## CHAPTER-7 TRIANGLES

## EXERCISE 7.4

- 1. Find all the angles of an equilateral triangle.
- 2. The image of an object placed at a point A before a plane mirror LM is seen at the point B by an observer at D as shown in (1) Prove that the image is as far behind the mirror as the object is in front of the mirror.

[Hint: CN is normal to the mirror. Also, angle of incidence = angle of reflection].

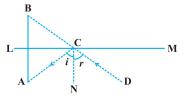


Figure 1

3. ABC is an isosceles triangle with AB = AC and D is a point on BC such that  $AD \perp BC$  (2). To prove that  $\angle BAD = \angle CAD$ , a student proceeded as follows: In  $\triangle ABD$  and  $\triangle ACD$ ,

$$AB = AC$$
 (Given)

$$\angle B = \angle C$$
 (because  $AB = AC$ ) (2)

and 
$$\angle ADB = \angle ADC$$
 (3)

$$\therefore \triangle ABD \cong \triangle ACD \tag{AAS}$$

So, 
$$\angle BAD = \angle CAD$$
 (CPCT) (5)

What is the defect in the above arguments?

[Hint: Recall how  $\angle B = \angle C$  is proved when AB = AC].

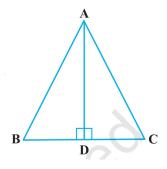


Figure 2

- 4. P is a point on the bisector of  $\angle ABC$ . If the line through P, parallel to BA meet BC at Q, prove that BPQ is an isosceles triangle.
- 5. ABCD is a quadrilateral in which AB = BC and AD = CD. Show that BD bisects both the angles ABC and ADC.

- 6. ABC is a right triangle with AB = AC. Bisector of  $\angle A$  meets BC at D. Prove that BC = 2AD
- 7. O is a point in the interior of a square ABCD such that OAB is an equilateral triangle. Show that  $\triangle OCD$  is an isosceles triangle.
- 8. ABC and DBC are two triangles on the same base BC such that A and D lie on the opposite sides of BC, AB = AC and DB = DC. Show that AD is the perpendicular bisector of BC.
- 9. ABC is an isosceles triangle in which AC = BC. AD and BE are respectively two altitudes to sides BC and AC. Prove that AE = BD.
- 10. Prove that sum of any two sides of a triangle is greater than twice the median with respect to the third side.
- 11. Show that in a quadrilateral ABCD,

$$AB + BC + CD + DA < (BD + AC) \tag{6}$$

12. Show that in a quadrilateral ABCD,

$$AB + BC + CD + DA > AC + BD \tag{7}$$

- 13. In a triangle ABC, D is the mid-point of side AC such that  $BD = \frac{1}{2}AC$ . Show that  $\angle ABC$  is a right angle.
- 14. In a right triangle, prove that the line-segment joining the mid-point of the hypotenuse to the opposite vertex is half the hypotenuse.
- 15. Two lines l and m intersect at the point O and P is a point on a line n passing through the point O such that P is equidistant from l and m. Prove that n is the bisector of the angle formed by l and m.
- 16. Line segment joining the mid-points M and N of parallel sides AB and DC, respectively of a trapezium ABCD is perpendicular to both the sides AB and DC. Prove that AD = BC.
- 17. ABCD is a quadrilateral such that diagonal AC bisects the angles A and C. Prove that AB = AD and CB = CD.
- 18. ABC is a right triangle such that AB = AC and bisector of angle C intersects the side AB at D. Prove that AC + AD = BC.
- 19. AB and CD are the smallest and largest sides of a quadrilateral ABCD. Out of  $\angle B$  and  $\angle D$  decide which is greater.
- 20. Prove that in a triangle, other than an equilateral triangle, angle opposite the longest side is greater than  $\frac{2}{3}$  of a right angle.
- 21. ABCD is quadrilateral such that AB = AD and CB = CD. Prove that AC is the perpendicular bisector of BD.