



**MS101 – DISCRETE MATHEMATICS
PROJECT**

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SCORE

PERCENTAGE



Assignment: Construct truth table; determine the properties of sentence.

1. $p \rightarrow q$

| p | q | $p \rightarrow q$ |
|---|---|-------------------|
| T | T | T |
| T | F | F |
| F | T | T |
| F | F | T |

Properties: Satisfiable

2. $(p \vee \sim p) \wedge (q \wedge \sim q)$

| p | q | $\sim p$ | $\sim q$ | $(p \vee \sim p)$ | $(q \wedge \sim q)$ | $(p \vee \sim p) \wedge (q \wedge \sim q)$ |
|---|---|----------|----------|-------------------|---------------------|--|
| T | T | F | F | T | F | F |
| T | F | F | T | T | F | F |
| F | T | T | F | T | F | F |
| F | F | T | T | T | F | F |

Properties: Contradictory

3. $p \leftrightarrow q$

| p | q | $p \leftrightarrow q$ |
|---|---|-----------------------|
| T | T | T |
| T | F | F |
| F | T | F |
| F | F | T |

Properties: Satisfiable



4. $\sim(p \wedge \sim p)$

| p | $\sim p$ | $(p \wedge \sim p)$ | $\sim(p \wedge \sim p)$ |
|---|----------|---------------------|-------------------------|
| T | F | F | T |
| F | T | F | T |

Properties: Valid

5. $\sim(p \vee \sim p)$

| p | $\sim p$ | $(p \vee \sim p)$ | $\sim(p \vee \sim p)$ |
|---|----------|-------------------|-----------------------|
| T | F | T | F |
| F | T | T | F |

Properties: Contradictory

6. $\sim(p \vee p)$

| p | $(p \vee p)$ | $\sim(p \vee p)$ |
|---|--------------|------------------|
| T | F | F |
| F | T | T |

Properties: Satisfiable

7. $(p \wedge \sim p) \vee (q \wedge \sim q)$

| q | p | $\sim p$ | $\sim q$ | $(p \wedge \sim p)$ | $(q \wedge \sim q)$ | $(p \wedge \sim p) \vee (q \wedge \sim q)$ |
|---|---|----------|----------|---------------------|---------------------|--|
| T | T | F | F | F | F | F |
| T | F | T | F | F | F | F |
| F | T | F | T | F | F | F |
| F | F | T | T | F | F | F |

Properties: Contradictory



8. $\sim(p \vee \sim q) \wedge (p \wedge \sim q)$

| p | q | $\sim p$ | $\sim q$ | $(p \vee \sim q)$ | $\sim(p \vee \sim q)$ | $(p \wedge \sim q)$ | $\sim(p \vee \sim q) \wedge (p \wedge \sim q)$ |
|---|---|----------|----------|-------------------|-----------------------|---------------------|--|
| T | T | F | F | T | F | F | F |
| T | F | F | T | T | F | T | F |
| F | T | T | F | F | T | F | F |
| F | F | T | T | T | F | F | F |

Properties: Contradictory

9. $(p \leftrightarrow q) \vee (q \leftrightarrow p)$

| p | q | $(p \leftrightarrow q)$ | $(q \leftrightarrow p)$ | $(p \leftrightarrow q) \vee (q \leftrightarrow p)$ |
|---|---|-------------------------|-------------------------|--|
| T | T | T | T | T |
| T | F | F | F | F |
| F | T | F | F | F |
| F | F | T | T | T |

Properties: Satisfiable

10. $\sim[(p \rightarrow q) \rightarrow r]$

| p | q | r | $(p \rightarrow q)$ | $[(p \rightarrow q) \rightarrow r]$ | $\sim[(p \rightarrow q) \rightarrow r]$ |
|---|---|---|---------------------|-------------------------------------|---|
| T | T | T | T | T | F |
| T | T | F | T | F | T |
| T | F | T | F | T | F |
| T | F | F | F | T | F |
| F | T | T | T | T | F |
| F | T | F | T | F | T |
| F | F | T | T | T | F |
| F | F | F | T | F | T |

Properties: Satisfiable



11. $[p \rightarrow (q \rightarrow r)] \wedge (p \rightarrow r)$

| p | q | r | $(q \rightarrow r)$ | $(p \rightarrow r)$ | $[p \rightarrow (q \rightarrow r)]$ | $[p \rightarrow (q \rightarrow r)] \wedge (p \rightarrow r)$ |
|---|---|---|---------------------|---------------------|-------------------------------------|--|
| T | T | T | T | T | T | T |
| T | T | F | F | F | F | F |
| T | F | T | T | T | T | T |
| T | F | F | T | F | T | F |
| F | T | T | T | T | T | T |
| F | T | F | F | T | T | T |
| F | F | T | T | T | T | T |
| F | F | F | T | T | T | T |

Properties: Satisfiable

12. $(p \wedge q) \rightarrow (p \rightarrow q)$

| p | q | $(p \wedge q)$ | $(p \rightarrow q)$ | $(p \wedge q) \rightarrow (p \rightarrow q)$ |
|---|---|----------------|---------------------|--|
| T | T | T | T | T |
| T | F | F | F | T |
| F | T | F | T | T |
| F | F | F | T | T |

Properties: Valid

13. $\sim p \rightarrow p$

| p | $\sim p$ | $\sim p \rightarrow p$ |
|---|----------|------------------------|
| T | F | T |
| F | T | F |

Properties: Satisfiable



14. $\sim p \rightarrow (q \vee p)$

| p | q | $\sim p$ | $(q \vee p)$ | $\sim p \rightarrow (q \vee p)$ |
|---|---|----------|--------------|---------------------------------|
| T | T | F | T | T |
| T | F | F | T | T |
| F | T | T | T | T |
| F | F | T | F | F |

Properties: Satisfiable

15. $\sim p \wedge \sim(\sim p \vee \sim q)$

| p | q | $\sim p$ | $\sim q$ | $(\sim p \vee \sim q)$ | $\sim(\sim p \vee \sim q)$ | $\sim p \wedge \sim(\sim p \vee \sim q)$ |
|---|---|----------|----------|------------------------|----------------------------|--|
| T | T | F | F | F | T | F |
| T | F | F | T | T | F | F |
| F | T | T | F | T | F | F |
| F | F | T | T | T | F | F |

Properties: Contradictory

16. $p \vee (q \rightarrow p)$

| p | q | $(q \rightarrow p)$ | $p \vee (q \rightarrow p)$ |
|---|---|---------------------|----------------------------|
| T | T | T | T |
| T | F | T | T |
| F | T | F | F |
| F | F | T | T |

Properties: Satisfiable



17. $(p \leftrightarrow q) \wedge [(\sim p \vee \sim q) \wedge p]$

| p | q | ~p | ~q | (p ↔ q) | (~p ∨ ~q) | [(~p ∨ ~q) ∧ p] | (p ↔ q) ∧ [(~p ∨ ~q) ∧ p] |
|---|---|----|----|---------|-----------|-----------------|---------------------------|
| F | T | F | F | T | F | F | F |
| F | F | F | T | F | T | T | F |
| T | T | T | F | F | T | F | F |
| T | F | T | T | T | T | F | F |

Properties: Contradictory

18. $(p \leftrightarrow q) \wedge (p \rightarrow q)$

| p | q | (p ↔ q) | (p → q) | (p ↔ q) ∧ (p → q) |
|---|---|---------|---------|-------------------|
| T | T | T | T | T |
| T | F | F | F | F |
| F | T | F | T | F |
| F | F | T | T | T |

Properties: Satisfiable

19. $[p \rightarrow (q \rightarrow r)] \wedge (r \rightarrow p)$

| p | q | r | (q → r) | [p → (q → r)] | (r → p) | [p → (q → r)] ∧ (r → p) |
|---|---|---|---------|---------------|---------|-------------------------|
| T | T | T | T | T | T | T |
| T | T | F | F | F | T | F |
| T | F | T | T | T | T | T |
| T | F | F | T | T | T | T |
| F | T | T | T | T | F | F |
| F | T | F | F | T | T | T |
| F | F | T | T | T | F | F |
| F | F | F | T | T | T | T |

Properties: Satisfiable



20. $(p \leftrightarrow q) \vee \sim [(\sim p \wedge q) \vee (p \wedge \sim q)]$

| p | q | ~p | ~q | (p ↔ q) | (~p ∧ q) | (p ∧ ~q) | $[(\sim p \wedge q) \vee (p \wedge \sim q)]$ | $\sim[(\sim p \wedge q) \vee (p \wedge \sim q)]$ | $(p \leftrightarrow q) \vee \sim [(\sim p \wedge q) \vee (p \wedge \sim q)]$ |
|---|---|----|----|---------|----------|----------|--|--|--|
| T | T | F | F | T | F | F | F | T | T |
| T | F | F | T | F | F | T | T | F | F |
| F | T | T | F | F | T | F | T | F | F |
| F | F | T | T | T | F | F | F | T | T |

Properties: Satisfiable