$$\frac{P(_B) \vdash P(_B1) \quad P(_B) \vdash _B1 \text{ inscope}}{\vdash \exists}$$

$$\frac{P(_B) \vdash \exists y. P(y) \quad _B \text{ inscope}}{\forall \vdash}$$

$$\forall x. P(x) \vdash \exists y. P(y)$$