

# Project 3

Start Assignment

**Due** Apr 14 by 11:59pm    **Points** 100    **Submitting** a file upload

## Constraint satisfaction problems (CSP) - Map Coloring

A  $k$ -coloring of a map is an assignment of  $k$  colors, one to each country, in such a way that no two countries sharing a border have the same color. This problem can be translated to a constraint graph. A coloring of a graph  $G$  assigns a color to each vertex of  $G$ , with the restriction that two adjacent vertices never have the same color. The chromatic number of  $G$ , written  $\chi(G)$ , is the smallest number of colors needed to color  $G$ .

In this project, we will experiment with map coloring techniques and compare the observed results in the context of USA and Australia maps.

- Compute the chromatic number of USA and Australia map.
- Experiment with both maps using the following methods [without heuristics]
  - Depth first search only
  - Depth first search + forward checking
  - Depth first search + forward checking + propagation through singleton domains
- Experiment with both maps using the following methods with heuristics where the order of variables needs to be defined in the following order MRV, Degree Constraint, and Least Constraining Value
  - Depth first search only
  - Depth first search + forward checking
  - Depth first search + forward checking + propagation through singleton domains
- Present the results in a tabular format
  - the number of backtracking happened and
  - the time required to compute the result.

### General instructions:

1. The project can be completed individually, or in a group of three max.
  - Many students work alone, which is good. If you prefer to work in a group, you are responsible for making your own group.
2. Map visualization is preferred but **not required**. For visualization you can use any framework or tool.

### Submission instructions:

1. Your program should be well documented, and you should turn in the following to canvas.
  - An external document describing the *map coloring problem* formulation, the program structure, global variables, the function/procedure to compute the heuristic function, and other functions/procedures, etc.
  - Your program source codes (with necessary inline documentation);
  - The execution results as specified above.
  - Each member must turn in everything in canvas.
2. 10% late submission penalty for each extra day. Cut-off: Three days after the deadline.

**Warning:** Any form of cheating will subject you to disciplinary act.

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Here is a guideline to experiment with map coloring algorithms.

### **Without Heuristics**

1. Define the order of states randomly for map coloring
2. Run the following algorithms for the same random order of states
  - Depth first search only
  - Depth first search + forward checking
  - Depth first search + forward checking + propagation through singleton domain
3. Repeat steps 1 and 2 at least four times.
4. Show the results in a table for both maps

### **With Heuristics**

1. Start with a state
2. Run the following algorithms - this time, you will use heuristics to select next variable and value where appropriate at runtime
  - Depth first search only
  - Depth first search + forward checking
  - Depth first search + forward checking + propagation through singleton domain
3. Repeat steps 1 and 2 at least four times.
4. Show the results in a table for both maps

Compare all results and analyze them.