2:
$$actual i$$
 assumption
3: $\neg R(i)$ assumption
4: $\exists x. \neg R(x)$

1: $\neg \exists x. \neg R(x)$ premise

¬ elim 4,1

contra (classical) 3-5 7: ∀y.R(y)

¥ intro 2-6