

# Impact of food availability and light on *A. lixula* larval growth - data analysis

```
library('dplyr')
```

```
## Warning: package 'dplyr' was built under R version 4.4.2
```

```
##
```

```
## Adjuntando el paquete: 'dplyr'
```

```
## The following objects are masked from 'package:stats':
```

```
##
```

```
## filter, lag
```

```
## The following objects are masked from 'package:base':
```

```
##
```

```
## intersect, setdiff, setequal, union
```

```
library('readr')
```

```
## Warning: package 'readr' was built under R version 4.4.2
```

```
library('ggplot2')
```

```
## Warning: package 'ggplot2' was built under R version 4.4.2
```

```
library('knitr')
```

```
library('tidyr')
```

```
## Warning: package 'tidyr' was built under R version 4.4.2
```

```
library('emmeans')
```

```
## Welcome to emmeans.
```

```
## Caution: You lose important information if you filter this package's results.
```

```
## See '? untidy'
```

```
library('rstan')
```

```
## Cargando paquete requerido: StanHeaders
```

```
##
```

```
## rstan version 2.32.6 (Stan version 2.32.2)
```

```
## For execution on a local, multicore CPU with excess RAM we recommend calling
```

```
## options(mc.cores = parallel::detectCores()).
```

```
## To avoid recompilation of unchanged Stan programs, we recommend calling
```

```
## rstan_options(auto_write = TRUE)
```

```
## For within-chain threading using `reduce_sum()` or `map_rect()` Stan functions,
```

```
## change `threads_per_chain` option:
```

```
## rstan_options(threads_per_chain = 1)
```

```
## Do not specify '-march=native' in 'LOCAL_CPPFLAGS' or a Makevars file
```

```
##
## Adjuntando el paquete: 'rstan'
## The following object is masked from 'package:tidyr':
##
##      extract
rstan::rstan_options(auto_write = TRUE)
library('brms')

## Warning: package 'brms' was built under R version 4.4.2
## Cargando paquete requerido: Rcpp
## Loading 'brms' package (version 2.22.0). Useful instructions
## can be found by typing help('brms'). A more detailed introduction
## to the package is available through vignette('brms_overview').
##
## Adjuntando el paquete: 'brms'
## The following object is masked from 'package:rstan':
##
##      loo
## The following object is masked from 'package:stats':
##
##      ar
options(mc.cores = parallel::detectCores()) # run all cores
library('bayesplot')

## Warning: package 'bayesplot' was built under R version 4.4.2
## This is bayesplot version 1.11.1
## - Online documentation and vignettes at mc-stan.org/bayesplot
## - bayesplot theme set to bayesplot::theme_default()
##      * Does _not_ affect other ggplot2 plots
##      * See ?bayesplot_theme_set for details on theme setting
##
## Adjuntando el paquete: 'bayesplot'
## The following object is masked from 'package:brms':
##
##      rhat
library('marginaleffects')
library('ggdist')

## Warning: package 'ggdist' was built under R version 4.4.2
##
## Adjuntando el paquete: 'ggdist'
## The following objects are masked from 'package:brms':
##
##      dstudent_t, pstudent_t, qstudent_t, rstudent_t
```

```
nchain = 4
niter = 2500
moment_matching = TRUE
```

## 1. Data overview

Making a data set containing only the data pertaining to *A. lixula*.

```
Al_df <- read_delim("larval_morphology.csv", delim = ",",
                   col_types = "fffnfifffiniif")
Al_df = drop_na(Al_df, length)
# make Al_df$larva by concatenating Al_df$species with Al_df$larva
Al_df$larva <- as.factor(paste0(Al_df$species, Al_df$larva))
Al_df <- Al_df[Al_df$species == "A1",]
#ensure correct order for levels
Al_df<-Al_df %>% mutate(lit = factor(lit, levels = c("DD", "LD", "LL")))
Al_df<-Al_df %>% mutate(rod = factor(rod, levels = c("BR", "PO", "ALA")))
head(Al_df)
```

```
## # A tibble: 6 x 15
##   larva side rod   length ate   Food_conc Food_species fed lit condition
##   <fct> <fct> <fct>   <dbl> <fct>   <int> <fct>   <fct> <fct> <fct>
## 1 A11 R BR 96.7 NO 10 D_tertiolecta Fed LD FSW
## 2 A11 R PO 112. NO 10 D_tertiolecta Fed LD FSW
## 3 A11 L BR 94.4 NO 10 D_tertiolecta Fed LD FSW
## 4 A11 L PO 110. NO 10 D_tertiolecta Fed LD FSW
## 5 A12 R BR 89.8 YES 10 D_tertiolecta Fed LD FSW
## 6 A12 R PO 111. YES 10 D_tertiolecta Fed LD FSW
## # i 5 more variables: larvae_per_well <int>, lar_ml <dbl>, hpf <int>,
## # dpf <int>, species <fct>
```

```
Al_df <- Al_df[Al_df$length > 0,]
Al_df <- Al_df[! is.na(Al_df$length),]
print(paste0('There are ', dim(Al_df)[1], ' measures from ', length(unique(Al_df$larva)), ' individual larvae.'))
```

```
## [1] "There are 729 measures from 161 individual larvae."
```

The chunk below produces a data summary for each condition. In column n we also calculate the number of observations.

```
Al_df %>% group_by(species, dpf, lit, rod, fed, lar_ml) %>%
  summarise(mean = mean(length, na.rm = TRUE), stdev = sd(length, na.rm = TRUE),
            n = n())
```

```
## `summarise()` has grouped output by 'species', 'dpf', 'lit', 'rod', 'fed'. You
## can override using the `.groups` argument.
```

```
## # A tibble: 23 x 9
## # Groups:   species, dpf, lit, rod, fed [23]
##   species dpf lit rod fed lar_ml mean stdev n
##   <fct> <int> <fct> <fct> <fct> <dbl> <dbl> <dbl> <int>
## 1 A1 3 LD BR Fed 12.5 95.9 4.59 35
## 2 A1 3 LD BR Starved 12.5 96.0 8.36 25
## 3 A1 3 LD PO Fed 12.5 115. 19.5 36
## 4 A1 3 LD PO Starved 12.5 127. 13.7 24
## 5 A1 3 LD ALA Starved 12.5 80.0 7.01 5
```

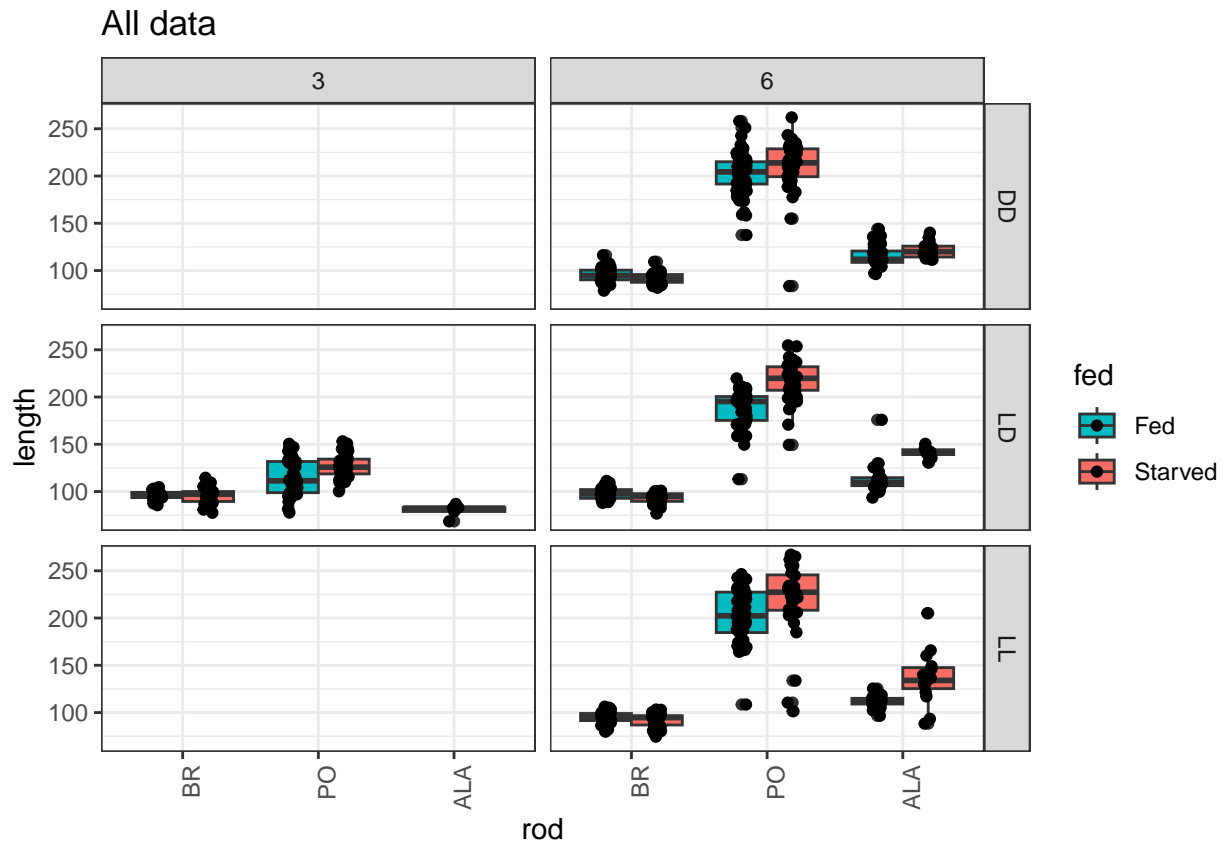
```
## 6 A1      6 DD    BR    Fed      12.5  95.2  7.31   54
## 7 A1      6 DD    BR    Starved  12.5  91.9  5.58   40
## 8 A1      6 DD    PO    Fed      12.5 202.  23.0   53
## 9 A1      6 DD    PO    Starved  12.5 210.  29.0   40
## 10 A1     6 DD    ALA    Fed      12.5 116.  10.7   36
## # i 13 more rows
```

## Experimental setup and aim

We are interested in investigating how the light dark cycle (lit) influences the phenotypic response to food availability (fed): larvae grow much shorter arms when food is abundant to save maternal storages; on the contrary, when food is scarce they develop much longer arms to maximize their capability to collect food. Three sets of spicules have been measured: Body Rod (BR), Post Oral (PO), and Anterolateral (ALA) arms .

## Plot data overview

```
Al_df %>%
  ggplot(aes(y=length,x=rod, fill=fed)) +
  geom_boxplot(position = position_dodge(width = 0.75)) +
  geom_jitter(position = position_jitterdodge(jitter.width = 0.15, dodge.width = 0.75)) +
  facet_grid(cols= vars(dpf),
             rows=vars(lit)
             ) +
  scale_fill_manual(values=c("#00BEC1", "#F86D63")) +
  #geom_violin() +
  theme_bw() +
  theme(axis.text.x = element_text(angle = 90, hjust = 1)) +
  ggtitle("All data")
```

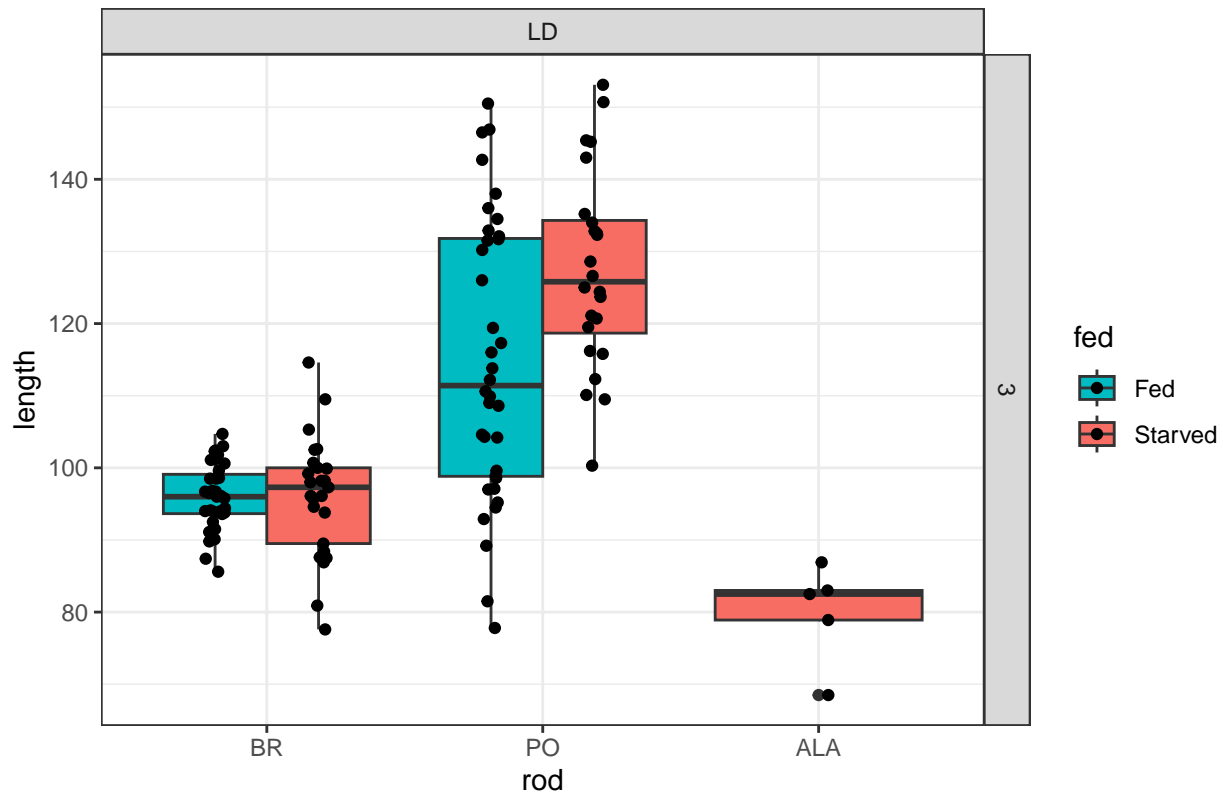


```

Al_df %>%
  filter(dpf=="3")%>%
  ggplot(aes(y=length,x=rod, fill=fed)) +
  facet_grid(dpf~lit) +
  geom_boxplot(position = position_dodge(width = 0.75)) +
  geom_jitter(position = position_jitterdodge(jitter.width = 0.15, dodge.width = 0.75))+
  scale_fill_manual(values=c("#00BBC1", "#F86D63"))+
  #geom_violin()+
  theme_bw()+
  theme(axis.text.x = element_text(angle = 0, hjust = 0.5)) +
  ggtitle("Data 3dpf")

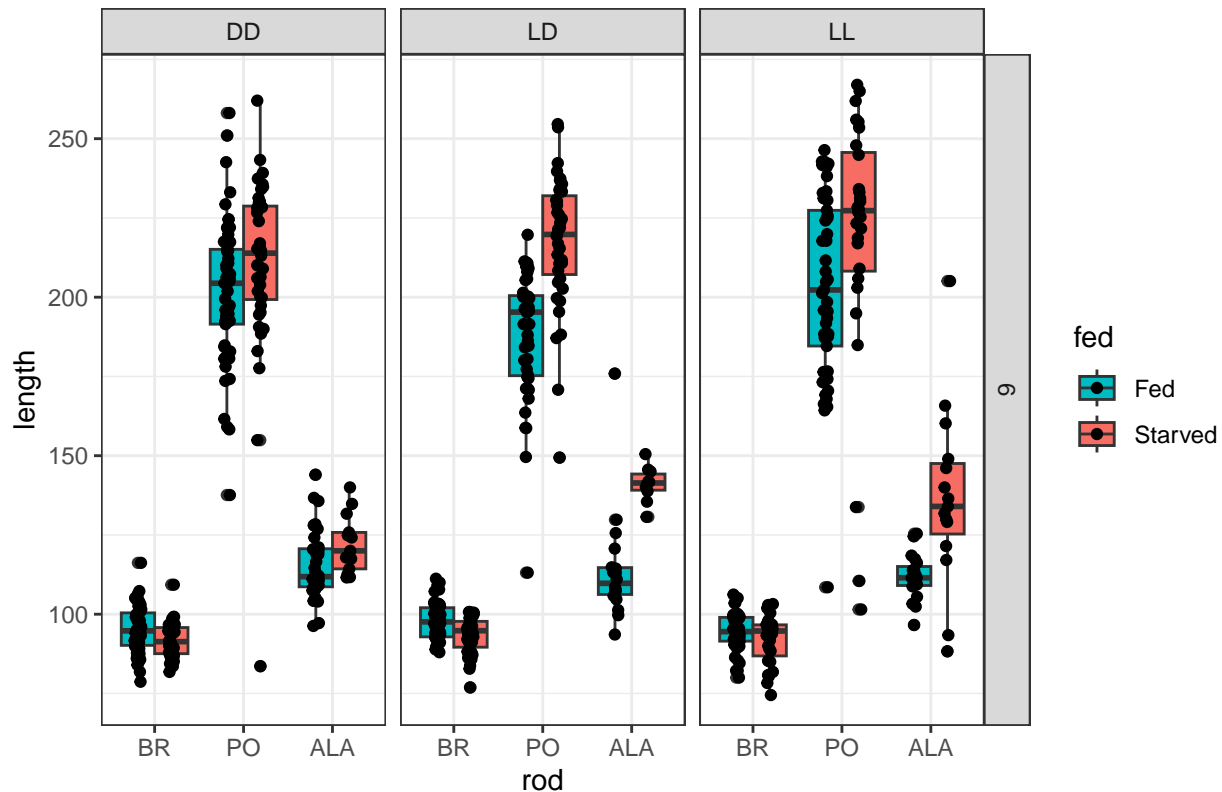
```

Data 3dpf



```
Al_df %>%
  filter(dpf=="6")%>%
  ggplot(aes(y=length,x=rod, fill=fed)) +
  facet_grid(dpf~lit) +
  geom_boxplot(position = position_dodge(width = 0.75)) +
  geom_jitter(position = position_jitterdodge(jitter.width = 0.15, dodge.width = 0.75))+
  scale_fill_manual(values=c("#00BBC1", "#F86D63"))+
  #geom_violin()+
  theme_bw()+
  theme(axis.text.x = element_text(angle = 0, hjust = 0.5)) +
  ggtitle("Data 3dpf")
```

## Data 3dpf



For the statistical analysis we select only larvae at 6dpf.

```
Al_df <- Al_df[Al_df$dpf == "6",]
Al_df
```

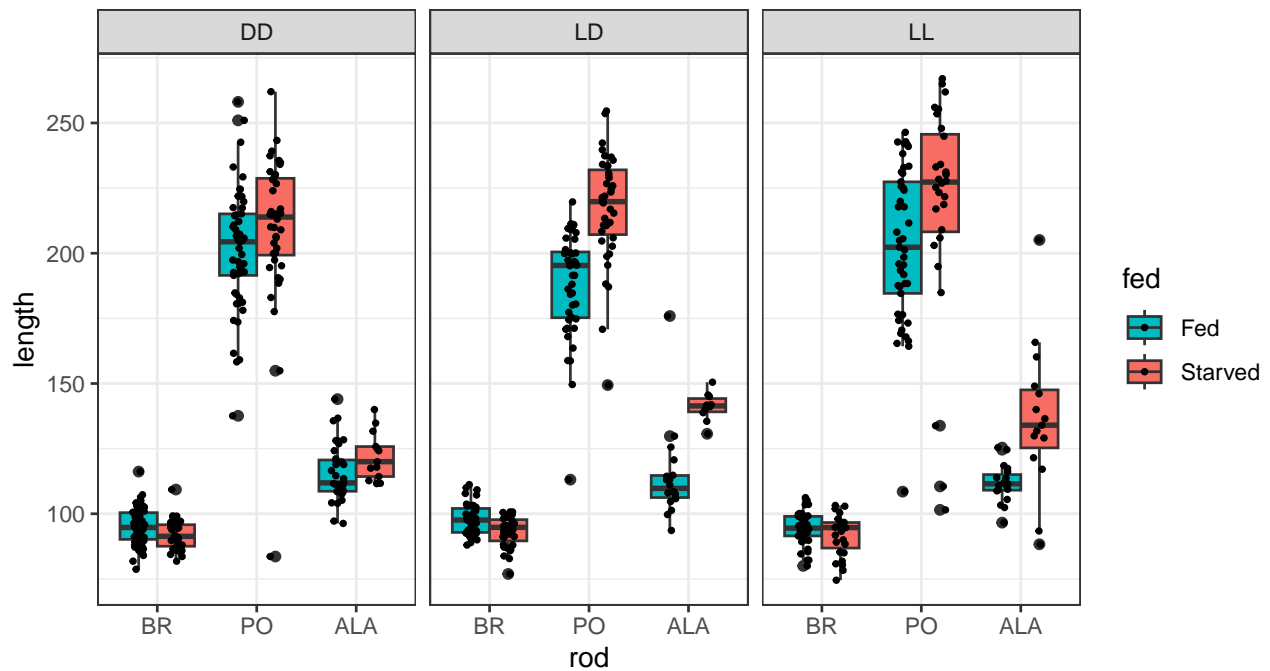
```
## # A tibble: 604 x 15
##   larva side rod   length ate   Food_conc Food_species fed   lit   condition
##   <fct> <fct> <fct>   <dbl> <fct>   <int> <fct>   <fct> <fct> <fct>
## 1 A142 R    PO    237. NO      0 NO      Starved LD   FSW
## 2 A142 L    BR     85.8 NO      0 NO      Starved LD   FSW
## 3 A142 L    PO    233. NO      0 NO      Starved LD   FSW
## 4 A143 R    BR    101. NO      0 NO      Starved LD   FSW
## 5 A143 R    PO    227. NO      0 NO      Starved LD   FSW
## 6 A143 R    ALA   141. NO      0 NO      Starved LD   FSW
## 7 A143 L    BR     86.2 NO      0 NO      Starved LD   FSW
## 8 A143 L    PO    236. NO      0 NO      Starved LD   FSW
## 9 A143 L    ALA   142. NO      0 NO      Starved LD   FSW
## 10 A144 R    BR     95.3 NO      0 NO      Starved LD   FSW
## # i 594 more rows
## # i 5 more variables: larvae_per_well <int>, lar_ml <dbl>, hpf <int>,
## #   dpf <int>, species <fct>
```

#Have a look at actual data at 6dpf to check best model

```
Al_df %>%
  ggplot(aes(y=length,x=rod, fill=fed)) +
  facet_grid(~ lit) +
  geom_boxplot(position = position_dodge(width = 0.75)) +
  geom_jitter(position = position_jitterdodge(jitter.width = 0.25, dodge.width = 0.75), size=0.7)+
```

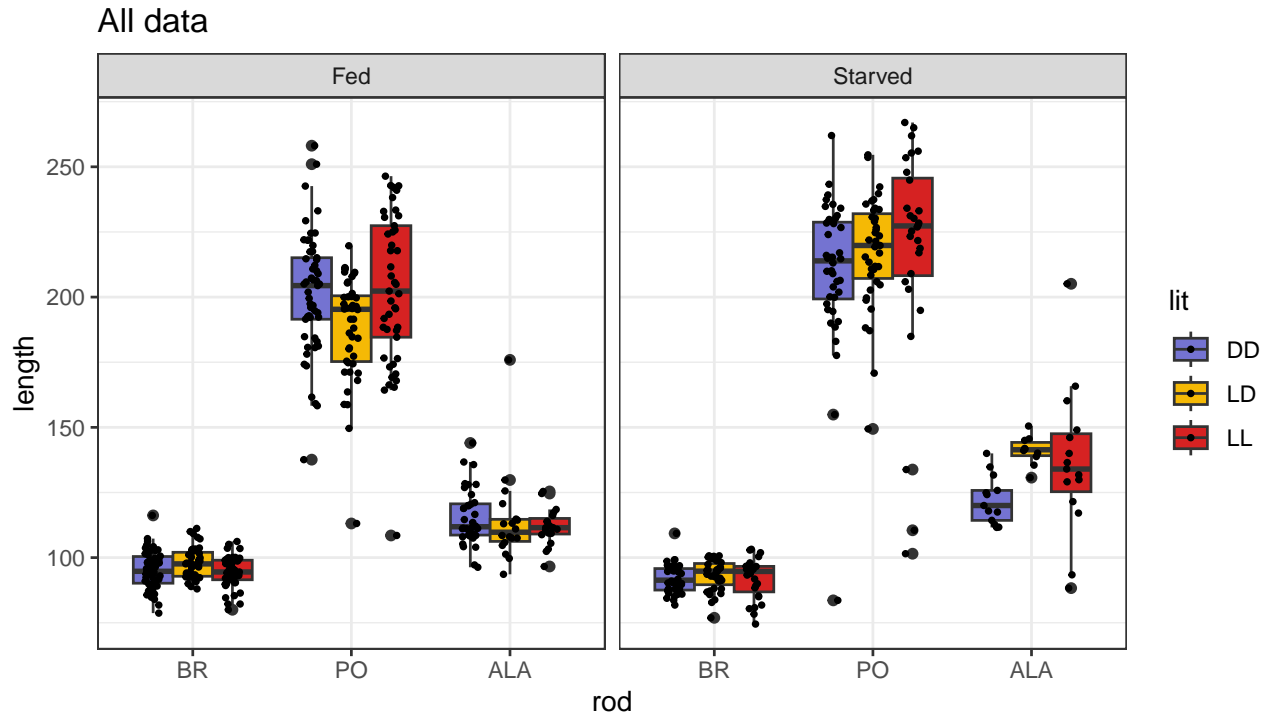
```
scale_fill_manual(values=c("#00BBC1", "#F86D63"))+
theme_bw()+
theme(axis.text.x = element_text(angle = 0, hjust = 0.5)) +
ggtitle("A. lixula data at 6 dpf")
```

A. lixula data at 6 dpf



```
Al_df %>%
  ggplot(aes(y=length, x=rod, fill=lit, )) +
  facet_grid(~ fed) +
  geom_boxplot(position = position_dodge(width = 0.75)) +
  geom_jitter(position = position_jitterdodge(jitter.width = 0.25, dodge.width = 0.75), size=0.7)+
  scale_fill_manual(values=c("#7473d1", "#f5b905", "#d62222" ))+
  #geom_violin()+
  theme_bw()+
  theme(axis.text.x = element_text(angle = 0, hjust = 0.5)) +
  ggtitle("All data")
```





## 2. Statistics

For the statistical analysis length is scaled by SD and centered at the data mean (L).

```
meanL <- mean(A1_df$length)
sdL <- sd(A1_df$length)
A1_df$L <- as.numeric(scale(A1_df$length))
A1_df <- droplevels(A1_df)
```

### Prior predictive test

Set priors on slope. Weakly informative priors are used to guide the model.

We are interested in investigating how feeding (fed), and light exposure (lit) influence arm length. Moreover, three sets of spicules have been measured Body Rod (BR), Post Oral (PO), and Anterolateral (ALA).

### M0 Single intercept

Each treatment should be replicated sufficiently within each larva to capture the treatment effect accurately. Typically, having at least 3-5 measurements per treatment per larva can provide a reasonable balance between model complexity and data sufficiency.

Ideally, we would represent the data as a nested structure, with larvae nested within species. This would allow us to estimate the variance components for the species and larva levels. However, given the low number of measures per larva, it might be challenging to estimate these variance components reliably. Therefore, we will start with a simpler model that includes only the larva level as a random effect.

```
get_prior(bf(L ~ 1 + (1|larva), sigma ~ 1), data=A1_df)
```

```
##           prior      class      coef group resp  dpar nlpar lb ub
## student_t(3, -0.5, 2.5) Intercept
## student_t(3, 0, 2.5)      sd                0
```

```
##      student_t(3, 0, 2.5)      sd      larva      0
##      student_t(3, 0, 2.5)      sd Intercept larva      0
##      student_t(3, 0, 2.5) Intercept      sigma
##      source
##      default
##      default
##      (vectorized)
##      (vectorized)
##      default

si_priors <- c(
  set_prior("normal(0, 0.5)", class = "Intercept"), # prior for intercept
  set_prior("student_t(3, 0, 0.5)", class = "sd", group = "larva"),
  set_prior("student_t(3, 0, 0.5)", dpar = "sigma", class = "Intercept")
)

si_priors <- c(
  set_prior("student_t(5, 0, 2)", class = "Intercept"), # prior for intercept

  set_prior("student_t(3, 0, 0.5)", class = "sd", group = "larva"),

  set_prior("student_t(5, 0, 1)", dpar = "sigma", class = "Intercept") # prior for residual sd
)
```

The zeroth model is built to check the effect of the group level and see how the data is distributed overall. The nesting structure explicitly acknowledges the hierarchical nature of the data. This helps to avoid pseudoreplication and ensures that the estimates of variance components are not biased.

```
Al_intercept_mod <- brm(
  bf(L ~ 1 + (1|larva), sigma ~ 1),
  family = gaussian,
  data=Al_df, prior = si_priors,
  chains = nchain,
  iter = niter, warmup = niter/2,
  save_pars = save_pars(all = TRUE),
)
Al_intercept_mod

## Family: gaussian
## Links: mu = identity; sigma = log
## Formula: L ~ 1 + (1 | larva)
##      sigma ~ 1
## Data: Al_df (Number of observations: 604)
## Draws: 4 chains, each with iter = 2500; warmup = 1250; thin = 1;
##      total post-warmup draws = 5000
##
## Multilevel Hyperparameters:
## ~larva (Number of levels: 130)
##      Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS
## sd(Intercept)      0.04      0.03      0.00      0.12 1.00      4289      3222
##
## Regression Coefficients:
##      Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS
## Intercept      0.00      0.04     -0.08      0.08 1.00      11165      3514
## sigma_Intercept 0.00      0.03     -0.06      0.06 1.00      12035      3606
##
```

```
## Draws were sampled using sampling(NUTS). For each parameter, Bulk_ESS
## and Tail_ESS are effective sample size measures, and Rhat is the potential
## scale reduction factor on split chains (at convergence, Rhat = 1).
```

```
default_prior(bf(L ~ rod + (1|larva), sigma ~ rod), data=Al_df)
```

```
##           prior      class      coef group resp  dpar nlpar lb ub
##           (flat)         b           rodALA
##           (flat)         b           rodPO
## student_t(3, -0.5, 2.5) Intercept
## student_t(3, 0, 2.5) sd                                0
## student_t(3, 0, 2.5) sd          larva                0
## student_t(3, 0, 2.5) sd Intercept larva              0
##           (flat)         b           sigma
##           (flat)         b           rodALA           sigma
##           (flat)         b           rodPO           sigma
## student_t(3, 0, 2.5) Intercept           sigma
## source
## default
## (vectorized)
## (vectorized)
## default
## default
## (vectorized)
## (vectorized)
## default
## (vectorized)
## (vectorized)
## default
```

```
priors <- c(
  set_prior("student_t(5, 0, 2)", class = "Intercept"), # prior for intercept
  set_prior("normal(0, 2)", class = "b"),

  set_prior("student_t(3, 0, 0.5)", class = "sd", group = "larva"),

  set_prior("student_t(5, 0, 2)", dpar = "sigma", class = "Intercept"), # prior for residual sd
  set_prior("normal(0, 1)", class = "b", dpar="sigma")
)
```

## M1 Rod model

```
Al_rod_mod <- brm(
  bf(L ~ rod + (1|larva), sigma ~ rod),
  family = gaussian,
  data=Al_df, prior = priors,
  chains = nchain,
  iter = niter, warmup = niter/2,
  save_pars = save_pars(all = TRUE),
  control = list(adapt_delta = 0.99),
)
Al_rod_mod
```

```
## Family: gaussian
```

```

## Links: mu = identity; sigma = log
## Formula: L ~ rod + (1 | larva)
##       sigma ~ rod
## Data: Al_df (Number of observations: 604)
## Draws: 4 chains, each with iter = 2500; warmup = 1250; thin = 1;
##       total post-warmup draws = 5000
##
## Multilevel Hyperparameters:
## ~larva (Number of levels: 130)
##       Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS
## sd(Intercept)    0.07     0.01    0.04    0.09 1.00    1201    1918
##
## Regression Coefficients:
##       Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS
## Intercept        -0.91     0.01   -0.93   -0.90 1.00    5659    4013
## sigma_Intercept  -2.29     0.07   -2.42   -2.15 1.00    1472    2402
## rodPO             2.00     0.03    1.94    2.07 1.00    7545    3282
## rodALA            0.47     0.03    0.41    0.53 1.00    8145    3572
## sigma_rodPO       1.63     0.08    1.46    1.79 1.00    1973    2652
## sigma_rodALA      1.14     0.10    0.95    1.35 1.00    2250    3011
##
## Draws were sampled using sampling(NUTS). For each parameter, Bulk_ESS
## and Tail_ESS are effective sample size measures, and Rhat is the potential
## scale reduction factor on split chains (at convergence, Rhat = 1).

```

## M2 Rod Fed model

```

Al_rod_fed_mod <- brm(
  bf(L ~ rod*fed + (1|larva), sigma ~ rod*fed),
  family = gaussian,
  data=Al_df, prior = priors,
  chains = nchain,
  iter = niter, warmup = niter/2,
  save_pars = save_pars(all = TRUE),
  control = list(adapt_delta = 0.99),
)
Al_rod_fed_mod

## Family: gaussian
## Links: mu = identity; sigma = log
## Formula: L ~ rod * fed + (1 | larva)
##       sigma ~ rod * fed
## Data: Al_df (Number of observations: 604)
## Draws: 4 chains, each with iter = 2500; warmup = 1250; thin = 1;
##       total post-warmup draws = 5000
##
## Multilevel Hyperparameters:
## ~larva (Number of levels: 130)
##       Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS
## sd(Intercept)    0.07     0.01    0.05    0.08 1.00    1209    2190
##
## Regression Coefficients:
##       Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk_ESS
## Intercept        -0.89     0.01   -0.91   -0.86 1.00    5296

```

```
## sigma_Intercept      -2.27      0.08     -2.42     -2.11 1.00      1797
## rodPO                 1.85      0.04      1.77      1.92 1.00      6537
## rodALA                0.33      0.03      0.27      0.38 1.00      7145
## fedStarved           -0.06      0.02     -0.10     -0.03 1.00      4858
## rodPO:fedStarved      0.37      0.07      0.24      0.50 1.00      6889
## rodALA:fedStarved     0.40      0.06      0.28      0.52 1.00      6765
## sigma_rodPO           1.47      0.10      1.27      1.66 1.00      2357
## sigma_rodALA          0.75      0.12      0.51      1.00 1.00      3015
## sigma_fedStarved     -0.13      0.12     -0.37      0.10 1.00      2789
## sigma_rodPO:fedStarved 0.32      0.15      0.03      0.61 1.00      3058
## sigma_rodALA:fedStarved 0.61      0.19      0.23      0.98 1.00      3587
##                               Tail_ESS
## Intercept              4008
## sigma_Intercept        1938
## rodPO                  3441
## rodALA                 4007
## fedStarved             4084
## rodPO:fedStarved       3678
## rodALA:fedStarved      4018
## sigma_rodPO            2666
## sigma_rodALA           3396
## sigma_fedStarved       3483
## sigma_rodPO:fedStarved 3068
## sigma_rodALA:fedStarved 3954
##
## Draws were sampled using sampling(NUTS). For each parameter, Bulk_ESS
## and Tail_ESS are effective sample size measures, and Rhat is the potential
## scale reduction factor on split chains (at convergence, Rhat = 1).
```

### M3 Rod Lit model

```
Al_rod_lit_mod <- brm(
  bf(L ~ rod*lit + (1|larva), sigma ~ rod*lit),
  family = gaussian,
  data=Al_df, prior = priors,
  chains = nchain,
  iter = niter, warmup = niter/2,
  control = list(adapt_delta=0.99),
  save_pars = save_pars(all = TRUE)
)
Al_rod_lit_mod

## Family: gaussian
## Links: mu = identity; sigma = log
## Formula: L ~ rod * lit + (1 | larva)
##          sigma ~ rod * lit
## Data: Al_df (Number of observations: 604)
## Draws: 4 chains, each with iter = 2500; warmup = 1250; thin = 1;
##        total post-warmup draws = 5000
##
## Multilevel Hyperparameters:
## ~larva (Number of levels: 130)
##          Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS
## sd(Intercept)    0.06      0.01    0.04    0.08 1.00      737      640
```

```
##
## Regression Coefficients:
##           Estimate Est.Error l-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS
## Intercept      -0.92      0.01   -0.95   -0.89 1.00      3699      4060
## sigma_Intercept -2.21      0.09   -2.40   -2.03 1.00      1553      2801
## rodPO           2.01      0.05    1.91    2.11 1.00      3816      3214
## rodALA          0.42      0.03    0.36    0.48 1.00      5253      3913
## litLD           0.03      0.02   -0.01    0.08 1.00      3601      4007
## litLL          -0.01      0.02   -0.05    0.04 1.00      3537      3696
## rodPO:litLD     -0.09      0.07   -0.24    0.05 1.00      4306      3713
## rodALA:litLD     0.08      0.08   -0.07    0.23 1.00      6431      3625
## rodPO:litLL      0.08      0.09   -0.10    0.26 1.00      5160      3741
## rodALA:litLL     0.11      0.08   -0.05    0.27 1.00      5985      3984
## sigma_rodPO      1.45      0.12    1.21    1.68 1.00      2061      2947
## sigma_rodALA      0.59      0.15    0.30    0.90 1.00      2141      3180
## sigma_litLD     -0.09      0.13   -0.35    0.17 1.00      2014      2782
## sigma_litLL     -0.10      0.14   -0.38    0.19 1.00      1816      3313
## sigma_rodPO:litLD 0.08      0.18   -0.25    0.43 1.00      2216      3243
## sigma_rodALA:litLD 0.68      0.22    0.23    1.12 1.00      2516      3656
## sigma_rodPO:litLL 0.41      0.18    0.05    0.76 1.00      2310      3748
## sigma_rodALA:litLL 0.85      0.22    0.41    1.29 1.00      2533      3802
##
## Draws were sampled using sampling(NUTS). For each parameter, Bulk_ESS
## and Tail_ESS are effective sample size measures, and Rhat is the potential
## scale reduction factor on split chains (at convergence, Rhat = 1).
```

## M4 Rod Fed Lit model

```
Al_rod_fed_lit_mod <- brm(
  bf(L ~ rod*fed*lit + (1|larva), sigma ~ rod*fed*lit),
  family = gaussian,
  data=Al_df, prior = priors,
  chains = nchain,
  iter = niter, warmup = niter/2,
  control=list(adapt_delta=0.999),
  save_pars = save_pars(all = TRUE)
)
Al_rod_fed_lit_mod

## Family: gaussian
## Links: mu = identity; sigma = log
## Formula: L ~ rod * fed * lit + (1 | larva)
##           sigma ~ rod * fed * lit
## Data: Al_df (Number of observations: 604)
## Draws: 4 chains, each with iter = 2500; warmup = 1250; thin = 1;
##           total post-warmup draws = 5000
##
## Multilevel Hyperparameters:
## ~larva (Number of levels: 130)
##           Estimate Est.Error l-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS
## sd(Intercept)    0.06      0.01    0.04    0.08 1.00      1006      2073
##
## Regression Coefficients:
##           Estimate Est.Error l-95% CI u-95% CI Rhat
```

## Intercept	-0.90	0.02	-0.93	-0.86	1.00
## sigma_Intercept	-2.14	0.11	-2.34	-1.93	1.00
## rodPO	1.92	0.06	1.80	2.03	1.00
## rodALA	0.36	0.04	0.29	0.44	1.00
## fedStarved	-0.06	0.03	-0.12	-0.00	1.00
## litLD	0.05	0.03	-0.01	0.10	1.00
## litLL	-0.02	0.03	-0.07	0.04	1.00
## rodPO:fedStarved	0.22	0.10	0.01	0.42	1.00
## rodALA:fedStarved	0.17	0.06	0.04	0.30	1.00
## rodPO:litLD	-0.28	0.08	-0.45	-0.13	1.00
## rodALA:litLD	-0.07	0.09	-0.24	0.11	1.00
## rodPO:litLL	0.05	0.10	-0.15	0.25	1.00
## rodALA:litLL	-0.07	0.05	-0.18	0.03	1.00
## fedStarved:litLD	-0.02	0.04	-0.10	0.05	1.00
## fedStarved:litLL	0.01	0.04	-0.07	0.10	1.00
## rodPO:fedStarved:litLD	0.39	0.14	0.13	0.66	1.00
## rodALA:fedStarved:litLD	0.38	0.11	0.16	0.59	1.00
## rodPO:fedStarved:litLL	0.10	0.19	-0.28	0.48	1.00
## rodALA:fedStarved:litLL	0.36	0.15	0.05	0.66	1.00
## sigma_rodPO	1.26	0.14	0.98	1.53	1.00
## sigma_rodALA	0.51	0.17	0.17	0.86	1.00
## sigma_fedStarved	-0.35	0.18	-0.69	0.00	1.00
## sigma_litLD	-0.31	0.18	-0.65	0.03	1.00
## sigma_litLL	-0.22	0.17	-0.54	0.11	1.00
## sigma_rodPO:fedStarved	0.57	0.22	0.14	1.01	1.00
## sigma_rodALA:fedStarved	0.22	0.29	-0.34	0.79	1.00
## sigma_rodPO:litLD	0.18	0.22	-0.25	0.62	1.00
## sigma_rodALA:litLD	0.78	0.27	0.26	1.32	1.00
## sigma_rodPO:litLL	0.46	0.22	0.02	0.89	1.00
## sigma_rodALA:litLL	-0.13	0.29	-0.69	0.42	1.00
## sigma_fedStarved:litLD	0.47	0.25	-0.03	0.96	1.00
## sigma_fedStarved:litLL	0.43	0.27	-0.10	0.96	1.00
## sigma_rodPO:fedStarved:litLD	-0.63	0.31	-1.25	-0.01	1.00
## sigma_rodALA:fedStarved:litLD	-1.49	0.46	-2.37	-0.59	1.00
## sigma_rodPO:fedStarved:litLL	-0.29	0.34	-0.94	0.37	1.00
## sigma_rodALA:fedStarved:litLL	0.97	0.43	0.17	1.82	1.00
##	Bulk_ESS	Tail_ESS			
## Intercept	2306	3432			
## sigma_Intercept	1998	2688			
## rodPO	2742	3386			
## rodALA	3399	3187			
## fedStarved	2196	3081			
## litLD	2193	3139			
## litLL	2190	2761			
## rodPO:fedStarved	2759	2717			
## rodALA:fedStarved	3501	3862			
## rodPO:litLD	3011	3683			
## rodALA:litLD	3689	3157			
## rodPO:litLL	3500	3447			
## rodALA:litLL	3897	3968			
## fedStarved:litLD	2236	3244			
## fedStarved:litLL	2480	3085			
## rodPO:fedStarved:litLD	2946	3307			
## rodALA:fedStarved:litLD	3291	3562			

```
## rodPO:fedStarved:litLL          3914    3597
## rodALA:fedStarved:litLL         5718    3950
## sigma_rodPO                    2410    2778
## sigma_rodALA                   2133    2934
## sigma_fedStarved               1704    2645
## sigma_litLD                   2090    3150
## sigma_litLL                   1979    2549
## sigma_rodPO:fedStarved         1933    2437
## sigma_rodALA:fedStarved        2056    2996
## sigma_rodPO:litLD             2346    3147
## sigma_rodALA:litLD            2738    3161
## sigma_rodPO:litLL             2374    3117
## sigma_rodALA:litLL            2248    2766
## sigma_fedStarved:litLD        1717    2647
## sigma_fedStarved:litLL        1993    2808
## sigma_rodPO:fedStarved:litLD  2031    3032
## sigma_rodALA:fedStarved:litLD 2836    3745
## sigma_rodPO:fedStarved:litLL  2304    3533
## sigma_rodALA:fedStarved:litLL 2336    3146
##
## Draws were sampled using sampling(NUTS). For each parameter, Bulk_ESS
## and Tail_ESS are effective sample size measures, and Rhat is the potential
## scale reduction factor on split chains (at convergence, Rhat = 1).
```

### 3. Evaluate models using LOO

```
Al_intercept_mod = add_criterion(Al_intercept_mod, criterion = "loo",
                                moment_match = TRUE, relloo = TRUE)
```

```
## No problematic observations found. Returning the original 'loo' object.
```

```
Al_rod_mod = add_criterion(Al_rod_mod, criterion = "loo",
                           moment_match = TRUE, relloo = TRUE)
```

```
## No problematic observations found. Returning the original 'loo' object.
```

```
Al_rod_lit_mod = add_criterion(Al_rod_lit_mod, criterion = "loo",
                               moment_match = TRUE, relloo = TRUE)
```

```
## Warning: Some Pareto k diagnostic values are too high. See help('pareto-k-diagnostic') for details.
```

```
## 2 problematic observation(s) found.
```

```
## The model will be refit 2 times.
```

```
##
```

```
## Fitting model 1 out of 2 (leaving out observation 192)
```

```
## Start sampling
```

```
##
```

```
## Fitting model 2 out of 2 (leaving out observation 305)
```

```
## Start sampling
```

```
Al_rod_fed_mod = add_criterion(Al_rod_fed_mod, criterion = "loo",
                               moment_match = TRUE, relloo = TRUE)
```

```
## Warning: Some Pareto k diagnostic values are too high. See help('pareto-k-diagnostic') for details.
```



```

## 1 problematic observation(s) found.
## The model will be refit 1 times.

##
## Fitting model 1 out of 1 (leaving out observation 158)
## Start sampling
Al_rod_fed_lit_mod = add_criterion(Al_rod_fed_lit_mod, criterion = "loo",
                                   moment_match = TRUE, reloo = TRUE)

## Warning: Some Pareto k diagnostic values are too high. See help('pareto-k-diagnostic') for details.
## 3 problematic observation(s) found.
## The model will be refit 3 times.

##
## Fitting model 1 out of 3 (leaving out observation 158)
## Start sampling

##
## Fitting model 2 out of 3 (leaving out observation 408)
## Start sampling

##
## Fitting model 3 out of 3 (leaving out observation 442)
## Start sampling

# Perform LOO comparison
loo_results <- loo_compare(Al_intercept_mod,
                          Al_rod_mod,
                          Al_rod_fed_mod,
                          Al_rod_lit_mod,
                          Al_rod_fed_lit_mod
                          )

loo_results

##              elpd_diff se_diff
## Al_rod_fed_lit_mod    0.0     0.0
## Al_rod_fed_mod      -20.9    10.8
## Al_rod_lit_mod       -51.7    14.1
## Al_rod_mod          -57.5    17.2
## Al_intercept_mod    -871.4    31.9

best_model_name <- rownames(loo_results)[1]
best_model <- get(best_model_name)

# Print the name of the best model
print(paste("The best model is:", best_model_name))

## [1] "The best model is: Al_rod_fed_lit_mod"

```

## Model Equation

The model assumes a normal distribution for the response variable:

$$Y_i \sim \mathcal{N}(\mu_i, \sigma_i)$$

where:

**Linear Predictor for the Mean ( $\mu_i$ ):**

$$\mu_i = \beta_0 + X_i\beta + u_{J_1[i]}Z_{1,i}$$

- $\beta_0$  (Intercept): The population-level intercept.
- $X_i\beta$ : Fixed effects (population-level predictors) with centered design matrix.
- $u_{J_1[i]}$ : Random effect for group-level predictor, where  $J_1[i]$  is the grouping index.
- $Z_{1,i}$ : Group-level predictor values.
- $u_{J_1[i]}$  follows a normal distribution:

$$u_{J_1[i]} \sim \mathcal{N}(0, \sigma_u)$$

where  $\sigma_u$  is the standard deviation of the group-level effect.

**Linear Predictor for the Standard Deviation ( $\sigma_i$ ):**

$$\log(\sigma_i) = \alpha_0 + X_{\sigma,i}\alpha$$

- $\alpha_0$  (Intercept\_sigma): Population-level intercept for the variance structure.
- $X_{\sigma,i}\alpha$ : Fixed effects for the variance model.

**Prior Distributions:**

$$\beta \sim \mathcal{N}(0, 2), \quad \beta_0 \sim t_5(0, 2)$$

$$\alpha \sim \mathcal{N}(0, 1), \quad \alpha_0 \sim t_5(0, 2)$$

$$\sigma_u \sim t_3(0, 0.5)$$

This structure allows the model to estimate both the mean and the variance of growth ( $Y$ ) while accounting for hierarchical effects from group-level predictors.

```
#saveRDS(best_model, file = paste0("./model_objects/", best_model_name, ".rds"))
```