

How much security does your restaking protocol *really* need?

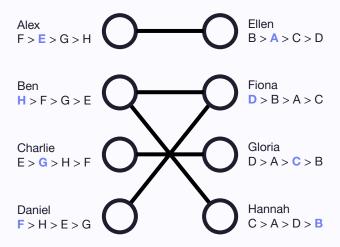
Scaling laws for security

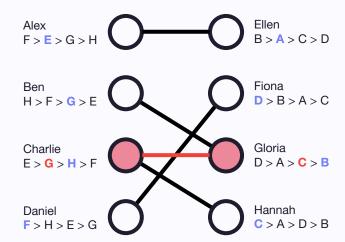
Tarun Chitra | Devcon Bangkok | November 14, 2024

A Tripartite Tale

- Restaking is a decentralized matching market
- 2. Threat model determines economic security
- 3. Minimum amount of security to pay for can be quantified by cascading risks

Act I: Matching Markets & Restaking

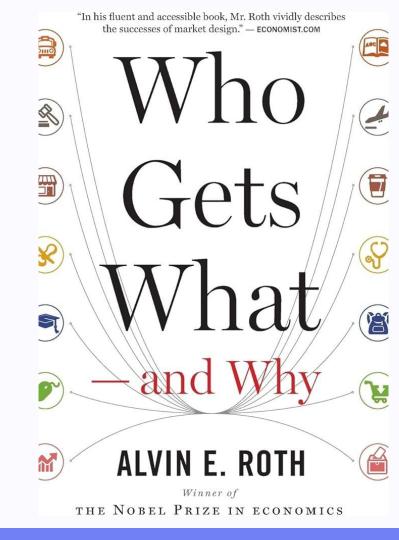




What is a matching market?

- Matching markets are everywhere
 - Kidney exchanges
 - Hospital <> Resident matching
 - Dating apps

- Main idea:
 - Supply: Inhomogenous goods (with some shared properties)
 - Demand: Buyers with constraints on what they can buy (i.e. kidney compatibility)



Matching vs Auctions

Auctions focus on maximizing profit for the seller or welfare of both the buyer and seller

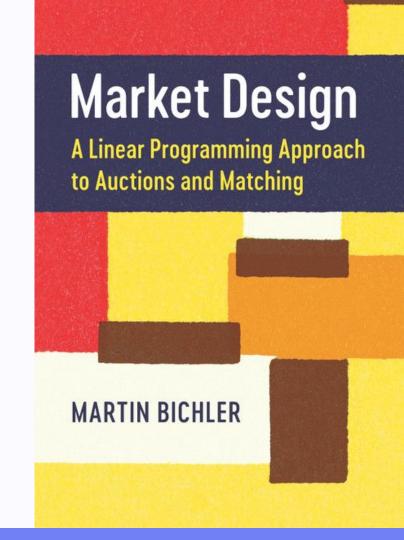
i.e. Good outcome for the seller to sell only 1% of their goods if it is revenue maximizing

Matching markets are focused on maximizing matches and stability to perturbations vs. pure profit

Allows for mechanism design without money

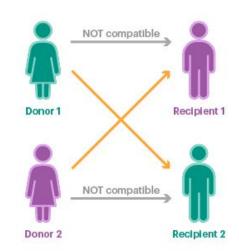
e.g. Stable Matching Theorem

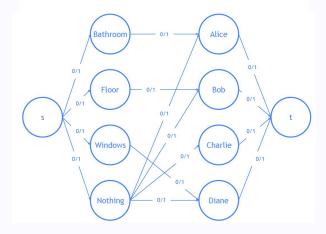
Crypto has both: MEV auctions vs. intents (matching)



Matching Markets & Graph Theory

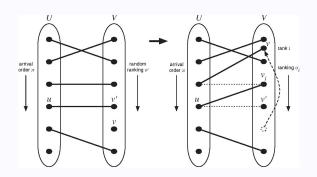
- Natural representation of a matching market is as a bipartite graph
 - One bipartition is the supply side, other is demand
- This graph is
 - Static (i.e. fixed ahead of time)
 - Has a central planner (i.e. National Kidney Registry) chooses the allocation or matching
- Decentralized matching markets don't have either of these features — parties utilize incentives to learn an (approximately) optimal matching





Restaking is a Decentralized Matching Market

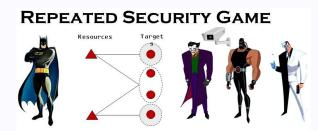
Why are decentralized matching markets so much harder to analyze?



Permissionlessness means you can be 'unmatched' with as people join and leave at will



No central planner → Rely purely on incentives to reach equilibria



Defending against multiple attacker types.

- 1. Each attacker type has different but known preferences.
- Attackers arrive in unknown order/frequency.
 Defender's goal:
- 1. Choose randomized strategies in an online fashion.

Requires explicit adversarial model

Act II: What is economic security?









Quantifying Economic Security in PoS

Defining economic security in an

sense is difficult, e.g.

But the cost is

linear in the discounted numéraire (e.g. stablecoin) value stake

Minimum percentage of stake needed for an attack

Expected time to execute attack

Cost of Attack = $\mathscr{C}(t) \ge Ce^{k\tau} p(t) \Sigma(t)$

Amount of asset staked

Price in numéraire terms of staking asset

Economic Security for Restaking

1. 📈

δΣ(t)

2.

$$\mathscr{C}^{R}(t) \ge Cg(\delta \Sigma(t))e^{k\tau}p(t)(1+\delta)(1-R)\Sigma(t)$$

Price impact function

(i.e. how much does the price go up when people buy of stake and add it to the network?)

Risk Measure

Percentage of stake that is lost under a worst or average case threat model

When is restaking safe?

$$\mathscr{C}^R(t) - \mathscr{C}(t) \geq 0$$

$$\updownarrow$$

$$Ce^{k\tau}p(t)\Sigma(t) \Big(g(\delta\Sigma(t))(1+\delta)(1-R)-1\Big) \geq 0$$

$$\updownarrow$$

$$R \leq 1 - \frac{1}{(1+\delta)g(\delta\Sigma(t))}$$
Dependence on dynamic elasticity of borrowers to incentives (e.g. points, tokens, fees)

Brief Detour: Comparison with Rollups

1.

2

Q: When does revenue from *n* rollups breakeven with monolithic L1 revenue?

A (C & Pai, 2024): n rollups need at most $\Theta(n^2)$ more revenue

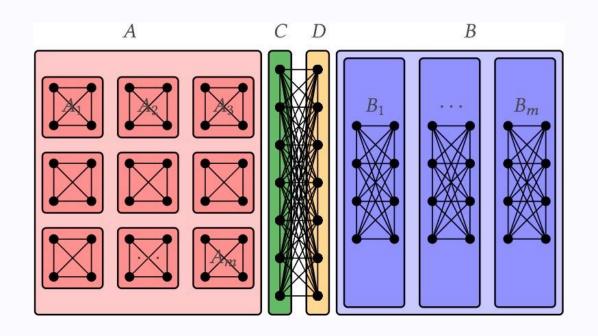
Q: When does revenue from S AVSs compensate for restaking risk?

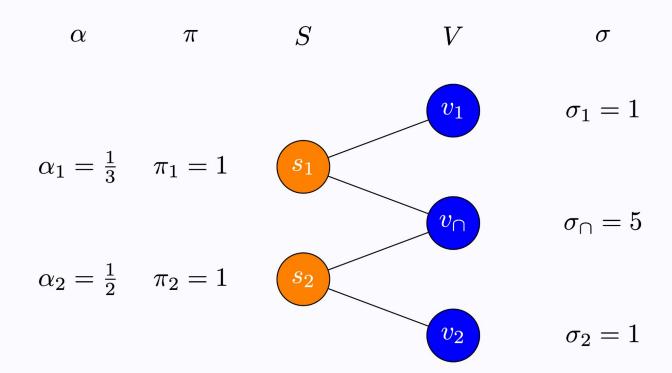
A (C & Pai, 2024): S rollups need at most $\Theta\left(1+\frac{1}{S^{3/2}}\right)$ more revenue

Question:

Can we model restaking risk the network price or stake dynamics?

Act III: Restaking Graphs, Cascades, and All That





Node Operators v_1 $\sigma_1 = 1$ v_{\cap} $\sigma_{\cap} = 5$

 α

 π

S

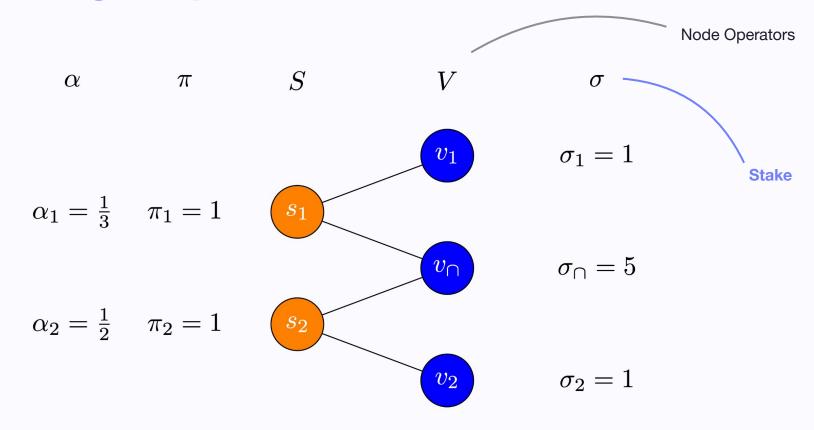
 $\alpha_1 = \frac{1}{3} \quad \pi_1 = 1$

 $\alpha_2 = \frac{1}{2} \quad \pi_2 = 1$



 v_2

 $\sigma_2 = 1$



Services (AVSs)

Node Operators

Stake

 α

 v_1

 v_{\cap}

 σ

$$\alpha_1 = \frac{1}{3} \quad \pi_1 = 1$$

$$\pi_1 = 1$$

 $\sigma_1 = 1$

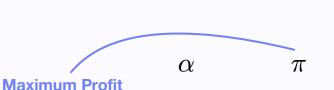


$$\alpha_2 = \frac{1}{2} \quad \pi_2 = 1$$

 s_2

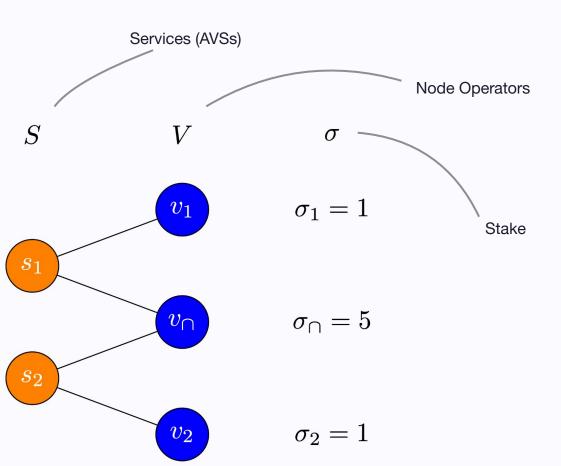
 v_2

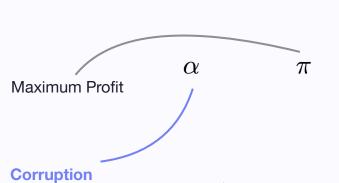
 $\sigma_2 = 1$





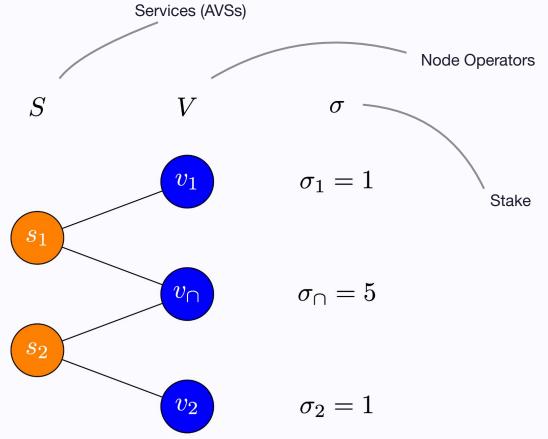
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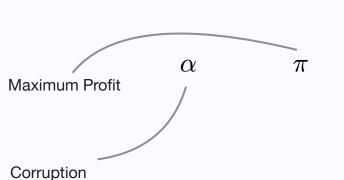


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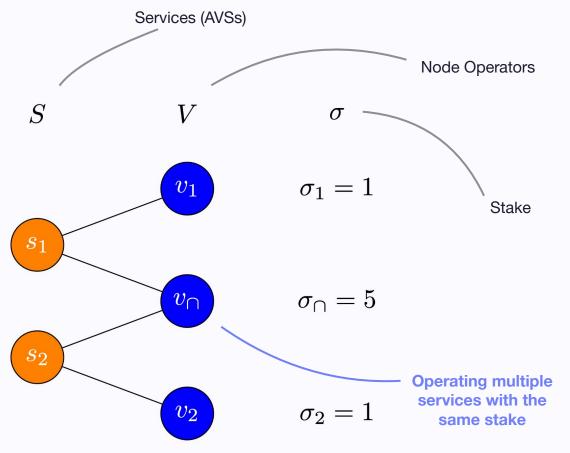


Threshold

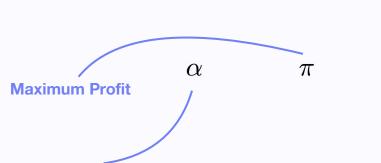


$$\alpha_1 = \frac{1}{3}$$
 $\pi_1 = 1$

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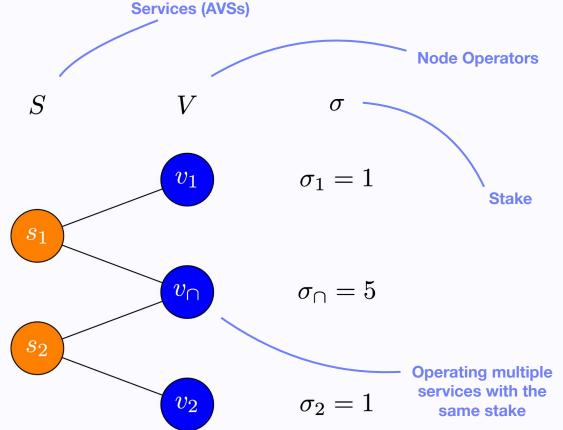
Threshold



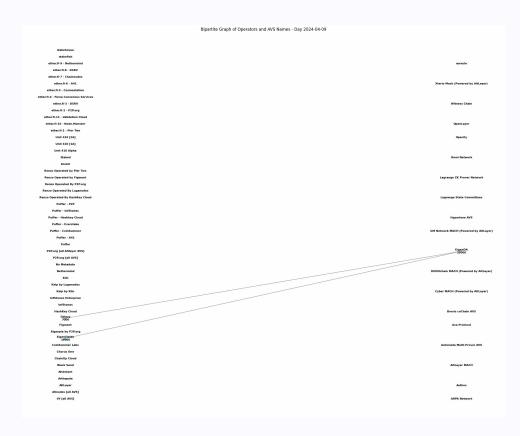
Corruption Threshold

$$\alpha_1 = \frac{1}{3} \quad \pi_1 = 1$$

$$\alpha_2 = \frac{1}{2} \quad \pi_2 = 1$$



Eigenlayer Restaking Graph over Time





Profitability

Feasibility

Profitability

Maximum Profit from Attacking Services $A \subseteq S$

>

Maximum Slashing Penalty for attacking cartel B ⊂ V

Feasibility

Profitability

Maximum Profit from Attacking Services $A \subset S$

>

Maximum Slashing Penalty for attacking cartel B ⊂ V

Feasibility

For every service $s \in A$:

Stake held by attacking cartel $B \subset V$ that is operating s

>

 a_s x total stake at s

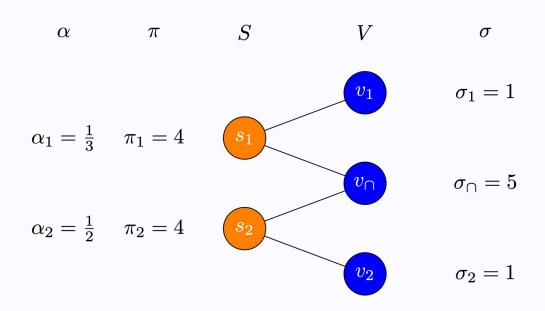
Profitability

$$\sum_{s \in A} \pi_s > \sum_{v \in B} \sigma_v$$

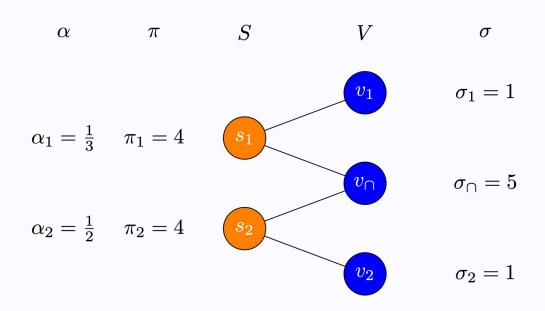
Feasibility

$$\forall s \in A \sum_{v \in B \cap \partial s} \sigma_v > \alpha_s \sum_{v \in B} \sigma_v$$

Def. from Eigenlayer whitepaper + Durvasula and Roughgarden, 2024



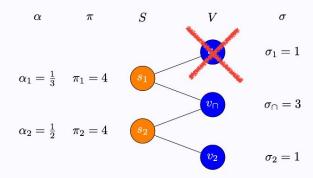
Each individual service is over-collateralized in that Profit < Stake at each service...



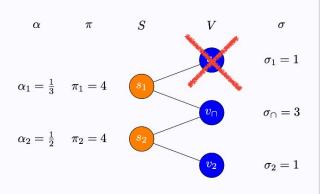
But all of the validators colluding can profitably attack both services:

$$8 = \pi_1 + \pi_2 > \sigma_1 + \sigma_0 + \sigma_2 = 7$$

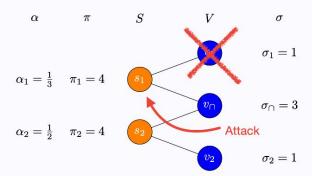
Step 1: Lose a fraction ψ of stake



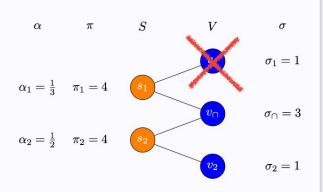
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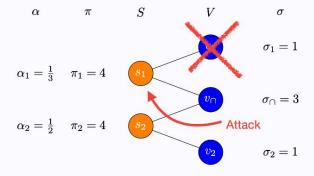
Step 2: Creates new profitable attacks



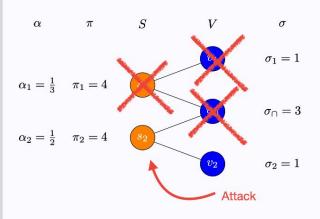
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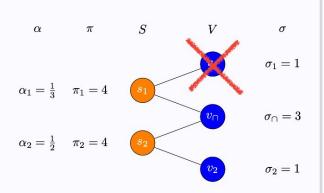
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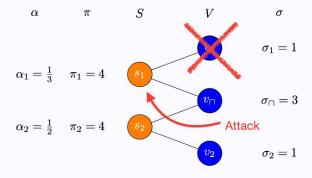
Step 3:
Repeat until no further attacks possible



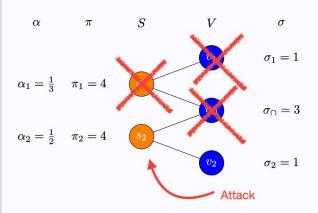
Step 1: Lose a fraction ψ of stake



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Step 3:
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This is the PoS version of a lending liquidation cascade

Quantifying Cascading Attacks

$$(A_1,B_1),\ldots,(A_T,B_T)$$

Valid Attack Sequence:

Services $(A_t \subseteq S)$, Operators $(B_t \subseteq V)$ forming a profitable and feasible attack after attacks $(A_1, B_1), ..., (A_{t-1}, B_{t-1})$ executed.

Quantifying Cascading Attacks

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$$R_{\psi}(G) =$$

Maximum percentage of stake that can be lost due to a cascade attack given an initial loss of ψ percent of stake

(Worst-case version of R in earlier analysis)

Quantifying Cascading Attacks

$$(A_1,B_1),\ldots,(A_T,B_T)$$

Valid Attack Sequence:

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$$R_{\psi}(G) = \max_{D \in D_{\psi}(G)} \max_{(A_1,B_1),...,(A_T,B_T)} \frac{\sum_{v \in \bigcup_t B_t} \sigma_v}{\sum_{v \in V} \sigma_v} \text{ Total stake lost in attack}$$
 Initial Stake in network

Set of validators with less than $\psi\%$ of total stake

How much stake do we need to secure an AVS?

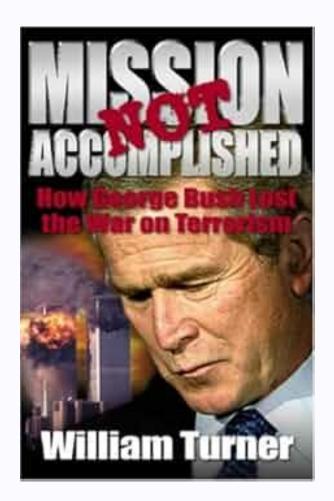


Enough stake σ such that R (G) is smaller than some tolerated amount (i.e. restaking network is willing to lose 5% of stake given $\psi \leq 33\%$)

Bad News

Theorem (Durvasula & Roughgarden, 2024):

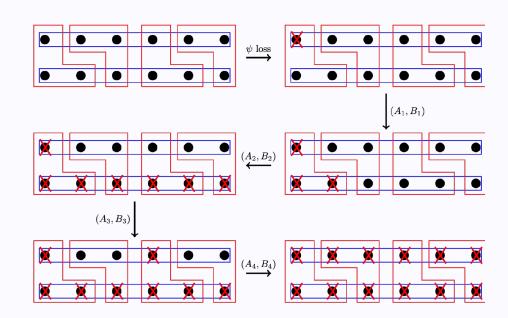
There exist an infinite family of graphs G_n with n validators such that $R_{\psi}(G_n) = 1$



Bad News

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If a restaking graph G is γ -overcollateralized, then $R_{\psi}(G) \leq \psi(1+\gamma^{-1})$

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Translation:

PoS analogue of "Your decentralized stablecoin needs to be sufficiently overcollateralized to avoid cascading depeg events"

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But:

Overcollateralization condition is so strong that for many graphs every service is overcollateralized as much as the total profit $\pi_1+...+\pi_S$

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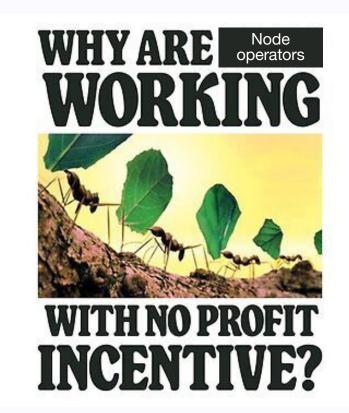
Overcollateralization condition is so strong that for many graphs every service is overcollateralized as much as the total profit $\pi_1 + ... + \pi_s$

Translation:

Two services with 1 ETH & 1,000,000 ETH of max profit — the 1 ETH service needs to attract 1,000,001 ETH to be secure to cascading attacks (!!!!)

Is this route to pricing AVS security a dead-end?

Act IV: Incentivized Restaking Graphs



Incentivized Restaking Graphs

 α

 π

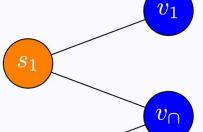
 σ

Rewards/points paid by each service

$$r_1 = \sqrt{K}$$

$$r_1 = \sqrt{K}$$
 $\alpha_1 = \frac{1}{3}$ $\pi_1 = (1+\epsilon)K$

$$r_2 = \sqrt{K}$$
 $\alpha_2 = \frac{1}{2}$ $\pi_2 = (1 + \epsilon)K$



 $\sigma_1 = 1$





 $\sigma_2 = 1$

Incentivized Restaking Graphs



 σ

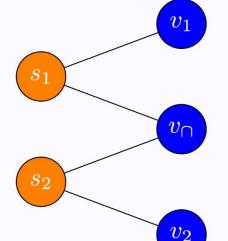
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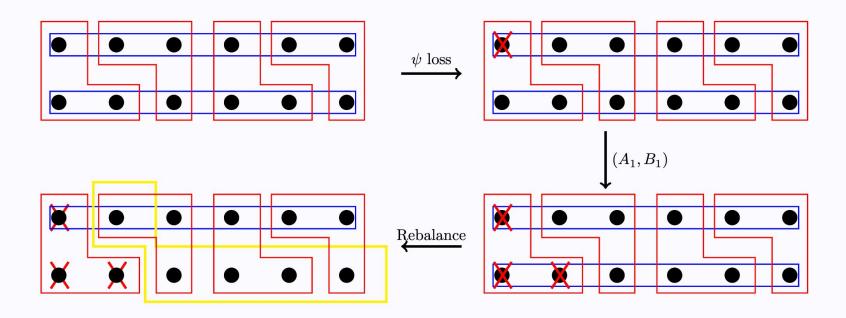
$$\alpha_2 = \frac{1}{2}$$

$$r_2 = \sqrt{K}$$
 $\alpha_2 = \frac{1}{2}$ $\pi_2 = (1 + \epsilon)K$



Validators can adjust stake in response to rewards (i.e. rebalancing)

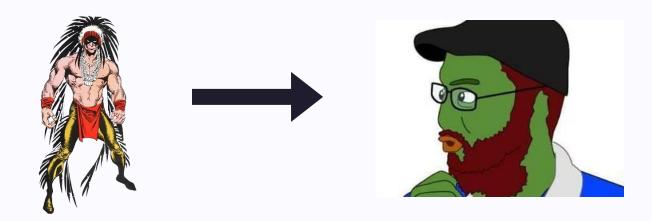
Rebalancing is All You Need





New Threat Model

Adversaries



We weaken the adversary to place realistic liquidity and cost of attack constraints on how many networks one could attack simultaneously

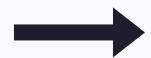
New Threat Model

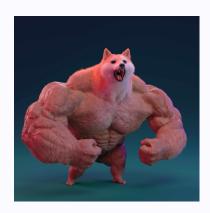
We strengthen node operators, who previously were static (i.e. never rebalanced stake across AVSs) to instead be dynamic

Operators rebalance according to the expected rewards paid by the services and services can adjust rewards to reduce risk

Node Operators







Good News

Theorem [Informal] (Chitra & Pai, 2024):

Given an incentivized restaking graph G where adversaries realize p-norm profit and rewards $r_s \ge KS^{1/p}$, then

$$R_{\psi}(G) \leq \psi + \frac{C}{S^{1-\frac{1}{p}}}$$

There is also an efficient convex approximation algorithm to compute the minimal rewards to achieve this bound

Good News

Interpretation:

When,

- Adversaries face costs...
- Node operators are smarter...
- Services (e.g. AVSs) pay sufficiently high rewards...

...only a small amount of stake can be lost in cascading attacks 🏆



[Note: The cascade guarantee degrades smoothly to the old model, p=1]

How do we reduce in practice?

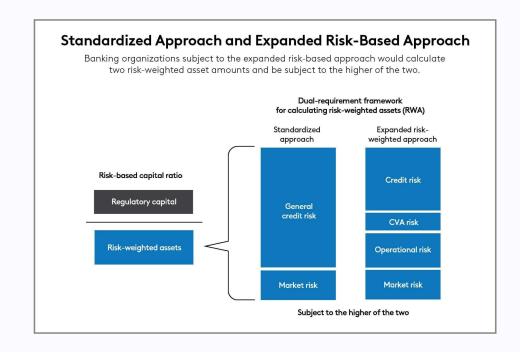
Eigenlayer (largest restaking network) proposed a new mechanism:

ervice reserves percentage $u_s \in (0,1)$ of stake only it can slash

Caps the maximum between services stake

Unique stake, adapted to market prices and elasticities, combined with incentives can provide guarantees that R is small

e.g. Basel III





Thanks!