### Recursion

#### **Guidance for Solutions:**

For each of these exercises, start by identifying the base case(s) for your recursive function — these are the conditions under which the function will stop calling itself. Then, determine how each function should break down its problem into smaller subproblems, eventually reaching a base case. Remember to test your functions with various inputs to ensure they work as expected.

#### 1. Sum of Natural Numbers

Write a recursive function that takes a number  $\, n \,$  and returns the sum of all natural numbers up to  $\, n \,$ . For example, if the input is  $\, 5 \,$ , the function should return  $\, 15 \,$  (i.e.,  $\, 5 \,$  +  $\, 4 \,$  +  $\, 3 \,$  +  $\, 2 \,$  +  $\, 1 \,$ ).

## 2. Reverse a String

Implement a recursive function that takes a string and returns its reverse. For example, given the string "hello", the function should return "olleh".

Certainly! Here are three simpler exercises focused on recursion. These exercises are designed to introduce the concept of recursion with more straightforward problems than the sum of natural numbers and reversing a string.

#### **Exercise 3: Count Down**

Write a recursive function that prints numbers from n down to 1. For example, if n is 5, the function should print 5, 4, 3, 2, 1.

# Exercise 4: Print an Array

Write a recursive function that prints all the elements of an array, one element per line. You can assume the array contains only numbers or strings.