rather than a one-time shift.

Parameter	Empirical Value	Model Value
Fraction of homeowners w/mortgage	0.66	0.72
Fraction of Homeowners w/HELOC	0.06	0.01
Aggr. mortgage debt/housing value	0.42	0.51
P10 LTV ratio for mortgages	0.15	0.02
P50 LTV ratio for mortgages	0.57	0.52
P90 LTV ratio for mortgages	0.92	0.92
Share of NW held by bottom quintile	0	0
Share of NW held by middle quintile	0.05	0.09
Share of NW held by top quintile	0.81	0.66
Share of NW held by top 10 percent	0.7	0.43
Share of NW held by top 1 percent	0.46	0.06
P10 house value/earnings	0.9	0.94
P50 house value/earnings	2.1	1.8
P90 house value/earnings	5.5	4.1

Table 11: Untargeted moments in calibration. The table is similar to table (3) in the main text but with credit conditions that evolve according to a Markov process rather than a one-time shift.

D Appendix: Learning Calibration

When constant, the learning gain g is set to minimize the mean squared errors of house price forecasts from the model relative to an empirical proxy constructed from the University of Michigan Surveys of Consumers. Because the Michigan Survey’s questions about future house prices are only available starting in 2007, there are no direct measures of house price expectations from 1999 to 2007 as shown by Kuchler et al. (2023, Table 2). To construct a house price expectations proxy, I exploit the 0.92 correlation between expected house price growth in the next 12 months (2007 start) and whether or not it is a relatively good time to sell a house (1992 start).⁴⁰

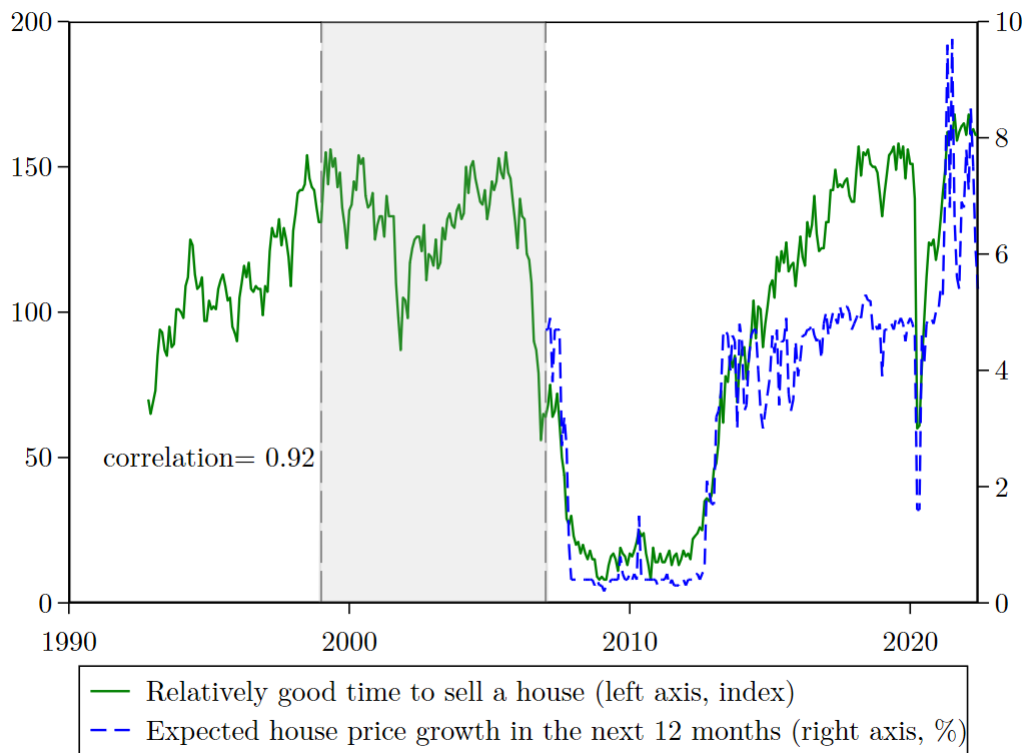


Figure 12: Responses from the University of Michigan Surveys of Consumers, percent of respondents who say it is a good time to sell a house less those who say it is a bad time plus 100 and the median expected house price growth in the next 12 months expressed as 12-month percentage change. The shaded bar between the dashed vertical lines denotes the U.S. housing boom (1999 to 2007).

Given the tight correlation between the two series, I create a backcast of the expected change in house prices going back to 1992 by projecting expectations y_t onto selling conditions

⁴⁰The **Relative** column of Table 43 is the **Good time to sell** column minus the **Bad time to sell** column plus 100. The survey asks, “Generally speaking, do you think now is a good time or a bad time to sell a house?” The **Median** column of Table 46 is the median response to the question, “By about what percent do you expect prices of homes like yours in your community to go (up/down), on average, over the next 12 months?”

x_t for $t = \{\text{Jan. 2007}, \dots, \text{Jun. 2022}\}$.

$$y_t = \beta_0 + \beta_1 x_t + e_t$$

Using the estimated coefficients $\hat{\beta}$, I then backcast the expectations series \hat{y}_t from the selling conditions series x_t when the former is not yet available, $t = \{\text{Jan. 1992}, \dots, \text{Dec. 2006}\}$.

$$\hat{y}_t = \hat{\beta}_0 + \hat{\beta}_1 x_t$$

Figure (13) shows that the backcasted empirical proxy has a good in sample fit with an r^2 near 1. Although the higher frequency movements of the two series differ, the backcast captures the path of expectations which is key for the study of the U.S. housing boom.

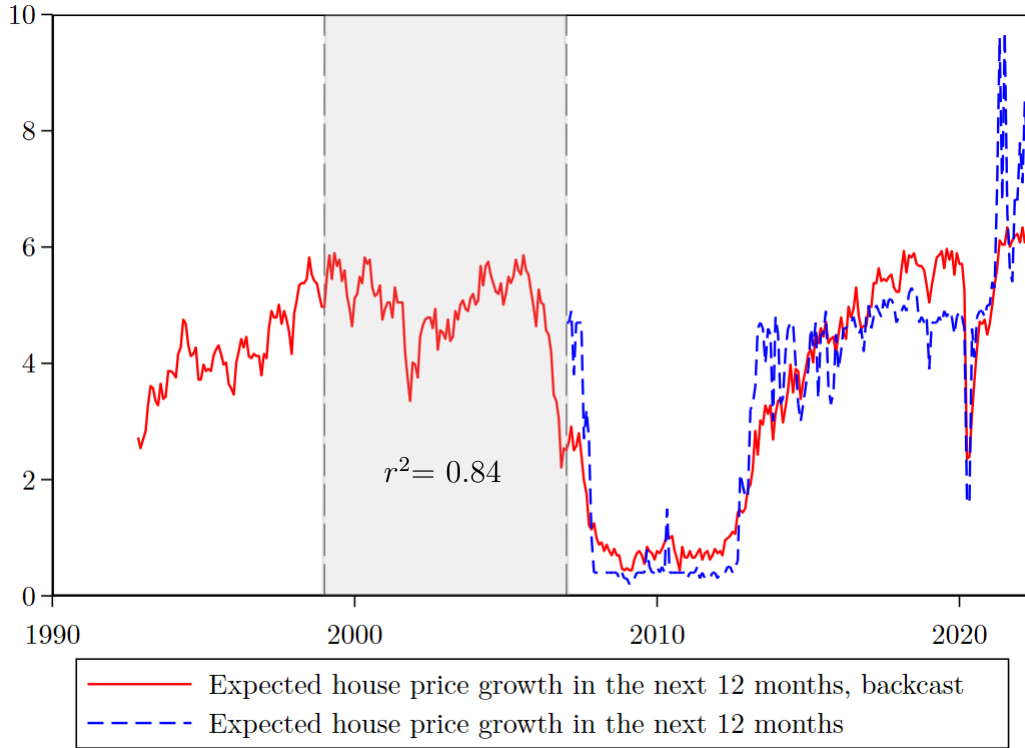


Figure 13: Median expected house price growth in the next 12 months from the University of Michigan Survey of Consumers, 12-month percentage change. Shaded bar between the dashed vertical lines marks the U.S. housing boom (1999 to 2007).

House price expectations from the model and the empirical proxy have four key differences that affect their comparability. Those from the model are for two-year real detrended house prices in levels while those from the data are for nominal expected 12-month growth rates. Calculations below discuss which differences affect the mean squared forecast error used to calibrate the constant learning gain.

Growth rates vs. levels: Forecast errors from growth rates and levels are roughly equivalent as shown by equations (20) and (21). Assuming the current month's house prices p_τ are known to survey participants, the h period ahead forecast error e_τ^{survey} for month τ can be defined as:

$$e_\tau^{survey} \equiv \log p_{\tau+h} - \log F_\tau p_{\tau+h}$$

Noting that the Michigan survey provides an expected 12-month growth rate $F_\tau g_{\tau+h}$ for $h = 12$, the above definition becomes:

$$e_\tau^{survey} \equiv \log p_{\tau+h} - \log (p_\tau (1 + F_\tau g_{\tau+h}))$$

Re-arranging and letting $\log(1 + F_\tau g_{\tau+h}) \approx F_\tau g_{\tau+h}$, the above expression becomes:

$$e_\tau^{survey} \equiv \log (p_{\tau+h}/p_\tau) - F_\tau g_{\tau+h} \quad (20)$$

In the model, the f period ahead forecast for period t in aggregate state Z_t with $Z, t \in \{Z, Z'\}$ is given as:

$$e_t^{model} \equiv \log p_{t+f} - \mathbb{E}_{Z_{t+f}}[a_{Z,t}^0 + a_{Z,t}^1 \log p_t] \quad (21)$$

Where the period t is two years and $f = 1$ so that the forecast is one period ahead.

Forecast horizon: To compare the empirical proxy's 12-month forecast horizon to the two-year forecast horizon from the model, I assume that survey respondents expect house price growth for the next 12 months to remain for the following 12 months. The imputed forecast for the next $2 \times h = 24$ can be written as:

$$\begin{aligned} e_\tau^{survey} &\equiv \log p_{\tau+2 \times h} - \log F_\tau p_{\tau+2 \times h} \\ &\quad \log p_{\tau+2 \times h} - \log (p_\tau (1 + F_\tau g_{\tau+h})^2) \\ &\quad \log (p_{\tau+2 \times h}/p_\tau) - 2 \times F_\tau g_{\tau+h} \end{aligned} \quad (22)$$

Imputing the forecast for the next two years via compounding may overstate expected house price growth in the next two years, $2 \times F_\tau g_{\tau+h} > F_\tau g_{\tau+2 \times h}$. Although Figure (14) shows that the forecast errors of house price growth at the 12-month and two-year horizons (equations 20 and 22) are quite similar throughout the housing boom, they differ in the later part when the two-year series is higher resulting in a larger mean squared error. However, because expected house prices for the next five years are at their all-time high at the end of the housing boom as shown in Panel (2a) in the main text, house price expectations for the next

two years may have indeed been higher than those for the next 12 months.⁴¹

Given the concerns about imputing the house price expectations for the next two years, one could instead calibrate the learning gain to the one-year forecast error. The resulting housing boom simulations would be like those shown in Figure (4) with a gain lower than $g=0.508$. With the lower value of the learning gain, the mean squared forecast error is closer to the 7.93 value of the one-year horizon rather than the 28.66 value at the two-year horizon. House prices still boom, but to a peak that is lower than the 75 percent match to the data observed in the main specification.

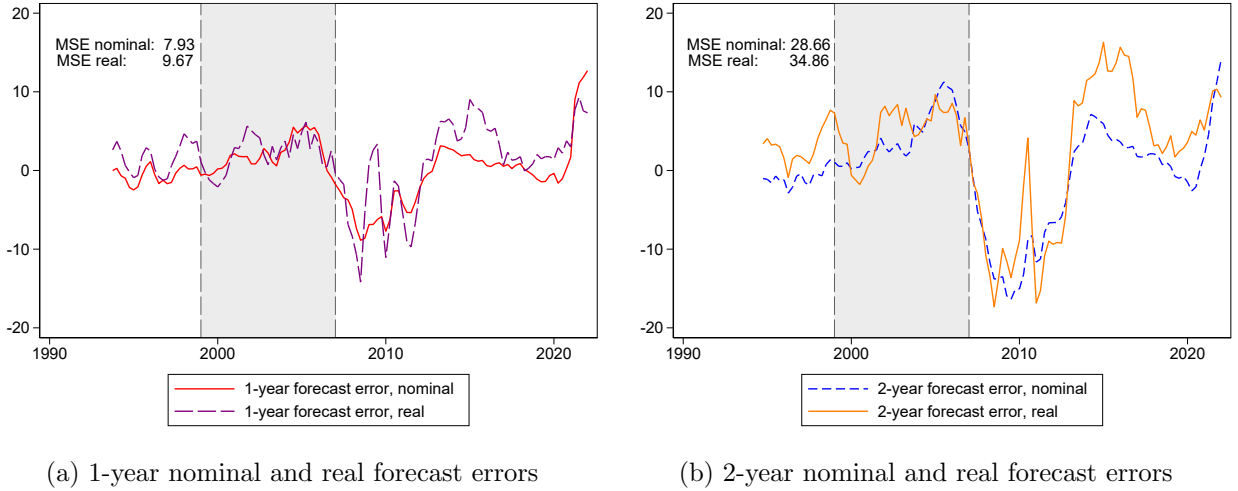


Figure 14: Panel (a): Real house price growth is the FHFA house price index scaled by the price index for non-durable consumption. Expected house price growth for the next 12 months is the empirical proxy constructed from the University of Michigan Survey of Consumers and is scaled by responses for expected inflation from the survey. Panel (b) is same as Panel (a), but with house price and inflation expectations both imputed to a two-year forecast horizon. The panels are given in the quarterly average of the 12-month percentage change. Shaded bar between the dashed vertical lines marks the U.S. housing boom (1999 to 2007).

Nominal vs. real: The real house price forecast error can be calculated by dividing both realized and expected house prices by actual and expected inflation. Let $\pi_{\tau+h}$ be one-year

⁴¹The expectations for the next five years are the **median** column of Table 47, "Expected Change in Home Values During the Next Five Years." The survey asks, "By about what percent per year do you expect prices of homes like yours in your community to go (up/down), on average, over the next five years or so?" Two problems prevent interpolation of the two-year expectations from the one- and give-year expectations. First, the one- and five-year expectations do not have a monotonic ordering. Survey respondents expected higher house price growth in the next five years than in the next one year from early 2007 to mid-2013, but the opposite ordering from mid-2013 throughout the remainder of the period shown in Panel (2a). Second, there is no tight correlation of five-year series with other series in the Michigan survey thereby precluding a backcasting exercise to obtain proxies for the pre-2007 period.

realized inflation and $F_\tau \pi_{\tau+h}$ be its expected value for month τ . The real forecast error is:

$$e_\tau^{survey,real} \equiv \log \left(\frac{p_{\tau+h}}{1 + \pi_{\tau+h}} \right) - \log \left(\frac{p_\tau(1 + F_\tau g_{\tau+h})}{(1 + F_\tau \pi_{\tau+h})} \right) \\ \underbrace{\log(p_{\tau+h}/p_\tau) - F_\tau g_{\tau+h}}_{e_\tau^{survey}} - (\pi_{\tau+h} - F_\tau \pi_{\tau+h}) \quad (23)$$

The real house price forecast error is the forecast error of nominal house price growth less the forecast for the inflation rate.⁴² Figure (14) shows that the real and nominal house price forecasts are roughly similar for both the one-year expectations and the two-year imputed expectations throughout the housing boom.⁴³ Within each forecast horizon, there is little difference between the real or nominal mean squared errors at the one-year horizon. At the two-year horizon, the real error is larger than the nominal error and corresponds most closely to the value of 37.88 obtained under a larger constant shown in Figure (4).

De-trending: The empirical real house price forecast errors are not affected by subtracting out a time trend like the one used to construct house prices in the model. The predicted linear time trend $\hat{\Gamma} p_{\tau+h}$ cancels from both sides of equation (23):

$$\log(p_{\tau+h}(1 - \Gamma)/(1 + \pi_\tau)) - \log(p_\tau(1 - \Gamma)(1 + F_\tau g_{\tau+h})/(1 + F_\tau \pi_{\tau+h}))$$

Additional caveats: Evidence from other surveys suggest that responses from the University of Michigan Survey of Consumers may actually underestimate expected house price growth which could lead to lower forecast errors than those presented above.⁴⁴ For this reason, I use the median house price expectations for the next 12 months instead of the mean as the former tends to run higher thus resulting in lower forecast errors. Moreover, figure (15) shows that the median point prediction for house price growth in the next 12 months from the NY Fed Survey of Consumer Expectations is not always higher than the empirical proxy used in this paper for the period in which they are both available.

⁴²The realized inflation series is the PCE price index for durables less consumption which is what is used elsewhere in the paper. Results are similar if the headline PCE price index is used instead.

⁴³The 2-year real forecast error is: $\log(p_{\tau+2 \times h}/p_\tau) - 2 \times F_\tau g_{\tau+2 \times h} - (\pi_{\tau+2 \times h} - 2 \times F_\tau \pi_{\tau+2 \times h})$.

⁴⁴Kuchler et al. (2023) note in footnote 5 that house price expectations from the NY Fed Survey of Consumer Expectations (2013 start) show patterns similar to those of the University of Michigan Survey of Consumers with average one-year expectations usually about 2 percentage points higher. De Stefani (2021) notes that house prices expectations from the University of Michigan Survey of Consumers are only available for homeowners which may be problematic because Kindermann et al. (2024) find that renters looking to buy houses are the most informed about house price expectations.

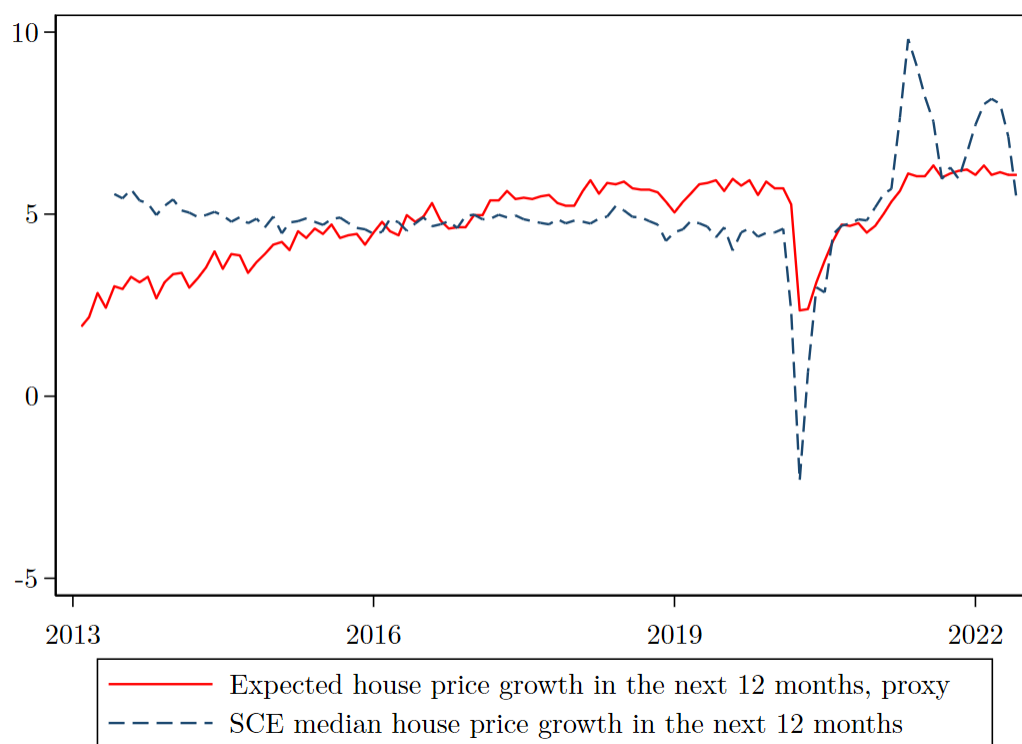


Figure 15: Expected house price growth for the next 12 months is the empirical proxy constructed from the University of Michigan Survey of Consumers and the median point prediction of expected house price growth for the next 12 months from the Federal Reserve Bank of New York Survey of Consumer Expectations, 12-month percentage change.

E Appendix: Comparison to Kaplan et al. (2020)

As noted in section 3.1, there are some small differences between the implementation in this paper relative to that of Kaplan et al. (2020). These differences require a slightly lower operating cost of the rental company Ξ to calibrate to the correct homeownership rate for households under 35 years of age and are listed below:

- The McClement’s scale on utility e_j is set so that $\{e_j\}_{j=21}^{30} = 1$ while in Kaplan et al. (2020) it is instead set at $\{e_j\}_{j=21}^{30} = \{e_j\}_{j=1}^8 > 1$.
- At age 30, agents who choose to stay in their house do not borrow HELOCs.
- Retired agents have $-\zeta(Z)$ in the mortgage pricing function.⁴⁵

Figure (16) shows that these differences have almost no implications on the main findings of Kaplan et al. (2020) and only affect magnitudes and time paths of impulse responses. All purple lines shown in Figure (16) are results from Kaplan et al. and all blue lines are from the code in this paper solved under the latter’s forecasting coefficients for house prices.

The differences noted above result in a slightly smaller boom in house prices, slightly larger drop in the rent-to-price ratio, and smaller rise in consumption, as shown in panels (16a), (16b), and (16f), respectively.

The effects are more substantial for the impulse responses for the normalized and un-normalized homeownership rate, leverage, and foreclosure rate as shown in panels (16c), (16g), (16d), and (16e), respectively. First, I note that leverage and the foreclosure rate (panels (16d) and (16e), respectively) both increase sharply in the bust with the degree of the increases depending on the operating cost of the rental company Ξ . The increases in the bust are relatively higher under the original high value of Ξ as shown by the dotted purple and blue lines than under the re-calibrated low value of Ξ as shown by the dashed purple and blue lines. Although the increase in both leverage and the foreclosure rate are lowest under this paper’s implementation with the re-calibrated low value of Ξ , panels (16d) and (16e) show that this can be accounted for, in part, due to the re-calibration.

Furthermore, the homeownership rate can also account for differences in the increase in leverage and foreclosures in the bust. The un-normalized homeownership rate shown in panel (16g) is relatively higher under the original high value of Ξ and lower under the re-calibrated lower value, as seen by the differences between the dotted and dashed lines. The purple lines from Kaplan et al. (2020) generally start from a higher homeownership rate than the blue lines of this paper. Finally, I note that for both the dashed lines and the dotted lines, the shape of the homeownership rate is quite similar.

⁴⁵The mortgage pricing function was updating before it finished the age loop. This was fixed by closing off several loops before going into the value function iteration step.

Figure (17) compares the exogenous beliefs version of Kaplan et al. (2020) to a version with credit conditions that loosen one time instead of credit conditions that evolve according to a Markov process. The figure shows that the impulse responses of housing boom simulations are nearly identical for all prices and quantities. This is the case because the probability of Markov credit conditions shifting is incredibly low at 1% so shutting it to 0% and having the shift be a surprise is quantitatively little different. This figure suggest that the model solved under endogenous beliefs and a one-time shift in credit conditions is readily comparable to its endogenous beliefs counterpart with Markov credit conditions.

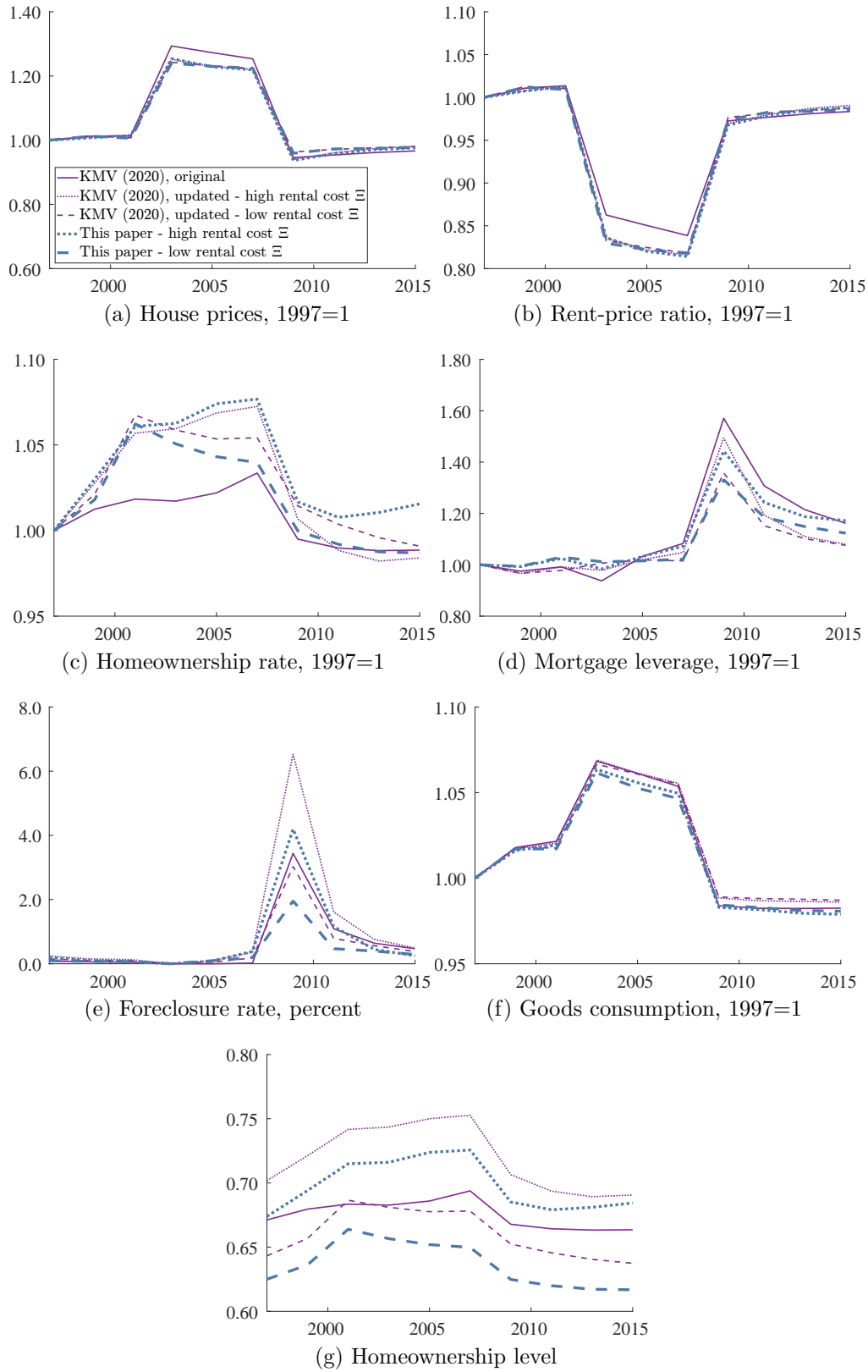


Figure 16: Housing boom impulse responses under exogenous beliefs, 1997=1.

Note: purple lines are results from Kaplan et al.'s (2020) code repository and blue lines are from the code of this paper, set to the same values of forecasting rule coefficients. The solid purple line is the original impulse responses. The dashed and dotted lines correct from some small discrepancies with the former solved under the original value of the operating cost of the rental company Ξ which is higher than the re-calibrated lower value.

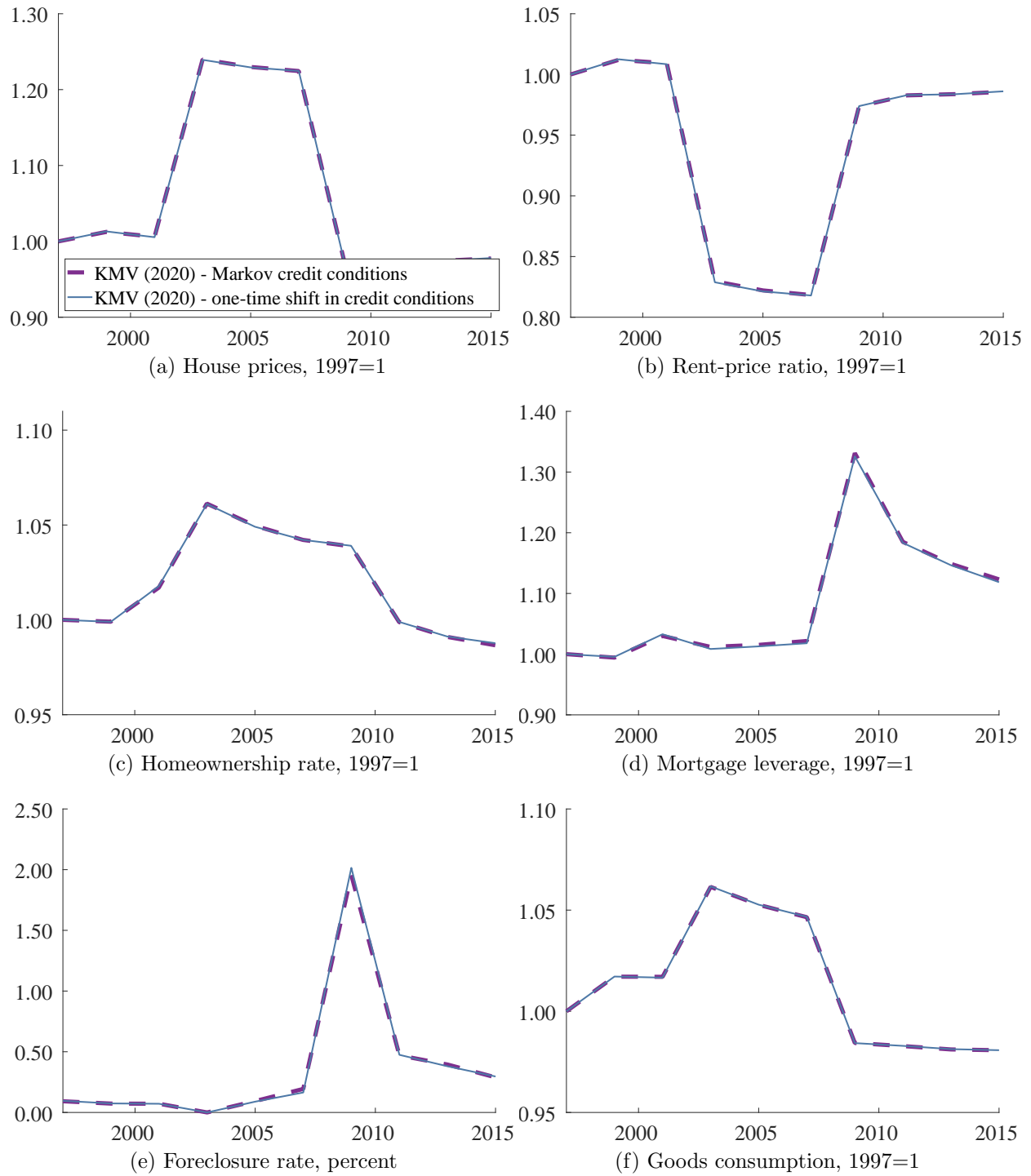


Figure 17: Housing boom impulse responses under exogenous beliefs, 1997=1.

Note: simulations are from this paper's code solved under Markov credit conditions as in (2020) and under a one-time shift in credit conditions as in this paper.

F Appendix: Alternative Housing Boom Simulations

F.1 Alternative fundamentals

Figure (18) shows counterfactual housing boom simulations that quantify the contributions of beliefs and credit conditions. Panel (18a) shows that house prices are highest and thus closest to matching the data in the main specification when there is a shift in income and credit conditions accompanied by endogenously optimistic beliefs. However, counterfactual simulations show that beliefs are quantitatively most important for determining booming house prices but credit conditions must loosen to account for other housing boom dynamics.

Panel (18a) shows via the dashed light blue lines that shutting down the shift in credit conditions, but still allowing for endogenous beliefs and the shock to income, results in house prices that boom, albeit less than in the main specification. This suggests that beliefs play an important role in generating an empirically consistent boom in house prices. Panels (18c)-(18e) show that without the loosening of credit conditions there are counterfactually low responses in the homeownership rate, mortgage leverage, and the foreclosure rate, respectively.

Shutting down beliefs, but allowing for shocks to income and credit conditions (red lines with circles), results in no boom in house prices as shown in Panel (18a).⁴⁶ Although there is an increase in homeownership as shown in Panel (18c), new homeowners mostly purchase the same sized house as they previously rented. Homeowners must upsize to push up house prices and this does not occur without optimistic beliefs about future house prices. The rent-price ratio (Panel 18b) remains flat, mortgage leverage counter factually rises (Panel 18d) and consumption and foreclosures remain counterfactually low (Panels 18f-18e).

Finally, figure (18) shows that simulations are similar whether credit conditions loosen via a one-time shock (red lines with circles) or are Markov (dotted black lines).

⁴⁶Forecasting coefficients \mathbf{a}_Z^{loose} are obtained via the multi-step fixed point method with fluctuations in aggregate income only and credit conditions set at their loose values. As in the main specification, the housing boom simulation then starts with the economy in the state with low aggregate income and tight aggregate credit conditions $\{\Theta(Z_{low}), \mathcal{C}(Z_{tight})\}$ along with the corresponding coefficients $\mathbf{a}_{Z_{low}, Z'}^{tight}$. As the economy transitions to the state with high aggregate income and loose credit conditions $\{\Theta(Z_{high}), \mathcal{C}(Z_{loose})\}$ coefficients take on the values $\mathbf{a}_{Z_{high}, Z'}^{loose}$.

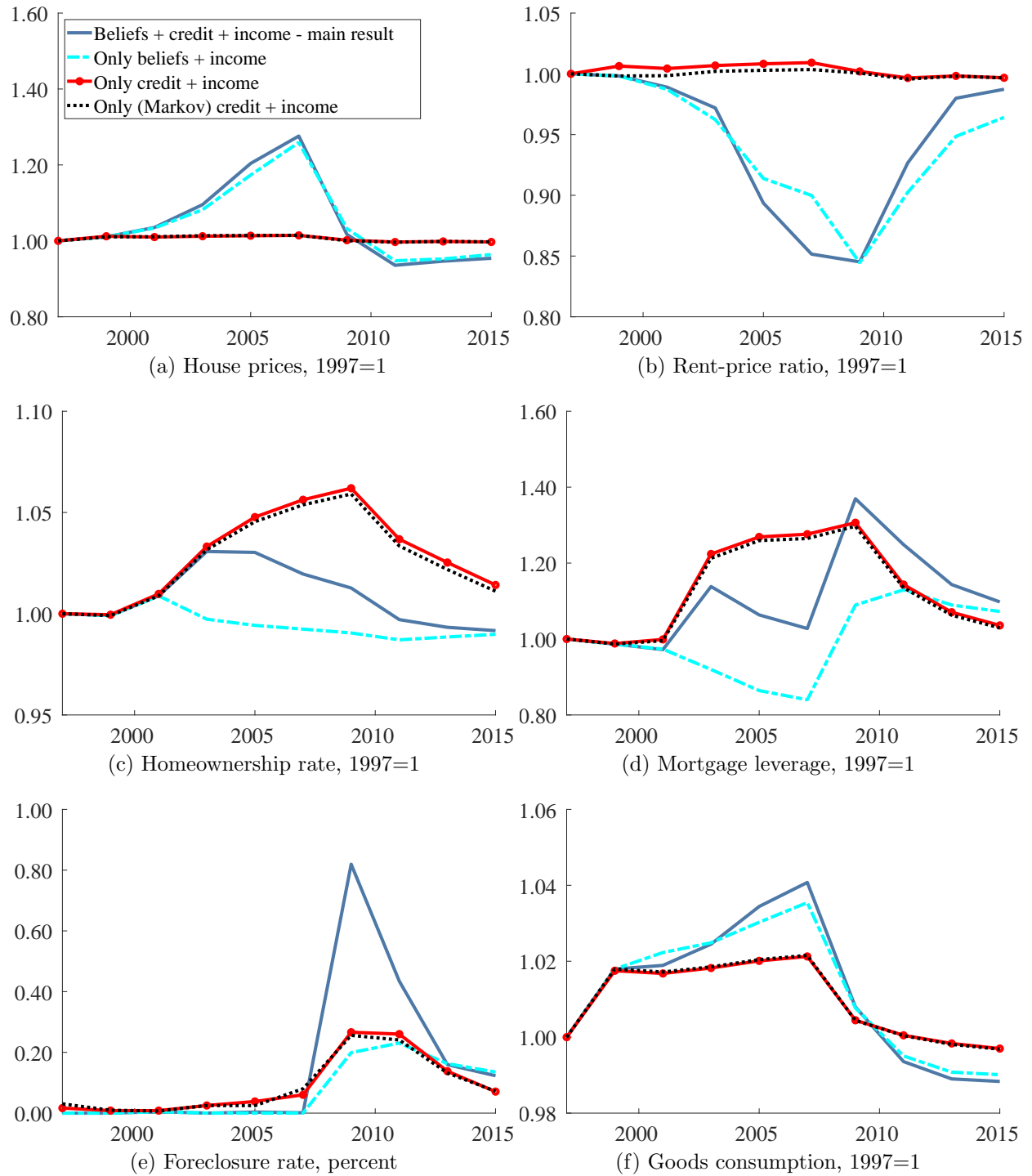


Figure 18: Counterfactual housing boom simulations from the model decomposition the effects of beliefs and credit conditions.

F.2 Alternative Forecast Error Formations

In equation (16) the lagged forecast error is defined as:

$$\mathbf{a}_{Z,t} = \mathbf{a}_{Z,t-1} + g_t \mathbf{x}_{t-2} \underbrace{(\log p_{t-1} - \mathbf{x}'_{t-2} \mathbf{a}_{Z,t-1})}_{e_{t-1}} \quad (16)$$

Because there is no definitive convention, this forecast error could take on other forms such as the lagged forecast error from a particular aggregate state or the realized forecast error shown below in equation (24) and (25), respectively.

$$e_{t-1} = \log p_{t-1} - \mathbf{x}'_{t-2} \mathbf{a}_{Z,t-2} \quad (24)$$

$$e_{Z,t-1} = \log p_{Z,t-1} - \mathbf{x}'_{Z,t-2} \mathbf{a}_{Z,t-1} \quad (25)$$

Figure (19) shows that these forecast error formations, “Alternative forecast error 1” and “Alternative forecast error 2” shown by the dashed light blue and red solid lines with a circle, respectively, have little material effect on housing boom simulations in most cases. They are quite close to the main results shown by the solid blue line.

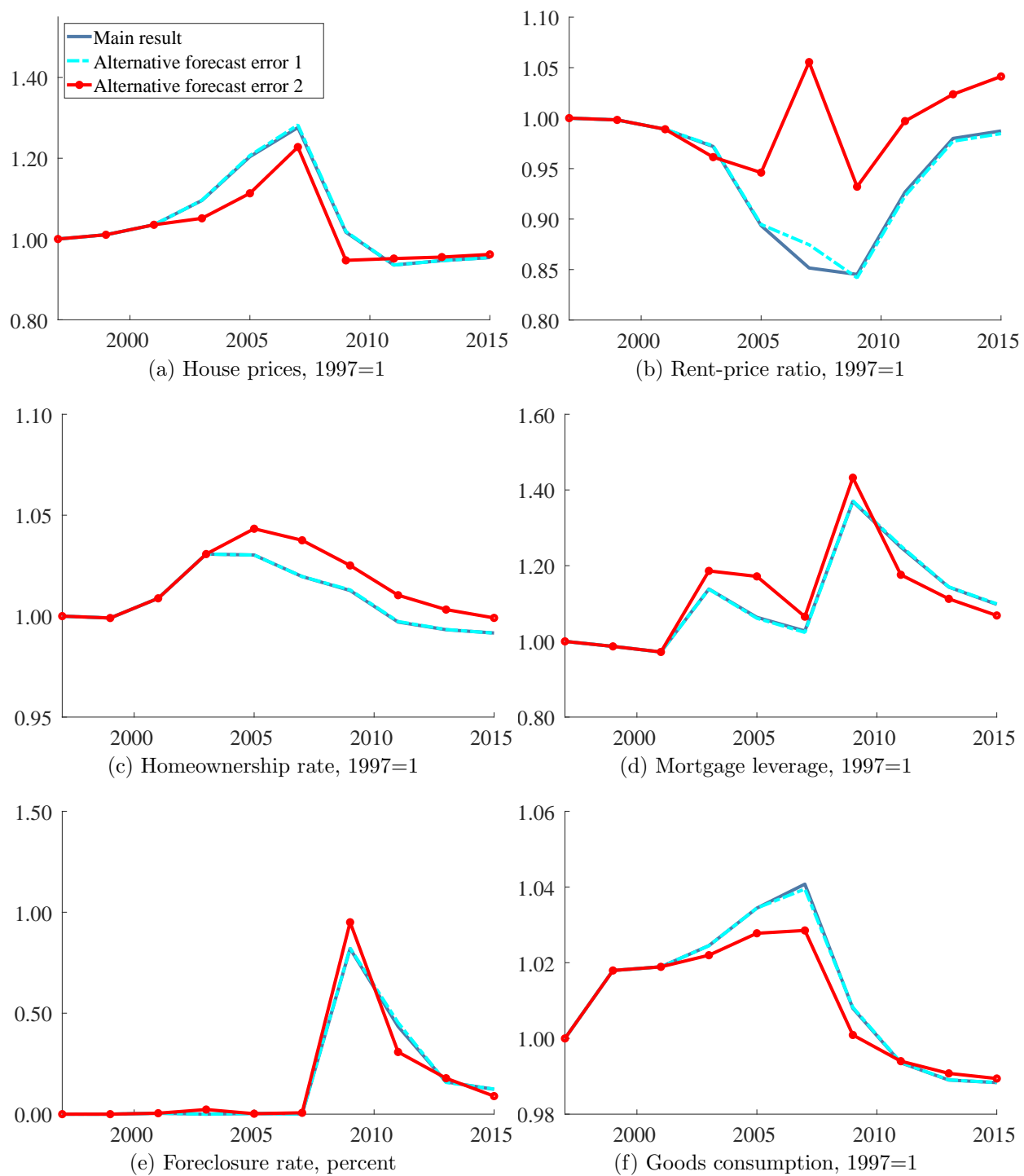


Figure 19: Housing boom simulations from the model under alternative forecast error formations.

F.3 Initial Forecast Error Calibrations

With the initial learning coefficients \mathbf{a}_0 set at their values for tight aggregate credit conditions and high income $\mathbf{a}_{Z_{high}, Z'_{high}}^{tight}$, the initial forecast error is 1 percent which is close to its empirical value of 1.36 percent. Figure (20), shows that the simulation results are similar if the constant coefficient a_0^0 is adjusted so that the initial forecast error attains a value of 1.36, while leaving the slope coefficient unchanged at $a_0^1 = a_{Z_{high}, Z'_{high}}^{1, tight}$ (dashed light blue lines). Furthermore, results are similar if the slope coefficient is adjusted and the constant coefficient is unchanged (solid red lines with circles). And finally, the housing boom dynamics are broadly similar if either coefficient is adjusted so that the initial forecast error is 1.5 times its empirical value (dashed black and dashed green lines with circles).

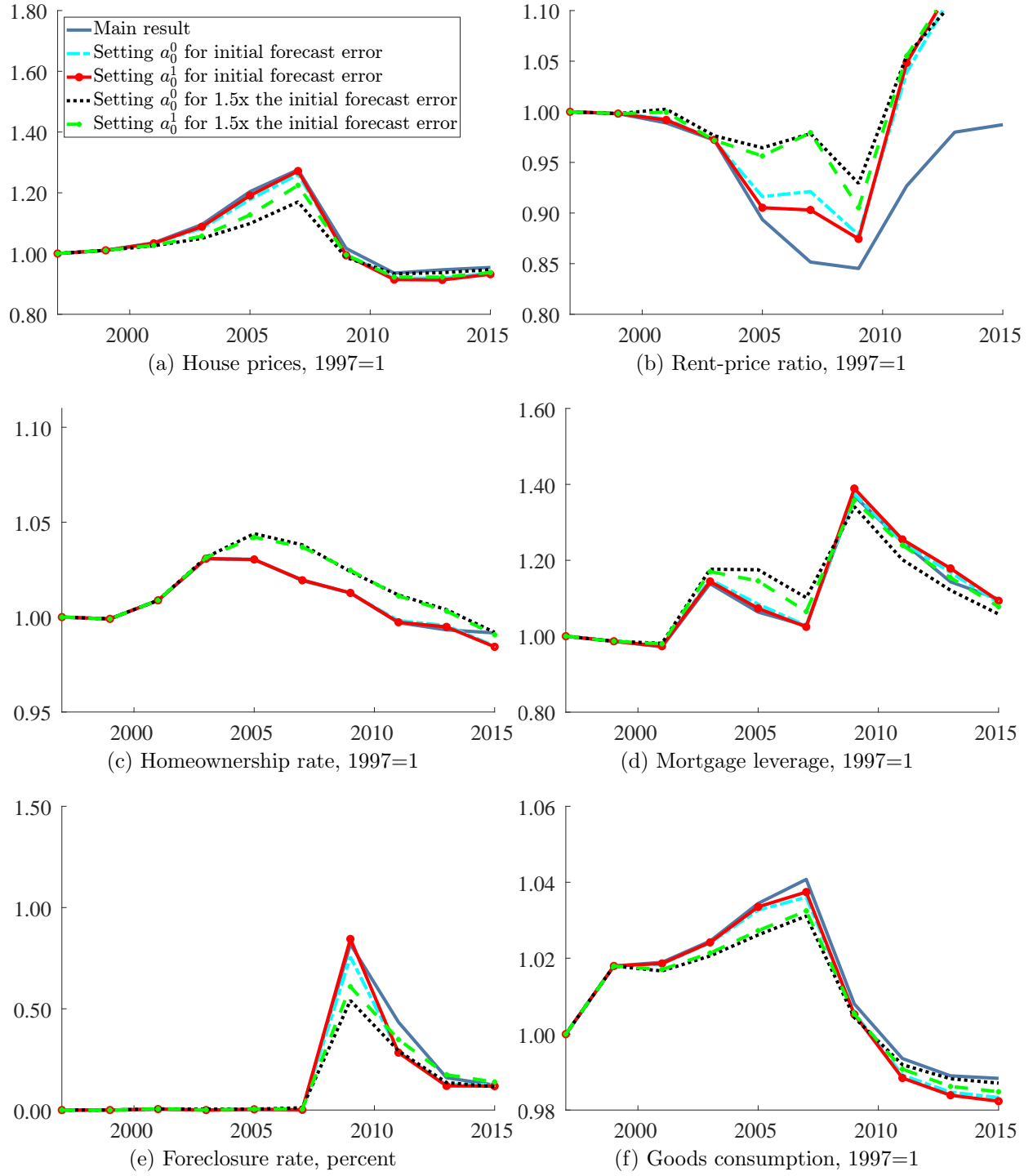


Figure 20: Housing boom simulations from the model under alternative forecast error calibrations.

F.4 Mixed and fixed learning gains

Figure (21) shows that housing boom simulations under different types of fixed learning gains are similar to the main result under a mixed learning gain. The mixed learning gain of main result (solid blue lines) is constant, $g_t = g$, when aggregate credit conditions loosen and income expands, but decreasing in all other aggregate states, $g_t = g_{t-1}/(1 + g_{t-1})$. In the decreasing gain simulation (dashed light blue lines), $g_t = 1$ in 2001 at the start of the housing boom and decreases to $g_t = g_{t-1}/(1 + g_{t-1})$ in the following periods. In the constant gain simulation (solid red lines with circles), $g_t = g = 0.508$ in all periods.

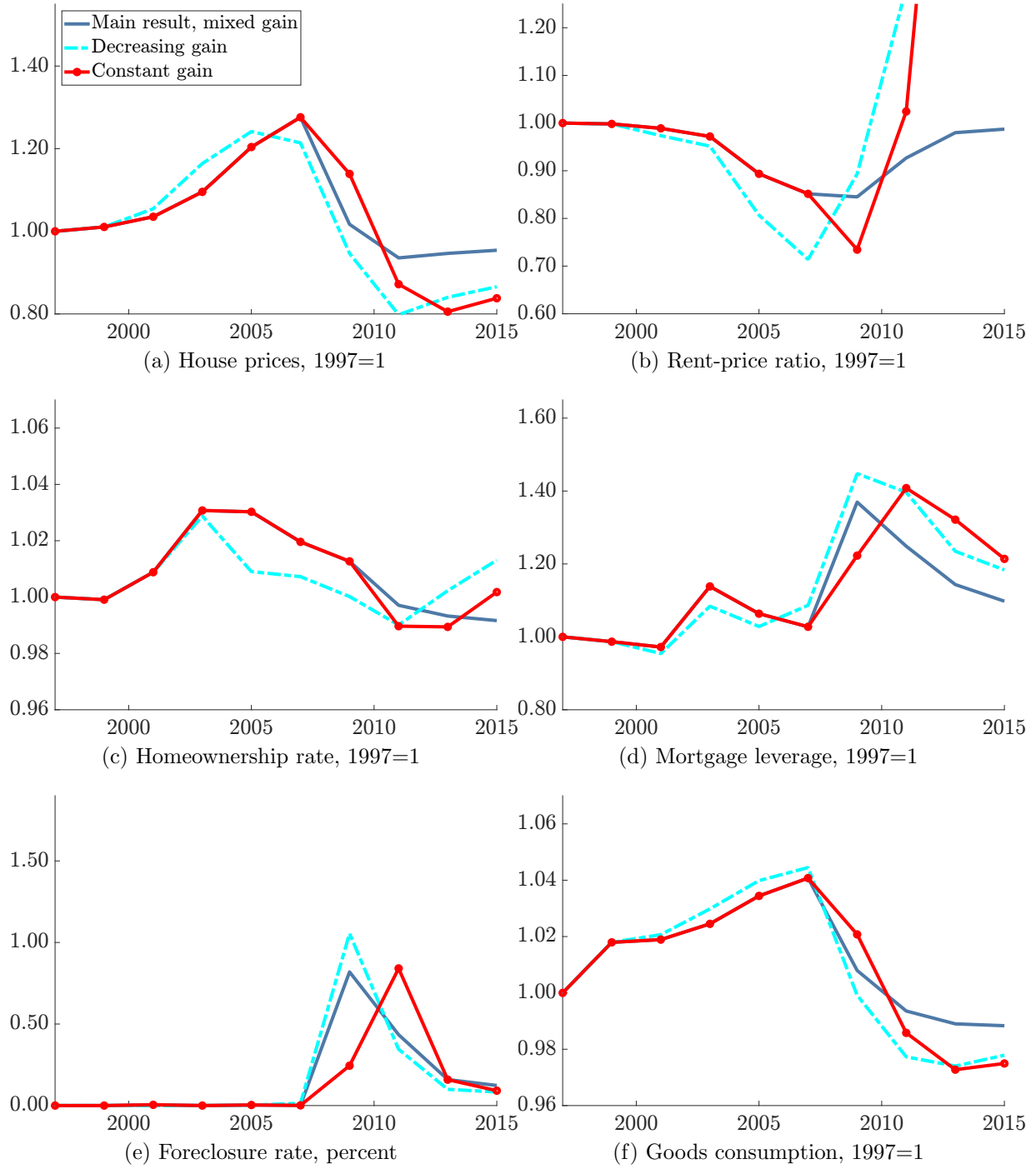


Figure 21: Housing boom simulations under fixed rather than mixed learning gains.

F.5 Exploring learning mechanisms

The results shown in figure (22) explore the properties of adaptive learning.

The simulation titled “Learning starts earlier” (dashed light blue lines), starts adaptive learning at the beginning of the simulation rather than when the economy transitions to the aggregate state characterized by looser credit conditions and high income in 2001 as under the main result (solid blue lines). The results are quite similar with notable differences being a steeper spike in the rent-price ratio, leverage, and foreclosures, shown in panels (22b), (22d), and (22e), respectively.

In the simulation titled “Longer boom” (solid red lines with circles), the housing boom state, characterized by the aggregate states with high income and looser credit conditions, counterfactually lasts for another 10 years rather than ending in 2009. The simulation paths are exactly the same as those of the main result (solid blue lines) until 2009. Thereafter, house prices, as shown in panel (22a), contract less suddenly than in the main simulation and reach a deeper trough by 2013. House prices rebound above their pre-boom values around 2018 which actually results in a second housing boom that peaks in late 2022. Although this path tracks the actual rebound in aggregate house prices in the data quite closely, it also results in counterfactual movements in other model prices and quantities shown. For example, the counterfactually large rebound in the price-to-rent ratio is the result of large oscillations in the house price forecast error pushing up rents counterfactually high.

The simulation titled “Alternative non-boom gain” (dotted black lines) initializes the post-boom learning gain at $g_t = g/(1 + g)$ as in Marcet and Nicolini (2003) rather than $g_t = g/(1 + t \times g)$ as in the main simulation. The simulations shown are exactly the same in the housing boom, but the slower decaying of g_t post-boom results in a deeper decline in house prices and other model quantities. Like in the “Learning starts earlier” simulation, the protracted bust in house prices is at the expensive of a counterfactually high rent-price ratio.

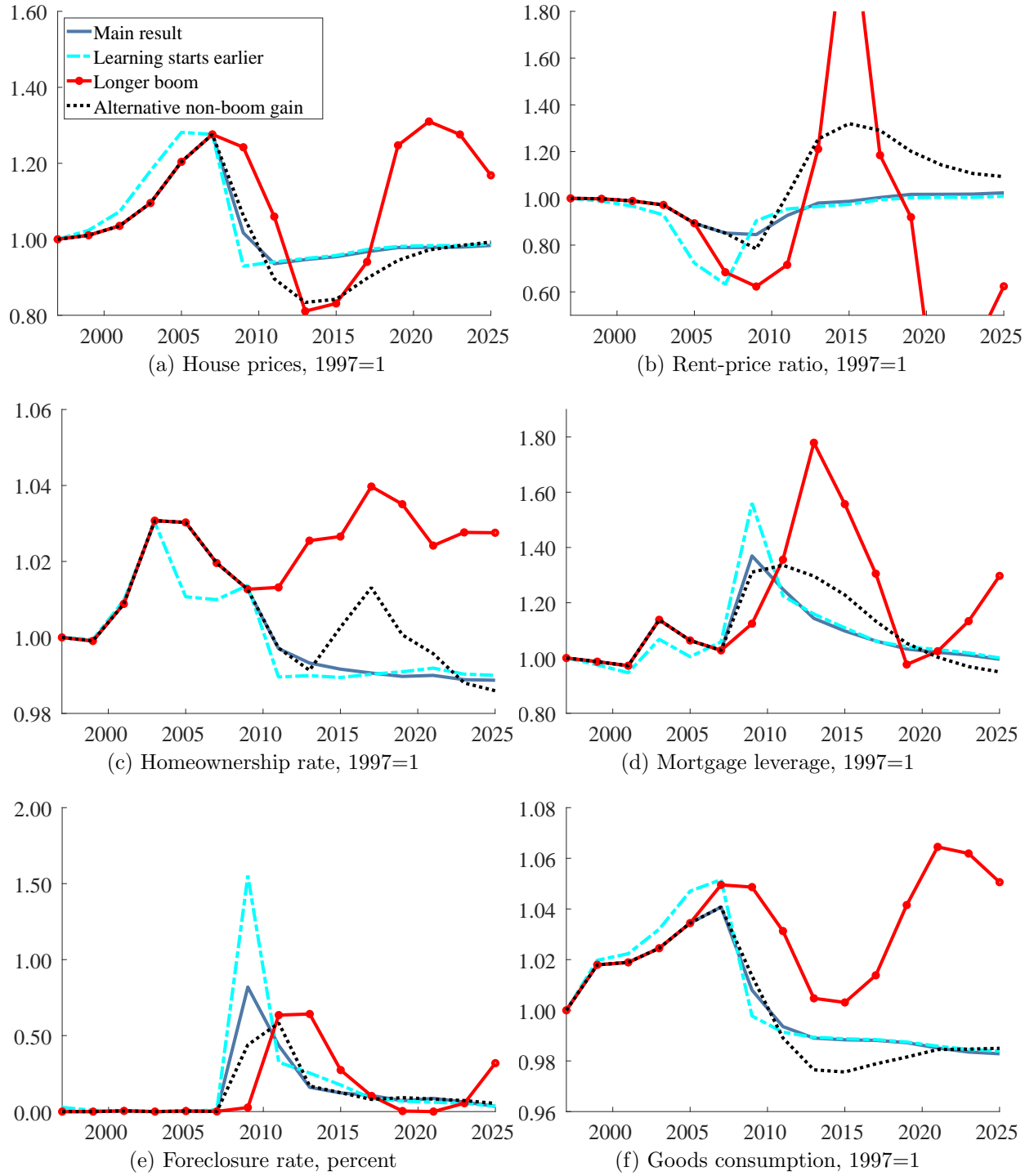
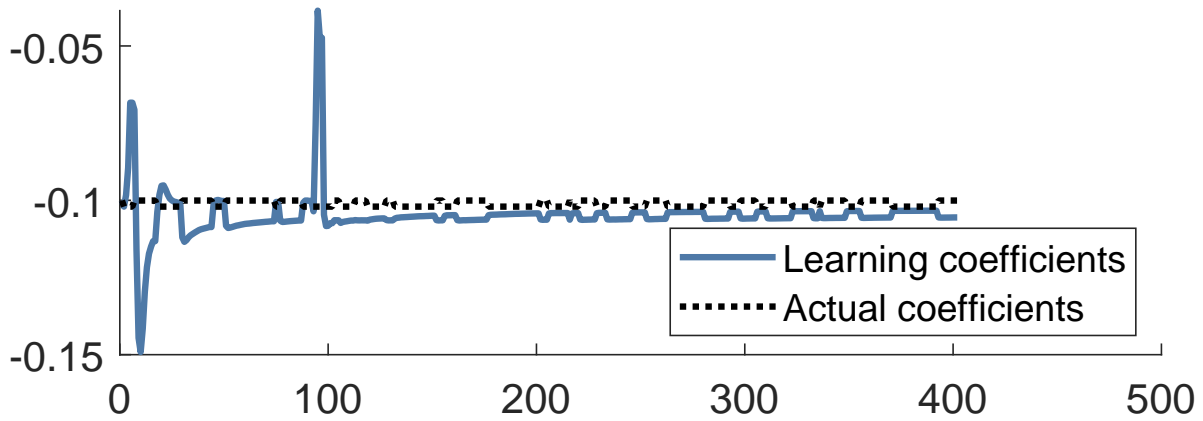


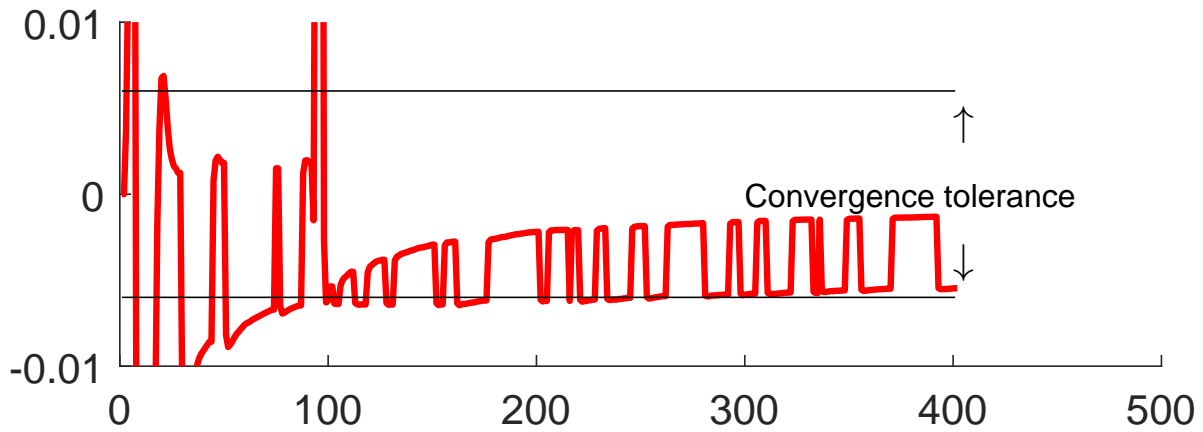
Figure 22: Housing boom simulations from the model that explore the properties of adaptive learning.

F.6 Convergence of Learning Coefficients

Figures (23) and (24) show that coefficients under adaptive learning settle at an ergodic distribution near their known counterparts. A counterfactual return to the housing boom state 100 periods (200 years) after the 2000s boom shows that coefficients adjust in response to forecast errors but revert back to an ergodic distribution in the non-boom state. Although there are observable differences between the learning coefficients and their known counterparts in panels (23a) and (24a), panels (23b) and (24b) show that these differences are well within the convergence tolerance used to solve for the fixed coefficients.



(a) Evolution of a_t^0 coefficient



(b) Difference between learning and known coefficients

Figure 23: Time path of beliefs for 400 periods. Period 0 is the start of the housing boom near period 100 there is another counterfactual unexpected loosening of credit conditions.

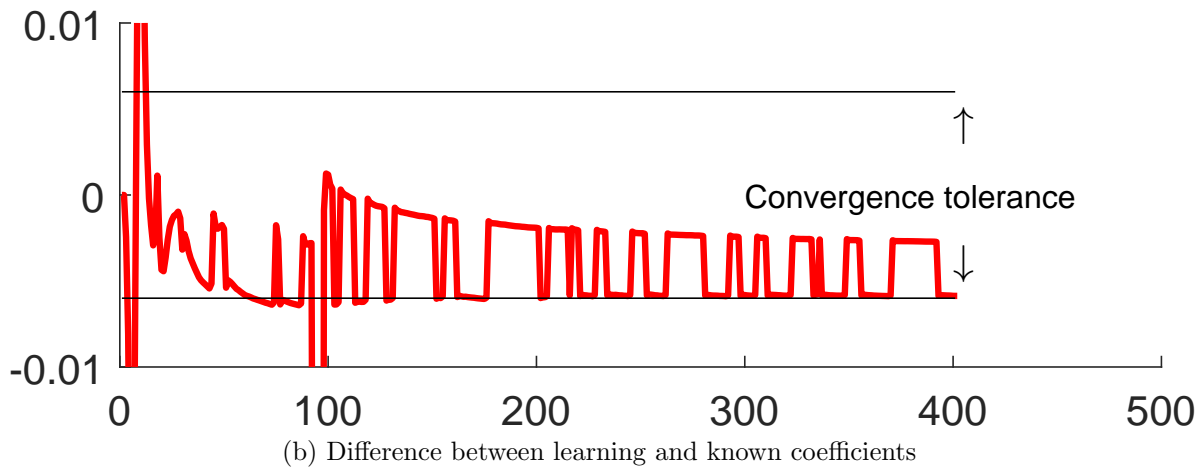
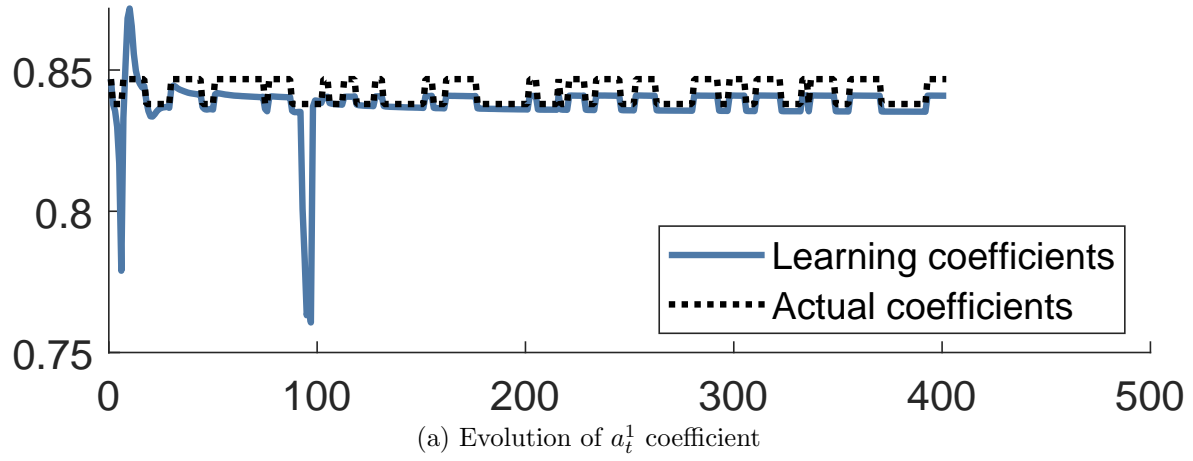


Figure 24: Time path of beliefs for 400 periods. Period 0 is the start of the housing boom and near period 100 there is another counterfactual unexpected loosening of credit conditions.

G Appendix: Data Definitions

The aggregate data definitions follow those in Appendix E.1 of Kaplan et al. (2020). They have been detrended using a linear time trend estimated from 1975 to 1997.

- **Consumption:** Quarterly nominal nondurable expenditures (line 8 of NIPA Table 2.3.5 Personal Consumption Expenditures by Major Type of Product) divided by the price index for nondurable consumption (line 8 of NIPA Table 2.3.4. Price Indexes for Personal Consumption Expenditures by Major Type of Product).
- **Homeownership:** Census Bureau U.S homeownership rate (Table 14) and by the age of household head (Table 19).
- **House Prices:** House price index for the entire United States (Federal Housing Finance Agency (FRED: USSTHPI)) divided by the price index for nondurable consumption (line 8 of NIPA Table 2.3.4. Price Indexes for Personal Consumption Expenditures by Major Type of Product).
- **Rent-Price Ratio:** Rents (Bureau of Labor Statistics Price Index for Rent of Primary Residences) divided by the FHFA house price index described above.
- **Foreclosures:** Number of consumers with new foreclosures and bankruptcies (Federal Reserve Bank of New York Quarterly Report on Household Debt and Credit) divided by the civilian noninstitutional population (FRED: CNP160V).
- **Leverage:** Flow of Funds Table B.101 Balance Sheet of Households and Nonprofit Organizations. Home mortgage liabilities (FL163165505) divided by the sum of household owner occupied housing at market value (LM155035015) and nonprofit organization real estate at Market Value (LM165035005).
- **Labor Productivity:** U.S. Total Labor Productivity (FRED: ULQELP01USQ661S)
- **Mortgage and Treasury Interest Rates:** 30-year fixed rate mortgage (FRED: GAGE30US) and 10-year Treasury at a constant maturity (FRED: GS10)
- **House price expectations:** University of Michigan Surveys of Consumers. The construction of the empirical proxy and data definitions are discussed in detail in Appendix D. New York Fed Survey of Consumer Expectations.

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