

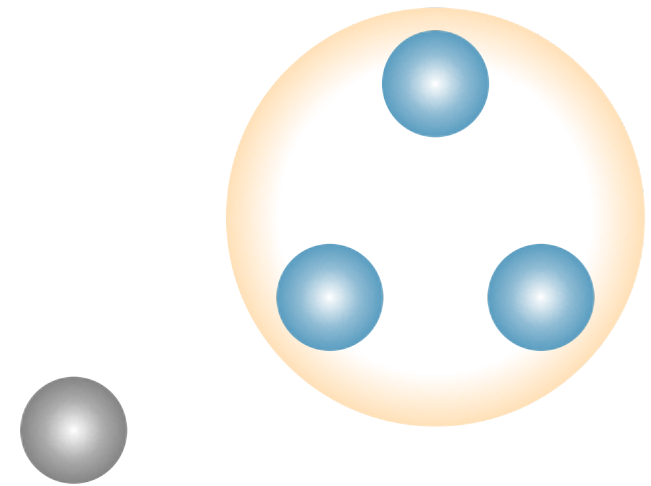
- Introduction to fault-tolerant distributed systems
- Models of distributed systems and related faults
- **Data replication**
- Distributed consensus
- State machine replication
- Database replication

- Let us consider the replication of a basic storage service
 - Elementary atomic read and write operations (mutable servers)
 - Multiple sequential client and server processes / replicas (concurrency model)
 - Crash faults (fault model)

Data replication

ROWA

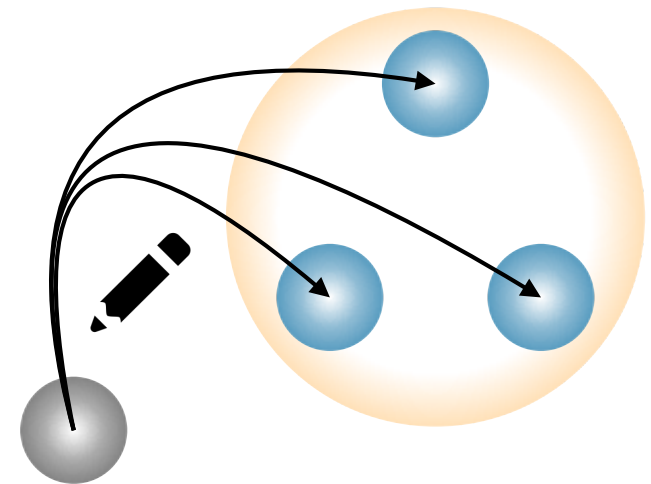
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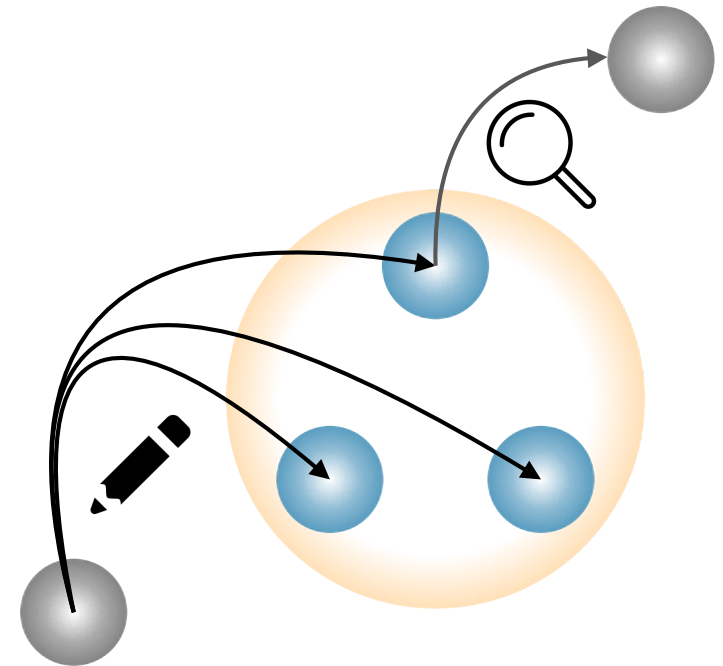
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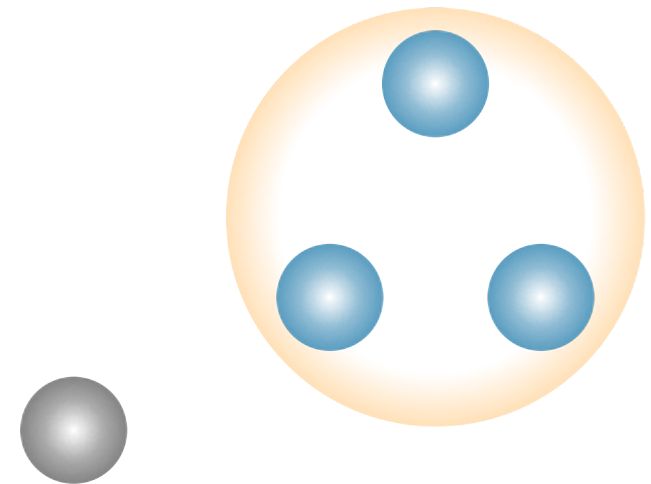


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Data replication

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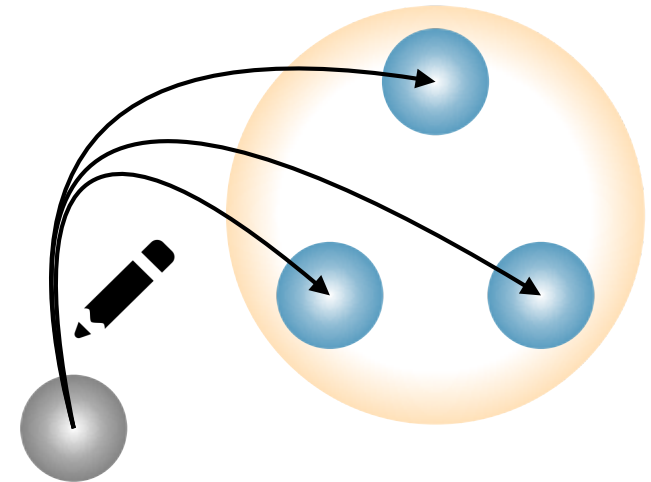
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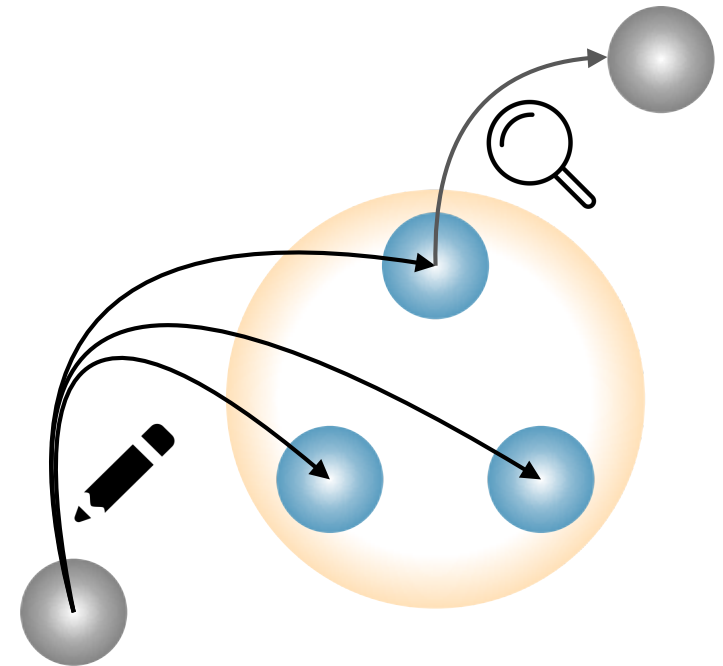
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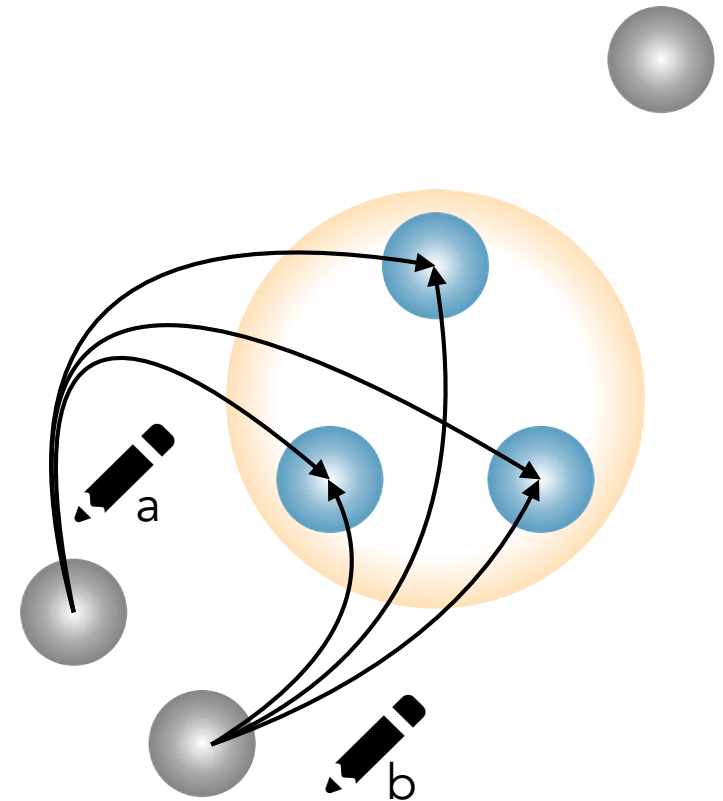
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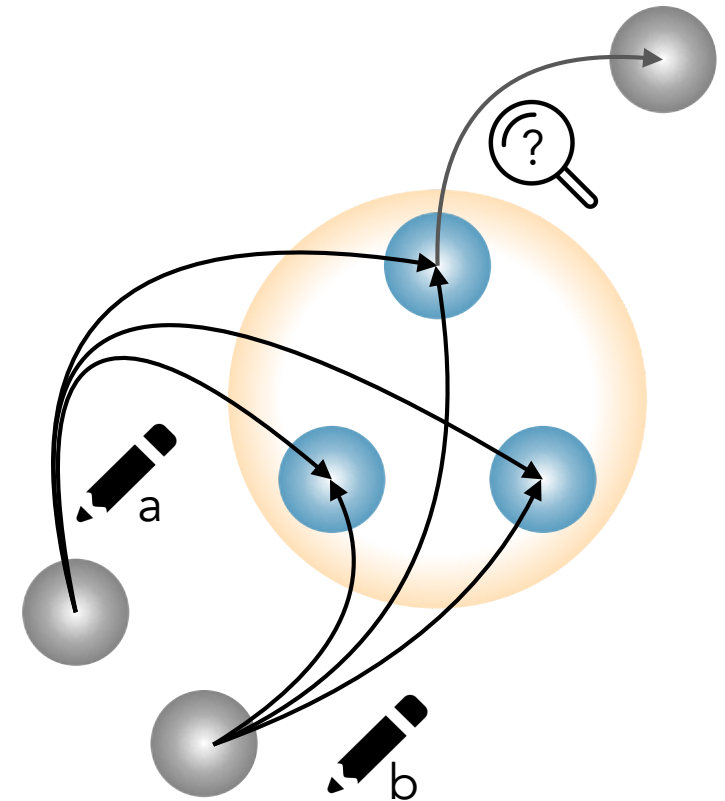
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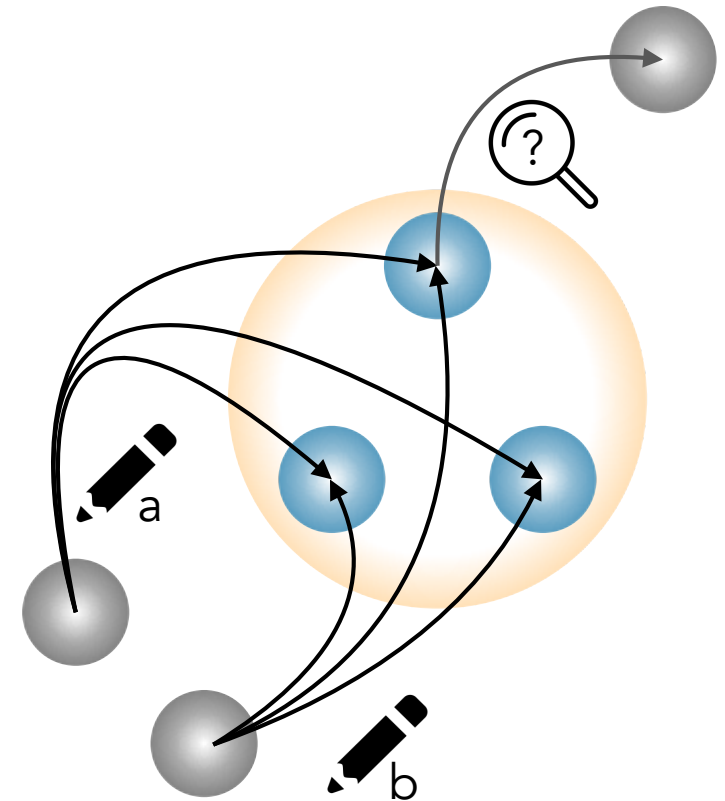
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Data replication

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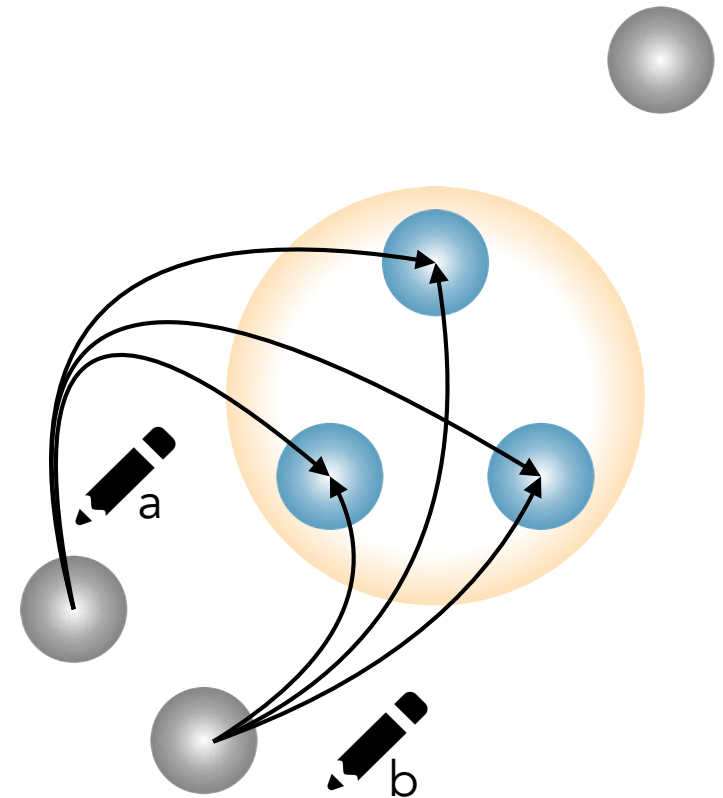
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 - What does a subsequent read return?
 - We may end up with replicas writing $a \rightarrow b$ and others writing $b \rightarrow a$ 😬



Data replication

ROWA

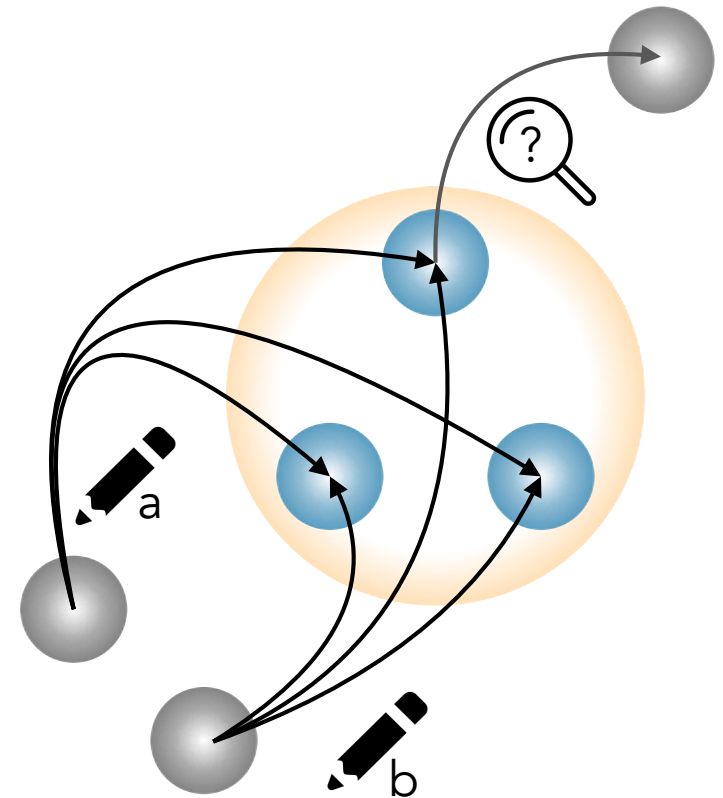
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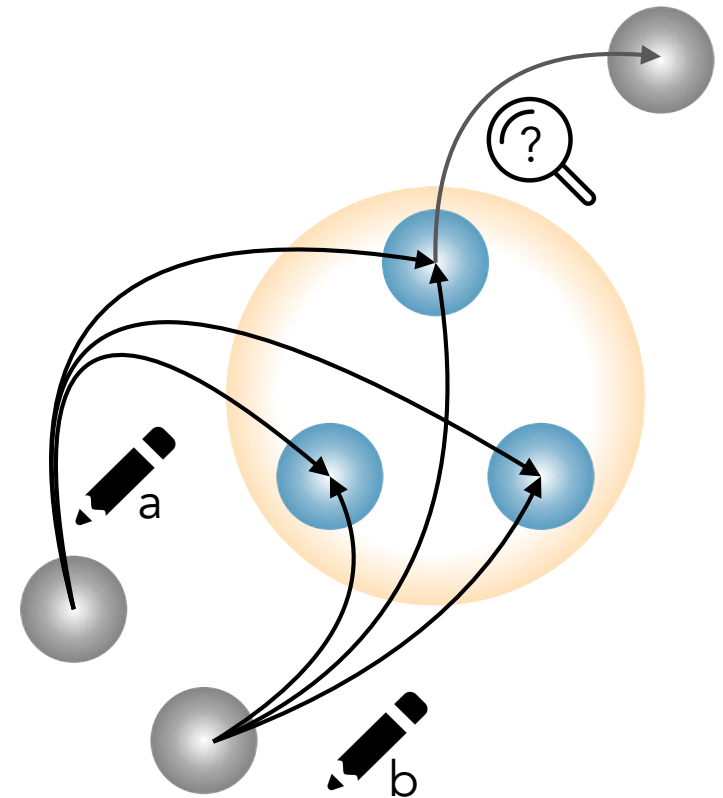
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 - What does a subsequent read return?
 - We may end up with replicas writing a and then b and others writing b and then a



Data replication

Data versioning

- How can we prevent stale writes?
- Let us add a *version* to the state of the replicas
 - v_i is replica i 's version, initially null
- Write operations now become more complex

At client proxies

```
write (value)
  _read (_, vmax) from some replica
  v_write (value, vmax+1) to all replicas
```

At replica i

```
_write (value, version)
  if version >  $v_i$  then
     $x_i$  = value
     $v_i$  = version
```

- How to define version? Is a simple scalar enough?
- Eg. version = (counter, pid)

```
 $v_i > v_j ::$ 
   $v_i.counter > v_j.counter$  OR
   $v_i.counter = v_j.counter$  AND  $v_i.pid > v_j.pid$ 
```


Data replication

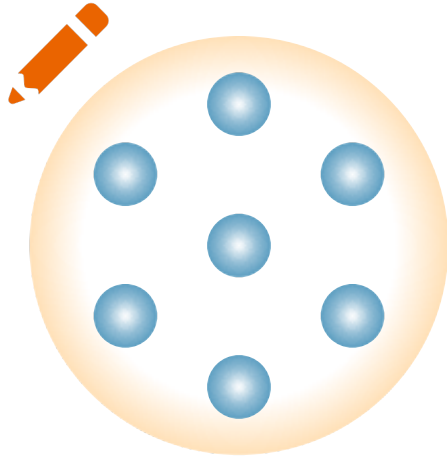
Quorums

- ROWA is not fault tolerant
- Let us introduce Quorums
 - A quorum is a set of replicas
 - We will refer to two quorums: a write quorum Q_w and a read quorum Q_r
 - We will write to some Q_w set of replicas and will read from some Q_r set
 - ROWA is a particular case in which $|Q_w| = n$ and $|Q_r| = 1$
- If we make $|Q_w| < n$ then the replicated system becomes fault tolerant
- Quorum replication requires that:
 - $|Q_r| + |Q_w| > n$, read and write quorums always intersect
 - $2 * |Q_w| > n$, any two write quorums always intersect

Data replication

Quorums

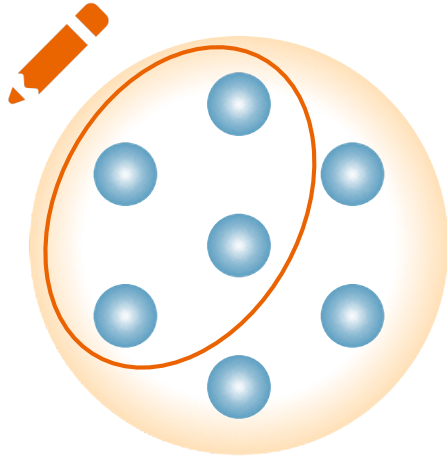
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Data replication

Quorums

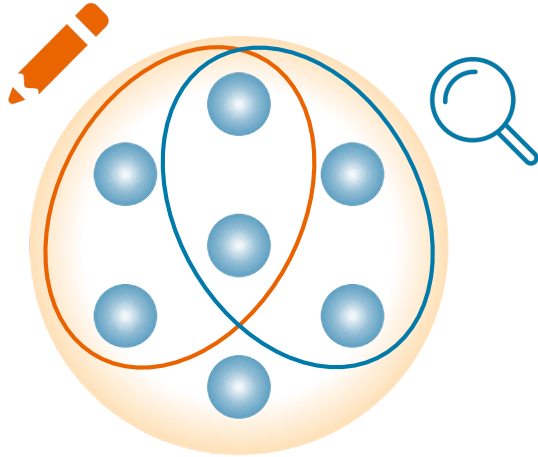
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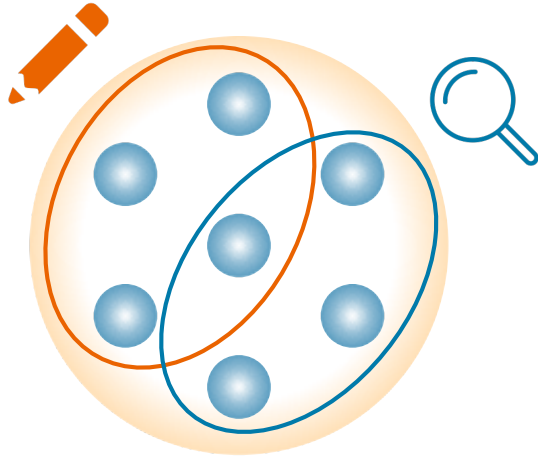
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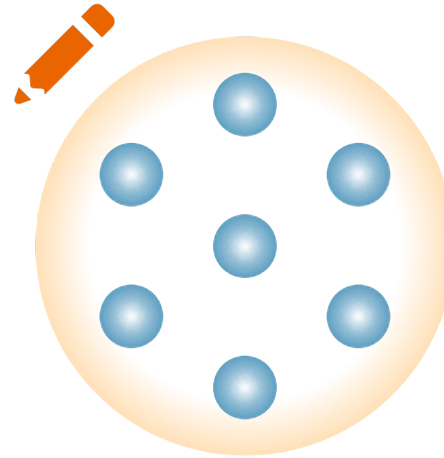
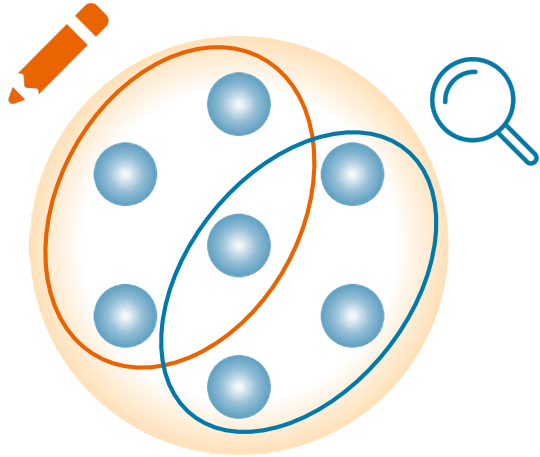
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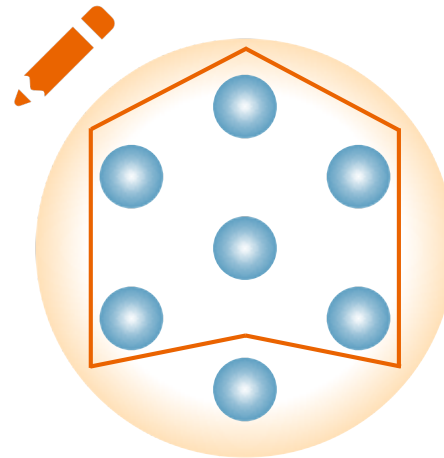
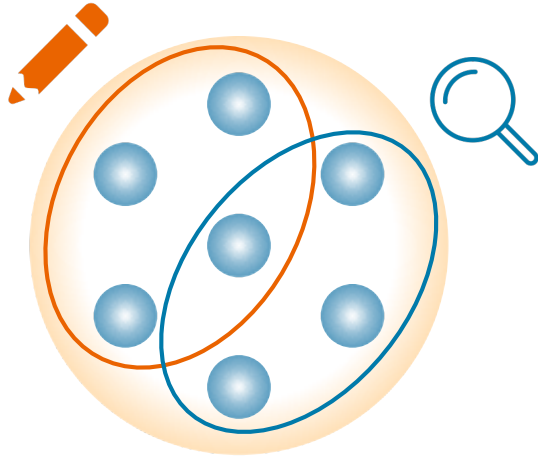
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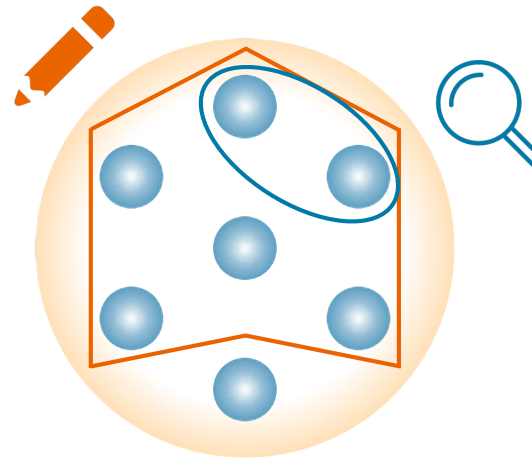
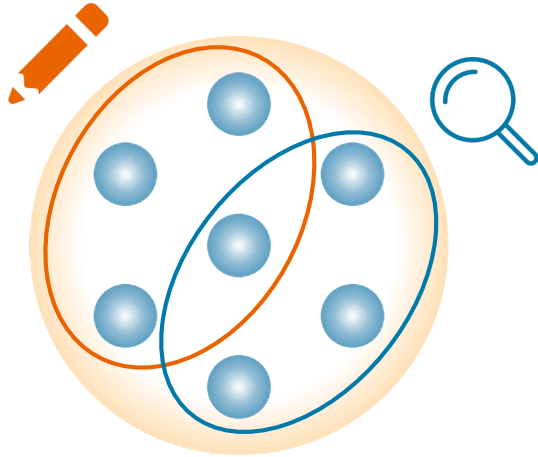
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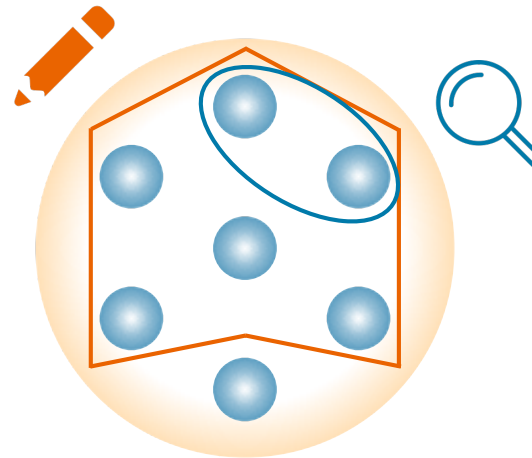
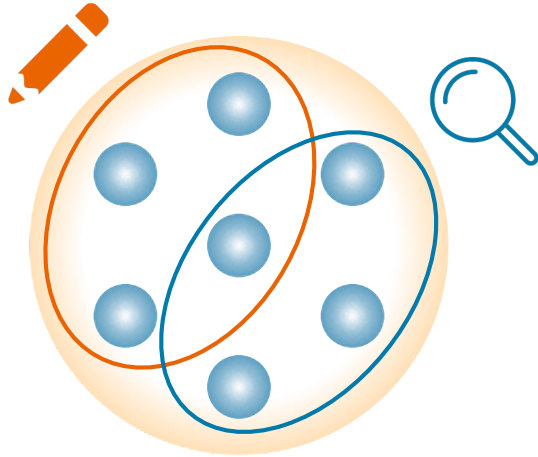


$$|Q_r| + |Q_w| > n$$

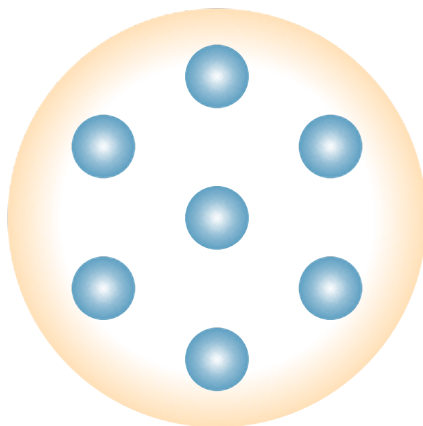
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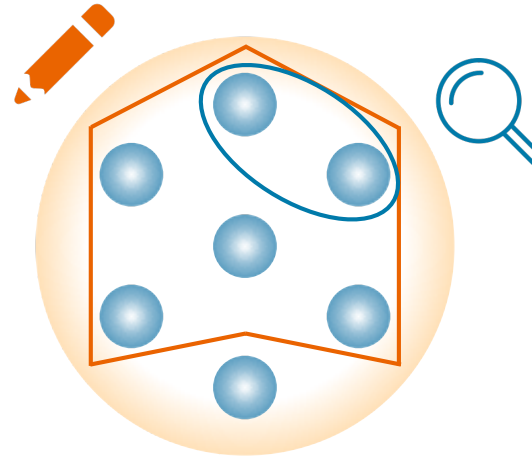
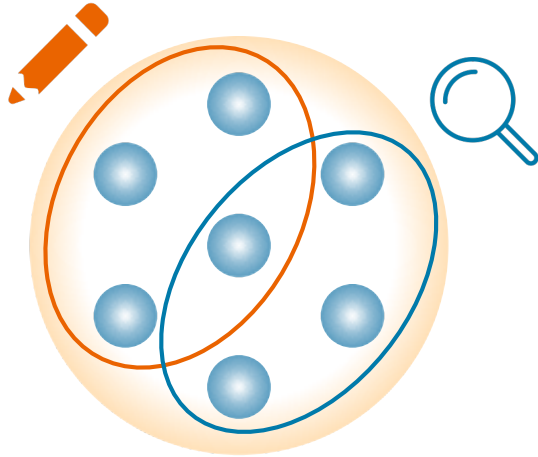
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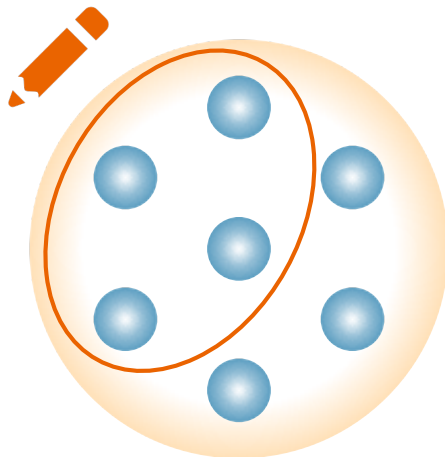
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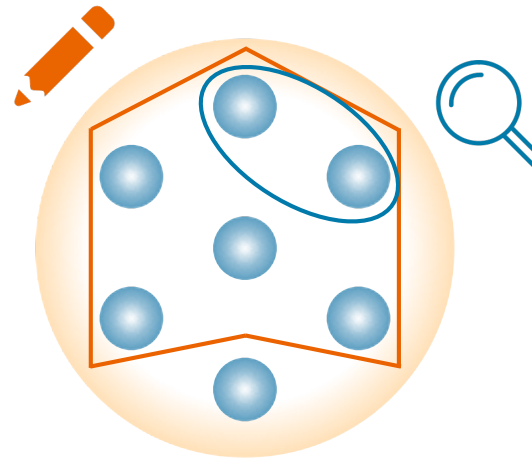
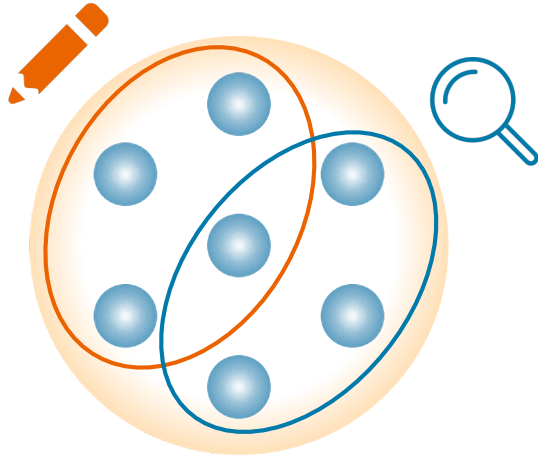
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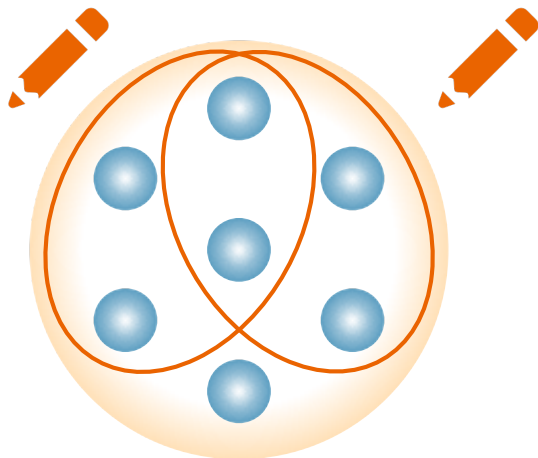
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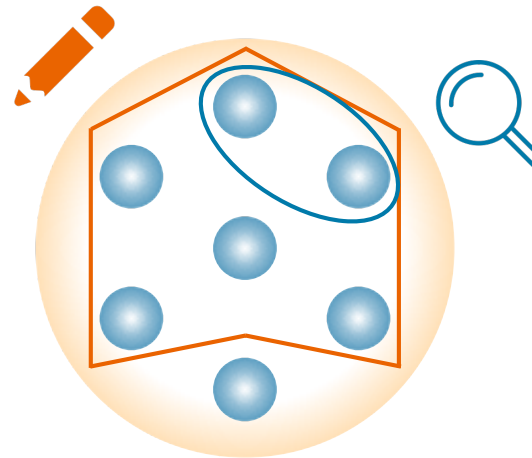
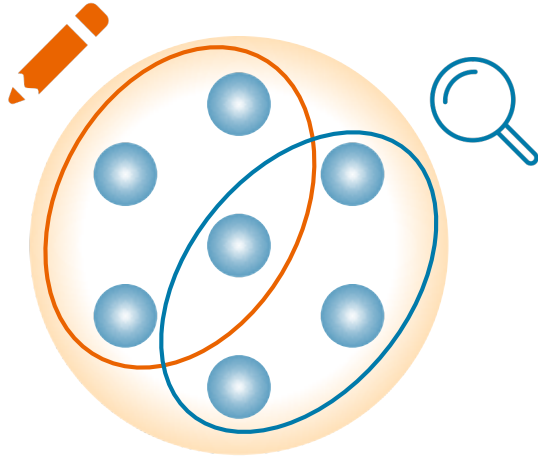
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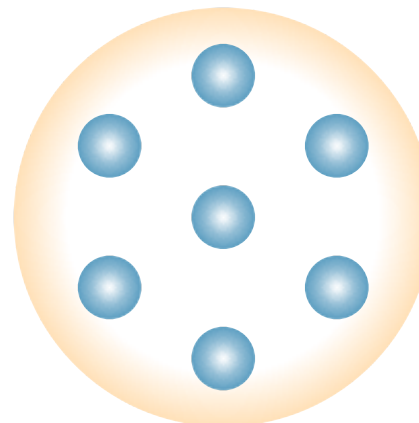
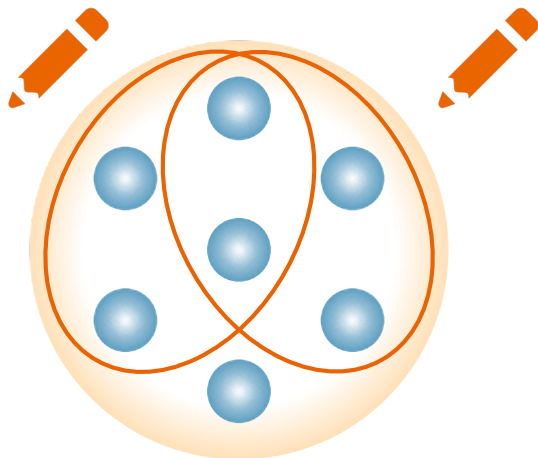
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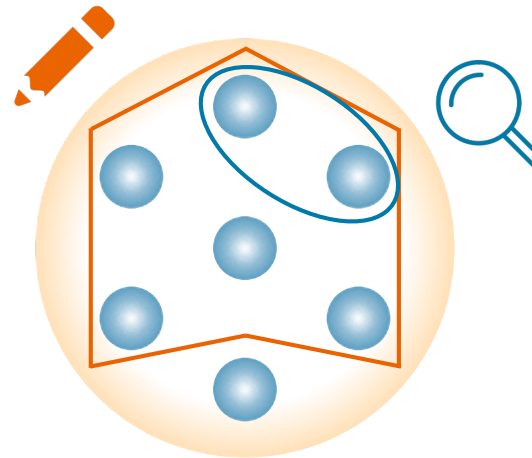
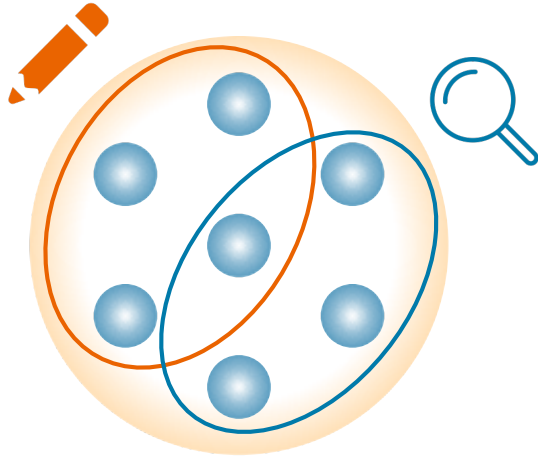
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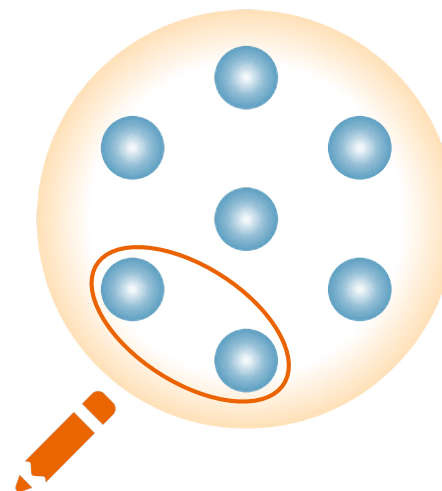
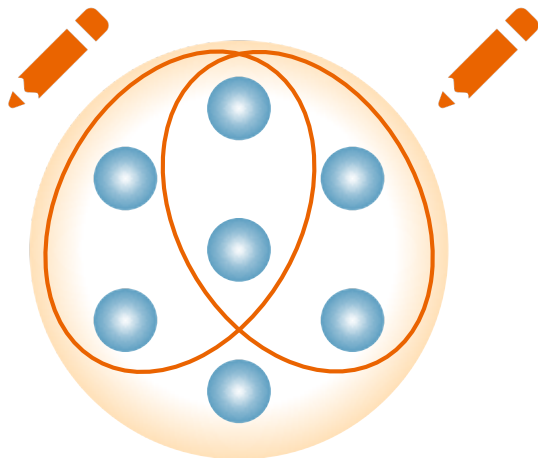
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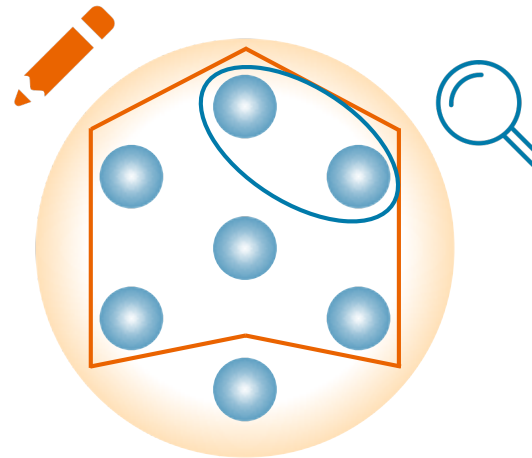
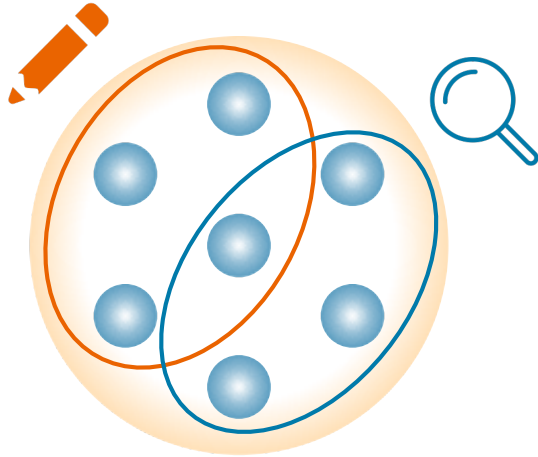
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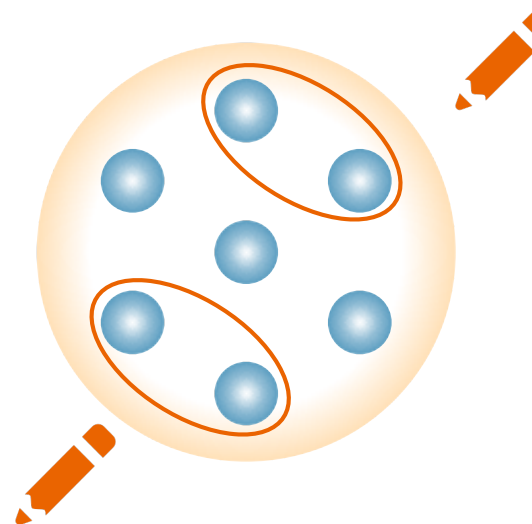
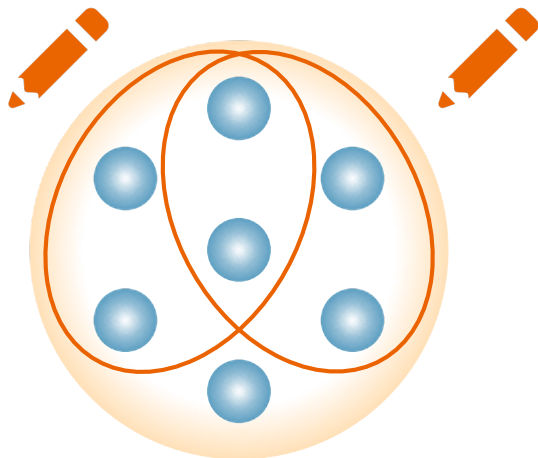
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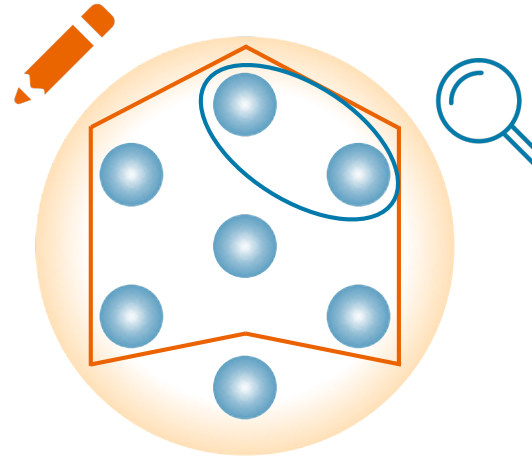
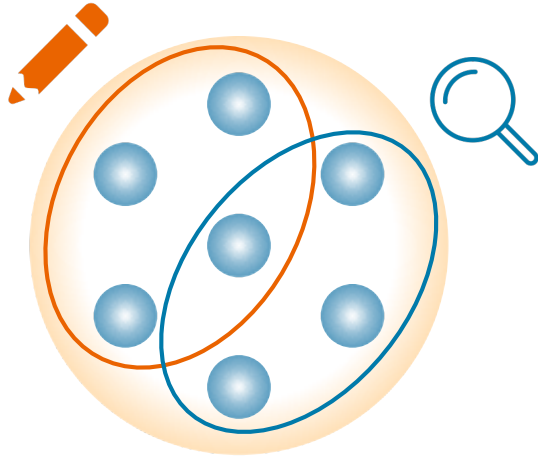
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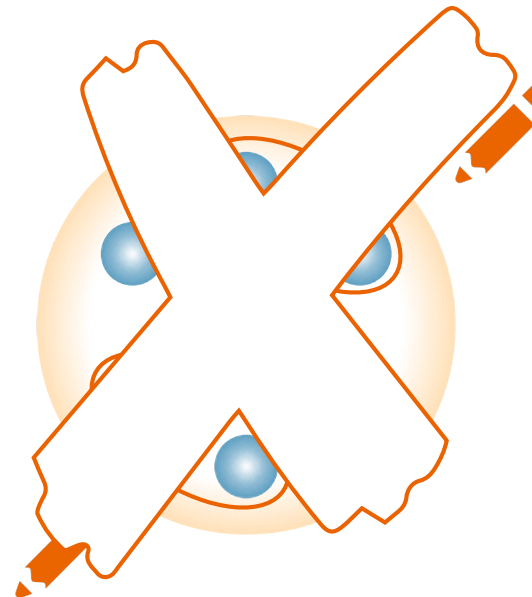
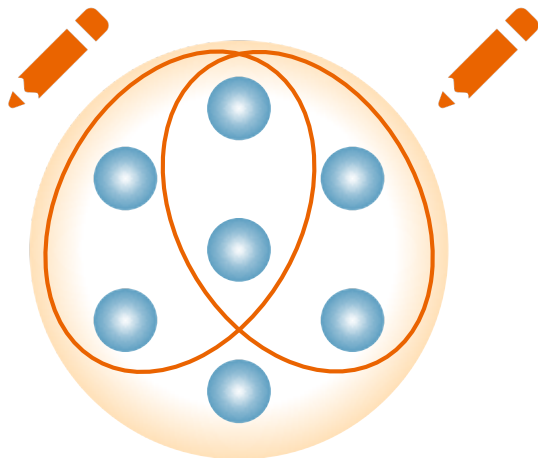
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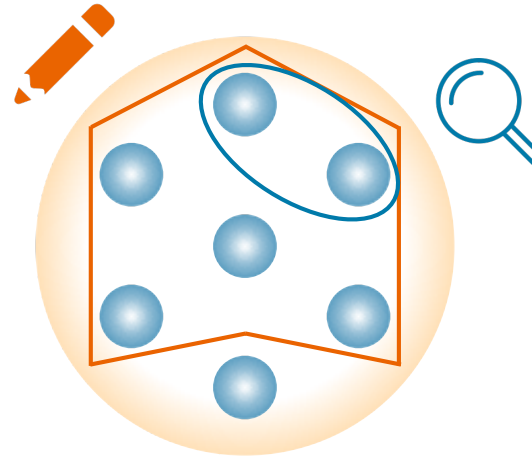
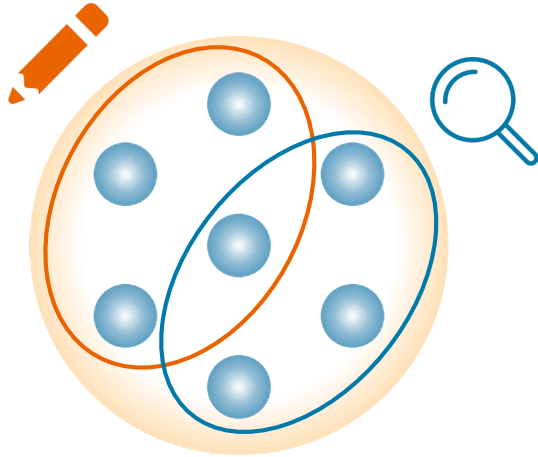


$$2 * |Q_w| > n$$

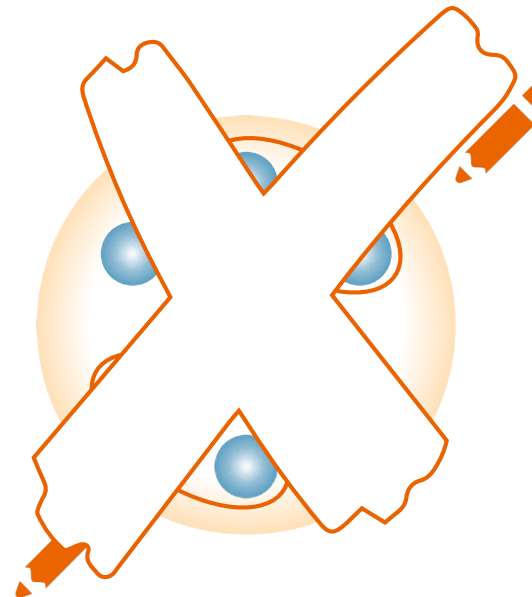
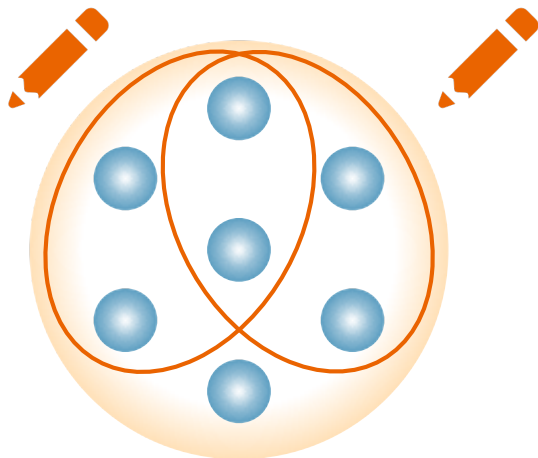
Data replication

Quorums

- Read and Write operations take Q_r and Q_w into account now



$$|Q_r| + |Q_w| > n$$



$$2 * |Q_w| > n$$

Data replication

Quorums

- Read and Write operations take Q_r and Q_w into account now
- Write operations now need to read from a Q_r

At client proxies

`read (value)`

`SetV = _read (x, v) from a Q_r`
`vmax = largest (_, v) from SetV`
`(value, vmax) from SetV`

`write (value)`

`SetV = _read (_, v) from a Q_r`
`vmax = largest (_, v) from SetV`
`_write (value, vmax+1) to a Q_w`

At replica i

`_read(value, version)`

`value = xi`
`version = vi`

`_write (value, version)`

`if version > vi then`
`xi = value`
`vi = version`

Data replication

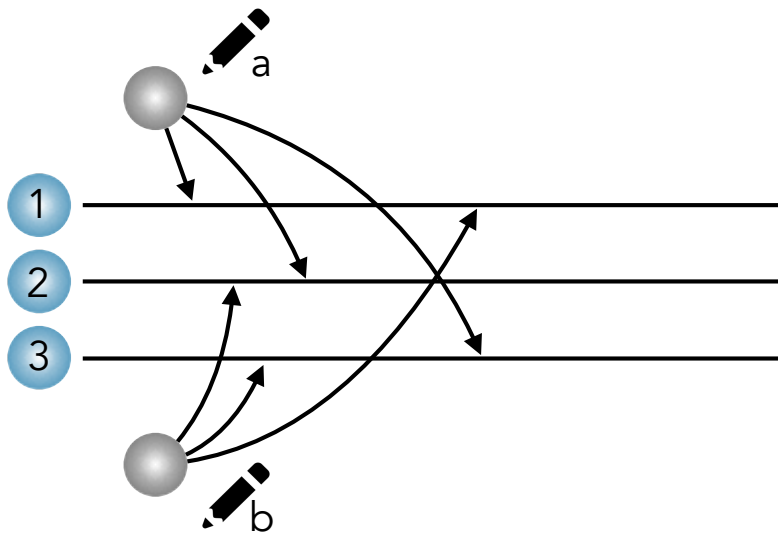
Quorums

- The use of quorums allows for trade-offs in several system aspects
- With omission faults fault tolerance can be maximised using strict majority quorums:
 - $|Q_r| = |Q_w| = \lceil (n + 1)/2 \rceil$
 - $|Q_w| = \lceil (n + 1)/2 \rceil$ also leads to the least expensive write operations
- $|Q_r|$ can determine workload bias; it determines the cost of reads and impacts the cost of writes
- For how it may impact throughput, latency, and network load see this chapter's reading material

Data replication

Order of writes

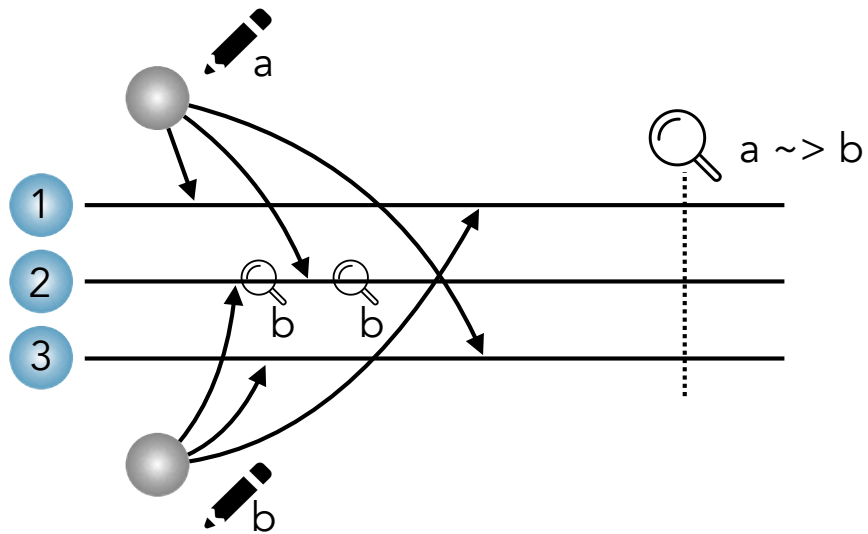
- Monotonic increasing versions + PID's



Data replication

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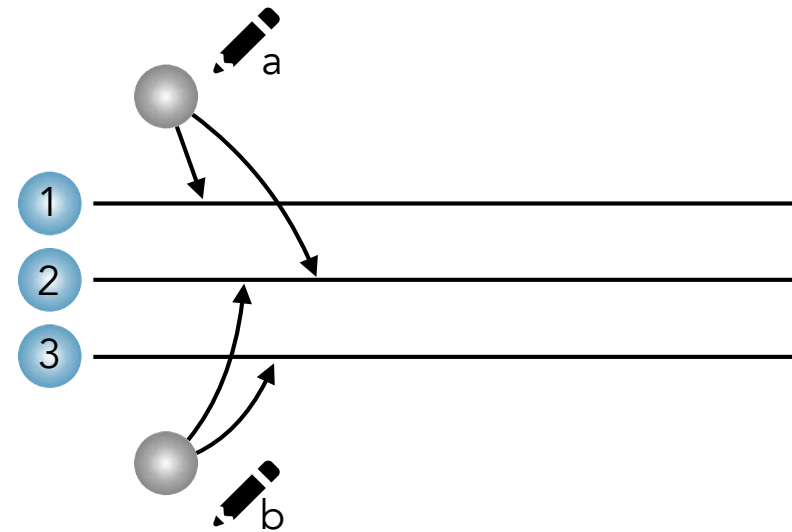
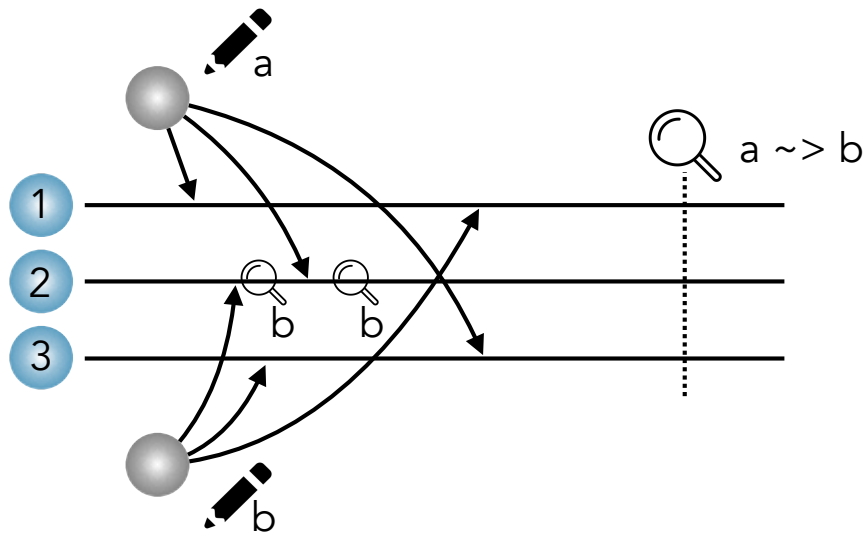
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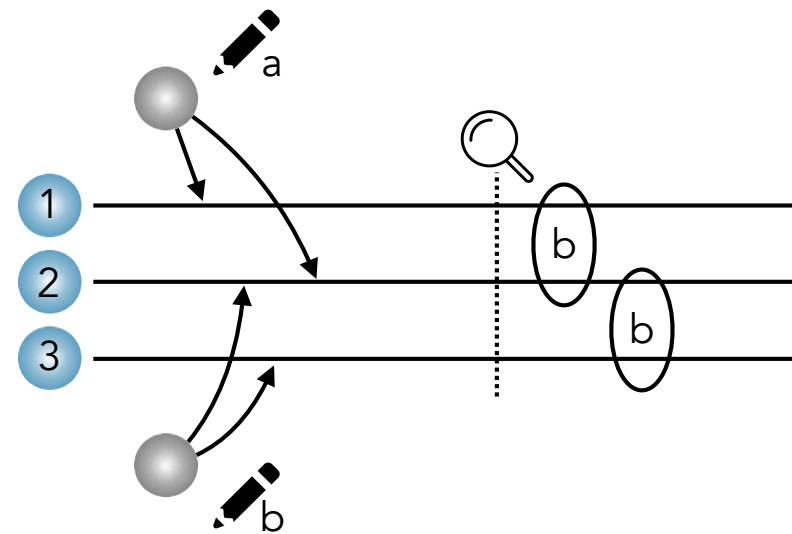
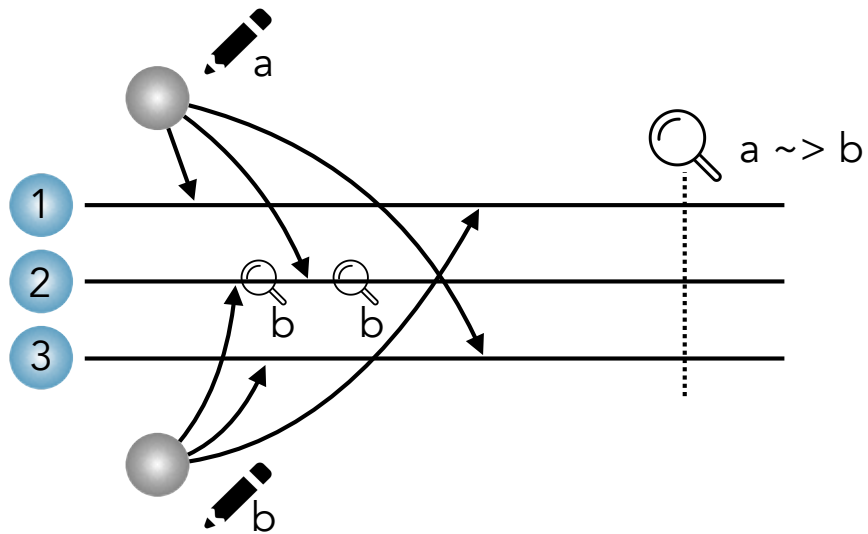
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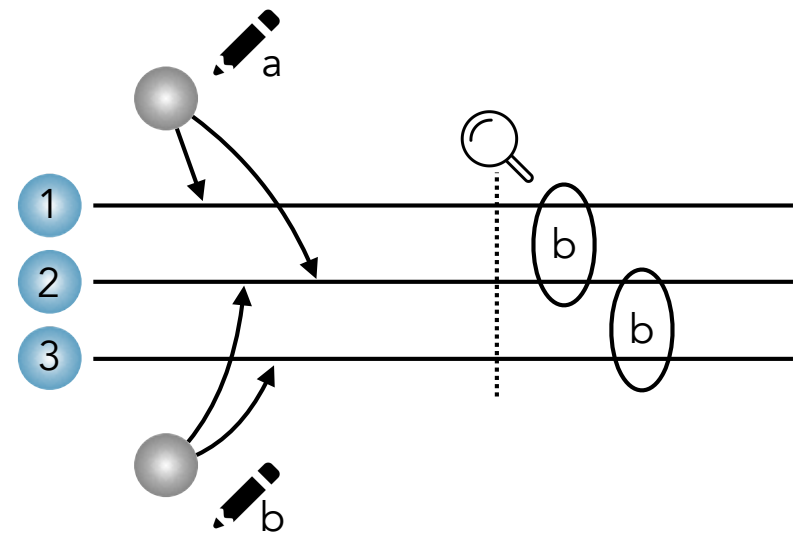
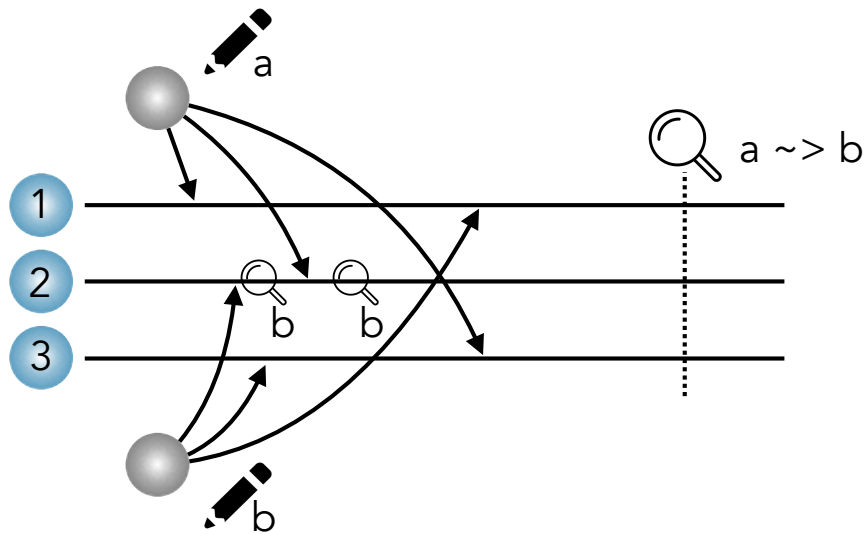
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Data replication

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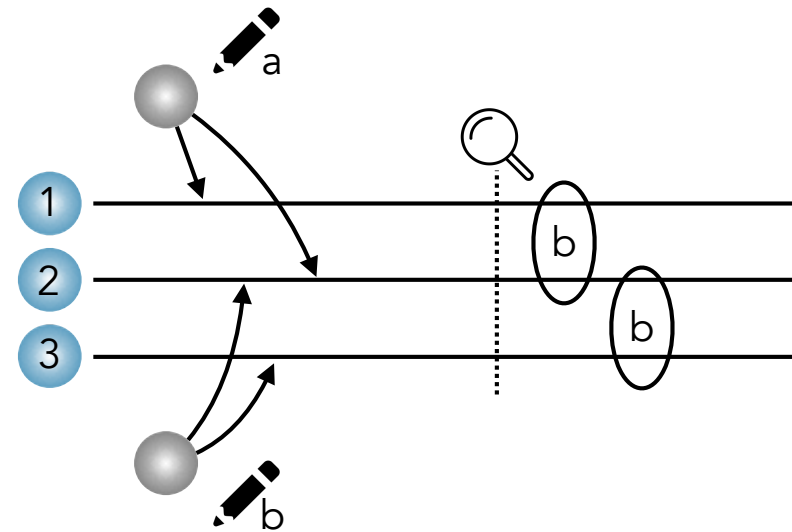
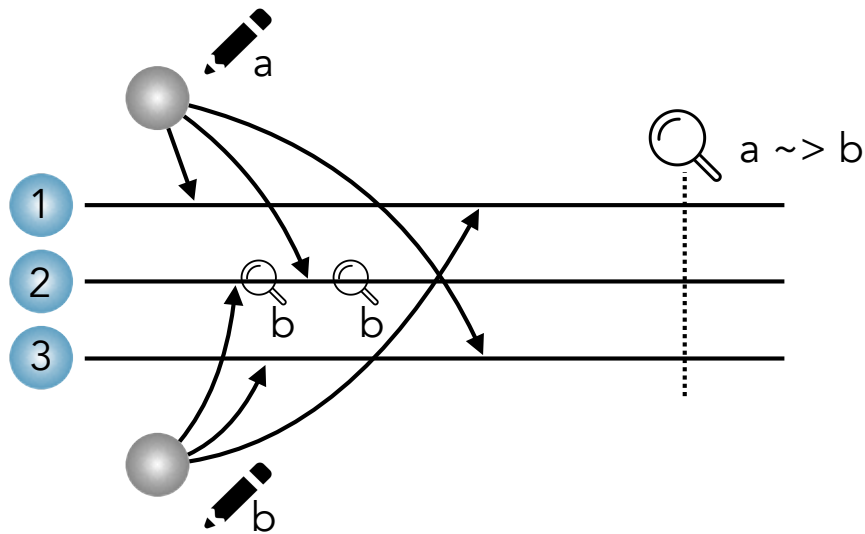


- Globally synchronised clocks

Data replication

Order of writes

- Monotonic increasing versions + PID's



- Globally synchronised clocks
- Causal ordering + PID's

Data replication

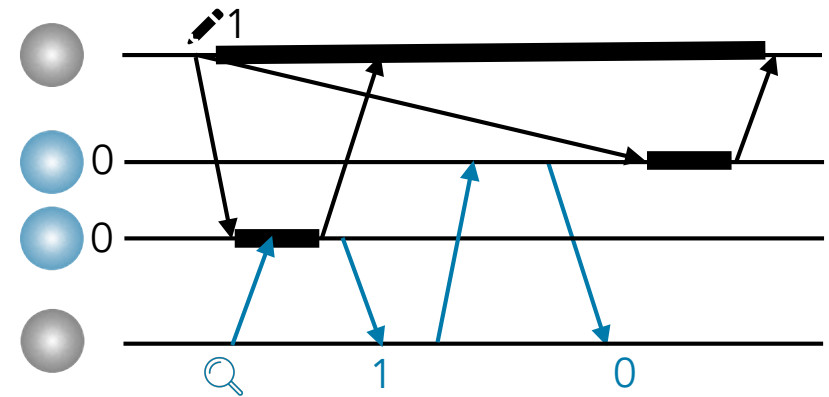
Concurrency control

- However, the lack of concurrency control of write operations may lead to basic semantics “inconsistencies”

Data replication

Concurrency control

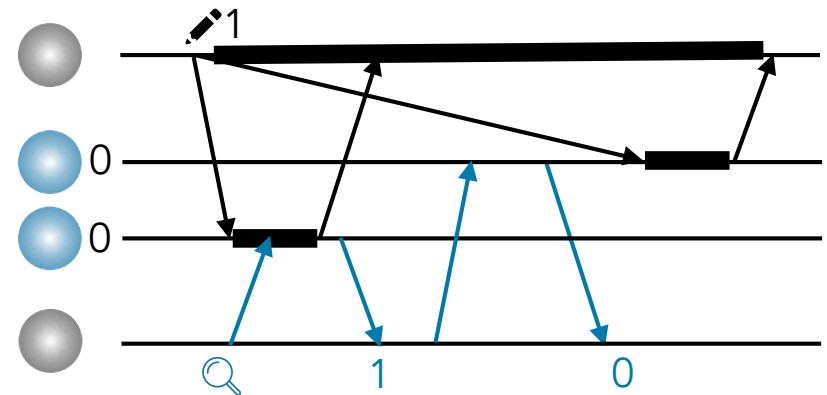
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 - Reading **within** a concurrent write may lead to **unexplainable** results



Data replication

Concurrency control

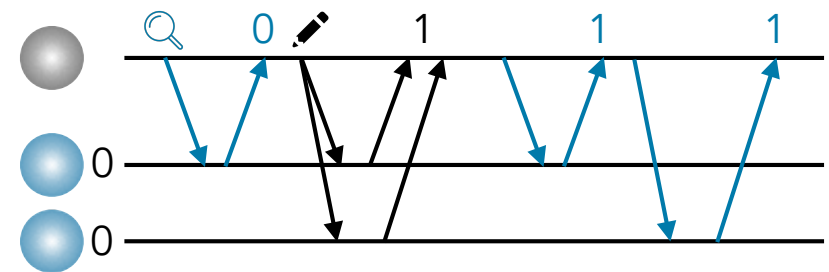
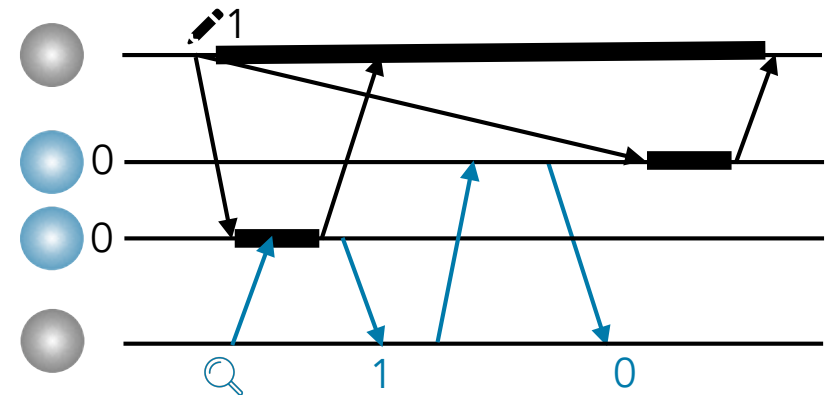
- ▶ However, the lack of concurrency control of write operations may lead to basic semantics “inconsistencies”
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Data replication

Concurrency control

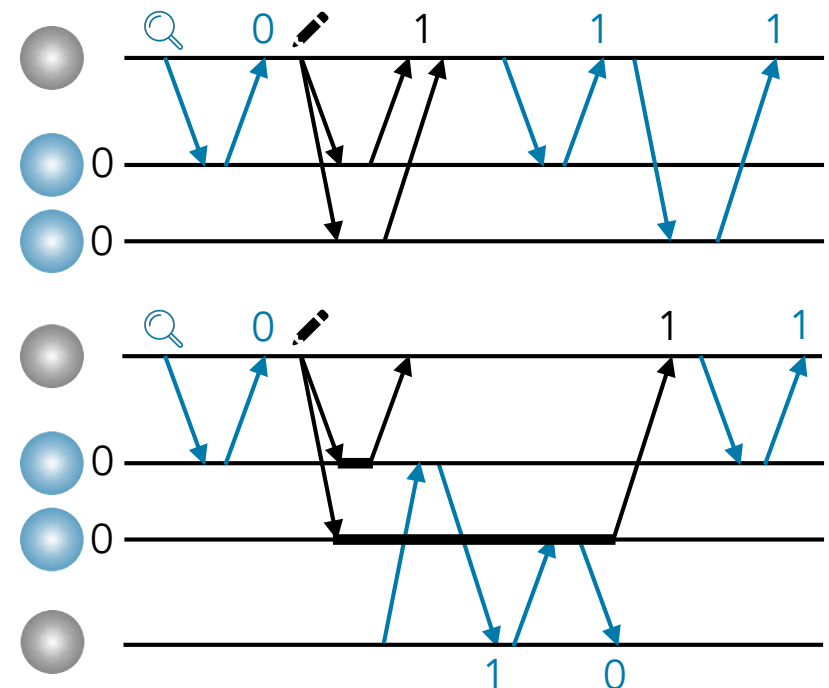
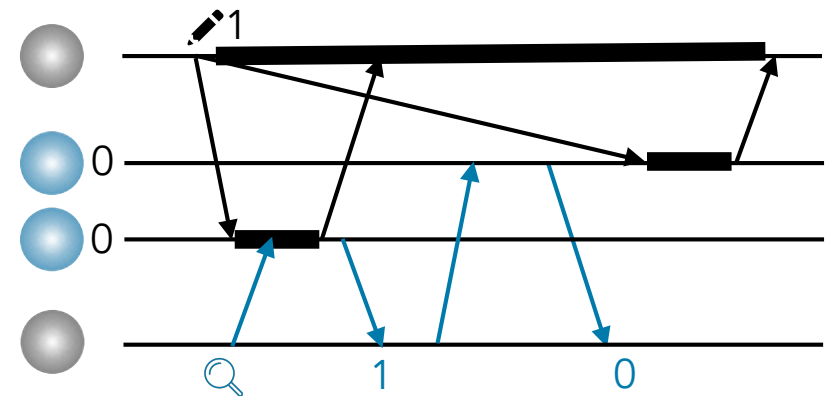
- ▶ However, the lack of concurrency control of write operations may lead to basic semantics “inconsistencies”
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 - ▶ One process (sequential) execution is OK



Data replication

Concurrency control

- ▶ However, the lack of concurrency control of write operations may lead to basic semantics “inconsistencies”
 - ▶ Reading **within** a concurrent write may lead to **unexplainable** results
- ▶ Consider an application that manages a non-decreasing variable
 - ▶ One process (sequential) execution is OK
 - ▶ A concurrent execution may easily violate the application semantics



Data replication

Locked quorums

- Read and Write operations take Q_r and Q_w into account now

At client proxies

```
read (value)
  SetL = _getlock() from a  $Q_r$ 
  if |SetL| == | $Q_r$ |
    SetV = _read (x, v) from a  $Q_r$ 
    vmax = largest (_, v) from SetV
    (value, vmax) from SetV
    res = OK
  else
    res = error
  _freelock() from SetL
  return res
```

```
write (value)
  SetL = _getlock() from a  $Q_w$ 
  if |SetL| == | $Q_w$ |
    SetV = _read (_, v) from a  $Q_r$ 
    vmax = largest (_, v) from SetV
    _write (value, vmax+1) to a  $Q_w$ 
    res = OK
  else
    res = error
  _freelock() from SetL
  return res
```

At replica i

```
_getlock()
  if lockedi == False
    lockedi = True
    return i
  else
    return error
```

```
_freelock()
  lockedi = False
```

```
_read(value, version)
  value = xi
  version = vi
```

```
_write (value, version)
  if version > vi then
    xi = value
    vi = version
```

Models of distributed systems and related faults

Reading material

- D. Gifford

“Weighted voting for replicated data”

SYMPOSIUM ON OPERATING SYSTEMS PRINCIPLES, 1979



- M. Whittaker, A. Charapko, J. Hellerstein, H. Howard, I. Stoica

“Read-Write Quorum Systems Made Practical”

PAPOC'21, 2021

