

Temă ~ protocolul Shamir

1.

$$n=6$$

$$m=3$$

$$\mathbb{Z}_{31}$$

$$(1, 13); (30, 9); (2, 18); (29, 4); (3, 25); (28, 13)$$

Determinați secretul f

$$F(x) = ax^2 + bx + c$$

$$F(1) = 13 \Leftrightarrow a + b + c = 13$$

$$F(30) = 9 \Leftrightarrow \underset{\substack{|| \\ -1}}{(-1)^2} a - b + c = 9$$

$$F(2) = 18 \Leftrightarrow 4a + 2b + c = 18$$

$$F(29) = 4 \Leftrightarrow \underset{\substack{|| \\ -2}}{(-2)^2} a - 2b + c = 4$$

$$F(3) = 25 \Leftrightarrow 9a + 3b + c = 25$$

$$F(28) = 13 \Leftrightarrow \underset{\substack{|| \\ -3}}{(-3)^2} a - 3b + c = 13$$

$$\begin{cases} a+b+c=13 \\ a-b+c=9 \\ 4a+2b+c=18 \end{cases} \Rightarrow \begin{cases} 2b=4 & |2^{-1}=16 \\ a-b+c=9 \\ 4a+2b+c=18 \end{cases} \Rightarrow \begin{cases} b=64=2 \\ a-2+c=9 \\ 4a+4+c=18 \end{cases}$$

$$2 \cdot 16 \equiv 1 \pmod{31} \Rightarrow 2^{-1} = 16 \pmod{31}$$

$$\Rightarrow \begin{cases} b=2 \\ a+c=11 \\ 4a+c=14 \end{cases} \quad (-)$$

$$3a=3 \quad |3^{-1}=$$

$$a=1$$

$$b=2$$

$$c=10$$

$$F(x) = x^2 + 2x + 10 \rightarrow \text{message secret}$$

$$\cancel{4} \rightarrow 10$$