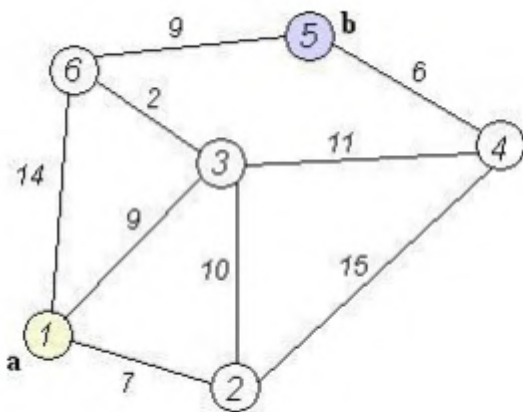


▼ Lab 2. Search

Task 2.1 Route Planning

Problem Descriptions

The image depicts a map where there are 6 cities, numbered from 1 to 6, and each is a node on the route. The distances between them, if connected directly, are shown on the edges in the graph. This task consists of finding the shortest route to city number five from city one.



To be able to solve the problem, we first need to define the required variables.

STATE: each city corresponds to a number between one and six as illustrated in the image.

ACTION: the action is the destination city to which we are moving, starting from the current state, which is the city where we are. For example, if we are currently in city 3 and the next city we are moving to is 6, the action will be 6.

GOAL TEST: it consists of verifying whether the current state is indeed the final destination, to understand if the goal has been reached. In this task the goal is city 5.

PATH COST: the cost of the route is indicated in the illustration. For implementation we create a 6x6 array, where each element is the distance between a pair of cities (0 for self-position and '#' for any unconnected cities).

Implementation and Results

```
1 !pip install simpleai
2 from simpleai.search import SearchProblem, astar, greedy, breadth_first, depth_first, uniform_cost
3 import math
```

```
1 COSTS = [
2     [0, 7, 9, 'inf', 'inf', 14],
```

```

3  [7, 0, 10, 15, 'inf', 'inf'],
4  [9, 10, 0, 11, 'inf', 2],
5  ['inf', 15, 11, 0, 6, 'inf'],
6  ['inf', 'inf', 'inf', 6, 0, 9],
7  [14, 'inf', 2, 'inf', 9, 0]
8 ]
9

```

```

1  class Route(SearchProblem):
2
3      # initialise with the initial and goal states. Do "-1" because the nodes start from 1.
4      def __init__(self, initial, goal):
5          self.initial = initial-1
6          self.goal = goal-1
7          super(Route, self).__init__(initial_state=self.initial)
8
9      # add all connected nodes, i.e. those with a cost of not 0 or inf
10     def actions(self, state):
11         actions = []
12         for action in range(len(COSTS[state])):
13             if COSTS[state][action] not in ['inf', 0]:
14                 actions.append(action)
15         return actions
16
17     # the result state is just the action as defined
18     def result(self, state, action):
19         return action
20
21     # check if goal is reached
22     def is_goal(self, state):
23         return state == self.goal
24
25     # return the cost between two states
26     def cost(self, state, action, state2):
27         return COSTS[state][action]
28

```

```

1  problem = Route(1, 5)
2  # result = breadth_first(problem, graph_search=True)
3  # result = depth_first(problem, graph_search=True)
4  result = uniform_cost(problem)
5
6  # Print the results
7  path = [x[1]+1 for x in result.path()]
8  print("The route is %s, and total cost is %s" %(path, result.cost))

```

The route is [1, 3, 6, 5], and total cost is 20

Discussions

In this task, three different search methods were compared, namely breadth-first search, depth-first search and uniform-cost search. Comparing the results obtained, it emerges that the

Breadth-first search and Depth-first search methods both give the solution 23, while Uniform-cost search has the solution 20. This means that Uniform-cost search gave us the optimal solution, which is the shortest solution.

▾ Lab 2. Search

Task 2.2 8-Puzzle Problem

Problem Descriptions

Implement a programme that solves the 8-puzzle problem, which can be described as follows: there are 8 numbered tiles and one empty tile in a 3x3 grid. The boxes are randomly shuffled, so the goal is to reorder them by ending with the empty one at the first position. The goal is also to reach the final result with the least number of moves.

In order to solve the problem, the required variables must first be defined:

STATE: the state of a numbered tile is the position of the tile in a 3x3 array in which there are the numbers 1 to 8 and the empty tile is indicated by 'E'. This is represented with a string containing dashes so that we can know the conformation of the puzzle at each given state.

ACTION: To make the implementation easier, we use the movement of the empty tile as the action, instead of the numbered ones. Since there are four possible movements (up, down, left, right), we need to check the boundary conditions to see which one is valid in the state we are in.

GOAL TEST: check if the current state is the goal state, i.e. "E-1-2-3-4-5-6-7-8".

PATH COST: Since cost is the number of moves used to solve the problem, the cost of one move will correspond to each step.

Implementation and Results

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2 from simpleai.search import SearchProblem, astar, greedy, breadth_first, depth_first
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```

5 # Convert string to list
6 def string_to_list(input_string):
7     return [x.split('-') for x in input_string.split('\n')]
8
9 # Find the 2D location of the input element
10 def get_location(rows, input_element):
11     for i, row in enumerate(rows):
12         for j, item in enumerate(row):
13             if item == input_element:
14                 return i, j
15
16 # Final result that we want to achieve
17 GOAL = "\
18 E-1-2
19 3-4-5
20 6-7-8"
21
22 # Starting point - solution depth = 26
23 # INITIAL = "\
24 7-2-4
25 5-E-6
26 8-3-1"
27
28 # Starting point - solution depth = 8
29 INITIAL = "\
30 1-4-2
31 5-E-8
32 3-6-7"
33
34 # Starting point - solution depth = 4
35 # INITIAL = "\
36 1-4-2
37 3-5-8
38 6-7-E"
39
40 # Create a cache for the goal position of each piece
41 goal_positions = {}
42 rows_goal = string_to_list(GOAL)
43 for number in '12345678E':
44     goal_positions[number] = get_location(rows_goal, number)
45
46 # Create the A* solver object
47 result = astar(PuzzleSolver(INITIAL))
48 # result = greedy(PuzzleSolver(INITIAL))
49 # result = breadth_first(PuzzleSolver(INITIAL))
50 # result = depth_first(PuzzleSolver(INITIAL))
51
52 # Print the results
53 for i, (action, state) in enumerate(result.path()):
54     print()
55     if action == None:
56         print('Initial configuration')
57     else:
58         print('Step %s: After moving %s into the empty space' %(i, action))
59     print(state)
60 print('Goal achieved!')

```

Initial configuration

1-4-2
5-E-8
3-6-7

Step 1: After moving 5 into the empty space

1-4-2
E-5-8
3-6-7

Step 2: After moving 3 into the empty space

1-4-2
3-5-8
E-6-7

Step 3: After moving 6 into the empty space

1-4-2
3-5-8
6-E-7

Step 4: After moving 7 into the empty space

1-4-2
3-5-8
6-7-E

Step 5: After moving 8 into the empty space

1-4-2

3-5-E
6-7-8

Step 6: After moving 5 into the empty space
1-4-2
3-E-5
6-7-8

Step 7: After moving 4 into the empty space
1-E-2
3-4-5
6-7-8

Step 8: After moving 1 into the empty space
E-1-2
3-4-5
6-7-8
Goal achieved!

Discussions

Simple case

In this task, we considered the simple case '1-4-2-3-5-8-6-7-E'. Using the A*, greedy and breadth-first search methods, we obtained a solution with a cost of 4 moves, instead the depth-first search method gives us a runtime error.

Using heuristics with the number of misplaced tiles, the A* search gave us a run time of 0.000246s, the greedy 0.000192s and breath-first search 0.000724s. So we can draw the conclusion that the greedy method is the fastest, and the breath-first the slowest.

Using instead a heuristic value for the sum of the distances of the tiles from their correct positions, we obtain a runtime of 0.000290s for A* search, 0.000314s for greedy search and 0.000714s for breath-first search. In this case we can conclude that A* gave the fastest solution and again breadth-first is the one with the highest runtime.

Difficult case

This task consists of implementing the A* method and greedy search starting with the case '7-2-4-5-E-6-8-3-1'.

Following the same approach as in the previous case and using heuristics for the numbers of misplaced tiles, both search methods give us a run time error.

Using the heuristic for the sum of the distances of the tiles from their target position, the A* method gives a run time of 22.5s, with 26 moves taken, while the greedy search still gives us an error.

Run time errors occurred because the nodes generated in the search were too excessive to be controlled and the calculation became too heavy for the memory and thus the RAM. Or the wrong heuristic values were used, which made it too difficult to solve the problem.

▾ Lab 2. Search

Task 2.3 Maze Solver

Problem Descriptions

What the algorithm has to solve is the delineation of a route that can take a person from a starting position to a given destination. Within the map, the starting position is represented by 'O' and each movement is indicated by 'x'. All obstacles that must then be avoided will be illustrated with "#". To start with, we define the state, action, goal test and path cost.

STATE: is the position on the map indicated by the x and y co-ordinates.

ACTION: is the movement that takes the person towards the destination. Possible movements are UP, DOWN, RIGHT, LEFT always considering obstacles close to the current state. To define diagonal movements for extended searches we can also use the commands LEFT UP, LEFT DOWN, RIGHT UP or RIGHT DOWN.

GOAL TEST: checks whether the co-ordinates of the destination point correspond with those of the current state.

PATH COST: The cost assigned to each movement is 1, but for diagonal movements in extended search, it is 1.4.

Implementation and Results

```
1 !pip install simpleai
2 from simpleai.search import SearchProblem, astar, greedy, breadth_first, depth_first, uniform_cost
3 import math
```

Requirement already satisfied: simpleai in /usr/local/lib/python3.6/dist-packages (0.8.2)

```
1 MAP = ""
2 #####
3 # # # #
4 ##### # #
5 # o # # #
6 # ### ##### #
7 # ##### # #
8 # # # # #####
9 # ##### # # x #
10 # # # #
11 #####
12 ""
13 MAP = [list(x) for x in MAP.split("\n") if x]
14
15 COSTS = {
16     "up": 1.0,
17     "down": 1.0,
18     "left": 1.0,
19     "right": 1.0,
20     # "up left": 1.4,
21     # "up right": 1.4,
22     # "down left": 1.4,
23     # "down right": 1.4,
24 }
25
```

```
1
2 class Maze(SearchProblem):
3
4     def __init__(self, board):
5         self.board = board
6         self.goal = (0, 0)
7         for y in range(len(self.board)):
8             for x in range(len(self.board[y])):
9                 if self.board[y][x].lower() == "o":
10                     self.initial = (x, y)
11                 elif self.board[y][x].lower() == "x":
12                     self.goal = (x, y)
13
14         super(Maze, self).__init__(initial_state=self.initial)
15
16     def actions(self, state):
17         actions = []
18         for action in list(COSTS.keys()):
19             newx, newy = self.result(state, action)
20             if self.board[newy][newx] != "#":
21                 actions.append(action)
```

```

22     return actions
23
24     def result(self, state, action):
25         x, y = state
26
27         if action.count("up"):
28             y -= 1
29         if action.count("down"):
30             y += 1
31         if action.count("left"):
32             x -= 1
33         if action.count("right"):
34             x += 1
35
36         new_state = (x, y)
37         return new_state
38
39     def is_goal(self, state):
40         return state == self.goal
41
42     def cost(self, state, action, state2):
43         return COSTS[action]
44
45     def heuristic(self, state):
46         x, y = state
47         gx, gy = self.goal
48         return math.sqrt((x - gx) ** 2 + (y - gy) ** 2)

```



```

1 problem = Maze(MAP)
2 result = astar(problem, graph_search=True)
3 # result = greedy(problem, graph_search=True)
4 # result = breadth_first(problem, graph_search=True)
5 # result = depth_first(problem, graph_search=True)
6 # result = uniform_cost(problem, graph_search=True)
7
8 path = [x[1] for x in result.path()]
9 for y in range(len(MAP)):
10     for x in range(len(MAP[y])):
11         print('.' if (x,y) in path[1:-1] else MAP[y][x], end=" ")
12     print()
13 print("A* Search: moves=%s, cost=%s." %(result.depth, result.cost))

```



```

#####
#   #   #
#####   #####   #   #
# o.# # ..... #   #
# .### ....#### .##### #
# .....#### .#   #
#   # # .# ##### #
# ##### # .....#x #
#   # # ... #
#####
A* Search: moves=33, cost=33.0.

```

Discussions

In this task, we could consider the direct distance between the current position and the target as a heuristic function. This distance can be calculated using the Pythagorean theorem.

The first method used for solving the task was Asearch, which gave a cost result of 33, also taking 33 moves. It is interesting to see how using the other methods all give us the exact same result, both in terms of cost and number of moves, but the calculated paths to the destination are different. However, if more obstacles were added in different positions, the A search would be the method that would still give us an optimal result.

If we consider the case where diagonal moves are added, in contrast, the values obtained earlier are reduced from 33 moves to 23, and from 33 to 26.93 in cost. Furthermore, if we use the breadth-first and uniform-cost methods, we obtain the same results. With the greedy search, on the other hand, the cost is 26.96, with the same number of moves, while with the depth-first search it gives us a higher number of moves, i.e. 38, and also a higher cost, of 49.597. The increase in cost and moves in the depth-first search is due to the fact that the algorithm had to go back after exploring all the nodes all the way through. Concluding, we can select the A* search as the optimal method over the others.

▼ Lab 3. Genetic Algorithms

Task 3.1 The Travelling Salesman Problem

Problem Descriptions

The problem is based on a salesman who has to visit a number of cities, 17 in this case, and has to find the best route in order to minimise the total distance of the travel and passing through each of the cities. To solve the problem, we know the distance between the various cities. The optimal solution for this problem would be:

OptTour = [0, 15, 11, 8, 4, 1, 9, 10, 2, 14, 13, 16, 5, 7, 6, 12, 3]

OptDistance = 2085

For the implementation of a genetic algorithm, it is necessary to define the encoding scheme, fitness function and genetic operators.

ENCODING SCHEME: We use symbolic encoding, i.e. the permutation of the 17 numbers representing the cities.

FITNESS FUNCTION: it is the sum of the distances between the cities that are neighbouring, also considering the distance between the last city and the first as the seller has to complete the round.

GENETIC OPERATORS: as a selection method we can use tournament selection, e.g. selecting the best three chromosomes. For crossover we can randomly choose a city within a string so that the next bits are swapped with another parent. However, we must consider maintaining string validity, i.e. all cities can only be present once. For mutation, it is sufficient to exchange two cities within the same string.

Implementation and Results

```
1 TourSize = 17
2 OptTour = [0, 15, 11, 8, 4, 1, 9, 10, 2, 14, 13, 16, 5, 7, 6, 12, 3],
3 OptDistance = 2085
4 distance_map = \
5     [[0, 633, 257, 91, 412, 150, 80, 134, 259, 505, 353, 324, 70, 211, 268, 246, 121],
6      [633, 0, 390, 661, 227, 488, 572, 530, 555, 289, 282, 638, 567, 466, 420, 745, 518],
7      [257, 390, 0, 228, 169, 112, 196, 154, 372, 262, 110, 437, 191, 74, 53, 472, 142],
8      [91, 661, 228, 0, 383, 120, 77, 105, 175, 476, 324, 240, 27, 182, 239, 237, 84],
9      [412, 227, 169, 383, 0, 267, 351, 309, 338, 196, 61, 421, 346, 243, 199, 528, 297],
10     [150, 488, 112, 120, 267, 0, 63, 34, 264, 360, 208, 329, 83, 105, 123, 364, 35],
11     [80, 572, 196, 77, 351, 63, 0, 29, 232, 444, 292, 297, 47, 150, 207, 332, 29],
12     [134, 530, 154, 105, 309, 34, 29, 0, 249, 402, 250, 314, 68, 108, 165, 349, 36],
13     [259, 555, 372, 175, 338, 264, 232, 249, 0, 495, 352, 95, 189, 326, 383, 202, 236],
```

```

14 [505, 289, 262, 476, 196, 360, 444, 402, 495, 0, 154, 578, 439, 336, 240, 685, 390],
15 [353, 282, 110, 324, 61, 208, 292, 250, 352, 154, 0, 435, 287, 184, 140, 542, 238],
16 [324, 638, 437, 240, 421, 329, 297, 314, 95, 578, 435, 0, 254, 391, 448, 157, 301],
17 [70, 567, 191, 27, 346, 83, 47, 68, 189, 439, 287, 254, 0, 145, 202, 289, 55],
18 [211, 466, 74, 182, 243, 105, 150, 108, 326, 336, 184, 391, 145, 0, 57, 426, 96],
19 [268, 420, 53, 239, 199, 123, 207, 165, 383, 240, 140, 448, 202, 57, 0, 483, 153],
20 [246, 745, 472, 237, 528, 364, 332, 349, 202, 685, 542, 157, 289, 426, 483, 0, 336],
21 [121, 518, 142, 84, 297, 35, 29, 36, 236, 390, 238, 301, 55, 96, 153, 336, 0]]

```

```

1 !pip install deap
2 import array
3 import random
4 import numpy as np
5 from deap import algorithms, base, creator, tools

```

```

1 # fitness function as the sum of all the distances between each consecutive cities in individual
2 def evalTSP(individual):
3     distance = distance_map[individual[-1]][individual[0]]
4     for gene1, gene2 in zip(individual[0:-1], individual[1:]):
5         distance += distance_map[gene1][gene2]
6     return distance,
7
8 # create creator.FitnessMin and creator.Individual to be used in the toolbox
9 creator.create("FitnessMin", base.Fitness, weights=(-1.0,))
10 creator.create("Individual", array.array, typecode='i', fitness=creator.FitnessMin)
11
12 # create the toolbox from the base
13 toolbox = base.Toolbox()
14
15 # add attribute generator to the toolbox
16 toolbox.register("indices", random.sample, range(TourSize), TourSize)
17
18 # initializers for individuals and population
19 toolbox.register("individual", tools.initIterate, creator.Individual, toolbox.indices)
20 toolbox.register("population", tools.initRepeat, list, toolbox.individual)
21
22 # genetic operators and fitness function
23 toolbox.register("mate", tools.cxPartiallyMatched)
24 toolbox.register("mutate", tools.mutShuffleIndexes, indpb=0.05)
25 # toolbox.register("select", tools.selRoulette)
26 toolbox.register("select", tools.selTournament, tournsize=3)
27 toolbox.register("evaluate", evalTSP)
28

```

```

1 random.seed(16)
2 pop = toolbox.population(n=500)
3 stats = tools.Statistics(lambda ind: ind.fitness.values)
4 stats.register("min", np.min)
5 algorithms.eaSimple(pop, toolbox, 0.7, 0.2, ngen=50, stats=stats)
6 # algorithms.eaSimple(pop, toolbox, 0.7, 0.2, ngen=50, stats=stats, verbose=False)
7
8 best = tools.selBest(pop, 1)[0]

```

```
9 print("Best: %s\nTotal Distance: %s" %(best.tolist(), best.fitness.values))
```

```
10 gen nevals min
0 500 3369
1 395 3307
2 384 3261
3 386 3269
4 402 2938
5 371 2938
6 372 2697
7 361 2671
8 388 2671
9 377 2671
10 391 2487
11 348 2487
12 379 2487
13 386 2521
14 357 2521
15 366 2481
16 358 2481
17 390 2336
18 376 2457
19 402 2373
20 366 2373
21 360 2373
22 375 2278
23 388 2278
24 385 2199
25 396 2176
26 367 2176
27 382 2142
28 368 2175
29 367 2128
30 366 2115
31 376 2115
32 389 2088
33 374 2088
34 381 2088
35 380 2085
36 377 2085
37 383 2085
38 380 2085
39 418 2085
40 380 2085
41 367 2085
42 352 2085
43 364 2085
44 388 2085
45 373 2085
46 393 2085
47 388 2085
48 377 2085
49 375 2085
50 379 2085
```

```
Best: [1, 9, 10, 2, 14, 13, 16, 5, 7, 6, 12, 3, 0, 15, 11, 8, 4]
```

```
Total Distance: (2085.0,)
```

Discussions

Looking at the final output, we can see that the solution was found after 50 generations, with a total distance of 2085. This is equivalent to the optimal distance of the solution described at the beginning, although the sequence of cities is not the same, probably because there is more than one combination that leads to the same result.

▼ Lab 3. Genetic Algorithms

Task 3.2 The 8-Queens Problem

Problem Descriptions

The 8-queens problem is based on placing 8 queens on the chessboard so that they cannot attack each other; to do this, there cannot be more than one piece on the same row, column or diagonal. First we define the encoding scheme, fitness value and genetic operators.

ENCODING SCHEME: We can consider three encoding schemes in this problem. In the first we do not set any of the three constraints (row, column or diagonal), so the algorithm will do all the work.

In the second encoding scheme we consider the 8 queens placed in different columns, in order from 0 to 7, and in this way we already satisfy one constraint. Since we may end up with numbers of equal values in the list as they are randomly generated, it will leave the genetic algorithm to enforce the row and diagonal constraints.

Scheme 3 applies both the column constraint (as scheme 2) and the row constraint, so the genetic algorithm only needs to satisfy the diagonal constraint.

FITNESS FUNCTION: as a fitness function we can consider the number of queens attacking each other, and so the algorithm will have to minimise this outcome by choosing the individuals with the smallest number, up to 0. Using encoding scheme 3, we need only worry about the queens on the diagonals, and since in an 8x8 chessboard there are 15 falling diagonals and 15 raising diagonals, we can use two lists of size 15 to store the number of attacking queens. In the 8x8 chessboard, we have 15 ($8 \times 2 - 1 = 15$) falling diagonals and 15 raising diagonals. So we can use two lists of size 15 to store the number of attacking queens. For a queen located at (x, y) , the index to the falling diagonal is $x+y$, and that to the raising diagonal is $x-y+7$.

GENETIC OPERATORS: Since it is a minimisation problem as the solution is found when no queen attacks another, we can use tournament selection as the selection method. We can apply crossover by swapping two parts of two chromosomes, which means swapping the positions of some queens in two different settings of the chessboard. We must always respect the constraints imposed earlier, i.e. we must apply the crossover without having two queens on the same row or column. For the mutation we will instead have to switch two queens within the same individual.

Implementation and Results

```
1 !pip install deap
2 import random
```

```

3 import numpy as np
4 from deap import algorithms, base, creator, tools
5
1 NB_QUEENS = 8
2 #NB_QUEENS = 12
3 def evalNQueens(individual):
4
5     # create 2 list for the falling diagonal (fd) and the raising diagonal (rd)
6     fd = np.zeros(2*NB_QUEENS-1)
7     rd = np.zeros(2*NB_QUEENS-1)
8
9     # count the number of queens placed on diagonals fd/rd
10    for i in range(NB_QUEENS):
11        fd[i+individual[i]] += 1
12        rd[NB_QUEENS-1-i+individual[i]] += 1
13
14    # sum the number of queens if more than 1 queen on a diagonal
15    return np.sum(fd[fd>1]) + np.sum(rd[rd>1]),
16
1 # enforce only 1 queen per column by using a list of NB_QUEENS
2 creator.create("FitnessMin", base.Fitness, weights=(-1.0,))
3 creator.create("Individual", list, fitness=creator.FitnessMin)
4
5 # enforce only 1 queen per row by using permutation
6 toolbox = base.Toolbox()
7 toolbox.register("permutation", random.sample, range(NB_QUEENS), NB_QUEENS)
8
9 # register all elements of the GA
10 toolbox.register("individual", tools.initIterate, creator.Individual, toolbox.permutation)
11 toolbox.register("population", tools.initRepeat, list, toolbox.individual)
12 toolbox.register("evaluate", evalNQueens)
13 toolbox.register("mate", tools.cxPartiallyMatched)
14 toolbox.register("mutate", tools.mutShuffleIndexes, indpb=2.0/NB_QUEENS)
15 toolbox.register("select", tools.selTournament, tournsize=3)
1
1 # run the GA to get the result
2 random.seed(64)
3 pop = toolbox.population(n=300)
4 algorithms.eaSimple(pop, toolbox, cxpb=0.5, mutpb=0.2, ngen=50, verbose=False)
5 best = tools.selBest(pop, 1)[0]
6 print("Best: %s. Fitness value: %s" %(best, best.fitness.values[0]))
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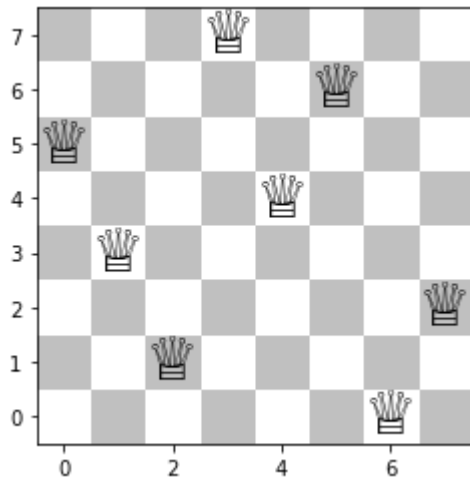
```

Best: [5, 3, 1, 7, 4, 6, 0, 2]. Fitness value: 0.0

```

7 plt.imshow(chessboard, cmap='gray', origin='lower', vmin=0, vmax=1)
8 for x in range(NB_QUEENS):
9     plt.text(x, best[x], '♚', fontsize=30, ha='center', va='center')

```



```

1 # run the GA to get the result
2 random.seed(64)
3 pop = toolbox.population(n=300)
4 algorithms.eaSimple(pop, toolbox, cxpb=0.5, mutpb=0.2, ngen=50, verbose=False)
5 best = tools.selBest(pop, 1)[0]
6 print("Best: %s. Fitness value: %s" %(best, best.fitness.values[0]))

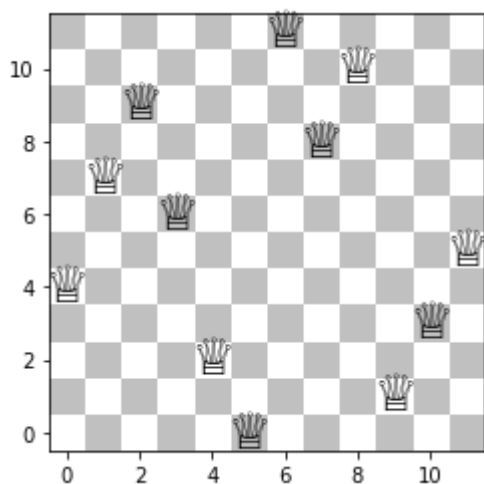
```

Best: [4, 7, 9, 6, 2, 0, 11, 8, 10, 1, 3, 5]. Fitness value: 0.0

```

1 # display the result
2 import matplotlib.pyplot as plt
3
4 chessboard = np.ones((NB_QUEENS, NB_QUEENS))
5 chessboard[1::2,0::2] = 0.75
6 chessboard[0::2,1::2] = 0.75
7 plt.imshow(chessboard, cmap='gray', origin='lower', vmin=0, vmax=1)
8 for x in range(NB_QUEENS):
9     plt.text(x, best[x], '♚', fontsize=25, ha='center', va='center')

```



Discussions

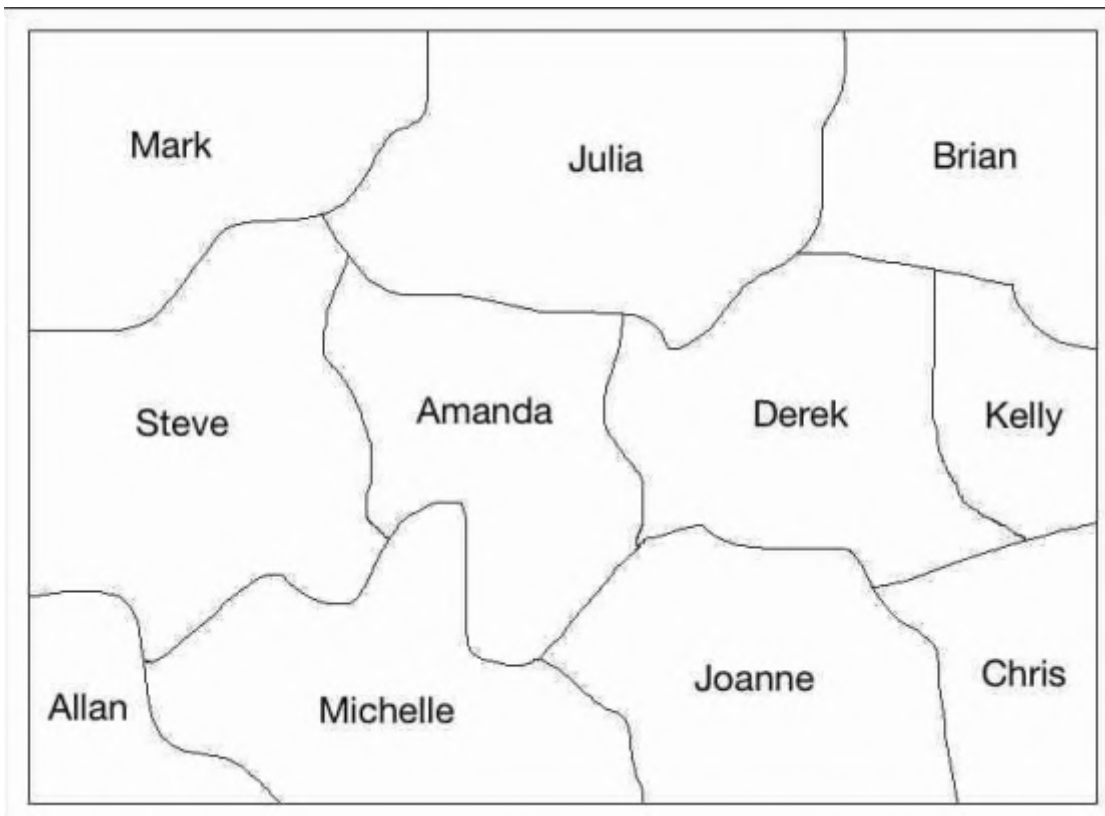
In this task, a genetic algorithm has been implemented which is able to place a given number of queens on a chessboard so that they do not attack each other. In particular, the case of an 8x8 chessboard with 8 queens was first considered and run, after which the number of queens was expanded to 12, and the chessboard then became 12x12.

▼ Lab 3. Genetic Algorithms

Task 3.3 The Map Colouring Problem

Problem Descriptions

The map colouring problem consists of using a given number of colours to colour a map, while taking into account that there must be no bordering regions with the same colour. In this task, there are 11 regions to be coloured and the colours that can be used are 4.



To define the bordering regions, we can use an upper triangular matrix where 1 stands for neighbouring and 0 does not. Choosing an upper triangular matrix over a full matrix is due to neighborhood mutuality, so we set the bottom of the matrix to zero. The encoding scheme, fitness function and genetic operators can now be defined.

ENCODING SCHEME: you can for instance use a list of 11 regions and assign each one a number from 0 to 3, representing the colour.

FITNESS FUNCTION: the number of neighbouring regions with the same colour has to be evaluated, in order to always have a lower number until zero is reached.

GENETIC OPERATORS: in this problem one could use tournament selection as a selection method, because the aim is to minimise the result. Cross over is then applied between two individuals thus exchanging the colours assigned to the regions and mutation, on the other hand, is applied by changing a number, that is a colour, within the same list of regions.

Implementation and Results

```
1 !pip install deap
2 import array
3 import random
4 import numpy as np
5 from deap import creator, base, tools, algorithms

1 # Specify the variables
2 numColour = 4
3 numNames = 11
4 colours = ('red', 'green', 'blue', 'gray')
5 names = ('Mark', 'Julia', 'Steve', 'Amanda', 'Brian',
6         'Joanne', 'Derek', 'Allan', 'Michelle', 'Kelly', 'Chris')
7
8 # Define the neighbours
9 neighbours = [ [0,1,1,0,0,0,0,0,0,0],
10               [0,0,1,1,1,0,1,0,0,0],
11               [0,0,0,1,0,0,0,1,1,0],
12               [0,0,0,0,0,1,1,0,1,0],
13               [0,0,0,0,0,0,1,0,0,1],
14               [0,0,0,0,0,0,1,0,1,1],
15               [0,0,0,0,0,0,0,0,1,1],
16               [0,0,0,0,0,0,0,0,1,0],
17               [0,0,0,0,0,0,0,0,0,0],
18               [0,0,0,0,0,0,0,0,0,1],
19               [0,0,0,0,0,0,0,0,0,0]]
20

1 def evalMapColouring(ind):
2     val = 0
3     for i in range(0, numNames):
4         for j in range(0, numNames):
5             if (neighbours[i][j] == 1) and (ind[i] == ind[j]):
6                 val += 1
7     return val,
8
9 creator.create("FitnessMin", base.Fitness, weights=(-1.0,))
10 creator.create("Individual", array.array, typecode='i', fitness=creator.FitnessMin)
11
12 toolbox = base.Toolbox()
13 toolbox.register("attr_colour", random.randint, 0, numColour-1)
14 toolbox.register("individual", tools.initRepeat, creator.Individual, toolbox.attr_colour, numNames)
15 toolbox.register("population", tools.initRepeat, list, toolbox.individual)
16
17 toolbox.register("evaluate", evalMapColouring)
18 toolbox.register("mate", tools.cxTwoPoint)
19 toolbox.register("mutate", tools.mutUniformInt, low=0, up=numColour-1, indpb=0.05)
20 toolbox.register("select", tools.selTournament, tournsize=3)
21
```

```

1 pop = toolbox.population(n=10)
2 stats = tools.Statistics(lambda ind: ind.fitness.values)
3 stats.register("min", np.min)
4 pop, log = algorithms.eaSimple(pop, toolbox, cxpb=0.8, mutpb=0.4, ngen=100,
5                               stats=stats, verbose=True)
6
7 best = tools.selBest(pop, 1)[0]
8 print("Best: %s. Fitness: %s." %(best.tolist(), evalMapColouring(best)[0]))
9 for i in range(numNames):
10  print("%s ==> %s" %(names[i], colours[best[i]]))

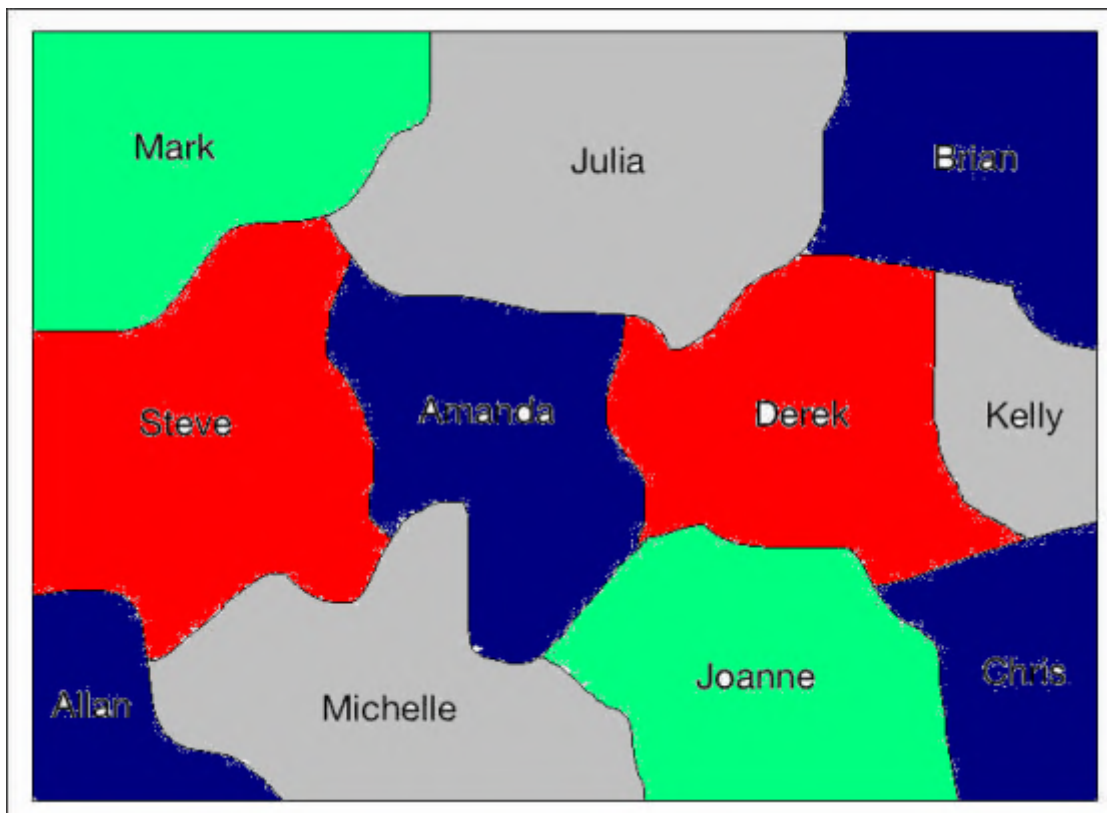
```

gen	nevals	min
0	10	2
1	10	0
2	10	1
3	9	1
4	9	1
5	8	0
6	8	0
7	9	0
8	8	0
9	10	0
10	7	0
11	10	0
12	8	0
13	6	0
14	8	0
15	8	0
16	10	0
17	10	0
18	10	0
19	9	0
20	7	0
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47	9	0
48	8	0
49	10	0
50	8	0
51	7	0
52	8	0
53	10	0
54	10	0
55	10	0
56	10	0

Discussions

As a final output we obtain the hundred generations it took to arrive at the solution, in which the fitness function is therefore zero. The solution corresponds to a string of 11 numbers from 0 to 3, which then indicates the 11 regions to which the 4 colours have been assigned in such a way that there are no equal neighbouring colours.



▼ Lab 4. Probabilistic Inference

Task 4.1 Iris Classification Using Naïve Bayes

Problem Descriptions

In this task a classification problem using the Naive Bayes theorem has to be solved. The Iris flower dataset, made famous by Fisher, will be used. It contains five variables, four are flower features, i.e. sepal length, petal length, sepal width and petal width, the fifth is the species, three in total. The task is therefore based on predicting the species of a particular flower based on the characteristics contained in the dataset.

The algorithm will first be run using two of the four flower characteristics contained in the dataset (sepal length and petal length), for simplicity and clarity's sake, then with all four.

Implementation and Results

```
1 !pip install sklearn
2 from sklearn import datasets
3 from sklearn.naive_bayes import GaussianNB
4 from sklearn.metrics import accuracy_score, classification_report, confusion_matrix
5 from sklearn.model_selection import train_test_split, cross_validate
6
7 import numpy as np
8 import matplotlib.pyplot as plt
9 from matplotlib import patches
10
11
12 # We only use two features (sepal and petal length)
13 iris = datasets.load_iris()
14 # X = iris.data
15 X = iris.data[:, [0,2]]
16 Y = iris.target
17
18 # split the dataset into training (80%) and testing (20%), and fit the data into the naive Bayes model
19 X_train, X_test, Y_train, Y_test = train_test_split(X, Y, test_size=0.2)
20 nb = GaussianNB()
21 nb.fit(X_train, Y_train)
22
23 # Use the naive Bayes model we just built to predict on the testing set, and display the results.
24 Y_pred = nb.predict(X_test)
25 acc = accuracy_score(Y_test, Y_pred)
26 cm = confusion_matrix(Y_test, Y_pred)
27 cr = classification_report(Y_test, Y_pred)
28 print("Accuracy:", acc)
29 print("Confusion Matrix:\n", cm)
30 print("Prior:\n", nb.class_prior_)
```

```

20 print("Mean:\n", nb.theta_)
21 print("Variance:\n", nb.sigma_)
22

```

Accuracy: 0.9333333333333333

Confusion Matrix:

```
[[10 0 0]
```

```
[ 0 9 1]
```

```
[ 0 1 9]]
```

Prior:

```
[0.33333333 0.33333333 0.33333333]
```

Mean:

```
[[4.985 1.4475]
```

```
[5.9775 4.275 ]
```

```
[6.5575 5.5275]]
```

Variance:

```
[[0.138275 0.03399375]
```

```
[0.29074375 0.214375 ]
```

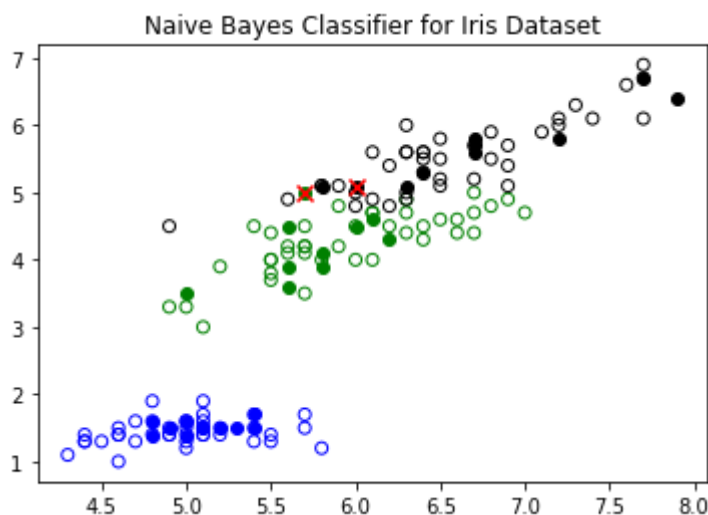
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[0.37194375 0.29849375]]
```

/usr/local/lib/python3.8/dist-packages/sklearn/utils/deprecation.py:103: FutureWarning: Attribute `sigma` is deprecated.
warnings.warn(msg, category=FutureWarning)

```

1  colours = 'bgk'
2  for i, colour in enumerate(colours):
3      train_data = X_train[Y_train == i]
4      plt.scatter(train_data[:,0], train_data[:,1], marker='o', facecolors='none', edgecolors=colour)
5      test_data = X_test[Y_pred == i]
6      plt.scatter(test_data[:,0], test_data[:,1], marker='o', facecolors=colour, edgecolors=colour)
7
8      error_data = X_test[Y_pred != Y_test]
9      plt.scatter(error_data[:,0], error_data[:,1], marker='x', facecolors='r', edgecolors='r', s=64)
10
11 #ellipse = patches.Ellipse(xy=nb.theta_[0], width=nb.sigma_[0][0]*10, height=nb.sigma_[0][1]*10, edgecolor='b')
12 #ellipse = patches.Ellipse(xy=(5,2), width=2, height=1)
13 #ax = plt.gca()
14 #ax.add_patch(ellipse)
15
16 plt.title("Naive Bayes Classifier for Iris Dataset")
17 plt.show()

```



```

1 # Now we use all four features
2 iris = datasets.load_iris()
3 X = iris.data
4 #X = iris.data[:, [0,2]]
5 Y = iris.target
6
7 # split the dataset into training (80%) and testing (20%), and fit the data into the naive Bayes model
8 X_train, X_test, Y_train, Y_test = train_test_split(X, Y, test_size=0.2)
9 nb = GaussianNB()
10 nb.fit(X_train, Y_train)
11
12 # Use the naive Bayes model we just built to predict on the testing set, and display the results.
13 Y_pred = nb.predict(X_test)
14 acc = accuracy_score(Y_test, Y_pred)
15 cm = confusion_matrix(Y_test, Y_pred)
16 cr = classification_report(Y_test, Y_pred)
17 print("Accuracy:", acc)
18 print("Confusion Matrix:\n", cm)
19 print("Prior:\n", nb.class_prior_)
20 print("Mean:\n", nb.theta_)
21 print("Variance:\n", nb.sigma_)

Accuracy: 0.9666666666666667
Confusion Matrix:
[[11  0  0]
 [ 0  9  1]
 [ 0  0  9]]
Prior:
[0.325  0.33333333 0.34166667]
Mean:
[[5.06666667 3.49230769 1.46666667 0.24358974]
 [5.8925  2.7275  4.245  1.3125 ]
 [6.55609756 2.95365854 5.52926829 1.97560976]]
Variance:
[[0.11504274 0.11763314 0.03452992 0.0096384 ]
 [0.26019375 0.10299375 0.193975  0.03909375]
 [0.41612136 0.09858418 0.28743605 0.06916122]]
/usr/local/lib/python3.8/dist-packages/sklearn/utils/deprecation.py:103: FutureWarning: Attribute `sigma_`
warnings.warn(msg, category=FutureWarning)

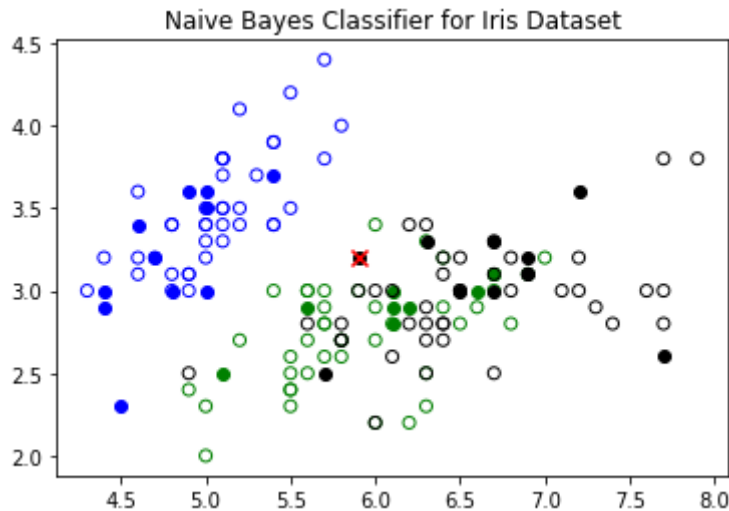
```

```

1 colours = 'bgk'
2 for i, colour in enumerate(colours):
3     train_data = X_train[Y_train == i]
4     plt.scatter(train_data[:,0], train_data[:,1], marker='o', facecolors='none', edgecolors=colour)
5     test_data = X_test[Y_pred == i]
6     plt.scatter(test_data[:,0], test_data[:,1], marker='o', facecolors=colour, edgecolors=colour)
7
8     error_data = X_test[Y_pred != Y_test]
9     plt.scatter(error_data[:,0], error_data[:,1], marker='x', facecolors='r', edgecolors='r', s=64)
10
11 # ellipse = patches.Ellipse(xy=nb.theta_[0], width=nb.sigma_[0][0]*10, height=nb.sigma_[0][1]*10, edgecolor='t
12 # # ellipse = patches.Ellipse(xy=(5,2), width=2, height=1)
13 # ax = plt.gca()
14 # ax.add_patch(ellipse)

```

```
15
16 plt.title("Naive Bayes Classifier for Iris Dataset")
17 plt.show()
```



Discussions

Naive Bayes has been used to formulate the algorithm, estimating the posterior probability of the species given the features, from the prior probability of each iris class and the conditional probability of the features taken separately, given the species.

To illustrate and make the result clearer, the data can be plotted in a scatter plot that differentiates the species with different colours, and uses solid markers for the testing set, empty markers for the training set, and red crosses for the misclassified patterns. The output showed that there was no clear distinction between two of the three species analysed, and therefore we obtained errors in their intersection boundary.

The first graph shows how, considering only the length of the sepals and petals, the species differ because they have different values, i.e. one has generally shorter petals and sepals than the others, one has intermediate values and several individuals of the last species have higher values. Considering the second graph, in which the classification was made according to all four characteristics, a more random distribution of the individuals is observed, meaning that the species that had a shorter length of petals and sepals compensates with a greater width.

▼ Lab 4. Probabilistic Inference

Task 4.2 Diabetes Diagnosis Using Naïve Bayes

Problem Descriptions

In this task, a medical diagnosis problem will be tackled, where the goal is to predict whether a patient has a disease or the level of disease progression. A diabetes dataset will be used, which contains 10 features and a quantitative measurement of diabetes progression. Patient observations correspond to personal data such as age, gender, height, weight, tests like blood sugar, heart rate, lipoproteins and symptoms e.g. fever or headache.

Implementation and Results

```
1 !pip install sklearn
2 from sklearn import datasets
3 from sklearn.naive_bayes import GaussianNB
4 from sklearn.metrics import accuracy_score, classification_report, confusion_matrix
5 from sklearn.model_selection import train_test_split, cross_validate
6
7 # import numpy as np
8 import matplotlib.pyplot as plt
9 # from matplotlib import patches
10 import math
```

```
1 diabetes = datasets.load_diabetes()
2 # X = diabetes.data[:,2:9]
3 X = diabetes.data
4 Y = [math.floor(x/150) for x in diabetes.target]
5
6 X_train, X_test, Y_train, Y_test = train_test_split(X, Y, test_size=0.25)
7
8 nb = GaussianNB()
9 nb.fit(X_train, Y_train)
10 Y_pred = nb.predict(X_test)
11 acc = accuracy_score(Y_test, Y_pred)
12 cm = confusion_matrix(Y_test, Y_pred)
13 cr = classification_report(Y_test, Y_pred)
14
15 print("Accuracy:", acc)
16 print("Confusion Matrix:\n", cm)
17 print("Prior:\n", nb.class_prior_)
18 print("Mean:\n", nb.theta_)
19 print("Variance:\n", nb.sigma_)
20
```

```
☞ Accuracy: 0.6756756756756757
Confusion Matrix:
[[47 19  0]
 [ 9 27  3]
 [ 1  4 11]]
Prior:
[0.51963746 0.45619335 0.02416918]
Mean:
[[-0.00526112 -0.00086013 -0.02101334 -0.01711349 -0.01028066 -0.00942024
  0.01451003 -0.01695366 -0.02041805 -0.01636978]
 [ 0.00819768  0.0008098  0.01752732  0.01635464  0.00827229  0.00545096
 -0.01389898  0.01414276  0.02383294  0.01368027]
 [ 0.01673474  0.02684968  0.06627691  0.0360742  0.00582679  0.00072159
 -0.03649777  0.03707644  0.04692384  0.06985588]]
Variance:
[[0.00221154 0.00225651 0.00146332 0.00166069 0.00212625 0.00201469
 0.00261449 0.00155957 0.00165128 0.00191088]
 [0.00218137 0.00226668 0.00203968 0.00217859 0.00239541 0.00236454
 0.0016172  0.00212146 0.00188261 0.00219692]
 [0.00168715 0.00170367 0.00112269 0.002369  0.00088885 0.00094093
 0.00037423 0.00182382 0.00121177 0.0020693 ]]
/usr/local/lib/python3.8/dist-packages/sklearn/utils/deprecation.py:103: FutureWarning: Attribute `sigma_` was deprecated in 1.0 and will be removed in 1.2. Use `warnings.warn(msg, category=FutureWarning)
```

Discussions

To simplify the resolution of the task, to make the progression measures classifiable, the original data were converted into three categories: 0 to 150, 150 to 300 and 300 and upwards. They were then divided into training set and testing set with a 3-1 split. From the output obtained, it

can be seen that in a realistic problem like this, the accuracy of the result hardly exceeds 0.70, due to the complexity of the dataset.

Problem Description:

Describe the problem here...

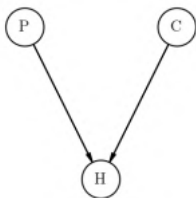
▼ Lab 4. Probabilistic Inference

Task 4.3 Monty Hall Problem Using Bayesian Network

Problem Descriptions

The Monty Hall problem is taken from a famous American TV show and is based on the contestant's probability of getting the prize by choosing between three doors, two of which hide a goat and one a car (the prize). The contestant is initially asked to choose a door, consequently the host will open one of the two remaining doors, where he knows there is no prize. Now the contestant is offered to swap the door chosen at the beginning for the remaining one, and it is on this choice that the game is based. This is because by swapping the door the contestant actually has twice the chance of winning, even though it may seem that the probability is 50%.

In order to solve this task, we can use the Bayesian Network, and therefore need to define three variables. Furthermore, the three doors will be identified as 0, 1 and 2. The first variable is the prize (P), which can hide behind each door, and so the prior probability is 1/3 for all three. The other variable is the contestant (C), i.e. his initial choice, and again the prior probability is 1/3. The last variable is the action performed by the host H, which depends on the position of the prize and the choice of the contestant. The Bayesian Network will thus be composed as in the following picture.



Later on, a variant of the game will also be implemented, with the same rules, but considering four doors instead of three.

Implementation and Results

```
1 !pip install pgmpy
2 from pgmpy.models import BayesianModel
3 from pgmpy.factors.discrete import TabularCPD

4 # Defining the network structure
5 model = BayesianModel([('Contestant', 'Host'), ('Prize', 'Host')])
6
7 # Defining the CPDs:
8 cpd_c = TabularCPD('Contestant', 3, [[1/3], [1/3], [1/3]])
9 cpd_p = TabularCPD('Prize', 3, [[1/3], [1/3], [1/3]])
10 cpd_h = TabularCPD('Host', 3, [[0, 0, 0, 0.5, 1, 0, 1, 0.5],
11                                [0.5, 0, 1, 0, 0, 0, 1, 0.5],
12                                [0.5, 1, 0, 1, 0.5, 0, 0, 0]],
13                                evidence=['Contestant', 'Prize'], evidence_card=[3, 3])
14
15 # cpd_c = TabularCPD('Contestant', 4, [[0.25], [0.25], [0.25], [0.25]])
16 # cpd_p = TabularCPD('Prize', 4, [[0.25], [0.25], [0.25], [0.25]])
17 # cpd_h = TabularCPD('Host', 4, [[0, 0, 0, 0, 0, 1/3, 0.5, 0.5, 0, 0.5, 1/3, 0.5, 0, 0.5, 0.5, 1/3],
18 #                                [1/3, 0, 0.5, 0.5, 0, 0, 0, 0, 0.5, 0, 1/3, 0.5, 0.5, 0, 0.5, 1/3],
19 #                                [1/3, 0.5, 0, 0.5, 0.5, 1/3, 0, 0.5, 0, 0, 0, 0.5, 0.5, 0, 1/3],
20 #                                [1/3, 0.5, 0.5, 0, 0.5, 1/3, 0.5, 0, 0.5, 0.5, 1/3, 0, 0, 0, 0, 0]],
21 #                                evidence=['Contestant', 'Prize'], evidence_card=[4, 4])
22
23 # Associating the CPDs with the network structure.
24 model.add_cpds(cpd_c, cpd_p, cpd_h)
25
26 # Inferring the posterior probability
27 from pgmpy.inference import VariableElimination
28
29 infer = VariableElimination(model)
30 posterior = infer.query(variables=['Prize'], evidence={'Contestant': 0, 'Host': 2}, show_progress=False, joint=False)
31 print(posterior['Prize'])
```

+-----+-----+
| Prize | phi(Prize) |

```

+-----+-----+
| Prize(0) | 0.3333 |
+-----+-----+
| Prize(1) | 0.6667 |
+-----+-----+
| Prize(2) | 0.0000 |
+-----+-----+

```

```

1 #We now implement the case with 4 doors
2
3 # Defining the network structure
4 model = BayesianModel([('Contestant', 'Host'), ('Prize', 'Host')])
5
6 # Defining the CPDs:
7
8 cpd_c = TabularCPD('Contestant', 4, [[0.25], [0.25], [0.25], [0.25]])
9 cpd_p = TabularCPD('Prize', 4, [[0.25], [0.25], [0.25], [0.25]])
10 cpd_h = TabularCPD('Host', 4, [[0, 0, 0, 0, 1/3, 0.5, 0.5, 0, 0.5, 1/3, 0.5, 0, 0.5, 0.5, 1/3],
11                                [1/3, 0, 0.5, 0.5, 0, 0, 0, 0, 0.5, 0, 1/3, 0.5, 0.5, 0, 0.5, 1/3],
12                                [1/3, 0.5, 0, 0.5, 0.5, 1/3, 0, 0.5, 0, 0, 0, 0, 0.5, 0.5, 0, 1/3],
13                                [1/3, 0.5, 0.5, 0, 0.5, 1/3, 0.5, 0, 0.5, 0.5, 1/3, 0, 0, 0, 0, 0]],
14                                evidence=['Contestant', 'Prize'], evidence_card=[4, 4])
15
16 # Associating the CPDs with the network structure.
17 model.add_cpds(cpd_c, cpd_p, cpd_h)

1 # Inferring the posterior probability
2 from pgmpy.inference import VariableElimination
3
4 infer = VariableElimination(model)
5 posterior = infer.query(variables=['Prize'], evidence={'Contestant': 0, 'Host': 2}, show_progress=False, joint=False)
6 print(posterior['Prize'])

```

```

+-----+-----+
| Prize | phi(Prize) |
+-----+-----+
| Prize(0) | 0.2500 |
+-----+-----+
| Prize(1) | 0.3750 |
+-----+-----+
| Prize(2) | 0.0000 |
+-----+-----+
| Prize(3) | 0.3750 |
+-----+-----+

```

Discussions

The output obtained depicts the probability of each door after one has been opened by the host. In the first case where there are three doors in total, we see how the result shows that the probability of the prize being behind the second door increases by 33%, and is therefore double the probability of the prize being hidden behind the door chosen by the contestant. This means that it is always better to change the initial choice in this game situation.

In the variant with 4 doors, on the other hand, the odds of finding the prize are distributed differently. However, we can see that the contestant still has less chance of winning if he stays with his initial choice, with which he has a 25% chance of winning. This is because, in this case, there being two remaining doors, the probability of finding the prize by changing doors is 37% (for both doors). Therefore, although the probability of winning in general is reduced, even in this situation it is better for the contestant to change his choice, and it is indifferent with which of the two remaining doors he decides to change.

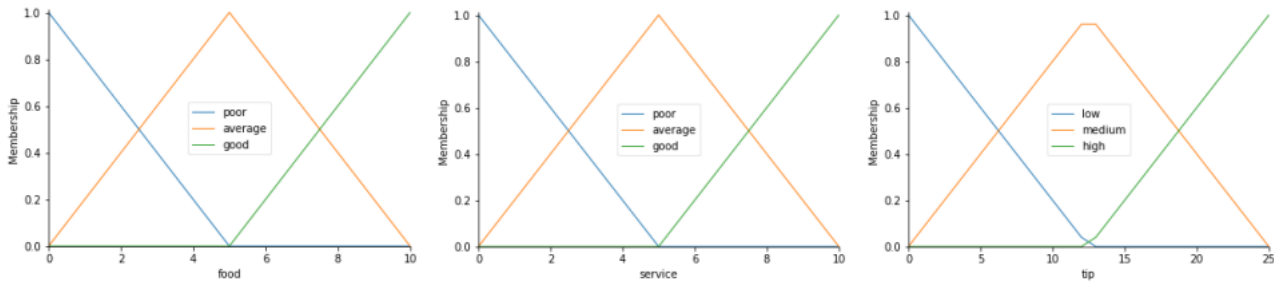
▼ Lab 5. Fuzzy Systems

Task 5.1 The Tipping Problem

Problem Descriptions

The tipping problem consists of working out, using a fuzzy system, what tip to give a restaurant, based on the quality of service and food. So in total we have two linguistic variables as input, namely service and food, and one variable as final output which corresponds to the tip. For food and service we have the values poor, average, and good. For the tip they are low, medium, and high. Moreover, “food” and “service” are defined in the scale of 0-10, while “tip” in the range of 0-25%.

The membership of the linguistic variables are defined in the same way for simplicity and are depicted in the following image:



There are three rules:

1. IF the service was good
OR the food quality was good
THEN the tip will be high.
2. IF the service was average
THEN the tip will be medium.
3. IF the service was poor
AND the food quality was poor
THEN the tip will be low.

Implementation and Results

```
1 !pip install scikit-fuzzy
2 import numpy as np
3 import skfuzzy as fuzz
4 from skfuzzy import control as ctrl

1 # New Antecedent/Consequent objects hold universe variables and membership functions
2 food = ctrl.Antecedent(np.arange(0, 11, 1), 'food')
3 service = ctrl.Antecedent(np.arange(0, 11, 1), 'service')
4 tip = ctrl.Consequent(np.arange(0, 26, 1), 'tip')
5
6 # Auto-membership function population is possible with .automf(3, 5, or 7)
7 food.automf(3)
8 service.automf(3)
9 tip.automf(3, names=['low', 'medium', 'high'])
10
11 # food.view()
12 # service.view()
13 # tip.view()

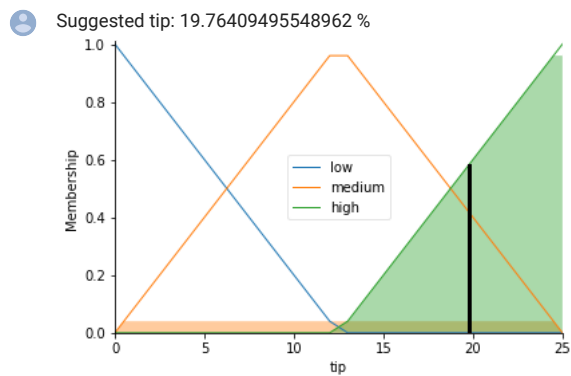
1 # Define the rules
2 rule1 = ctrl.Rule(food['poor'] | service['poor'], tip['low'])
3 rule2 = ctrl.Rule(service['average'], tip['medium'])
4 rule3 = ctrl.Rule(service['good'] | food['good'], tip['high'])
5
6 # Create the control system and its simulation
7 tipping_ctrl = ctrl.ControlSystem([rule1, rule2, rule3])
8 tipping = ctrl.ControlSystemSimulation(tipping_ctrl)

1 # Pass inputs to the ControlSystem
2 tipping.inputs({'food': 6.5, 'service': 9.8})
```

```

3
4 # Crunch the numbers
5 tipping.compute()
6 print("Suggested tip:", tipping.output['tip'], "%")
7 tip.view(sim=tipping)
8

```



Discussions

To test the functioning of the algorithm, two judgement values were chosen to be assigned to the input variables, namely 6.5 for food and 9.8 for service.

The solution obtained is a tip of 19.8% and as the graph depicts, the value belongs to the "high" range of the output variable, which is tip.

▼ Lab 5. Fuzzy Systems

Task 5.2 Project Risk Assessment

Problem Descriptions

The problem addressed in this task regards the project risk assessment, i.e. it consists of calculating the risk of a project, which in this case can be low, normal or high by having project funding (inadequate, marginal, adequate) and staffing (small, large) as linguistic variables. In addition, the following rules will be applied:

1. IF project funding is adequate
 OR project staffing is small
 THEN risk is low
2. IF project funding is marginal
 AND project staffing is large
 THEN risk is normal
3. IF project funding is inadequate
 THEN risk is high

Implementation and Results

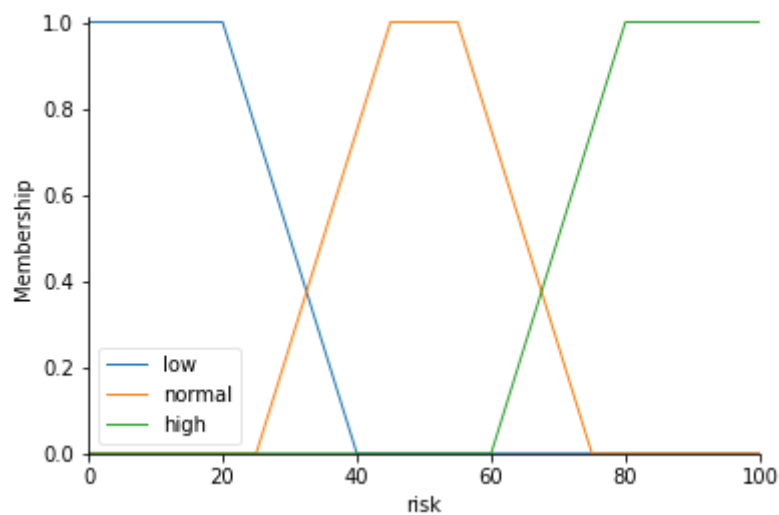
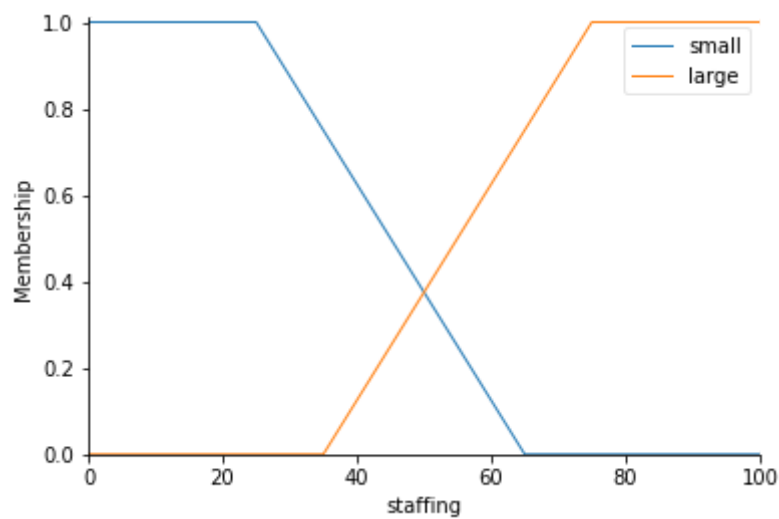
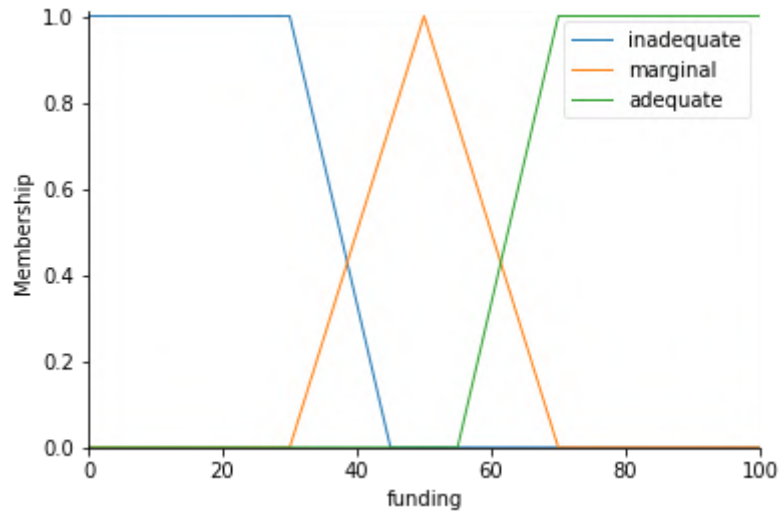
```
1 !pip install scikit-fuzzy
2 import numpy as np
3 import skfuzzy as fuzz
4 from skfuzzy import control as ctrl

5
6 # Linguistic variables for antecedents/consequent
7 funding = ctrl.Antecedent(np.arange(0, 101, 1), 'funding')
8 staffing = ctrl.Antecedent(np.arange(0, 101, 1), 'staffing')
9 risk = ctrl.Consequent(np.arange(0, 101, 1), 'risk')
10
11 # membership functions for each linguistic values
12 funding['inadequate'] = fuzz.trapmf(funding.universe, [0, 0, 30, 45])
13 funding['marginal'] = fuzz.trimf(funding.universe, [30, 50, 70])
14 funding['adequate'] = fuzz.trapmf(funding.universe, [55, 70, 100, 100])
15 staffing['small'] = fuzz.trapmf(staffing.universe, [0, 0, 25, 65])
16 staffing['large'] = fuzz.trapmf(staffing.universe, [35, 75, 100, 100])
17 risk['low'] = fuzz.trapmf(risk.universe, [0, 0, 20, 40])
18 risk['normal'] = fuzz.trapmf(risk.universe, [25, 45, 55, 75])
19 risk['high'] = fuzz.trapmf(risk.universe, [60, 80, 100, 100])
20
```

```

16 funding.view()
17 staffing.view()
18 risk.view()

```



```

1 # Define the rules
2 rule1 = ctrl.Rule(funding['adequate'] | staffing['small'], risk['low'])
3 rule2 = ctrl.Rule(funding['marginal'] & staffing['large'], risk['normal'])
4 rule3 = ctrl.Rule(funding['inadequate'], risk['high'])
5 # rule4 = ctrl.Rule(funding['inadequate'] & staffing['large'], risk['high'])
6
7 # Create the control system and its simulation

```

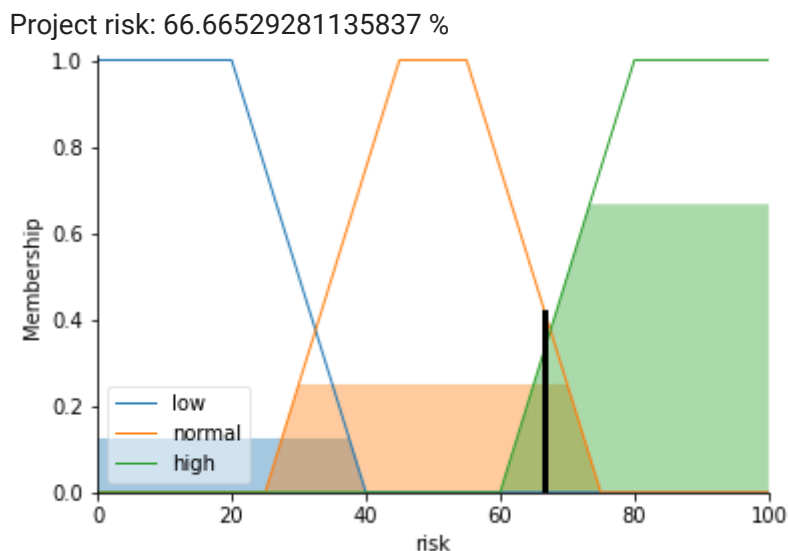


```

8 ctrl_sys = ctrl.ControlSystem([rule1, rule2, rule3])
9 # ctrl_sys = ctrl.ControlSystem([rule1, rule2, rule3, rule4])
10 ctrl_sim = ctrl.ControlSystemSimulation(ctrl_sys)

1 # Pass inputs to the ControlSystem
2 ctrl_sim.inputs({'funding': 35, 'staffing': 60})
3
4 # Crunch the numbers
5 ctrl_sim.compute()
6 print("Project risk:", ctrl_sim.output['risk'], "%")
7 risk.view(sim=ctrl_sim)
8

```



```

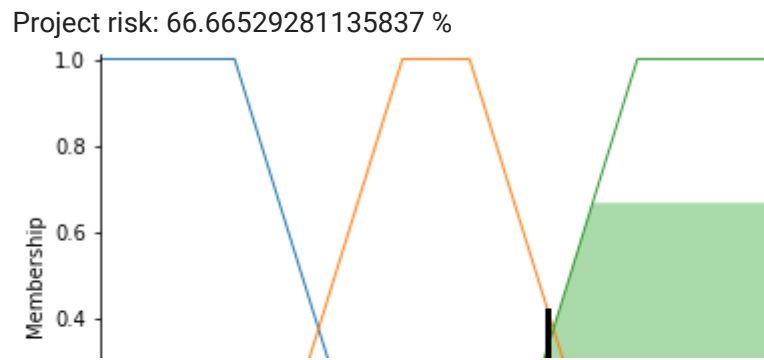
1 # We now add another rule
2 rule1 = ctrl.Rule(funding['adequate'] | staffing['small'], risk['low'])
3 rule2 = ctrl.Rule(funding['marginal'] & staffing['large'], risk['normal'])
4 rule3 = ctrl.Rule(funding['inadequate'], risk['high'])
5 rule4 = ctrl.Rule(funding['inadequate'] & staffing['large'], risk['high'])
6
7 # Create the control system and its simulation
8 ctrl_sys = ctrl.ControlSystem([rule1, rule2, rule3, rule4])
9 ctrl_sim = ctrl.ControlSystemSimulation(ctrl_sys)

```

```

1 # Pass inputs to the ControlSystem
2 ctrl_sim.inputs({'funding': 35, 'staffing': 60})
3
4 # Crunch the numbers
5 ctrl_sim.compute()
6 print("Project risk:", ctrl_sim.output['risk'], "%")
7 risk.view(sim=ctrl_sim)
8

```



Discussions

In this task, the risk of a project was calculated using funding and staffing as variables and implementing an algorithm with fuzzy logic. Two cases were evaluated, the first by applying three rules as described above, in the second a fourth rule was then added, the following: IF project funding is inadequate AND project staffing is large THEN risk is high In both cases, the project risk (output variable) was calculated considering funding=35% and staffing=60%. The solution obtained is the same for both cases implemented, i.e. the risk is 66.7%.

▼ Lab 5. Fuzzy Systems

Task 5.3 Washing Machine Fuzzy Controller

Problem Descriptions

The objective of this task is to programme a washing machine controller following fuzzy logic. We will again use two input variables, namely degree of dirtiness and size of load of clothes, and one output variable, the washing time. The linguistic values are the following: Degree of Dirtiness: SD(small), MD(medium), LD(large) Size of Load of Clothes: SL(small), ML(medium), LL(large) Washing Time: VS(very short), S(short), M(medium), L(long), VL(very long)

In this case, the rules are contained in a Fuzzy Associative Memory (FAM):

		Size of load of clothes		
		SL	ML	LL
Degree of dirtiness	SD	VS	M	L
	MD	S	M	L
	LD	M	L	VL

Fuzzy Associative Memory

The rules in the table can be interpreted as in the following example:

IF dirtiness is SD

AND load is SL

THEN washing time is VS

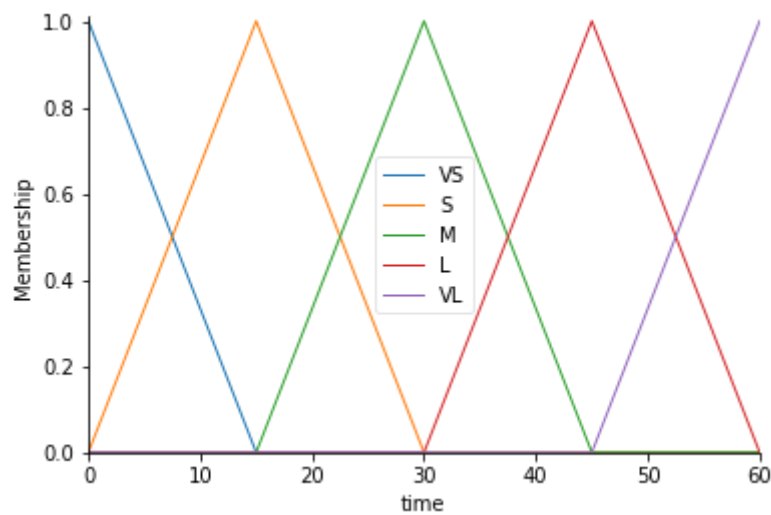
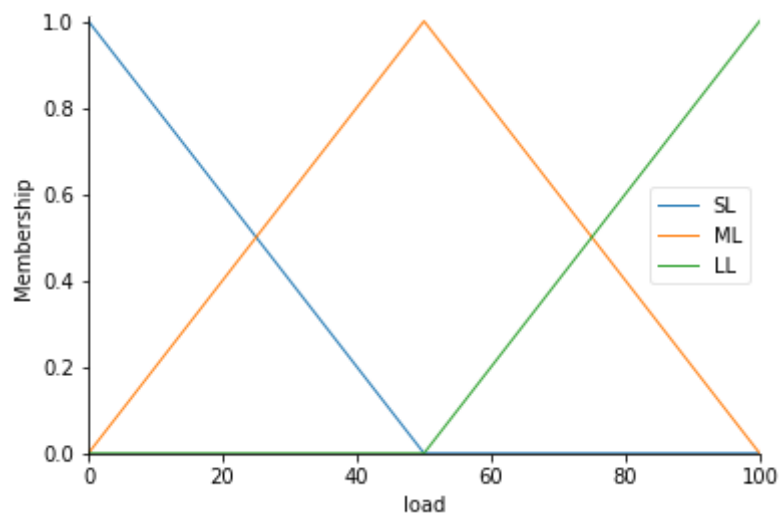
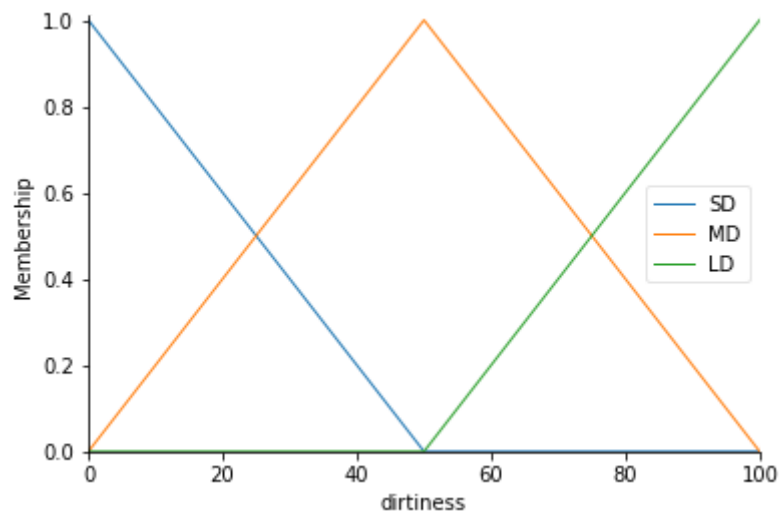
Implementation and Results

```
1 !pip install scikit-fuzzy
2 import numpy as np
3 import skfuzzy as fuzz
4 from skfuzzy import control as ctrl

1 # Linguistic variables for antecedents/consequent
2 dirtiness = ctrl.Antecedent(np.arange(0, 101, 1), 'dirtiness')
3 load = ctrl.Antecedent(np.arange(0, 101, 1), 'load')
4 time = ctrl.Consequent(np.arange(0, 61, 1), 'time')
5
6 # membership functions for each linguistic values
7 dirtiness.automf(3, names=['SD', 'MD', 'LD'])
8 load.automf(3, names=['SL', 'ML', 'LL'])
9 time.automf(5, names=['VS', 'S', 'M', 'L', 'VL'])
10
11 dirtiness.view()
```

12 load.view()

13 time.view()



1 # Define the rules

2 rule1 = ctrl.Rule(dirtiness['SD'] & load['SL'], time['VS'])

3 rule2 = ctrl.Rule(dirtiness['SD'] & load['ML'], time['M'])

4 rule3 = ctrl.Rule(dirtiness['SD'] & load['LL'], time['L'])

5 rule4 = ctrl.Rule(dirtiness['MD'] & load['SL'], time['S'])

6 rule5 = ctrl.Rule(dirtiness['MD'] & load['ML'], time['M'])

7 rule6 = ctrl.Rule(dirtiness['MD'] & load['LL'], time['L'])

8 rule7 = ctrl.Rule(dirtiness['LD'] & load['SL'], time['M'])

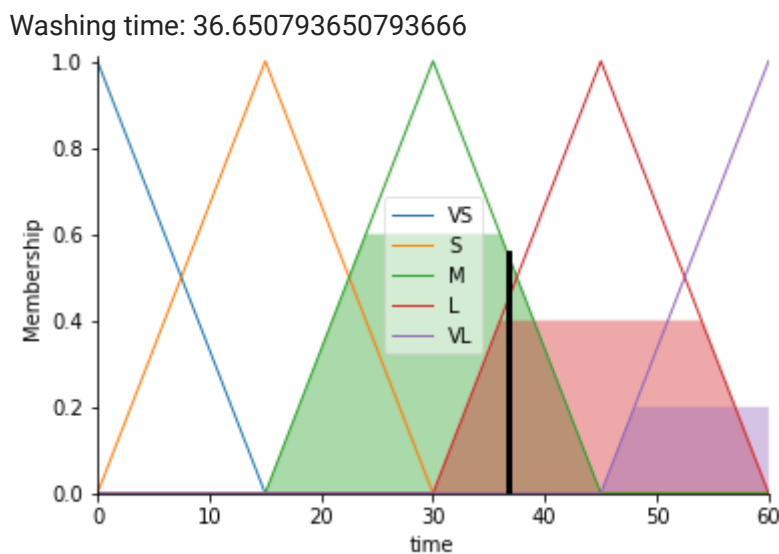
9 rule8 = ctrl.Rule(dirtiness['LD'] & load['ML'], time['L'])

```

10 rule9 = ctrl.Rule(dirtiness['LD'] & load['LL'], time['VL'])
11
12 # Create the control system and its simulation
13 ctrl_sys = ctrl.ControlSystem([rule1, rule2, rule3, rule4, rule5, rule6, rule7, rule8, rule9])
14 ctrl_sim = ctrl.ControlSystemSimulation(ctrl_sys)

1 # Pass inputs to the ControlSystem
2 ctrl_sim.inputs({'dirtiness': 60, 'load': 70})
3
4 # Crunch the numbers
5 ctrl_sim.compute()
6 print("Washing time:", ctrl_sim.output['time'])
7 time.view(sim=ctrl_sim)
8

```



Discussions

In this task, a washing machine controller was implemented, which is based on two variables: the degree of dirtiness and the size of load of clothes. To test the operation of the control system, two values were chosen for the two variables, namely 60% for the degree of dirtiness and 70% for the size of load. The result obtained refers to the output variable, the washing time, and is 36.7.

▼ Lab 6. Natural Language Processing

Task 6.1 Sentiment Analysis

Problem Descriptions

This task consists of implementing one of the most widespread problems in the field of natural language processing, sentiment analysis, which, however, does not always prove easy to tackle, due to the different writing styles, the various slangs and the different meanings that certain expressions may have. The text to be analysed here is taken from the "movie_review" dataset, which is a dataset with 1000 positive and 1000 negative reviews.

Implementation and Results

```
1 !pip install nltk
2 import nltk
3 from nltk.corpus import movie_reviews
4
5 nltk.download('movie_reviews')

1 from sklearn.naive_bayes import MultinomialNB
2 from sklearn.feature_extraction.text import TfidfVectorizer
3 from sklearn import metrics
4 from sklearn.model_selection import train_test_split

1 # Get the positive and negative review IDs
2 fileids_pos = movie_reviews.fileids('pos')
3 fileids_neg = movie_reviews.fileids('neg')
4
5 # Load the reviews
6 raw_data = []
7 for i in range(len(fileids_pos)):
8     raw_data.append(movie_reviews.raw(fileids_pos[i]))
9 for i in range(len(fileids_neg)):
10    raw_data.append(movie_reviews.raw(fileids_neg[i]))
11
12 # The corresponding labels for the reviews, 0 for positive, 1 for negative
13 labels = [0] * len(fileids_pos) + [1] * len(fileids_neg)
14
15 # Split the training and testing set by 80-20%
16 X_train, X_test, Y_train, Y_test = train_test_split(raw_data, labels, test_size=0.2)

1 # Calculate the tf-idf features from the training set
2 tfidf = TfidfVectorizer(use_idf=True)
3 tfidf_data = tfidf.fit_transform(X_train)
4 print(tfidf_data.shape)
5
6 # Train the naive Bayes model for prediction
7 classifier = MultinomialNB().fit(tfidf_data, Y_train)

(1600, 36323)

1 # Performance on the testing set
2 testing_tfidf = tfidf.transform(X_test)
3 predictions = classifier.predict(testing_tfidf)
4 print(metrics.classification_report(Y_test, predictions, target_names=['pos', 'neg']))

      precision    recall  f1-score   support

    pos       0.85       0.72       0.78        202
    neg       0.75       0.87       0.81        198

 accuracy                   0.80         400
 macro avg       0.80       0.80       0.79         400
 weighted avg       0.80       0.80       0.79         400

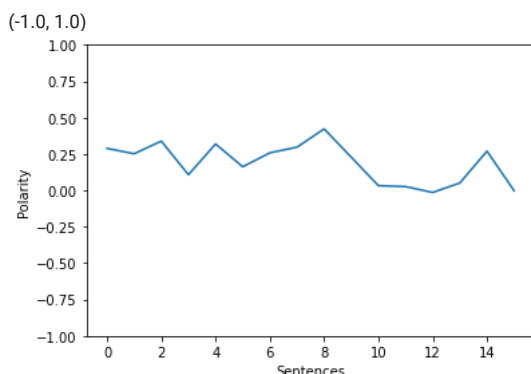
1 print(X_train[0])
2 print(testing_tfidf[0])
```

this summer , one of the most racially charged novels in john grisham's series , a time to kill , was made into a major motion picture .
on january 3 of this year , director rob reiner basically re-released the film under the title of ghosts of mississippi .
based on the true story of 1963 civil rights leader medgar evers' assassination , ghosts of mississippi revolves around the 25-year legal battle faced by myrlie everett
so she turns to assistant district attorney and prosecutor bobby delaughter (alec baldwin , heaven's prisoners) to imprison the former kkk member .

ghosts sets its tone with an opening montage of images from african-american history , from slave-ship miseries to life in the racist south of the 1960's . but all too soon , the white folks take over , intoning lines like " what's america got to do with anything ? this is mississippi ! " as beckwith , james woods , with his head larded with latex most of the time as an old man , teeters between portraying evil and its character . meanwhile , goldberg turns in a very serious and weepy performance as the wife who wouldn't let her husband's death rest until she got the conviction . both deserve serious oscar-consideration . this brings us to the dull performance of baldwin . let's face it , trying to match matthew mcconaughey's wonderful acting in a time to kill is basically impossible . and baldwin is living proof of this , as no emotions could be felt . it seemed as if he actually had to struggle to shed a single tear . either poor acting or poor directing , but something definitely went wrong . another strange mishap was the fact that goldberg's facial features didn't change , as she looked the same in the courtroom as she did holding her husband's de yet woods' was plastered with enough make up to make him look like goldberg's father . at least the make-up was realistic . with some emotional moments in the poorly written script , ghosts of mississippi lacked in heart , when its predecessor , a time to kill , brought tears to everyone don't get me wrong , the movie wasn't all that bad , but if you've seen grisham's masterpiece , then don't expect this one to be an excellent film .

```
(0, 36159) 0.024837241123616738
(0, 36118) 0.02496890661256656
(0, 35916) 0.01597939248903686
(0, 35880) 0.04634574818967332
(0, 35807) 0.04439093334039668
(0, 35798) 0.03403515751271626
(0, 35738) 0.02127478922613567
(0, 35645) 0.0478429542949432
(0, 35639) 0.041540331049150586
(0, 35613) 0.01703286568659344
(0, 35461) 0.05432866927690065
(0, 35457) 0.058892525187043396
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(0, 35359) 0.033339353193436234
(0, 35217) 0.22746568301190154
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(0, 34292) 0.055269121495952644
(0, 34205) 0.0701393734376125
(0, 33509) 0.034090387972316186
(0, 33382) 0.056306179744235935
(0, 32913) 0.05058568122083257
(0, 32740) 0.07897824865407392
(0, 32714) 0.11405249622690902
:
(0, 4372) 0.03496569959466136
(0, 4138) 0.15926783608170172
(0, 4114) 0.06665287013989037
(0, 4097) 0.04628013738109607
(0, 4068) 0.06726270397373887
(0, 3980) 0.032723278318862015
(0, 3065) 0.011568650440543398
(0, 3071) 0.000430043650005000
```

```
1 # Evaluate the sentiment for each sentence in a review, and plot the variation of sentiment
2 import matplotlib.pyplot as plt
3
4 sentences = X_test[0].split('.')
5
6 testing_tfidf = tfidf.transform(sentences)
7 predictions = classifier.predict_proba(testing_tfidf)
8 polarity = [x[0] - x[1] for x in predictions]
9 # polarity = [x[0] if (x[0] > x[1]) else -x[1] for x in predictions]
10
11 plt.xlabel('Sentences')
12 plt.ylabel('Polarity')
13 plt.plot(polarity)
14 plt.ylim(-1, 1)
```



Discussions

The first output we get is performance data, namely precision, recall, f1-score and support. Specifically, precision is the ability of a classification model to identify all data points in a relevant class. Precision is the ability to return only the data points in a class. The f1 score provides the harmonic mean of accuracy and recall. Finally, support is the number of samples of the true response that fall into that class. The polarity graph at the end refers to the overall sentiment transmitted by a particular text, phrase or word, and can be expressed as a numerical score known as a 'sentiment score'. As we see from the graph, this score can be a number between -1.00 and 1.00, with 0 representing neutral sentiment.

▼ Lab 6. Natural Language Processing

Task 6.2 Text Classification

Problem Descriptions

In this task, a classification method will again be implemented, but in this case more than two classes will be considered. The dataset to be analysed is a set of messages belonging to 20 news groups, such as comp.graphics, sci.space, tal.religion.misc. etc. For the representation of the text, we will still use word count features such as th or tf-idf, and the Naïve Bayes method.

Implementation and Results

```
1 from sklearn.datasets import fetch_20newsgroups
2 from sklearn.naive_bayes import MultinomialNB
3 from sklearn.feature_extraction.text import TfidfVectorizer
```

[+ Codice](#)[+ Testo](#)

```
1 # Get the training dataset for the specified categories
2 categories = ['rec.sport.hockey', 'talk.religion.misc',
3              'comp.graphics', 'sci.space']
4 training_data = fetch_20newsgroups(subset='train', categories=categories)
```

```
1 # Create the tf-idf transformer
2 tfidf = TfidfVectorizer(use_idf=True)
3 # tfidf = TfidfVectorizer(use_idf=False)
4 training_tfidf = tfidf.fit_transform(training_data.data)
5 print(training_tfidf.shape)
6
7 # Train a Multinomial Naive Bayes classifier
8 classifier = MultinomialNB().fit(training_tfidf, training_data.target)
9
```

(2154, 35956)

```
1 from sklearn import metrics
2
3 testing_data = fetch_20newsgroups(subset='test', categories=categories)
4 testing_tfidf = tfidf.transform(testing_data.data)
5 predictions = classifier.predict(testing_tfidf)
6 print(metrics.classification_report(testing_data.target, predictions, target_names=categories))
7
```

	precision	recall	f1-score	support
rec.sport.hockey	0.97	0.90	0.93	389
talk.religion.misc	0.93	0.99	0.96	399
comp.graphics	0.83	0.98	0.90	394
sci.space	1.00	0.72	0.84	251
accuracy		0.92		1433
macro avg	0.93	0.90	0.91	1433
weighted avg	0.93	0.92	0.92	1433

```
1 errors = [i for i in range(len(predictions)) if predictions[i] != testing_data.target[i]]
2
3 for i, post_id in enumerate(errors[:5]):
4     print("-----")
5     print("%s -> %s\n" %(testing_data.target_names[testing_data.target[post_id]],
6                        testing_data.target_names[predictions[post_id]]))
7     print(testing_data.data[post_id])
8
```

comp.graphics -> sci.space

From: robert@slipknot.rain.com (Robert Reed)
Subject: Re: ACM SIGGRAPH (and ACM in general)
Reply-To: Robert Reed <robert@slipknot.rain.com>
Organization: Home Animation Ltd.
Lines: 50

In article <1993Apr29.023508.11556@koko.csustan.edu> rsc@altair.csustan.edu (Steve Cunningham) writes:
|
|And no, SIGGRAPH 93 has not skipped town -- we're preparing the best
|SIGGRAPH conference yet!

Speaking of SIGGRAPH, I just went through the ordeal of my annual registration for SIGGRAPH and re-upping of membership in the ACM last night, and was I ever grossed out! The new prices for membership are almost highway robbery!

For example:

SIGGRAPH basic fee went from \$26 last year to \$59 this year for the same thing, a 127% increase. Those facile enough to arrange a trip to the annual conference could reduce this to \$27 by selecting SIGGRAPH Lite, which means SIGGRAPH is charging an additional \$32 (or so) for the proceedings and the art show catalog, essentially.

TOPLAS went up 40% in cost, way outstripping the current inflation rate.

Basic SIGCHI fees remained the same, but whereas before SIGCHI membership included UIST and Human Factors conferences proceedings, these are now an extra cost option. Bundling that back into the basic rate, equivalent services have gone up 100% in cost.

SIGOIS membership cost has up 33%, but they've also split out the Computer Supported Cooperative Work conference proceedings that used to be included with membership. Adding that cost back in means this SIG also has doubled its membership fee.

What really galls me is that the ACM sent out brochures a couple months ago touting their new approach to providing member services, and tried to make it sound like they were offering NEW services. But with the exception of a couple, like SIGGRAPH, all the "plus" services appear to be just splitting the costs into smaller piles so that they don't look so big. But their recommended changes to my membership would have me paying 90% more than last year for a 31% increase in services (measured by cost, not by value), and, curiously, a 31% inflation rate on the publications I got last year.

Is anyone out there as galled by this extortion as I am?

Robert Reed Home Animation Ltd. 503-656-8414
robert@slipknot.rain.com 5686 First Court, West Linn, OR 97068

SHOOTING YOURSELF IN THE FOOT IN VARIOUS LANGUAGES AND SYSTEMS

Motif: You spend days writing a UIL description of your foot, the trajectory, the bullet, and the intricate scrollwork on the ivory handles of the gun. When you finally get around to pulling the trigger, the gun
.....

Discussions

During the implementation of the algorithm, problem was simplified by choosing only four categories: 'rec.sport.hockey', 'talk.religion.misc', 'comp.graphics', 'sci.space'. Subsequently, the texts were converted into tf-idf or tf vectors and then trained on the Naïve Bayes classifier. For the testing set, the one provided by the dataset was used, then simply converted and the classification done.

▼ Lab 6. Natural Language Processing

Task 6.3 Topic Modelling

Problem Descriptions

In this topic modelling task, the objective is to discover the semantic structure of a vast text corpus. One method of topic modelling is the latent Dirichlet, which is based on considering a different hidden topic for each document in a corpus. This is done by maximising the posterior probability of the corpus given the topic and words.

Implementation and Results

```
1 import nltk
2 from nltk.corpus import stopwords
3 from nltk.stem.snowball import SnowballStemmer
4 from gensim import models, corpora
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25 ]

1 # Clean the data by using stemming and stopwords removal
2 nltk.download('stopwords')
3 stemmer = SnowballStemmer('english')
4 stop_words = stopwords.words('english')
5 texts = [
6     [stemmer.stem(word) for word in document.lower().split() if word not in stop_words]
7     for document in documents
8 ]

1 # Create a dictionary from the words
2 dictionary = corpora.Dictionary(texts)
3
4 # Create a document-term matrix
5 doc_term_mat = [dictionary.doc2bow(text) for text in texts]
6
7 # Generate the LDA model
8 num_topics = 2
9 ldamodel = models.Ldamodel.LdaModel(doc_term_mat,
10     num_topics=num_topics, id2word=dictionary, passes=25)
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```

```

9  for text in list_of_strings:
10     details = text.split('*')
11     print("%-12s:%0.2f%%" %(details[1], 100*float(details[0])))
12

0.035*"intellig" + 0.035*"human" + 0.025*"machin" + 0.015*"field" + 0.015*"call"
0.036*"play" + 0.036*"team" + 0.036*"goal" + 0.026*"ball" + 0.026*"game"

Top 5 contributing words to each topic:

Topic 0
"intellig" :3.50%
"human" :3.50%
"machin" :2.50%
"field" :1.50%
"call" :1.50%

Topic 1
"play" :3.60%
"team" :3.60%
"goal" :3.60%
"ball" :2.60%
"game" :2.60%

1  new_docs = [
2
3  ""
4  Jager thinks this is just the start of AI eating the beautiful
5  game. "We have a dedicated team that focuses only on artificial
6  intelligence and machine learning for sports teams," he
7  says. "That is not only for soccer, but for Formula One and
8  American football. We have a baseball team, and we're talking
9  right now with cricket teams."
10
11
12 ""
13 ]
14
15 new_texts = [
16 [stemmer.stem(word) for word in document.lower().split() if word not in stop_words]
17 for document in new_docs
18 ]
19 new_doc_term_mat = [dictionary.doc2bow(text) for text in new_texts]
20
21 vector = ldamodel[new_doc_term_mat]
22 print(vector[0])
23

[(0, 0.5067322), (1, 0.49326774)]

```

Discussions

To apply the topic modelling algorithm, initially two texts with different content have been analysed, one on artificial intelligence and one on football. The texts have then been cleaned by removing the stop words and applying stemming. After this, a dictionary has been created and a document-term matrix constructed using the bag-of-words (BoW) model. The result we obtain is two groups of words, five for each text, from which we can extrapolate the two topics. Once we have trained the LDA implemented above, we can enter a new text to see if it contains the topics obtained previously. In fact, in the last part of the code, a new document was analysed and the output obtained shows that both topics are present, "AI" and "football".almost with the same percentage.

▼ Lab 7. Image Processing

Task 7.1 Face Detection

Problem Descriptions

The objective of this task is to implement an algorithm capable of performing a face detection operation from any image, exploiting the Haar cascade method. This is still one of the most widely used, although it is not always the most accurate, as it requires a frontal position of the face. The method to be used works by exploiting features, i.e. a synthetic representation calculated from pixel values. These are called Haar features and are calculated from the difference of the sums of pixels of two or more adjacent rectangular areas. The idea that gives the Haar cascade method its name, however, is the attempt to reduce the computational cost by organising the detection algorithm in a cascade of classifiers. These are applied in sequence to a certain window or portion of the image and if the features do not match a face, that window is immediately discarded and the algorithm moves on to the next one. The idea is that since the vast majority of tested windows are negative (i.e. do not contain the object), it is beneficial to reject them with as little computation as possible.

Implementation and Results

```
1 !pip install opencv-python
2 import cv2
3 from google.colab.patches import cv2_imshow

1 # Load the face detection model from the model file
2 !wget 'https://github.com/yongminli/data/raw/main/haarcascade_frontalface_default.xml'
3 face_cascade = cv2.CascadeClassifier('haarcascade_frontalface_default.xml')

1 # Load the model file and image files to Google Colab
2 from google.colab import files
3 file = files.upload()
4 file = files.upload()
5 file = files.upload()
```

▼ Testo del titolo predefinito

```
1 #@title Testo del titolo predefinito
2 # Read an input image
3 img = cv2.imread('Picture 1.jpg')
4 #img = cv2.imread('Picture 2.jpg')
5 #img = cv2.imread('Picture 3.jpg')
6
7 # Convert it into a grayscale image
8 gray = cv2.cvtColor(img, cv2.COLOR_BGR2GRAY)
9
10 # Detect faces
11 faces = face_cascade.detectMultiScale(image=gray, scaleFactor=1.2, minNeighbors=5, minSize=(50,50))
12 #faces = face_cascade.detectMultiScale(image=gray, minNeighbors=9)
13
14 # Display the detection results
15 for (x, y, w, h) in faces:
16     cv2.rectangle(img, (x, y), (x+w, y+h), (0, 255, 0), 2)
17 cv2_imshow(img)
18
19
20
```

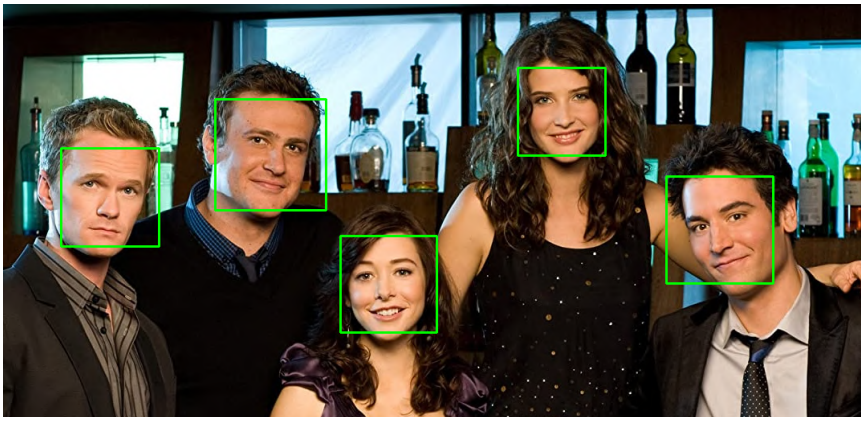




```

1
2
3
4
5 # Read an input image
6 #img = cv2.imread('Picture 1.jpg')
7 img = cv2.imread('Picture 2.jpg')
8 #img = cv2.imread('Picture 3.jpg')
9
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18 for (x, y, w, h) in faces:
19     cv2.rectangle(img, (x, y), (x+w, y+h), (0, 255, 0), 2)
20 cv2.imshow(img)
21
22

```



```

1 # Read an input image
2 #img = cv2.imread('Picture 1.jpg')
3 #img = cv2.imread('Picture 2.jpg')
4 img = cv2.imread('Picture 3.jpg')
5
6 # Convert it into a grayscale image
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14 for (x, y, w, h) in faces:
15     cv2.rectangle(img, (x, y), (x+w, y+h), (0, 255, 0), 2)
16 cv2.imshow(img)
17
18

```



Discussions

First of all, looking at the results, one can see that after processing the image, we obtain an output photo in which the detected faces are highlighted by a green rectangle. To test the implemented method, three images with different characteristics were chosen. In the first one, the faces present are all positioned frontally, which makes Haar's features particularly efficient. However, although all faces are detected correctly, there are some additional incorrect detections, such as the shoe of a player. This probably means that the positioning of light and shadow can sometimes deceive the classifier. In the second one there are fewer faces and they are more or less all frontal, which is why the algorithm detects them efficiently. Finally, the last image represents a series of players in motion, where therefore the faces are turned in different

directions, and in fact in the output image only some of the faces present have been detected, precisely because this method has difficulty in recognising faces that are not in a frontal position.

In addition, all photos were processed with the same value for the 'minNeighbors' parameter, but this can actually affect the result obtained. It specifies how many neighbours each candidate rectangle must have in order to maintain it. In other words, this parameter influences the quality of the detection. A higher value results in fewer detections but higher quality, with the advantage of eliminating false positives, but with the risk of ignoring faces.

▼ Lab 7. Image Processing

Task 7.2 Image Segmentation

Problem Descriptions

The topic addressed in this task is image segmentation, in other words, being able to detect and distinguish objects within an image.

Partitioning is done on the basis of the characteristics of pixels that are grouped into different regions. For the implementation, we will use a pre-built R-CNN model of approximately 246MB, to detect and contour objects in the picture.

Implementation and Results

```
1 !pip install pixellib
2 import pixellib
3 from pixellib.instance import instance_segmentation
4 import cv2
5 from google.colab.patches import cv2_imshow
6 !pip install tensorflow==2.4
```

```
1 # Download the mask rcnn model
2 !wget https://github.com/ayoolaolafenwa/PixelLib/releases/download/1.2/mask_rcnn_coco.h5 -O mask_rcnn_coco.h5
3 path = ""
4
5 # Alternatively you can save the data to your Google Drive, and load the data from there
6 #from google.colab import drive
7 #drive.mount('/content/drive')
8 #path = "/content/drive/My Drive/data/"
9
```

```
1 # Create the model object and load the trained model
2 model = instance_segmentation()
3 model.load_model(path + "mask_rcnn_coco.h5")
```

WARNING:tensorflow:From /usr/local/lib/python3.8/dist-packages/tensorflow/python/util/deprecation.py:605: calling map_fn_v2 (from tensorflow.python.ops.map_fn) is deprecated and will be removed in a future version. Instructions for updating:
Use fn_output_signature instead

```
1 # Load the image files to Google Colab
2 from google.colab import files
3 #file = files.upload()
4 #file = files.upload()
5 file = files.upload()
```

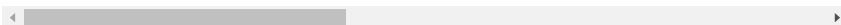
Nessun file selezionato Upload widget is only available when the cell has been executed in the current browser session. Please rerun this cell to enable.
Saving pic6.png to pic6.png

```
1 input = path + "pic1.jpg"
2 img = cv2.imread(input)
3 cv2_imshow(img)
4
```



```
1 segmask, output = model.segmentImage(input, show_bboxes= False)
2 #print(segmask)
3
4 cv2_imshow(output)
```

/usr/local/lib/python3.8/dist-packages/tensorflow/python/keras/engine/training.py:2325: UserWarning: warnings.warn("`Model.state_updates` will be removed in a future version. '



```
1 input = path + "pic2.jpg"
2 img = cv2.imread(input)
3 cv2_imshow(img)
```



```
1 segmask, output = model.segmentImage(input, show_bboxes= False)
2 #print(segmask)
3
4 cv2_imshow(output)
```



```
1 input = path + "pic6.jpg"
2 img = cv2.imread(input)
3 cv2.imshow(img)
```



```
1 segmask, output = model.segmentImage(input, show_bboxes= False)
2 #print(segmask)
3
4 cv2.imshow(output)
```




Discussions

In order to test the implemented algorithm, three images with different characteristics were inserted to understand just how the model behaves. The first depicts a road junction, with therefore several elements to be detected. The algorithm in this case was quite efficient, as most of the people, cars and traffic lights in the picture were highlighted. In the second picture, it was tested with animals, although with fewer elements than in the first. Again, almost all dogs and people present were detected, although it is evident how it struggles to portion out two figures that are overlapping, for example two dogs in the picture. This is especially evident in the last image, in which a busy road is shown, and it is clear that in the right-hand roadway, where the cars are further apart, the model is more efficient, compared to the left where there is a lot of overlap.

▾ Lab 7. Image Processing

Task 7.3 Object Recognition

Problem Descriptions

The last task concerns object recognition, a computer vision technique to identify objects in images or videos. The model that will be used is YOLO (You Only Look Once), currently one of the most advanced as it only scans the image once, as the name suggests, unlike the R-CNN, Fast R-CNN and Faster R-CNN methods. There will be two models within the algorithm, a version called 'yolov3' which is more precise but slower, and a version called 'yolov3-tiny' which is the opposite, faster and less accurate.

Implementation and Results

```
1 !pip install cvlib
2 import cvlib
3 from cvlib.object_detection import draw_bbox, YOLO

1 # Download the YOLOv3 model configuration, weights and labels files
2 #!wget https://github.com/yongminli/data/raw/main/yolov3-tiny.cfg -O yolov3-tiny.cfg
3 #!wget https://github.com/yongminli/data/raw/main/yolov3-tiny.weights -O yolov3-tiny.weights
4 #!wget https://github.com/yongminli/data/raw/main/yolov3.txt -O yolov3.txt
5
6 #!wget http://www.brunel.ac.uk/~csstyyl/tmp/yolov3.cfg -O yolov3.cfg
7 #!wget http://www.brunel.ac.uk/~csstyyl/tmp/yolov3.weights -O yolov3.weights
8 #!wget http://www.brunel.ac.uk/~csstyyl/tmp/yolov3.txt -O yolov3.txt
9 #path = " "
10
11 # Alternatively you can save the data to your Google Drive, and load the data from there
12 from google.colab import drive
13 drive.mount('drive')
14 path = "drive/My Drive/data/"
15
```

Mounted at drive

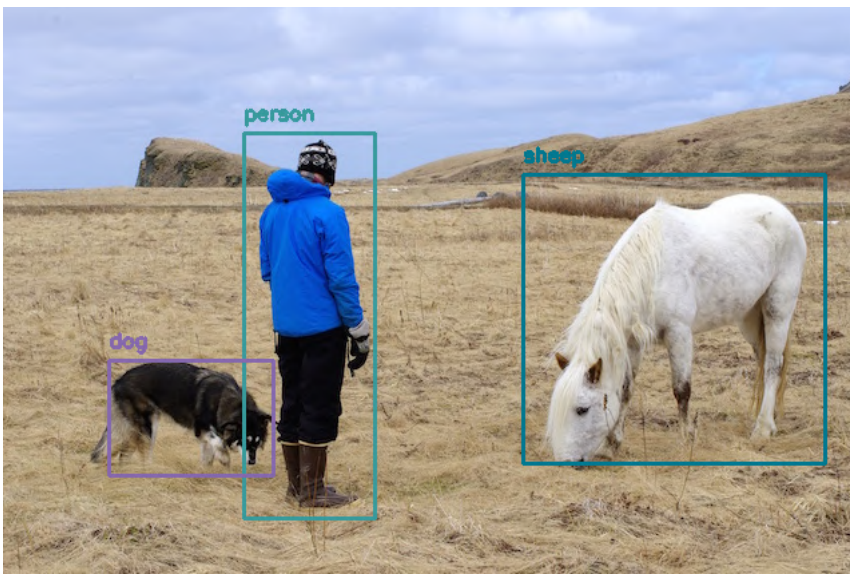
```
1 # The default YOLO model files
2 #config = path + 'yolov3.cfg'
3 #weights = path + 'yolov3.weights'
4 #labels = path + 'yolov3.txt'
5
6 # # Alternative the "tiny" version of YOLO, which is faster but less accurate
7 config = path + 'yolov3-tiny.cfg'
8 weights = path + 'yolov3-tiny.weights'
9 labels = path + 'yolov3.txt'
10
11 # Construct the YOLOv3 Model
12 yolo = YOLO(weights, config, labels)
13
```

[INFO] Initializing YOLO ..

```
1 # # Load the image files to Google Colab
2 from google.colab import files
3 file = files.upload()
```

Scegli file Nessun file selezionato Upload widget is only available when the cell has been executed in the current browser session. Please rerun this cell to enable

```
1 import cv2
2 from google.colab.patches import cv2_imshow
3
4 # Read an image file
5 img = cv2.imread(path+'objects1.jpg')
6 img = cv2.imread(path+'objects2.jpg')
7 cv2_imshow(img)
8
9 print()
10
11 # Detect objects from the image, and display the results
12 bbox, label, conf = yolo.detect_objects(img)
13 # bbox, label, conf = yolo.detect_objects(img, confidence=0.25, nms_thresh=0.2)
14 yolo.draw_bbox(img, bbox, label, conf)
15 cv2_imshow(img)
```



Discussions

To test the algorithm, it was used an image in which there is a person and two different animals. The purpose of the yolo method is then to detect all the elements in the image, frame them, and specify what they are. As mentioned above, for this task we tried using two versions of Yolo ("yolov3" and "yolov3-tiny"), which perform differently. In the first case, using the 'yolov3' version, the result obtained is efficient, as all the elements in the picture were detected and each was given the right name. In the second case, on the contrary, by applying the 'tiny' version, the result was obtained faster, but the efficiency of the detection decreased, because the algorithm was able to detect all the elements, but was not precise in the definition of the horse, which was mistaken for another animal.