

9th MATHS
CHAPTER-7
TRIANGLES

EXERCISE 7.4

- Find all the angles of an equilateral triangle.
- The image of an object placed at a point A before a plane mirror LM is seen at the point B by an observer at D as shown in (1) Prove that the image is as far behind the mirror as the object is in front of the mirror.

[Hint: CN is normal to the mirror. Also, angle of incidence = angle of reflection].

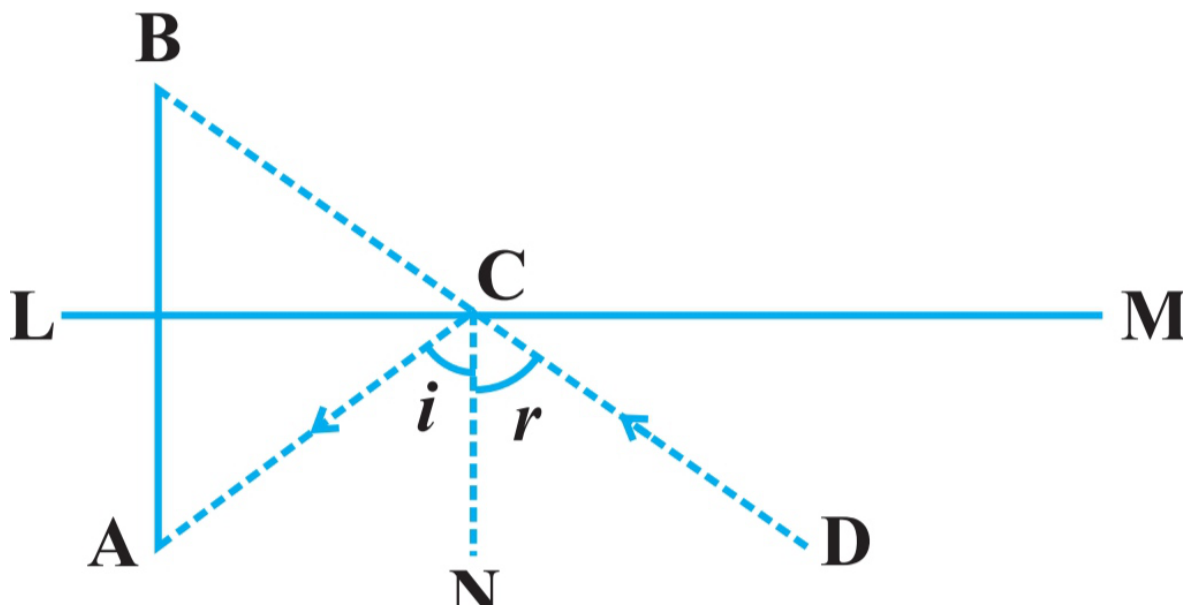


Figure 1

- ABC is an isosceles triangle with $AB = AC$ and D is a point on BC such that $AD \perp BC$ (2). To prove that $\angle BAD = \angle CAD$, a student proceeded as follows:
In $\triangle ABD$ and $\triangle ACD$,

$AB = AC$	(Given)	(1)
$\angle B = \angle C$	(because $AB = AC$)	(2)
and $\angle ADB = \angle ADC$		(3)
$\therefore \triangle ABD \cong \triangle ACD$	(AAS)	(4)
So, $\angle BAD = \angle CAD$	(CPCT)	(5)

What is the defect in the above arguments?

[Hint: Recall how $\angle B = \angle C$ is proved when $AB = AC$].

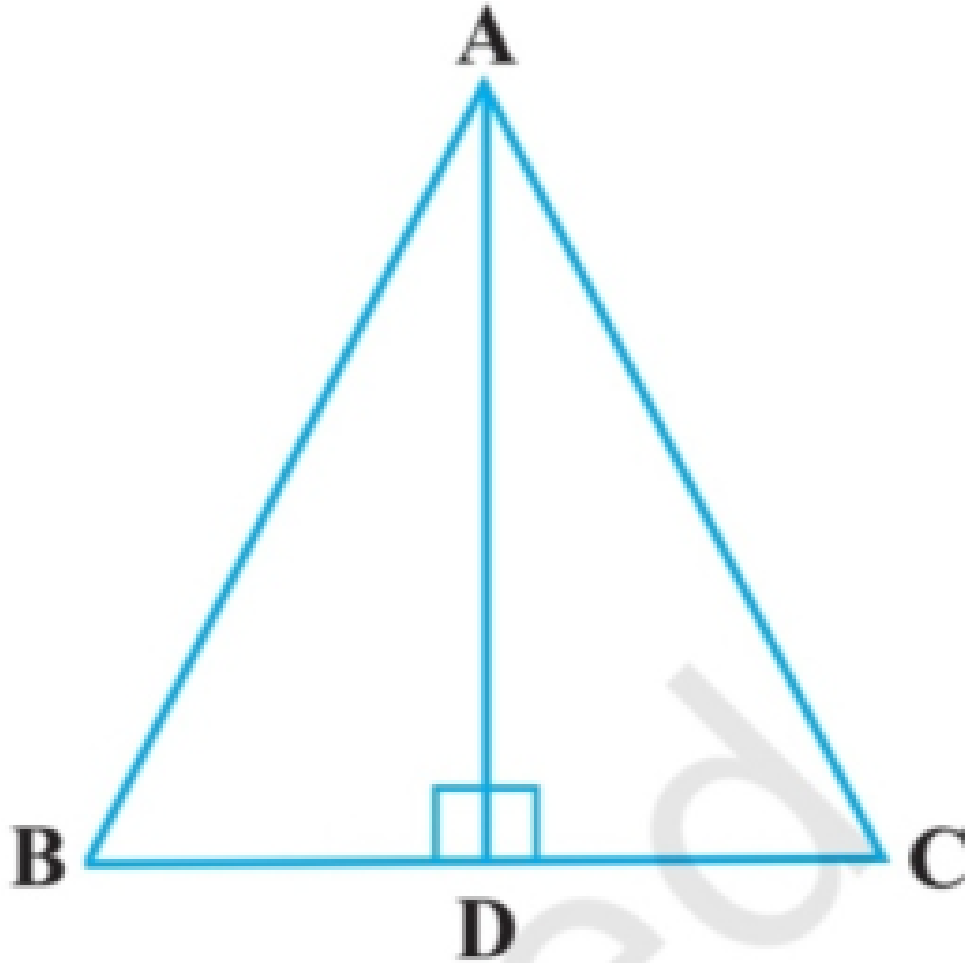


Figure 2

4. P is a point on the bisector of $\angle ABC$. If the line through P , parallel to BA meet BC at Q , prove that BPQ is an isosceles triangle.
5. $ABCD$ is a quadrilateral in which $AB = BC$ and $AD = CD$. Show that BD bisects both the angles ABC and ADC .
6. ABC is a right triangle with $AB = AC$. Bisector of $\angle A$ meets BC at D . Prove that $BC = 2AD$
7. O is a point in the interior of a square $ABCD$ such that OAB is an equilateral triangle. Show that $\triangle OCD$ is an isosceles triangle.
8. ABC and DBC are two triangles on the same base BC such that A and D lie on the opposite sides of BC , $AB = AC$ and $DB = DC$. Show that AD is the perpendicular bisector of BC .

9. ABC is an isosceles triangle in which $AC = BC$. AD and BE are respectively two altitudes to sides BC and AC . Prove that $AE = BD$.
10. Prove that sum of any two sides of a triangle is greater than twice the median with respect to the third side.
11. Show that in a quadrilateral $ABCD$,

$$AB + BC + CD + DA < (BD + AC) \quad (6)$$

12. Show that in a quadrilateral $ABCD$,

$$AB + BC + CD + DA > AC + BD \quad (7)$$

13. In a triangle ABC , D is the mid-point of side AC such that $BD = \frac{1}{2}AC$. Show that $\angle ABC$ is a right angle.
14. In a right triangle, prove that the line-segment joining the mid-point of the hypotenuse to the opposite vertex is half the hypotenuse.
15. Two lines l and m intersect at the point O and P is a point on a line n passing through the point O such that P is equidistant from l and m . Prove that n is the bisector of the angle formed by l and m .
16. Line segment joining the mid-points M and N of parallel sides AB and DC , respectively of a trapezium $ABCD$ is perpendicular to both the sides AB and DC . Prove that $AD = BC$.
17. $ABCD$ is a quadrilateral such that diagonal AC bisects the angles A and C . Prove that $AB = AD$ and $CB = CD$.
18. ABC is a right triangle such that $AB = AC$ and bisector of angle C intersects the side AB at D . Prove that $AC + AD = BC$.
19. AB and CD are the smallest and largest sides of a quadrilateral $ABCD$. Out of $\angle B$ and $\angle D$ decide which is greater.
20. Prove that in a triangle, other than an equilateral triangle, angle opposite the longest side is greater than $\frac{2}{3}$ of a right angle.
21. $ABCD$ is quadrilateral such that $AB = AD$ and $CB = CD$. Prove that AC is the perpendicular bisector of BD .