

# Assignment: 3.

## Combinational Logic Circuit.

(1) Explain Half Adder in detail.

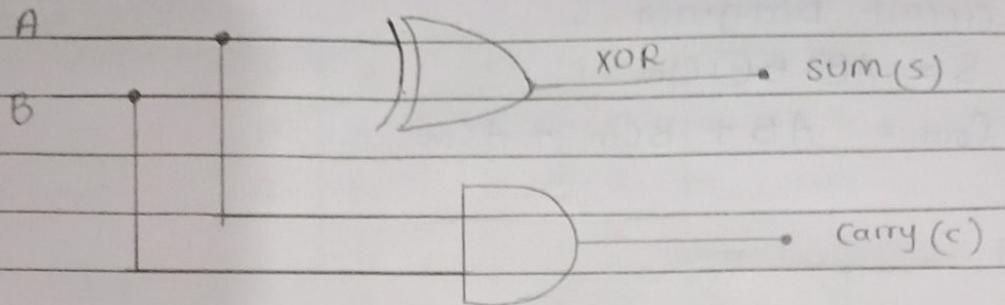
- A Half Adder is a fundamental digital circuit used to perform the addition of two single-bit binary numbers.
- It has two inputs, (A) & (B), and two outputs which are sum (S) and carry(c).
- Sum (S) :- The bitwise sum of the inputs, which is equivalent to the result of an XOR Operation betn (A) and (B).
- Carry (c) :- The bitwise carry, which is the result of an AND operation between (A) and (B).

$$S = A + B$$

$$C = A \cdot B$$

Truth table:-

A	B	sum(s)	carry(c)
0	0	0	0
0	1	1	0
1	0	1	0
1	1	0	1



(2) Explain full Adder in detail.

- A full Adder is a digital circuit that performs addition of binary numbers.
- It adds three bits : two significant bits and one carry bit from a previous addition .
- $(S)$  = Sum bit
- $(C)$  = Carry out bit' which is the carry bit for the next addition.
- $(C_{in})$  = carry bit from the previous addition.

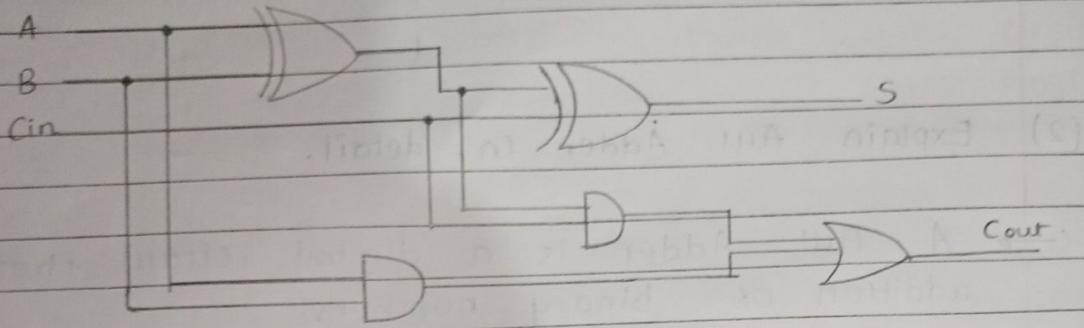
Truth table :-

A	B	$(C_{in})$	S	$(C_{out})$
0	0	0	0	0
0	0	1	1	0
0	1	0	1	0
0	1	1	0	1
1	0	0	1	0
1	0	1	0	1
1	1	0	0	1
1	1	1	1	1

Circuit Diagram :-

$$S = A \oplus B \oplus C_{in}$$

$$C_{out} = AB + BC_{in} + AC_{in}$$



(3) Explain Half Subtractor in detail.

- A Half Subtractor is a combinational logic circuit designed to perform the subtraction of two binary digits.
- It takes two inputs and produces two outputs.
- In output one is (D) difference and other is (B) Borrow.
- Borrow indicates whether a '1' has been borrowed from the next higher bit.

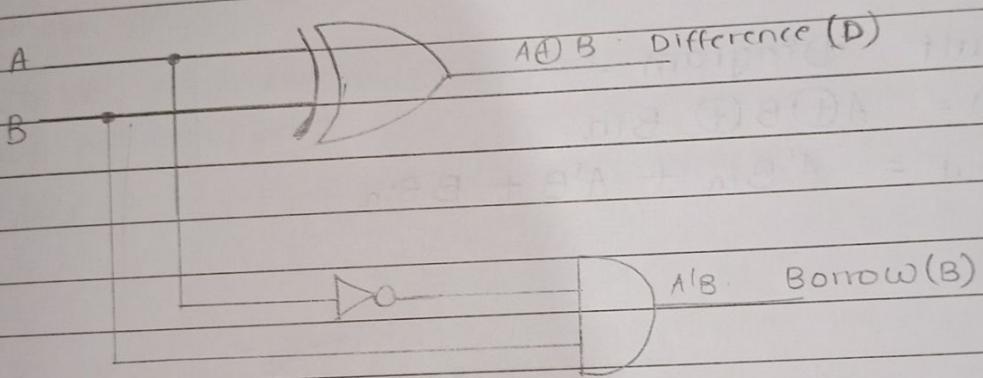
Truth Table :-

A	B	(D)	(B'our)
0	0	0	0
0	1	1	1
1	0	1	0
1	1	0	0

$$D = A \oplus B$$

$$B = A'B$$

Circuit Diagram :-



(4) Explain full subtractor in detail.

- A full subtractor is a combinational logic circuit used to perform the subtraction of three bits.
- It takes (A), (B) and (B'our) as inputs.
- And produces two outputs : Difference (D) and (B) - Borrow out.

Truth Table:-

A	B	(Bin)	D	(Bout)
0	0	0	0	0
0	0	1	1	1
0	1	0	1	1
0	1	1	0	1
1	0	0	1	0
1	0	1	0	0
1	1	0	0	0
1	1	1	1	1

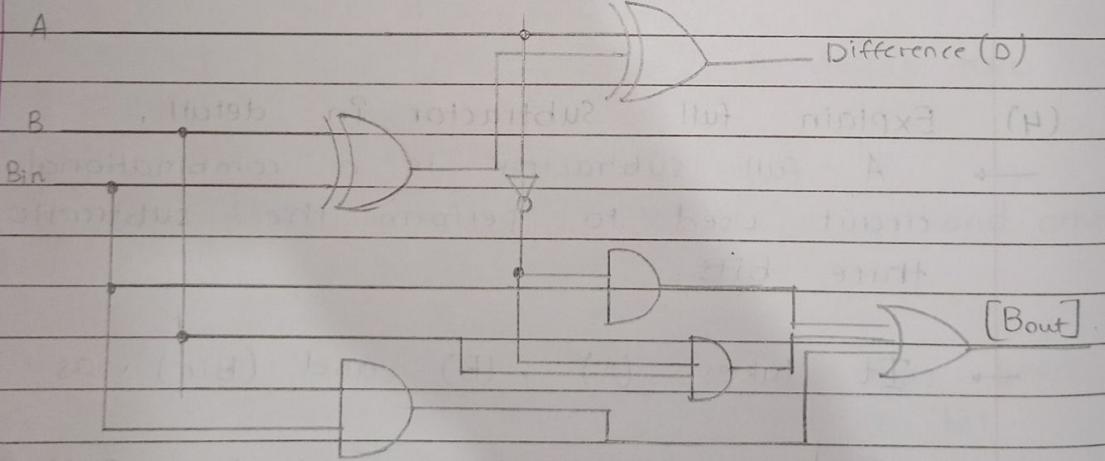
Circuit Diagram:-

$$D = A \oplus B \oplus \text{Bin}$$

$$\text{Bout} = A' \text{Bin} + A'B + B \cdot \text{Bin}$$

A	B	Bin	A' 0	1	1	1
0	0	00	1	1	1	1
0	1	01		1		
1	0	11				
1	1	10				

$$A' \text{Bin} + B \cdot \text{Bin} + A'B$$



(5) Explain BCD to Excess - 3 code conversion.

- BCD → Binary - Coded Decimal and Excess - 3 are both binary encoding schemes used to represent decimal numbers.
- First represent decimal digits (0-9) by a 4-bit binary number in BCD.

0	0000
1	0001
2	0010
3	0011
4	0100
5	0101
6	0110
7	0111
8	1000
9	1001

- Each decimal digit is represented by a 4-bit binary number that is the standard BCD code plus 3.

eg :- 3 in Excess - 3 = 0011 + 1001

Convert each digit to BCD:-

$$4 \text{ in BCD} = 0100$$

$$7 \text{ in BCD} = 0111$$

Now add 3 to each BCD digit;

$$4 = 0100 + 0011 = 0111 = (4)$$

$$7 = 0111 + 0011 = 1010 = (7)$$

∴ The excess-3 code for decimal no. 47  
is 01111010.

### (6) Short note on BCD adder.

→ A Binary-coded decimal (BCD) adder is a digital circuit that performs arithmetic addition on numbers represented in BCD format.

→ BCD is a method of encoding decimal no. where each digit is represented by its own binary sequence.

→ Steps in a BCD Adder.

→ Add the BCD Digits : Perform a 4-bit binary addition on the two BCD Digits.

→ Check if the sum is greater than 9 or if there is a carry from the previous stage.

→ If the sum is greater than 9, add 8·6 to the sum to convert it back to a valid BCD digit.

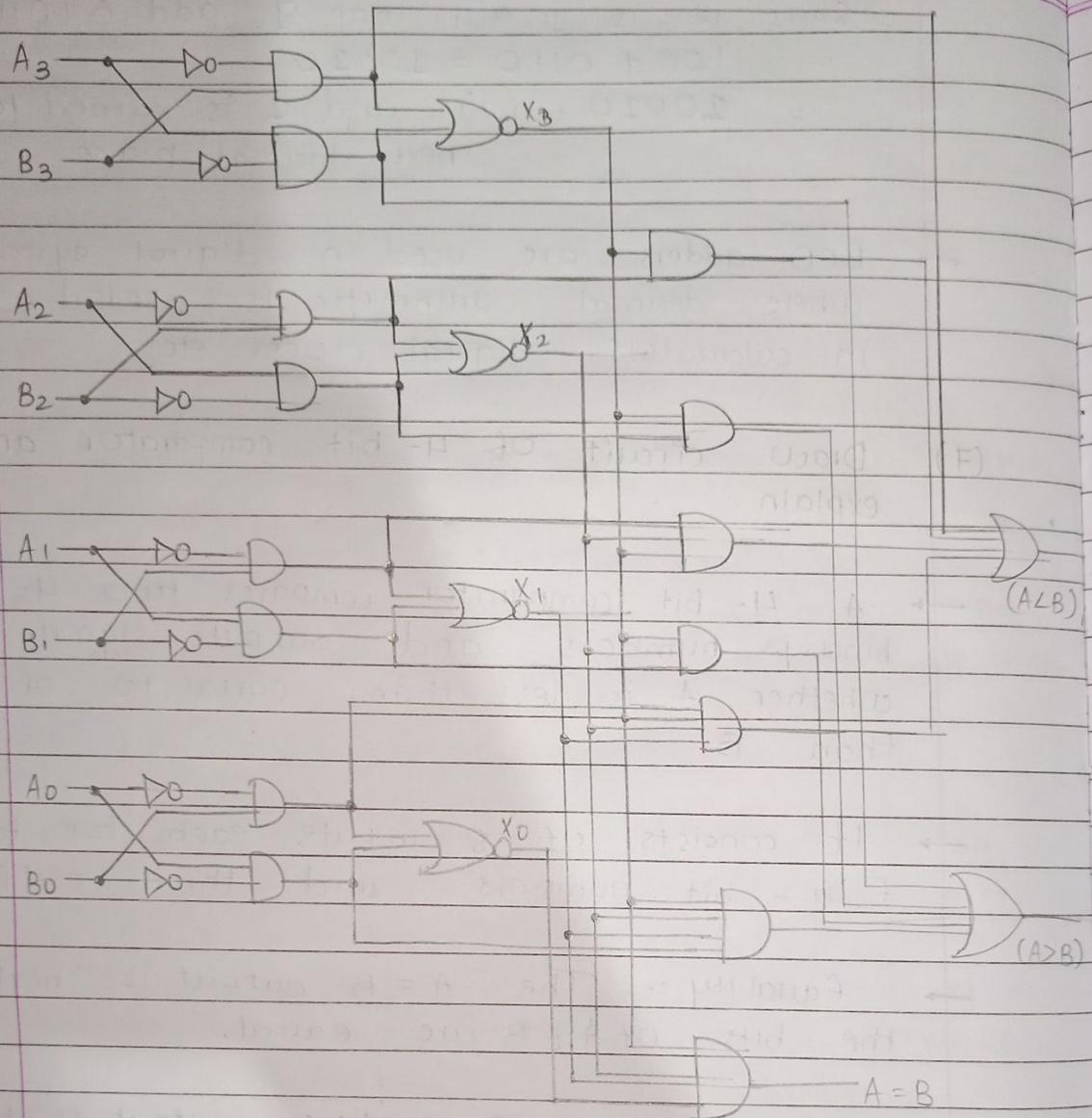
$$\text{eg: } 5 \& 7 = 0101 + 0111 = 1100. (12)$$

Since 12 is greater than 9, add 6 (0110) to 1100  
 $= 1100 + 0110 = 10010$   
 ~~$= 10010 = (2)$~~  and 1 is carried to the next decimal place.

→ BCD adders are used in digital systems where decimal arithmetic is needed, such as in calculators, digital clocks etc

(7) Draw circuit of 4-bit comparator and explain.

- A 4-bit comparator compares two 4-bit binary numbers and outputs signals indicating whether A is less than, equal to, or greater than B.
- It consists of 8 inputs each for two four-bit numbers and three outputs.
- Equality :- The  $A = B$  output is high if all the bits of A & B are equal.
- Greater than :- The  $A > B$  output is high if the MSB where A & B differ is 1 in A and 0 in B.
- Less than : The  $A < B$  output is high if the MSB where A & B differ is 0 in A and 1 in B.



(8) Give comparisons between encoder and decoder.

Encoder	Decoder
→ Converts input data into a different format or code.	→ Converts encoded data back to its original format.
→ It compresses data, transform to diffn domain.	→ Decompress data, retrieve original information
→ Data compression, feature extraction, signal processing are uses.	→ Data Decompression, signal reconstruction are uses.
→ Original data are Input	→ Encoded or compressed data are Input
→ Encoded or compressed data is produced in output	→ Original or reconstructed data are produced in O/P
→ Direction of operation is forward.	→ Direction of operation is backward.
→ eg:- Huffman encoder, audio / video codecs, neural network encoders	→ eg:- Huffman decoder, audio / video codecs, neural network decoders

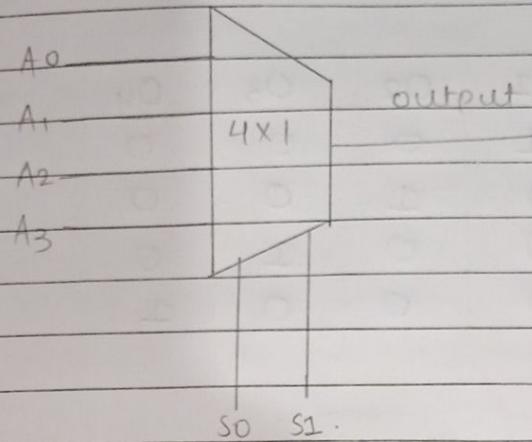
(g) Explain 4x1 line Multiplexer in detail.

- A 4x1 Multiplexer (MUX) is a digital switch that selects one of four input signals and forwards it to single output line.
- It operates using control signals to determine which input is connected to the output.
- Input :- A 4x1 MUX has four data inputs, as  $A_0, A_1, A_2, A_3$
- It uses two control signals  $S_0$  and  $S_1$  to select which input to route to the output.
- The values of  $S_0$  and  $S_1$ , determine which of the four inputs is connected to the output.

(10)

- If  $S_1 \& S_0 = 00$  output =  $A_0$
- If  $S_1 \& S_0 = 01$  output =  $A_1$
- If  $S_1 \& S_0 = 10$  output =  $A_2$
- If  $S_1 \& S_0 = 11$  output =  $A_3$ .
- The main advantage of a multiplexer is its ability to handle multiple inputs with minimal hardware by using a selection mechanism.

Circuit :-



Truth Table .

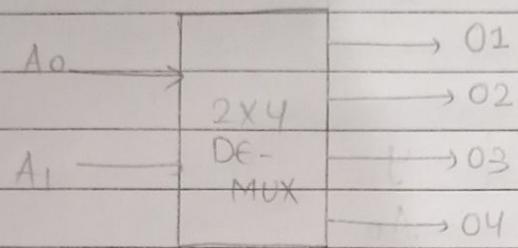
S <sub>0</sub>	S <sub>1</sub>	Y
0	0	A <sub>0</sub>
0	1	A <sub>1</sub>
1	0	A <sub>2</sub>
1	1	A <sub>3</sub>

(10) Draw a 2x4 line decoder and explain in detail !

- 2x4 Decoder have two Input lines and 4 output lines
- lets say A<sub>0</sub> and A<sub>1</sub> is Input and in Output we get 01, 02, 03, 04.

Truth table:-

$A_0$	$A_1$	$O_1$	$O_2$	$O_3$	$O_4$
0	0	1	0	0	0
0	1	0	1	0	0
1	0	0	0	1	0
1	1	0	0	0	1



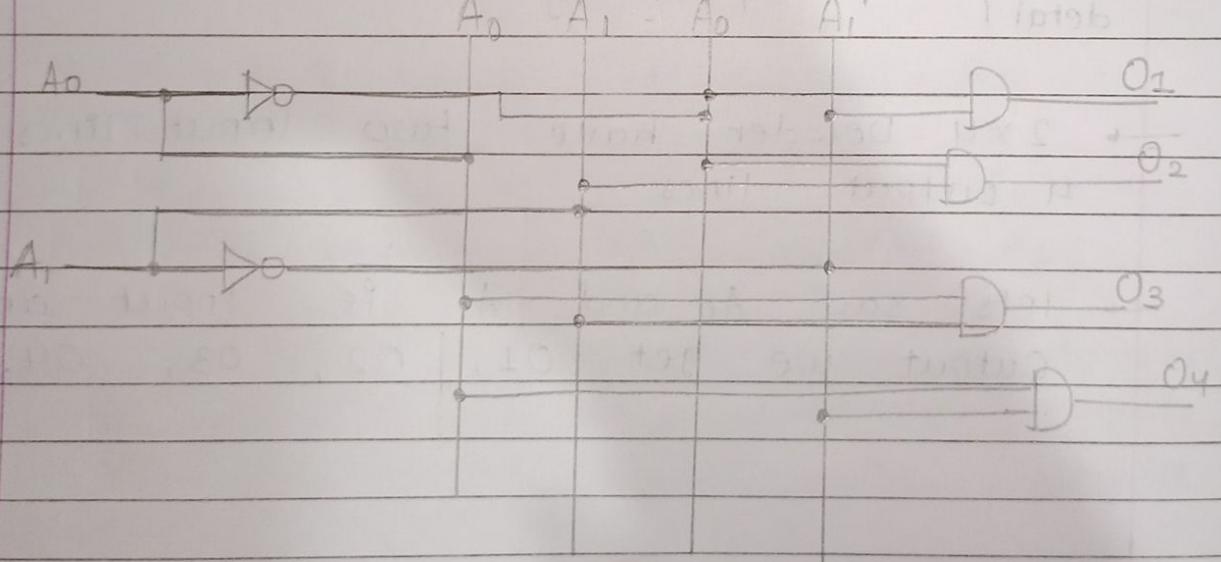
Circuit Diagram.

$$\text{we have, } O_1 = A_0' A_1'$$

$$O_2 = A_0' A_1$$

$$O_3 = A_0 A_1'$$

$$O_4 = A_0 A_1$$



### (II) Comparison between multiplexer and de-Multiplexer.

#### Multiplexer

- Combines multiple input signals into a single output signal.
- Multiple Inputs, One output
- Uses control signals to select which input to send to the output.
- Selects one input from many and routes it to the output.
- Typically implemented using logic gates and flip-flops to select input
- 4 X 1 MUX (4 inputs, 1 output)

#### De-Multiplexer

- It Distributes a single input signal to multiple outputs.
- One input, multiple outputs.
- Uses control signals to select which output the input will go to.
- Routes the input signal to one of many outputs based on control signals.
- Typically implemented using logic gates and flip-flops to control output selection.
- 1 X 4 DE-MUX (1 input, 4 outputs).

(12) Explain Binary parallel adder.

- A binary parallel adder is a digital circuit that adds two binary numbers simultaneously, producing a sum and a carry output for each bit position.
- A parallel adder uses multiple full adders connected in parallel to handle all bits of the binary no. at once.
- for ex:- If we are adding two 4-bit numbers, you will use four full adders in parallel.
- The first full adder processes the least significant bits (LSB) and the subsequent adders handle the higher-order bits.
- The final carry-out from the last full adder is the carry-out of the entire addition oper<sup>n</sup>.

