

# What is the value of the LP position?

Under no arbitrage, position of numeraire  $\mathbf{R_1}$  and asset  $\mathbf{R_2}$  with price  $\mathbf{p}$  at time  $\mathbf{t}$  has value

$$V(p,t) = \text{minimize} \qquad R_1 + pR_2$$
  
subject to  $R \in S_t$ 

where  $\mathbf{S}_{\mathbf{t}}$  is the set of allowable states of the AMM at time  $\mathbf{t}$ .

Constant function market maker (CFMM):

$$S_t = \{R \mid \varphi(R) \ge k\}$$

### **Example: Constant Product AMM**

For a constant product AMM with  $\, \varphi(R) = \sqrt{R_1 R_2} \, \Box$ 

$$V(p,t) = 2k(\sqrt{p} - \sqrt{p_0}) + \mathbf{fees}(t)$$

#### Considerations:

- Do I want this derivative?
- What rebalancing costs do I pay arbitrageurs? (LVR)
- How can I hedge the price movement?

### Replicating Market Makers: V $\rightarrow \phi$

### Examples in practice:

- Zero coupon bonds at maturity (yield token pools)
- Weighted portfolios (geometric mean MMs, perpetual exchange lending pools)
- Covered calls & other options
- [Proposed] prediction markets

### General theory [Angeris et al. 2021, 2023]

• For **V** concave, homogeneous, increasing:

$$\phi(R) = \inf_{p>0} \left( \frac{R_1 + pR_2}{V(p)} \right)$$

# Why do some work & some fail?

Key factors (hypotheses):

Ease of **hedging** price movement

Amount extracted by **arbitrage** 

Usefulness of custom V(p, t)

(if desire "delta neutral" strategy)

(LVR or "rebalancing fees")

(is the portfolio value useful?)

# There are over \$10T of assets in ETFS

Let's bring passive liquidity on chain.

