

1: $\neg \exists x. \neg R(x)$ premise

...

2: \perp

3: $\forall y. R(y)$ contra (constructive) 2