



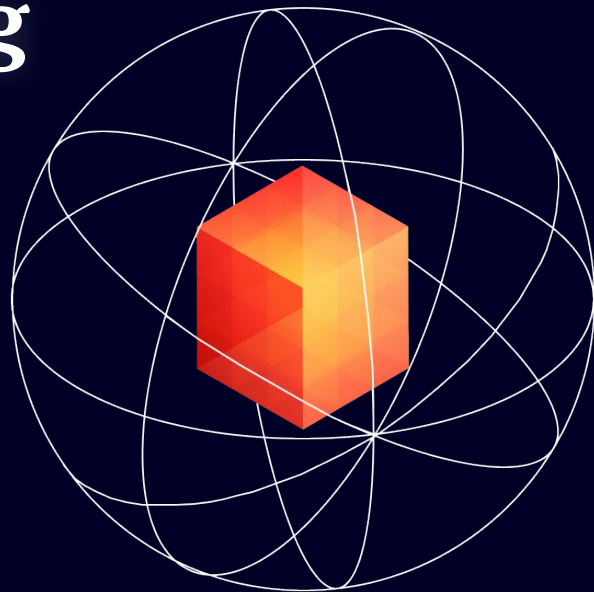
# Beyond Recursive Proving for Validity Rollups

Advanced Proving for Starknet

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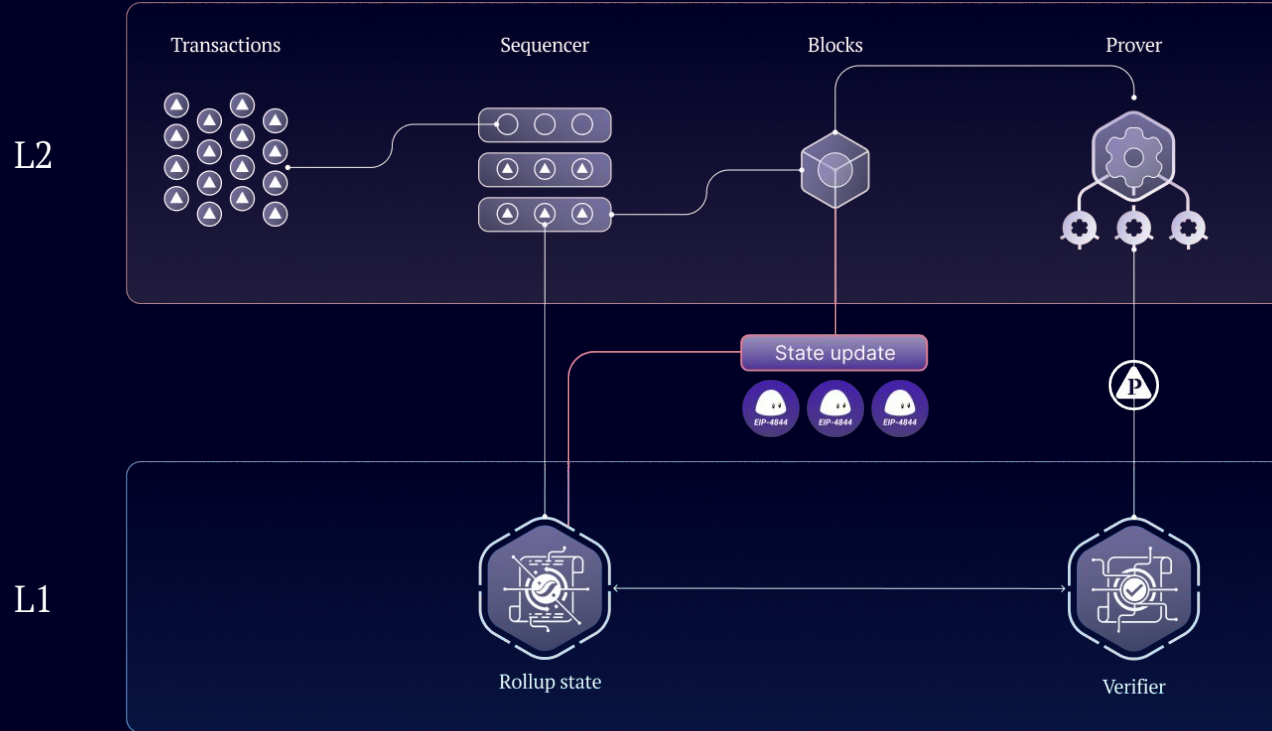


## Section 1

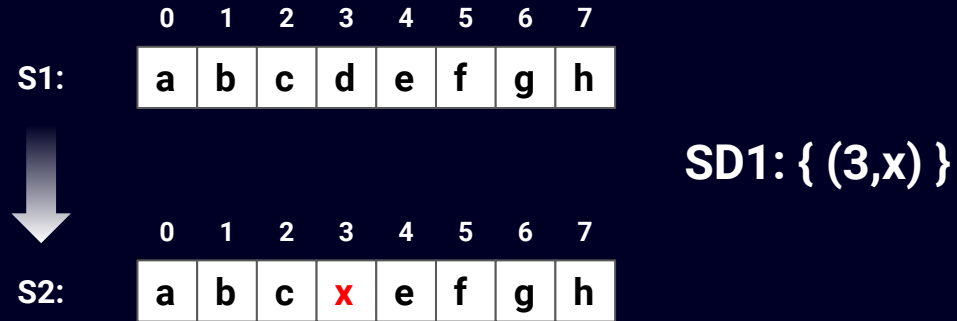
# Basics of Validity Rollups



# Basics of L2 Validity Rollups



# What is State Diff?



## Per Block Proving

State A, txs



**Statement:**

Txs correctly  
sequenced on input  
state resulting in  
output state



State B,  
State Diff

## Per Block on L1

- Verify block proof
- Publish state diff
- Update state  
(+ messaging)

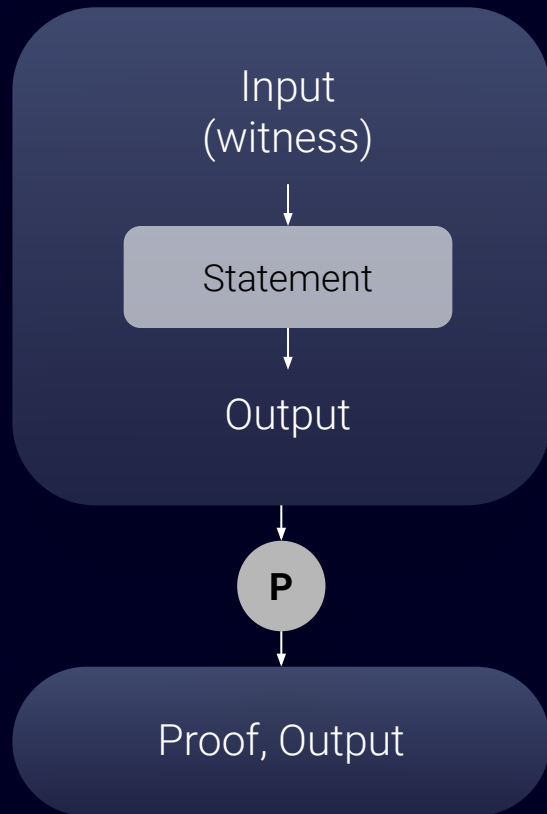
**Costly unless blocks  
are big (can mean long  
block times)**

## Section 2

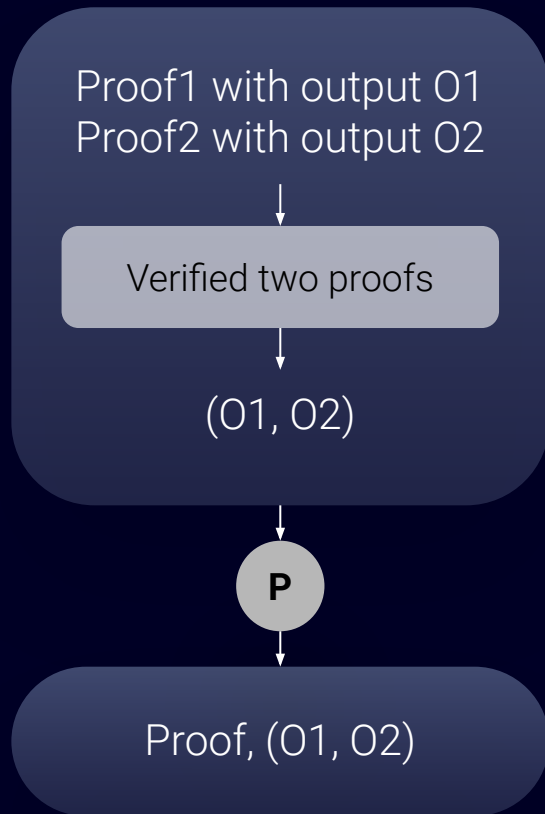
# Validity Rollups with Recursive Proving



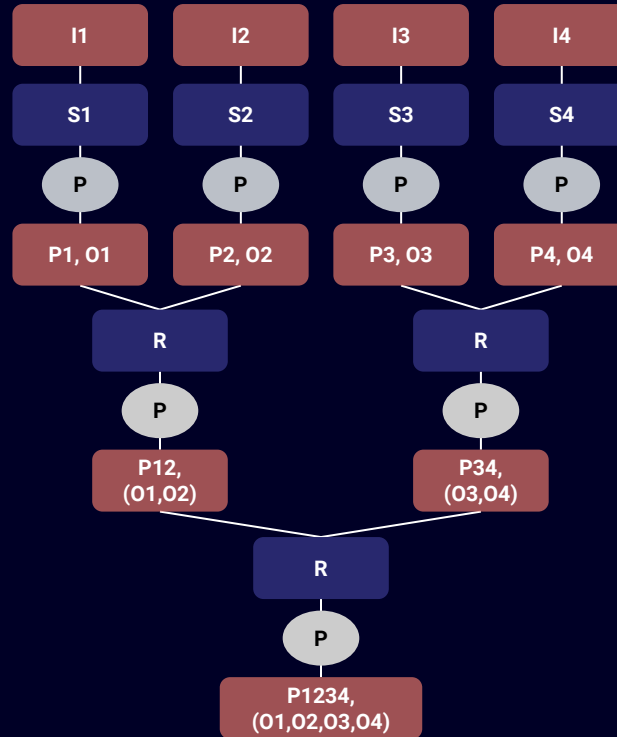
## Generic Proving



## Recursive Proving

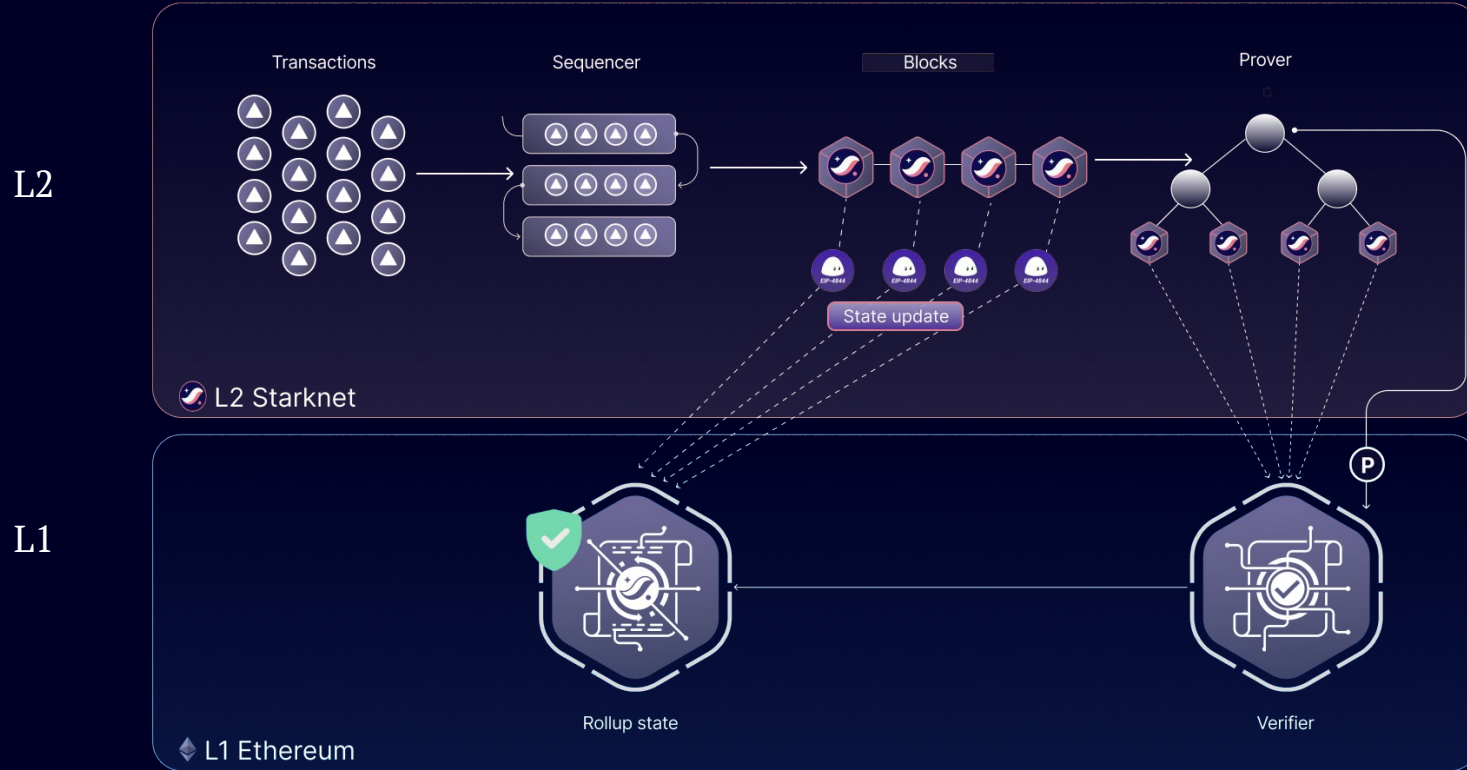


# One Proof for Many Statements

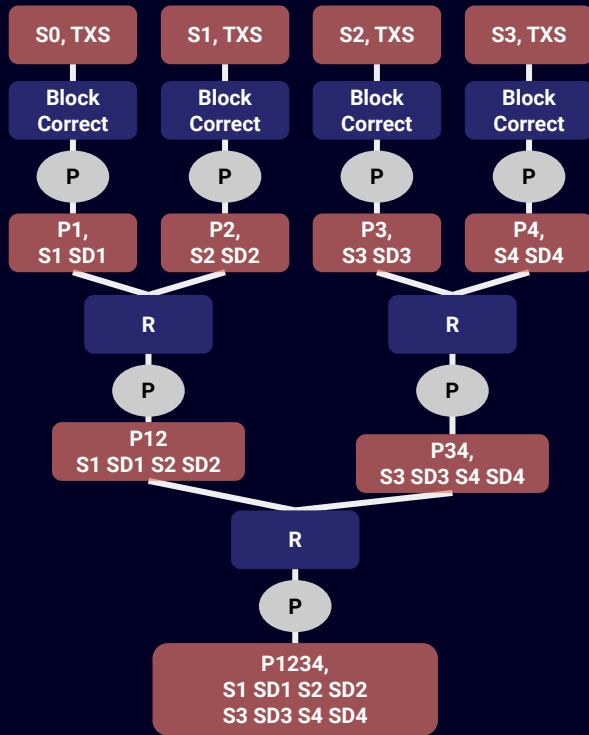




# L2 Validity Rollup with Recursive Proving



# Validity Rollup With Recursion



## Per Recursion on L1:

- Verify block proof

## Per Block on L1:

- Publish state diff
- Update state  $S_i \rightarrow S_{i+1}$  (+ messaging)

Less Costly unless blocks are very small (e.g., we want fast finality)

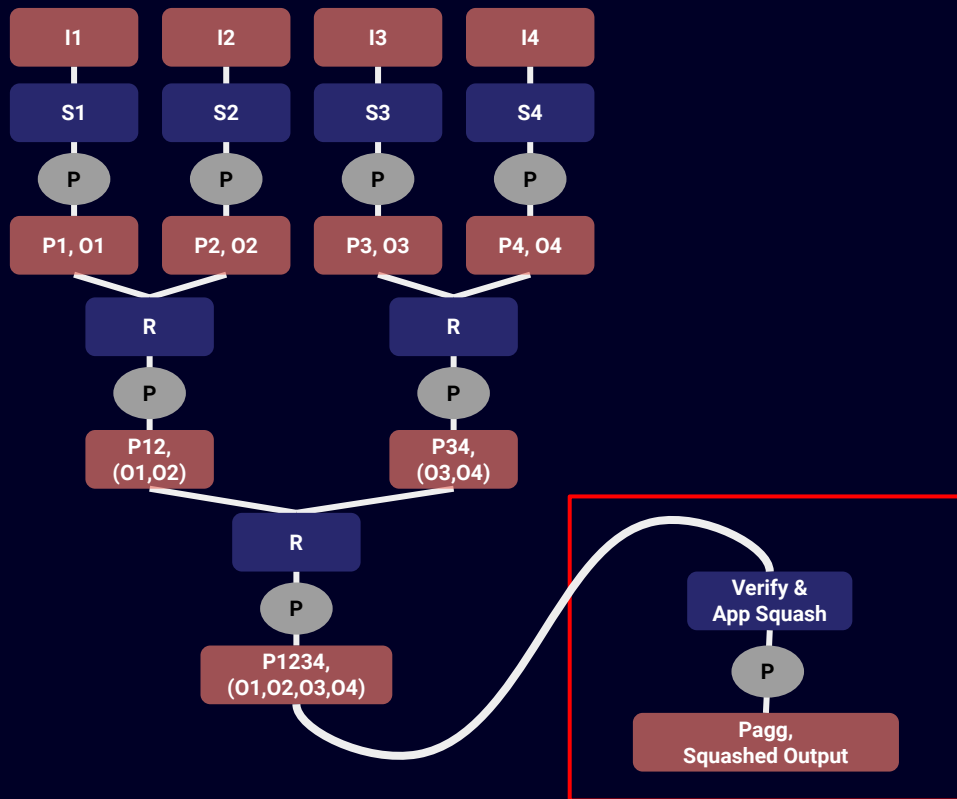
We would like to optimize per block updates

Section 3

# Validity Rollups with Applicative Recursion



# One Proof for Many Statements + Applicative Squash



# State Diff Aggregation

S1: 

0	1	2	3	4	5	6	7
a	b	c	d	e	f	g	h

S2: 

0	1	2	3	4	5	6	7
a	b	c	x	e	f	g	h

S3: 

0	1	2	3	4	5	6	7
a	b	c	x	e	y	z	h

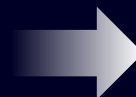
S4: 

0	1	2	3	4	5	6	7
a	b	c	v	e	y	w	h

SD1: { (3,x) }

SD2: { (5,y), (6,z) }

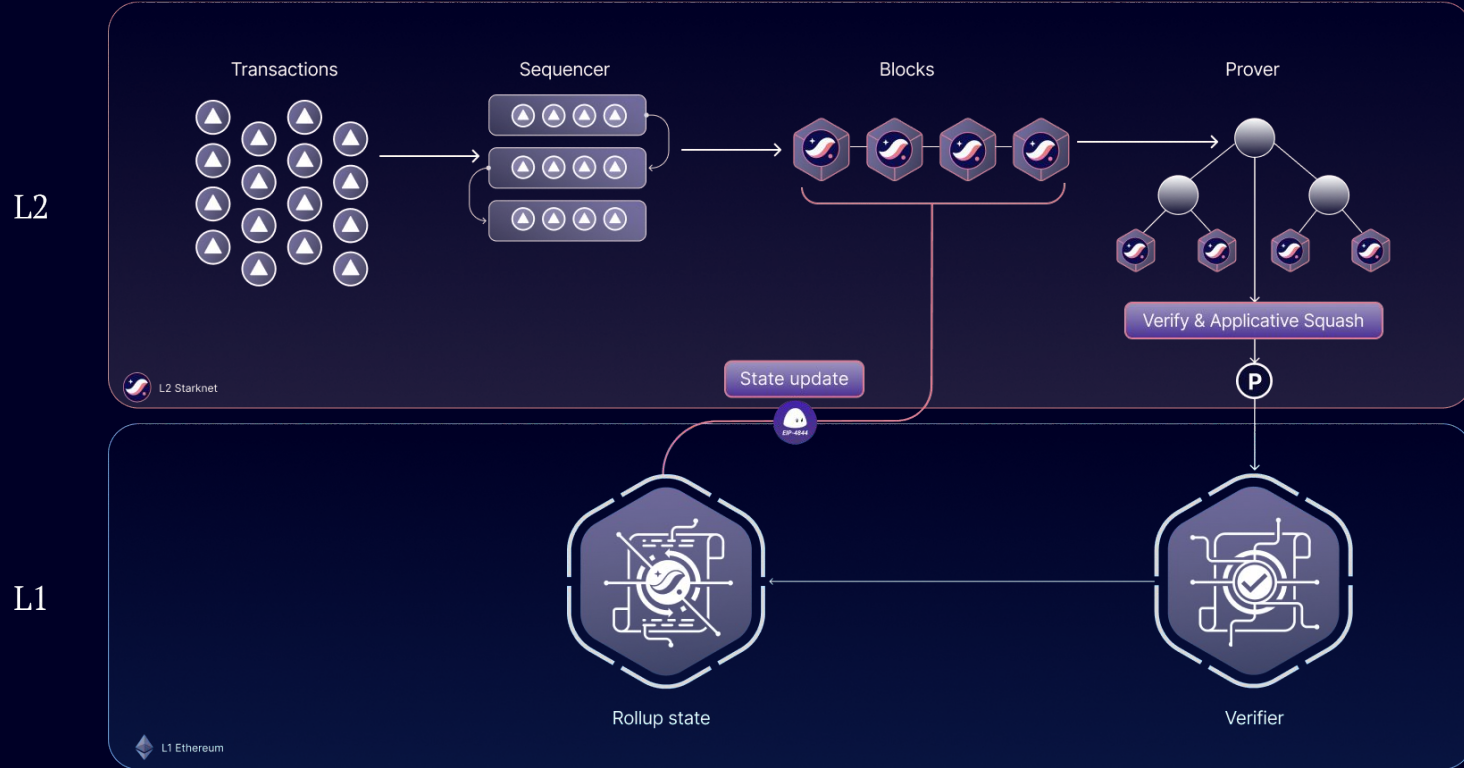
SD3: { (3,v), (6,w) }



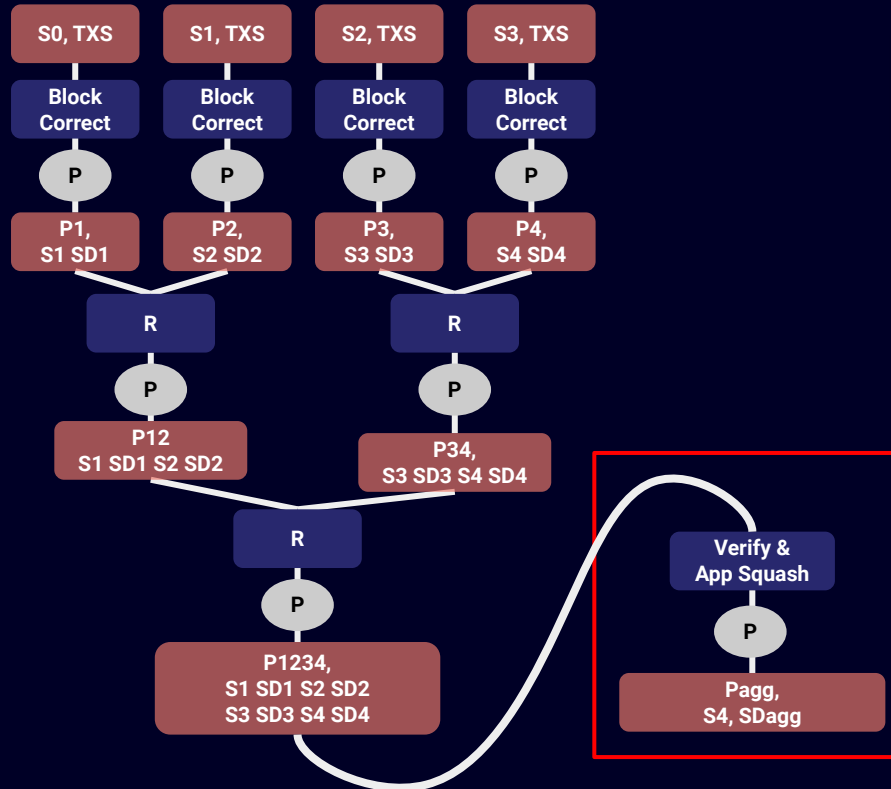
**SDagg: { (3,v), (5,y), (6,w) }**

(Only the last update)

# L2 Validity Rollup with Applicative Recursion



# Validity Rollup With Applicative Recursion



## Per Recursion on L1:

- Verify block proof (Pagg)

## Per Recursion on L1:

- Publish state diff
- Update final state directly (+ messaging)

The more blocks per recursion,  
the lower the L1 cost  
L2 finality can be very fast!

## What else can Applicative Recursion do?

- Stateless Data Compression
  - Represent the data more efficiently
- Remove the need for state updates on L1:
  - $S1 \rightarrow S2, S2 \rightarrow S3, S3 \rightarrow S4$  becomes  $S1 \rightarrow S4$
- Segmentation of large statements
  - E.g., prove that the state of a VM at the end of one segment is the state of the VM at the beginning of another segment
- Your idea here :)



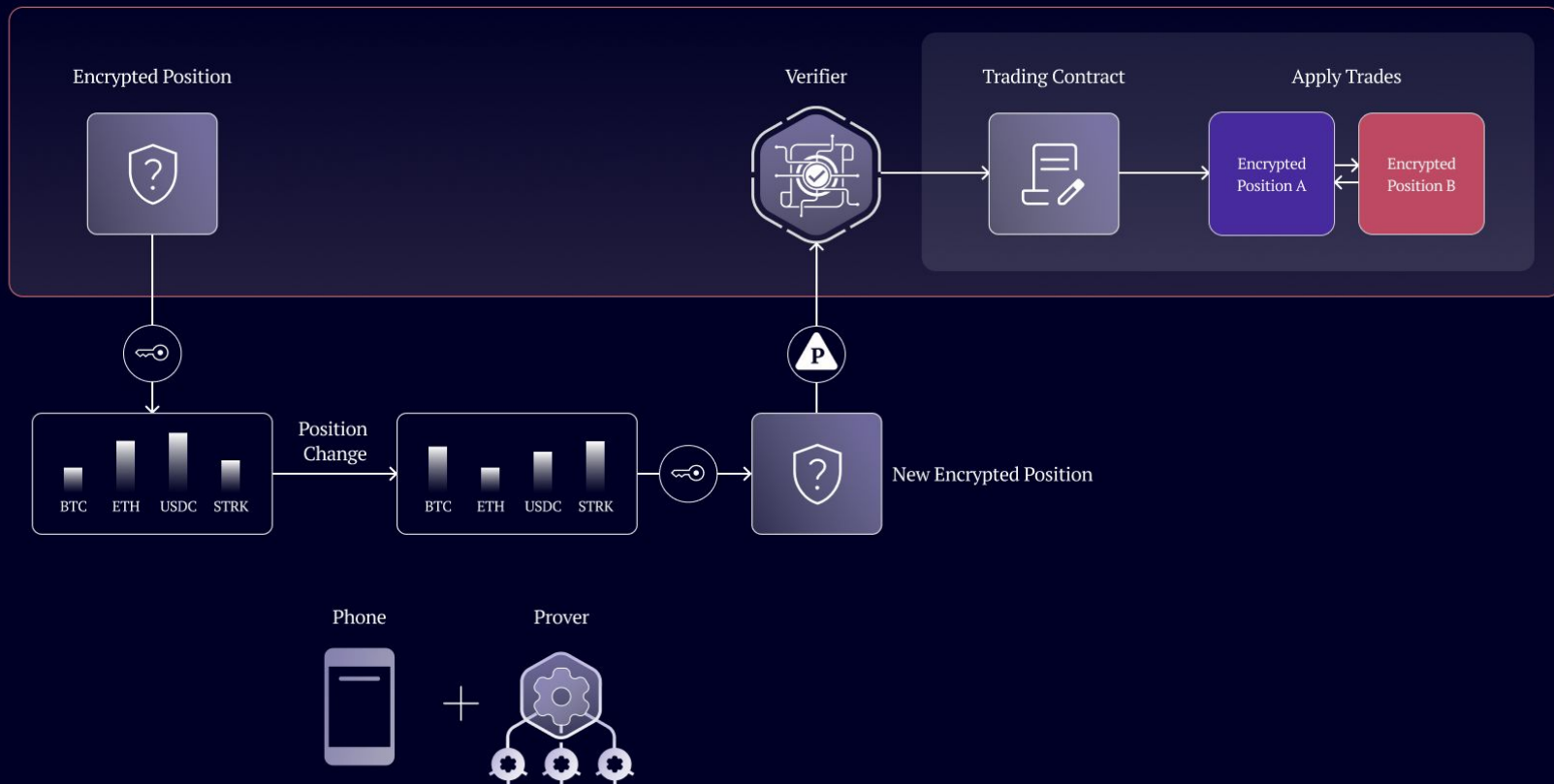
## Section 4

# Other Use Cases for Offchain Proofs

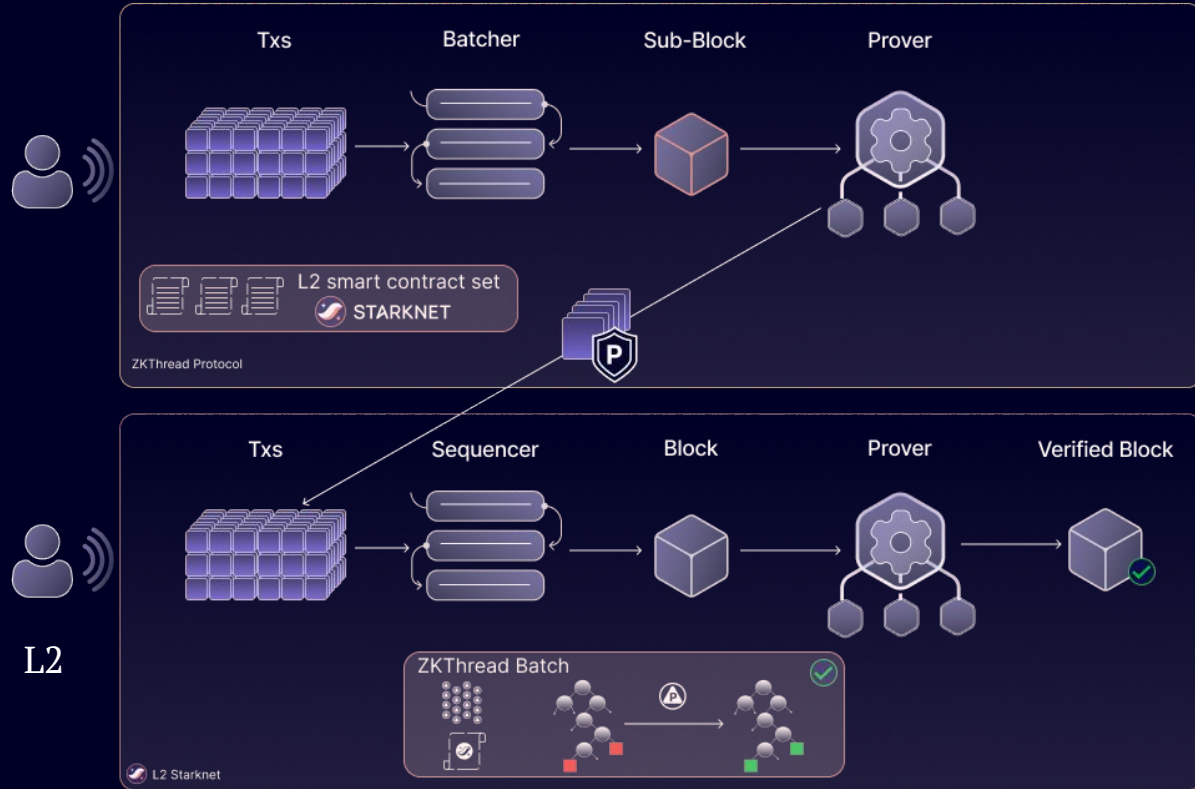


# Offchain Proofs for Privacy

L2



# Offchain Proofs for ZK Threads





# Thank you!

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