

(HW3)

(PA)

$$1. \quad \bar{X} \pm 2.81 \frac{\sigma}{\sqrt{n}}$$

$$z_{\frac{\alpha}{2}} = 2.81 \quad \frac{\alpha}{2} = 0.0025 \quad \alpha = 0.005$$

$$\text{conf. lv.} = 0.995$$

$$2) \quad \bar{X} \pm 1.44 \frac{\sigma}{\sqrt{n}}$$

$$z_{\frac{\alpha}{2}} = 1.44 \quad \frac{\alpha}{2} = 0.0745 \quad \alpha = 0.149$$

$$cl = 1 - \alpha = 0.8502$$

$$3. \quad cl = 1 - \alpha = 0.997 \quad \alpha = 0.003$$

$$z_{\alpha/2} = z_{0.0015} = 2.96$$

$$4. \quad cl = 0.75 \quad \alpha = 0.25$$

$$z_{\alpha/2} = z_{0.125} = 1.155$$

(p2)

$$1) \sigma = 0,75$$

$$1) \alpha = 0,05$$

$$n = 20$$

$$\bar{X} = 4,85$$

$$\bar{X} \pm Z_{\alpha/2} \frac{\sigma}{\sqrt{n}}$$

$$4,85 \pm 1,96 \frac{0,75}{\sqrt{20}}$$

$$(4,52; 5,18)$$

$$2) \alpha = 0,02$$

$$n = 16$$

$$\bar{X} = 4,56$$

$$Z_{0,01} = 2,32$$

$$4,56 \pm 2,32 \frac{0,75}{\sqrt{16}}$$

$$3) \alpha = 0,05 \quad w = 0,4$$

$$2 \cdot Z_{\alpha/2} \frac{\sigma}{\sqrt{n}} = w$$

$$n = \left(\frac{2 \cdot 1,96 \cdot 0,75}{0,4} \right)^2 = 34,022 \quad n = 35$$

$$4) \alpha = 0,01$$

$$z_{0,005} = 2,58$$

$$n = \left(\frac{2,58 \cdot 18,94}{0,4} \right)^2 = (19,67)^2 \approx 386$$

$$n = 386$$

P3

$$n = 49$$

$$\bar{x} = 35,02$$

$$s = 18,94$$

$$1) \alpha = 0,05$$

$$35,02 \pm 1,96 \cdot \frac{18,94}{\sqrt{49}}$$

$$35,02 \pm \frac{18,56}{\sqrt{49}} = 35 \pm 5,59$$

$$(29,43; 40,6)$$

2)

$$\bar{x} \pm t_{0,025, n-1} \cdot s \sqrt{1 + \frac{1}{n}}$$

$$35,02 \pm 2,064 \cdot 18,94 \sqrt{1 + \frac{1}{49}}$$

$$35,02 \pm 39,09 \frac{3,1 \sqrt{85}}{2 \sqrt{11}}$$

$$35,02 \pm 39,5$$

$$(-3,48; 79,5)$$

P.4

$$n = 126$$

$$\bar{x} = 29.2$$

$$\mu = 18.2$$

significance level $\alpha = 0.05$ $\alpha/2 = 0.025$

$$29.2 \pm 1.96 \frac{7.5}{\sqrt{126}}$$

$$[27.89, 30.51]$$

we reject H_0 and accept H_a