

1: $\neg \exists x. \neg R(x)$ premise

...

2: $\exists x. \neg R(x)$

3: \perp \neg elim 2,1

4: $\forall y. R(y)$ contra (constructive) 3