# A Second Look at Overloading

Pseudocode — Example

```
let cons :: \forall a. a \rightarrow [a] \rightarrow [a] = \lambda x. \lambda lst. x : lst in ..
```

```
let evil :: (\forall a. a \rightarrow a) \rightarrow Unit = \lambda id. id 42; id "foo"; in ...
```

```
e := x
                                                              \tau := \alpha
       \lambda x. e
                                                                       \mid 	au_1 
ightarrow 	au_2
         \mid e_1 \mid e_2 \mid
                                                           \pi_{lpha}:=o_i:lpha	o	a_i i\in\mathbb{N}
         |  let x = e_2 in e_1
                                                             \sigma := \tau
                                                                       | \forall \alpha.\pi_{\alpha} \Rightarrow \sigma
p := e
         \mid \mathbf{inst} \ o : \sigma_T = e \ \mathbf{in} \ p
```

```
inst eq : Nat \rightarrow Nat \rightarrow Bool = \lambda x. \lambda y. .. in inst eq : \forall \alpha. (eq : \alpha \rightarrow \alpha \rightarrow Bool) \Rightarrow [\alpha] \rightarrow [\alpha] \rightarrow Bool = .. in eq [0] [0]
```

$$( ext{INST}) \quad rac{\Gamma dash e : \sigma_T \quad \Gamma, \ o : \sigma_T dash p : \sigma \quad orall (o : \sigma_{T'}) \in \Gamma : T 
eq T'}{\Gamma dash ext{inst } o : \sigma_T = e ext{ in } p : \sigma}$$

$$(orall \mathrm{I}) \qquad \qquad rac{\Gamma, \,\, \pi_lpha dash e : \sigma \quad \, \mathrm{fresh} \,\, lpha}{\Gamma dash e : orall lpha . \pi_lpha \Rightarrow \sigma}$$

$$(orall \mathrm{E}) \qquad \qquad rac{\Gamma dash e : orall lpha. \ \pi_lpha \Rightarrow \sigma \qquad \Gamma dash [ au/lpha] \pi_lpha}{\Gamma dash e : [ au/lpha] \sigma}$$

System 0 — Typing

```
\| \text{inst } eq : \mathbb{N} \to \mathbb{N} \to \mathbb{B} = e_1 \text{ in }
           inst eq: \forall \alpha. \ (\text{eq}: \alpha \to \alpha \to \mathbb{B}) \Rightarrow [\alpha] \to [\alpha] \to \mathbb{B} = e_2 \text{ in}
           |eq| |0| |0| \|_{\emptyset}
= [[\text{inst } eq: \forall \alpha. \ (\text{eq}: \alpha \to \alpha \to \mathbb{B}) \Rightarrow [\alpha] \to [\alpha] \to \mathbb{B} = ... \text{ in}]
           eq \ \llbracket 0 
bracket \llbracket 0 
bracket \llbracket e_1 
bracket x. 	ext{ if } x 	ext{ is } \mathbb{N} 	ext{ then } \llbracket e_1 
bracket x 
bracket
= \llbracket eq \ [0] \ [0] \rrbracket_{\{eq:=\lambda x. \text{ if } x \text{ is List then } \llbracket e_2 \rrbracket \ x \text{ else } \lambda x. \text{ if } x \text{ is } \mathbb{N} \text{ then } \llbracket e_1 \rrbracket \ x\}
=(\lambda x. \text{ if } x \text{ is } [\alpha] \text{ then } \llbracket e_2 \rrbracket x \text{ else } \lambda x. \text{ if } x \text{ is } \mathbb{N} \text{ then } \llbracket e_1 \rrbracket x) [0]
= [e_2] [0] [0]
```

```
inst eq : Nat \rightarrow Nat \rightarrow Bool = \lambda.. in inst eq : \forall \alpha. (eq : \alpha \rightarrow \alpha \rightarrow Bool) \Rightarrow [\alpha] \rightarrow [\alpha] \rightarrow Bool = \lambda.. in eq [0] [0]
```

### System 0

```
let eq<sub>0</sub> :: Nat \rightarrow Nat \rightarrow Bool

= \lambda.. in

let eq<sub>1</sub> :: \forall \alpha. (\alpha \rightarrow \alpha \rightarrow Bool) \rightarrow [\alpha] \rightarrow [\alpha] \rightarrow Bool

= \lambda eq_0. \lambda.. in

eq<sub>1</sub> eq<sub>0</sub> [\alpha] [\alpha]
```

Hindley Milner

System 0 — Translation to Hindley Milner

```
let max :: \forall \beta. (gte : \beta \rightarrow \beta \rightarrow Bool) \Rightarrow \forall \alpha. (\alpha \leq \{key: \beta\}) \Rightarrow \alpha \rightarrow \alpha \rightarrow \alpha = \lambda x. \lambda y. if gte x.key y.key then x else y in max {field: "a", key: 1} {field: "b", key: 2}
```

### Records + Subtyping

```
inst field : \forall \alpha. \forall \beta. R_0 \alpha \beta \rightarrow \alpha = \lambda R_0 x y. x in inst key : \forall \alpha. \forall \beta. R_0 \alpha \beta \rightarrow \beta = \lambda R_0 x y. y in let max :: \forall \beta. (gte : \beta \rightarrow \beta \rightarrow Bool) \Rightarrow \forall \alpha. (key : \alpha \rightarrow \beta) \Rightarrow \alpha \rightarrow \alpha \rightarrow \alpha = \lambda x. \lambda y. if gte (key x) (key y) then x else y in max (R_0 "a" 1) (R_0 "b" 2)
```

System 0

System 0 — Relationship with Record Typing

# Repository

github.com/Mari-W/popl

## References

- A Second Look at Overloading 1995
  Martin Odersky, Philip Wadler, Martin Wehr
- A Theory of Type Polymorphism in Programming 1978 Hindley Milner