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# Examining Cronbach Alpha, Theta, Omega Reliability Coefficients According to the Sample Size

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Differentiations according to the sample size of different reliability coefficients are examined. It is concluded that the estimates obtained by Cronbach alpha and teta coefficients are not related with the sample size, even the estimates obtained from the small samples can represent the population parameter. However, the Omega coefficient requires large sample sizes.

Key words: Cronbach alpha, theta, omega, reliability, scale, sample size.

#### Introduction

A scale is needed to measure and that scale must be reliable and valid. The scale's reliability does not matter in the case of measuring the concrete characteristics. But, it is an important problem in the case of measuring the abstract characteristics. So, it is necessary to analyze the reliability of the scales using some statistical

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methods. In making a reliability analysis, the reliability coefficients that are suitable in obtaining the reliability of the scale and the structure of the empirical study must be examined. Sample size is also important to determine the reliability level of the scale. Thus, one of the dimensions that must be examined is the changes in Cronbach alpha, theta, and omega coefficients according to the sample size.

### Reliability

The scale, used to get some information on a defined subject, must have some properties. Reliability, a property that a scale must have, is an indicator of consistency of measurement values obtained from the measurements repeated under the same circumstances (Gay, 1985; Carmines & Zeller, 1982; Arkin & Colton, 1970; O'Connor, 1993; Carey, 1988).

The reliability of the scale can be examined by different ways. The reliability of the scale can be examined by applying the scale once, applying the scale twice or applying the equivalent scales once. In case of applying the scale once, the reliability of internal consistency is examined. The reliability coefficient ranges between 0 and 1.

Methods of Internal Consistency

If the reliability can be estimated by applying the scale once, the error in reliability estimation will be less than the other reliability estimation methods. In this kind of reliability estimation, wrong management, scoring, temporary changes in personal performance affect the internal consistency, the leading affect will be the content sampling (O'Connor, 1993).

Another method, split-half, denotes the homogeneity indices of the items in the scales. It pertains to the relationship level between the responses of the items and the total scale score (Oncu, 1994). An increase in homogeneity in the set of items increases this reliability estimate (O'Connor, 1993). The idea that the internal consistency methods depend upon is that every measurement tool is constructed to realize an objective and those have known equal weights (Karasar, 2000). The internal consistency methods are preferred because they are economical and easy to apply (Oncu, 1994).

#### Cronbach Alpha

The Alpha coefficient method (Cronbach, 1951), is a suitable method that can be used for likert scale items (e.g., 1-3, 1-4, 1-5). Thus, it is not limited to the true-false or correct-incorrect format (Oncu, 1994).

Cronbach alpha coefficient is weighted standard variations mean, obtained by dividing the total of the k items in the scale, to the general variance (Thorndike et al., 1991).

$$\alpha = \frac{n}{(n-1)} \left[ 1 - \frac{\sum_{i=1}^{n} \sigma_{Y_i}^2}{\sigma_x^2} \right]$$

n: Number of the items

 $\sigma_{Y_i}$ : i<sup>th</sup> item's standard deviation

 $\sigma_{V}$ : General standard deviation

(2.1)

If the items are standardized, coefficient is calculated by using the items' correlation mean or variance-covariances' mean (Carmines & Zeller, 1982; Ozdamar, 1999a; SPSS, 1991; SPSS, 1999).

Calculation of alpha coefficient due to the correlation mean,

$$\alpha = \frac{n \overline{\rho}}{1 + (n-1)\overline{\rho}}$$
(2.2)

Calculation of alpha coefficient due to the variance-covariance mean,

$$\alpha = \frac{n \overline{\sigma_{XX}} / \overline{\sigma_X}}{1 + (n - 1)\overline{\sigma_{XX}} / \overline{\sigma_X}}$$
(2.3)

When the formula for calculating Cronbach alpha using the correlation means between items is examined, it can be seen that it is proportionally related with the number of the items and the mean of the correlation between items (Carmines & Zeller, 1982). If the correlation between the items is negative, alpha coefficient will also be negative. Because this situation will spoil the scale's additive property, it also causes a spoil in the reliability model and the scale is no more additive (Ozdamar, 1999a). The coefficient is equal to the mean of all probable coefficients using split-half method (Carmines & Zeller, 1982; Gursakal, 2001).

### Theta Coefficient

The Theta coefficient depends on the principal components analysis. In principal components analysis, the components are in descending order due to the variances of (2ch)of the constructions (Carmines & Zeller, 1982). The first component is the linear component with the maximum variance. The second component is the linear component with the second maximum variance. Components can be explained by the component variances defined by the percentage values to explain the variance of the original data set in order (Ozdamar, 1999b). Theta coefficient depends on that property. The Theta coefficient, takes into account the eigenvalue that maximum explains the event, is calculated as follows:

$$\theta = (N/N-1)(1-1/\lambda_i)$$

N: Number of items

 $\lambda_i$ : The largest eigenvalue (the first eigenvalue)

(2.4)

Omega Coefficient

Another coefficient for linear dependencies is the Omega coefficient proposed by Heise and Bohrnstedt (1970). It depends on the factor analysis model. Omega coefficient is modeled on factor analysis. In this type of modeling, in calculating the coefficient, before factoring "1" values on diagonal in the correlation matrix are replaced with the communality values. The Omega coefficient can be calculated with two ways, using variance-covariance matrix and correlation matrix (Carmines & Zeller, 1982).

When studied with variance-covariance matrix,

$$\Omega = 1 - \left( \sum \sigma_i^2 - \sum \sigma_i^2 h_i^2 \right) / \left( \sum \sum \sigma_{x_i x_j} \right)$$

$$h_{i}^{^{2}} \colon \text{Communality of the $i^{\text{th}}$ item} \tag{2.5}$$

When studied with correlation matrix,

$$\Omega = 1 - \left( a - \sum_{i} h_{i}^{2} \right) / (a + 2b)$$

a: Number of items

b: Sum of the correlations among items

(2.6)

There are some differences between the Theta and Omega coefficients. They depend on different factor-analytic models. The Theta coefficient depends on principal components model, whereas the Omega coefficient depends on factor analysis model. Therefore, in calculating the eigenvalues for Theta coefficients, the diagonal 1.0 values are used, but in calculating the Omega coefficients,

communality values that are not related with 1.0 values are used (Carmines & Zeller, 1982).

There is a relationship between Alpha, Theta, and Omega coefficients. If the items take parallel values, three coefficients are equal each other and will be 1.0. Otherwise, the relationship of magnitude for the coefficients will be  $\alpha < \theta < \Omega$ . Among these internal consistency coefficients,  $\alpha$  gives the lower bound of the reliability coefficient and  $\Omega$  gives the upper bound of the reliability coefficient (Carmines & Zeller, 1982).

#### Methodology

To compare the Alpha, Theta and Omega coefficients, a data set has been used from an instrument developed by Ercan et al. (2004) to measure patient satisfaction in the secondary health-care units. To obtain the effects of different number of items and different sample sizes, 3 different scales are constructed with 39, 34, and 30 items by subtracting some items from the scale with 43 items. Because all the subjects did not answer all the items, the subject numbers in the scales are also different. There are 170 subjects answered all of the 43 items, 240 subjects answered all of the 39 items, 230 subjects answered all of the 34 items, and 320 subjects answered all of the 30 items.

After giving a number to each of the subjects, samples are constructed by producing random numbers using MINITAB 13.2 beginning from 10 and increasing 10 units each of those random numbers. The same procedure was repeated 10 times and for each of the samples Cronbach alpha, Theta and Omega reliability coefficients are calculated.

SPSS 13.0 was used for these analyses. Statistical comparisons are performed in order to determine if alpha, theta and omega coefficients change or not according to the sample size and in order to determine the sample size that the reliability coefficients begin to get stable. Before the between group comparisons, the homogeneity of variances is tested using the Levene statistic. If the variances are found to be homogeneous, then analysis of variance

|   |   | radic=4.1. The homogene | ity test results for | the scale with 50 he | 1115         |
|---|---|-------------------------|----------------------|----------------------|--------------|
|   |   | Levene Statistic        | Degree of            | Degree of            | Significance |
|   |   |                         | Freedom 1            | Freedom 2            | level (p)    |
| · | α | 5.631                   | 31                   | 288                  | < 0.001      |
|   | θ | 5.578                   | 31                   | 288                  | < 0.001      |
|   | Ω | 1.531                   | 31                   | 288                  | 0.040        |

Table-4.1: The homogeneity test results for the scale with 30 items

Table-4.2: Significance level in comparison of  $\alpha$ ,  $\theta$  and  $\Omega$  reliability coefficients according to different sample sizes using Kruskal-Wallis test for the scale with 30 items

|                        | α      | θ      | Ω       |
|------------------------|--------|--------|---------|
| $\chi^2$               | 23.706 | 46.720 | 259.636 |
| Degree of freedom      | 31     | 31     | 31      |
| Significance level (p) | 0.822  | 0.035  | < 0.001 |

Bonferroni correction: 
$$\alpha^* = 1 - (1 - \alpha)^{1/k}$$

$$\alpha^* = 1 - (1 - 0.05)^{1/32} = 0.0016$$

and Tukey HSD post-hoc comparison test are applied. If the variances are heterogeneous, Kruskal-Wallis and Mann-Withney U tests are applied to make reliability comparisons according to sample size. The level of significance in multiple comparisons is determined after Bonferrroni correction  $(\alpha^* = 1 - (1 - \alpha)^{1/k})$  k: number of groups).

#### Results

The results of comparisons  $\alpha$ ,  $\theta$  and  $\Omega$  coefficients according to different sample sizes are given in Table 4.1, 4.2, 4.3, 4.4 for the scale with 30 items.

Table-4.3: Significance level (p values  $\times$  10<sup>-3</sup>) in comparison of  $\theta$  reliability coefficients according to different sample sizes using Mann-Whitney U test for the scale with 30 items ( $\alpha$ \*=0.0016).

| n 1        | 10 20 | 30 40   | 50    | 60  | 70  | 80  | 90  | 100 | 110 12 | 20 13             | 0 14 | 0 150 | 160              | 170 | 180   | 190 2 | 200 2 | 210 2 | 220 2 | 230 2 | 240 2 | 50 2 | 60 2 | 270 2 | 280 2 | 290 30 | 00 31 | 0 320 |
|------------|-------|---------|-------|-----|-----|-----|-----|-----|--------|-------------------|------|-------|------------------|-----|-------|-------|-------|-------|-------|-------|-------|------|------|-------|-------|--------|-------|-------|
| 10         | 631   | 315 315 | 315   | 280 | 353 | 393 | 393 | 353 | 353 39 | 3 39              | 3 35 | 3 315 | 353              | 315 | 353   | 353   | 315 3 | 315 3 | 315 3 | 353 3 | 353 3 | 53 3 | 93 3 | 315 3 | 3153  | 315 43 | 36 43 | 6 436 |
| 20         |       | 912 684 | 1 796 | 529 | 579 | 100 | 529 | 631 | 529 52 | 29 52             | 9 63 | 1 353 | 315              | 190 | 165   | 089   | 123 1 | 190 1 | 123 1 | 23 ′  | 105 0 | 89 1 | 65 ( | )52 ( | 75 (  | 75 12  | 23 07 | 5 063 |
| 30         |       | 315     | 5 393 | 218 | 315 | 529 | 247 | 218 | 218 19 | 0 19              | 0 19 | 0 165 | 143              | 105 | 105   | 089   | 105 1 | 123 ( | 75 (  | 89 (  | 089 1 | 05 1 | 23 ( | 063 ( | 75 (  | 75 07  | 75 10 | 5 089 |
| 40         |       |         | 853   | 684 | 912 | 796 | 579 | 853 | 481 52 | 29 35             | 3 28 | 0 218 | 3 143            | 123 | 123   | 123 · | 123 ′ | 123 ( | )89 1 | 43 ′  | 123 1 | 23 1 | 23 ( | 089 ( | 063 ( | 75 12  | 23 12 | 3 123 |
| 50         |       |         |       | 529 | 971 | 853 | 436 | 684 | 353 52 | 29 19             | 0 16 | 5 247 | <sup>7</sup> 143 | 052 | 034 ( | 052 ( | )75 ´ | 105 1 | 105 1 | 05 (  | 035   | 52 0 | 75 C | )75 ( | )52 ( | 35 02  | 23 02 | 3 023 |
| 60         |       |         |       |     | 796 | 353 | 971 | 912 | 912 10 | 00 91             | 2 91 | 2 796 | 739              | 529 | 436   | 247 3 | 315 4 | 181 4 | 136 4 | 136 2 | 218 2 | 18 3 | 93 1 | 190 1 | 190 2 | 247 35 | 53 16 | 5 123 |
| 70         |       |         |       |     |     | 739 | 739 | 912 | 631 79 | 96 39             | 3 43 | 6 529 | 247              | 165 | 143   | 089   | 190 ′ | 143 1 | 165 1 | 05 1  | 105 1 | 65 2 | 18 1 | 143 1 | 105 0 | 063 07 | 75 07 | 5 089 |
| 80         |       |         |       |     |     |     | 315 | 529 | 247 28 | 30 10             | 5 08 | 9 123 | 3 052            | 011 | 004   | 009 ( | )11(  | )23 ( | )190  | 19 (  | 004 0 | 05 0 | 09 ( | 009 ( | 05 (  | 005 00 | 2 00  | 2 002 |
| 90         |       |         |       |     |     |     |     | 971 | 796 97 | <sup>7</sup> 1 73 | 9 79 | 6 579 | 353              | 280 | 247   | 218 3 | 353 2 | 280 1 | 165 1 | 65 1  | 123 1 | 903  | 15 ( | 089 ( | )89 1 | 105 10 | )5 14 | 3 218 |
| 100        |       |         |       |     |     |     |     |     | 739 79 | 6 48              | 1 48 | 1 315 | 315              | 218 | 190   | 165   | 190 2 | 218 1 | 143 1 | 65 2  | 218 1 | 43 2 | 47 1 | 123 1 | 143 1 | 105 21 | 18 19 | 0 143 |
| 110        |       |         |       |     |     |     |     |     | 97     | <sup>7</sup> 1 79 | 6 85 | 3 529 | 481              | 315 | 315   | 247 2 | 247 2 | 280 1 | 165 1 | 90 2  | 247 1 | 65 2 | 80 1 | 105 1 | 143 1 | 143 16 | 55 16 | 5 143 |
| 120        |       |         |       |     |     |     |     |     |        | 57                |      |       |                  |     |       |       |       |       |       | _     |       |      | _    |       |       | 35 03  |       |       |
| 130        |       |         |       |     |     |     |     |     |        |                   | 63   | _     | _                |     |       | _     |       |       |       |       |       |      | _    |       | _     | 247 16 |       |       |
| 140        |       |         |       |     |     |     |     |     |        |                   |      | 853   | 3 739            | 481 | 315   | 143   | 143 2 | 247 3 | 353 2 | 247 ( | 052 0 | 75 1 | 23 1 | 123 1 | 105 ( | 75 02  | 23 04 | 3 023 |
| 150        |       |         |       |     |     |     |     |     |        |                   |      |       | 579              |     |       |       |       |       |       |       |       |      |      |       |       | 75 07  |       |       |
| 160        |       |         |       |     |     |     |     |     |        |                   |      |       |                  |     |       |       |       |       |       | _     |       |      |      |       |       | 105 07 |       |       |
| 170        |       |         |       |     |     |     |     |     |        |                   |      |       |                  |     |       |       |       |       |       |       |       |      |      |       |       | 136 28 |       |       |
| 180        |       |         |       |     |     |     |     |     |        |                   |      |       |                  |     | - ;   |       |       |       |       |       |       |      |      |       |       | 393 35 |       |       |
| 190        |       |         |       |     |     |     |     |     |        |                   |      |       |                  |     |       | (     |       |       |       |       |       |      |      |       |       | 796 85 |       |       |
| 200        |       |         |       |     |     |     |     |     |        |                   |      |       |                  |     |       |       | (     |       |       |       |       |      | _    |       |       | 12 79  |       |       |
| 210        |       |         |       |     |     |     |     |     |        |                   |      |       |                  |     |       |       |       | 1     |       |       |       |      |      |       |       | 579 57 |       |       |
| 220        |       |         |       |     |     |     |     |     |        |                   |      |       |                  |     |       |       |       |       | 5     |       |       |      | _    |       |       | 31 57  |       |       |
| 230        |       |         |       |     |     |     |     |     |        |                   |      |       |                  |     |       |       |       |       |       |       |       | _    | _    |       |       | 181 91 |       |       |
| 240        |       |         |       |     |     |     |     |     |        |                   |      |       |                  |     |       |       |       |       |       |       |       |      | _    |       |       | 353 91 |       |       |
| 250        |       |         |       |     |     |     |     |     |        |                   |      |       |                  |     |       |       |       |       |       |       |       | 5    | _    |       |       | 796 97 |       |       |
| 260        |       |         |       |     |     |     |     |     |        |                   |      |       |                  |     |       |       |       |       |       |       |       |      | ٠    |       |       | 218 28 |       |       |
| 270<br>280 |       |         |       |     |     |     |     |     |        |                   |      |       |                  |     |       |       |       |       |       |       |       |      |      |       |       | 739 91 |       |       |
| 290        |       |         |       |     |     |     |     |     |        |                   |      |       |                  |     |       |       |       |       |       |       |       |      |      |       |       | 971 97 |       | 2 529 |
| 300        |       |         |       |     |     |     |     |     |        |                   |      |       |                  |     |       |       |       |       |       |       |       |      |      |       |       | 91     |       | 2 684 |
| 310        |       |         |       |     |     |     |     |     |        |                   |      |       |                  |     |       |       |       |       |       |       |       |      |      |       |       |        | 91    | 481   |
| 320        |       |         |       |     |     |     |     |     |        |                   |      |       |                  |     |       |       |       |       |       |       |       |      |      |       |       |        |       | 401   |
| 320        |       |         |       |     |     |     |     |     |        |                   |      |       |                  |     |       |       |       |       |       |       |       |      |      |       |       |        |       |       |

Table-4.4: Significance level (p values×  $10^{-3}$ ) in comparison of  $\Omega$  reliability coefficients according to different sample sizes using Mann-Whitney U test for the scale with 30 items ( $\alpha$ \*=0.0016).

| n   | 10 20 30 40 50 60 70 80 90 100 110 120 130 140 150 160 170 180 190 200 210 220 230 240 250 260 270 280 290 300 310 320 |
|-----|--|
| 10  | $000\ 000\ 000\ 000\ 000\ 000\ 000\ 000$   |
| 20  | 052002000000000000000000000000   |
| 30  | $023\ 002\ 002\ 001\ 000\ 000\ 000\ 000\ 000$  |
| 40  | 08900900700000000000000000000000   |
| 50  | 123105011000000000000000000000000  |
| 60  | $853\ 123\ 011\ 001\ 000\ 000\ 000\ 000\ 000\ 00$  |
| 70  | $280\ 023\ 005\ 003\ 001\ 000\ 000\ 000\ 000\ 000\ 000$  |
| 80  | 218 019 015 005 000 000 000 000 000 000 000 000  |
| 90  | 353247089009005001001000000000000000000000   |
| 100 | 853 481 075 035 007 004 001 001 000 000 000 000 000 000 000  |
| 110 | 579 075 063 009 005 000 001 000 000 000 000 000 000 000  |
| 120 | 165 165 019 011 005 004 000 000 000 000 000 000 000 000  |
| 130 | 912 315 247 105 052 009 005 005 004 001 000 002 002 000 000 000 000 000 000  |
| 140 | 353 190 052 029 007 004 004 003 001 001 001 002 000 000 000 000 000 000  |
| 150 | 684 190 143 052 015 015 009 004 005 004 007 000 000 000 000 000 000  |
| 160 | 436 218 075 035 035 019 007 004 009 007 001 000 000 000 000  |
| 170 | 247 123 165 105 123 043 023 075 052 007 004 004 002 003 003  |
| 180 | 436 393 393 315 123 123 247 218 063 035 007 019 023 023  |
| 190 | 739 853 971 579 393 579 579 315 143 075 105 123 123  |
| 200 | 971 912 739 853 684 684 280 190 143 143 029 029  |
| 210 | 971 796 631 912 739 315 165 190 143 075 063  |
| 220 | 631 684 100 912 436 190 165 123 123 123  |
| 230 | 971 912 912 529 247 143 063 043 105  |
| 240 | 100 971 481 165 105 075 035 075  |
| 250 | 100 218 165 052 035 011 029  |
| 260 | 353 165 105 105 052 07 <del>5</del>  |
| 270 | 393 280 280 353 481  |
| 280 | 631 853 739 100  |
| 290 | 971 912 971  |
| 300 | 853 100  |
| 310 | 912  |
| 320 |  |
|     |  |

The results of comparisons  $\alpha$ ,  $\theta$  and  $\Omega$  coefficients according to different sample sizes

are given in Table 4.5, 4.6, 4.7 for the scale with 34 items.

Table-4.5: The homogeneity test results for the scale with 34 items

|   | Levene    | Degree of | Degree of | Significance level |
|---|-----------|-----------|-----------|--------------------|
|   | Statistic | freedom 1 | freedom 2 | (p)                |
| α | 11.003    | 22        | 207       | < 0.001            |
| θ | 10.477    | 22        | 207       | < 0.001            |
| Ω | 3.238     | 22        | 207       | < 0.001            |

Table-4.6: Significance level in comparison of  $\alpha$ ,  $\theta$  and  $\Omega$  reliability coefficients according to different sample sizes using Kruskal-Wallis test for the scale with 34 items

| bampie bizeb abing thruc | onar wants test for t | ile beate with 5 i i | terris  |
|--------------------------|-----------------------|----------------------|---------|
|                          | α                     | θ                    | Ω       |
| $\chi^2$                 | 6.329                 | 8.960                | 176.741 |
| Degree of freedom        | 22                    | 22                   | 22      |
| Significance level (p)   | 1.000                 | 0.994                | < 0.001 |

Bonferroni correction: 
$$\alpha^* = 1 - (1 - \alpha)^{1/k}$$

$$\alpha^* = 1 - (1 - 0.05)^{1/23} = 0.0022$$

Table-4.7: Significance level (p values×  $10^{-3}$ ) in comparison of Ω reliability coefficients according to different sample sizes using Mann-Whitney U test for the scale with 34 items ( $\alpha$ \*=0.0022)

| t   | o ai | ffere | nt sa | amp | le si | zes ı | ısınş | g Ma | ann- | Whi | tney | U te | est fo | or th | e sca | ale v | vith | <i>34</i> 1 | tems | (α1 | ·=0.0 | JU22 | <u>2)                                    </u> |
|-----|------|-------|-------|-----|-------|-------|-------|------|------|-----|------|------|--------|-------|-------|-------|------|-------------|------|-----|-------|------|---|
| n   | 10   | 20    | 30    | 40  | 50    | 60    | 70    | 80   | 90   | 100 | 110  | 120  | 130    | 140   | 150   | 160   | 170  | 180         | 190  | 200 | 210   | 220  | 230   |
| 10  |      | 000   | 000   | 000 | 000   | 000   | 000   | 000  | 000  | 000 | 000  | 000  | 000    | 000   | 000   | 000   | 000  | 000         | 000  | 000 | 000   | 000  | 000   |
| 20  |      |       | 004   | 000 | 000   | 000   | 000   | 000  | 000  | 000 | 000  | 000  | 000    | 000   | 000   | 000   | 000  | 000         | 000  | 000 | 000   | 000  | 000   |
| 30  |      |       |       | 280 | 043   | 007   | 001   | 001  | 000  | 000 | 000  | 000  | 000    | 000   | 000   | 000   | 000  | 000         | 000  | 000 | 000   | 000  | 000   |
| 40  |      |       |       |     | 247   | 043   | 009   | 004  | 002  | 000 | 000  | 000  | 000    | 000   | 000   | 000   | 000  | 000         | 000  | 000 | 000   | 000  | 000   |
| 50  |      |       |       |     |       | 481   | 143   | 063  | 023  | 003 | 000  | 000  | 000    | 000   | 000   | 000   | 000  | 000         | 000  | 000 | 000   | 000  | 000   |
| 60  |      |       |       |     |       |       | 280   | 143  | 052  | 009 | 001  | 000  | 000    | 000   | 000   | 000   | 000  | 000         | 000  | 000 | 000   | 000  | 000   |
| 70  |      |       |       |     |       |       |       | 853  | 353  | 143 |      |      |        |       |       |       |      |             | 000  |     |       |      |   |
| 80  |      |       |       |     |       |       |       |      | 579  | 247 | 075  | 089  | 043    | 029   | 004   | 011   | 001  | 002         | 000  | 000 | 000   | 000  | 000   |
| 90  |      |       |       |     |       |       |       |      |      | 739 | 315  | 247  | 123    | 123   | 023   | 015   | 007  | 005         | 002  | 001 | 002   | 001  | 002   |
| 100 |      |       |       |     |       |       |       |      |      |     | 684  | 739  | 247    | 218   | 075   | 052   | 043  | 009         | 005  | 003 | 002   | 001  | 002   |
| 110 |      |       |       |     |       |       |       |      |      |     |      | 971  | 579    | 315   | 052   | 105   | 035  | 011         | 005  | 003 | 002   | 001  | 002   |
| 120 |      |       |       |     |       |       |       |      |      |     |      |      | 436    | 280   | 063   | 075   | 023  | 011         | 002  | 001 | 002   | 001  | 015   |
| 130 |      |       |       |     |       |       |       |      |      |     |      |      |        | 912   | 218   | 190   | 075  | 035         | 005  | 003 | 003   | 002  | 015   |
| 140 |      |       |       |     |       |       |       |      |      |     |      |      |        |       | 247   | 123   | 043  | 019         | 002  | 001 | 002   | 001  | 002   |
| 150 |      |       |       |     |       |       |       |      |      |     |      |      |        |       |       | 971   | 315  | 218         | 015  | 003 | 009   | 003  | 015   |
| 160 |      |       |       |     |       |       |       |      |      |     |      |      |        |       |       |       | 218  | 280         | 011  | 004 | 005   | 002  | 002   |
| 170 |      |       |       |     |       |       |       |      |      |     |      |      |        |       |       |       |      | 912         | 280  | 075 | 052   | 019  | 019   |
| 180 |      |       |       |     |       |       |       |      |      |     |      |      |        |       |       |       |      |             | 280  | 123 | 089   | 052  | 105   |
| 190 |      |       |       |     |       |       |       |      |      |     |      |      |        |       |       |       |      |             |      | 436 | 353   | 218  | 796   |
| 200 |      |       |       |     |       |       |       |      |      |     |      |      |        |       |       |       |      |             |      |     | 912   | 631  | 684   |
| 210 |      |       |       |     |       |       |       |      |      |     |      |      |        |       |       |       |      |             |      |     |       | 631  | 280   |
| 220 |      |       |       |     |       |       |       |      |      |     |      |      |        |       |       |       |      |             |      |     |       |      | 165   |
| 230 |      |       |       |     |       |       |       |      |      |     |      |      |        |       |       |       |      |             |      |     |       |      |   |

The results of comparisons  $\alpha$ ,  $\theta$  and  $\Omega$ coefficients according to different sample sizes

are given in Table 4.8, 4.9, 4.10, 4.11 for the scale with 39 items.

Table-4.8: The homogeneity test results for the scale with 39 items

|   | Levene<br>Statistic | Degree of freedom 1 | Degree of freedom 2 | Significance level |
|---|---------------------|---------------------|---------------------|--------------------|
| α | 10.692              | 23                  | 216                 | (p)<br><0.001      |
| θ | 12.048              | 23                  | 216                 | <0.001             |
| Ω | 1.418               | 23                  | 216                 | 0.104              |

Table-4.9: Significance level in comparison of  $\alpha$  and  $\theta$  reliability coefficients according to different sample sizes using Kruskal-Wallis test for the scale with 39 items

|                        | α     | θ     |
|------------------------|-------|-------|
| $\chi^2$               | 7.206 | 8.702 |
| Degree of freedom      | 23    | 23    |
| Significance level (p) | 0.999 | 0.997 |

Table-4.10: Significance level in comparison of  $\Omega$  reliability coefficients according to different sample

sizes by analysis of variance for the scale with 39 items

|                | Sum of   | Degrees of | Sum of     | F       | Significance |
|----------------|----------|------------|------------|---------|--------------|
|                | Squares  | freedom    | Squares    |         | level (p)    |
| Between groups | 0.00536  | 23         | 0.0002329  |         |              |
| Within groups  | 0.000352 | 216        | 0.00000163 | 142.881 | < 0.001      |
| Total          | 0.00571  | 239        |            |         |              |

Bonferroni correction: 
$$\alpha^* = 1 - (1 - \alpha)^{1/k}$$

$$\alpha^* = 1 - (1 - 0.05)^{1/24} = 0.0021$$

Table-4.11: Significance level (p values  $\times$  10<sup>-3</sup>) in comparison of  $\Omega$  reliability coefficients according to different sample sizes using Tukey's HSD post-hoc comparison test for the scale with 39 items ( $\alpha$ \*=0.0021).

| n   | 10 | 20  | 30  | 40  | 50  | 60  | 70  | 80  | 90  | 100 | 110  | 120 | 130 | 140 | 150 | 160 | 170 | 180 | 190 | 200 | 2    | 102  | 2023  | 30 240 | 0 |
|-----|----|-----|-----|-----|-----|-----|-----|-----|-----|-----|------|-----|-----|-----|-----|-----|-----|-----|-----|-----|------|------|-------|--------|---|
| 10  |    | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 000  | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 00   | 0 00 | 00 00 | 00 00  | 0 |
| 20  |    |     | 002 | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 000  | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 00   | 000  | 00 00 | 00 00  | 0 |
| 30  |    |     |     | 031 | 000 | 000 | 000 | 000 | 000 | 000 | 000  | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 00   | 0 00 | 00 00 | 00 00  | 0 |
| 40  |    |     |     |     | 729 | 000 | 000 | 000 | 000 | 000 | 000  | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 00   | 0 00 | 00 00 | 00 00  | 0 |
| 50  |    |     |     |     |     | 899 | 003 | 000 | 000 | 000 | 000  | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 00   | 0 00 | 00 00 | 00 00  | 0 |
| 60  |    |     |     |     |     |     | 781 | 000 | 000 | 000 | 000  | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 00   | 0 00 | 00 00 | 00 00  | 0 |
| 70  |    |     |     |     |     |     |     | 100 | 972 | 322 | 2029 | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 00   | 0 00 | 00 00 | 00 00  | 0 |
| 80  |    |     |     |     |     |     |     |     | 100 | 986 | 561  | 035 | 005 | 002 | 000 | 000 | 000 | 000 | 000 | 000 | 00   | 0 00 | 00 00 | 00 00  | 0 |
| 90  |    |     |     |     |     |     |     |     |     | 100 | 947  | 227 | 051 | 021 | 004 | 000 | 000 | 000 | 000 | 000 | 00   | 0 00 | 00 00 | 00 00  | 0 |
| 100 |    |     |     |     |     |     |     |     |     |     | 100  | 934 | 617 | 411 | 159 | 021 | 001 | 000 | 000 | 000 | 00   | 0 00 | 00 00 | 00 00  | 0 |
| 110 |    |     |     |     |     |     |     |     |     |     |      | 100 | 991 | 953 | 749 | 264 | 035 | 001 | 000 | 000 | 00   | 0 00 | 00 00 | 00 00  | 0 |
| 120 |    |     |     |     |     |     |     |     |     |     |      |     | 100 | 100 | 100 | 963 | 558 | 086 | 011 | 003 | 00   | 0 80 | 00 00 | 00 00  | 0 |
| 130 |    |     |     |     |     |     |     |     |     |     |      |     |     | 100 | 100 | 100 | 908 | 330 | 069 | 020 | 05   | 550  | 01 00 | 1000   | 0 |
| 140 |    |     |     |     |     |     |     |     |     |     |      |     |     |     | 100 | 100 | 977 | 525 | 147 | 049 | 11   | 190  | 02 00 | 200    | 0 |
| 150 |    |     |     |     |     |     |     |     |     |     |      |     |     |     |     | 100 | 999 | 836 | 388 | 170 | 33   | 350  | 1201  | 000    | 1 |
| 160 |    |     |     |     |     |     |     |     |     |     |      |     |     |     |     |     | 100 | 996 | 863 | 610 | 82   | 211  | 04 09 | 1018   | 8 |
| 170 |    |     |     |     |     |     |     |     |     |     |      |     |     |     |     |     |     | 100 | 999 | 975 | 99   | 975  | 14 47 | '9 17  | 1 |
| 180 |    |     |     |     |     |     |     |     |     |     |      |     |     |     |     |     |     |     | 100 | 100 | 10   | 009  | 75 96 | 3775   | 0 |
| 190 |    |     |     |     |     |     |     |     |     |     |      |     |     |     |     |     |     |     |     | 100 | ) 10 | 001  | 00 10 | 00 984 | 4 |
| 200 |    |     |     |     |     |     |     |     |     |     |      |     |     |     |     |     |     |     |     |     | 10   | 00 1 | 00 10 | 00 999 | 9 |
| 210 |    |     |     |     |     |     |     |     |     |     |      |     |     |     |     |     |     |     |     |     |      | 1    | 00 10 | 0099   | 1 |
| 220 |    |     |     |     |     |     |     |     |     |     |      |     |     |     |     |     |     |     |     |     |      |      | 10    | 00 100 | 0 |
| 230 |    |     |     |     |     |     |     |     |     |     |      |     |     |     |     |     |     |     |     |     |      |      |       | 100    | 0 |
| 240 |    |     |     |     |     |     |     |     |     |     |      |     |     |     |     |     |     |     |     |     |      |      |       |        |   |
| -   |    |     |     |     |     |     |     |     |     |     |      |     |     |     |     |     |     |     |     |     |      |      |       |        | _ |

The results of comparisons  $\alpha$ ,  $\theta$  and  $\Omega$  coefficients according to different sample sizes

are given in Table 4.12, 4.13, 4.14 for the scale with 43 items.

Table-4.12: The homogeneity test results for the scale with 43 items

|   | Levene    | Degree of | Degree of | Significance level |
|---|-----------|-----------|-----------|--------------------|
|   | Statistic | freedom 1 | freedom 2 | (p)                |
| α | 6.313     | 16        | 153       | < 0.001            |
| θ | 7.654     | 16        | 153       | < 0.001            |
| Ω | 2.463     | 16        | 153       | 0.002              |

Table-4.13: Significance level in comparison of  $\alpha$ ,  $\theta$  and  $\Omega$  reliability coefficients according to different sample sizes using Kruskal-Wallis test for the scale with 43 items

|                        | α      | θ     | Ω       |
|------------------------|--------|-------|---------|
| $\chi^2$               | 11.248 | 7.026 | 141.750 |
| Degree of freedom      | 16     | 16    | 16      |
| Significance level (p) | 0.794  | 0.973 | < 0.001 |

Bonferroni correction: 
$$\alpha^* = 1 - (1 - \alpha)^{1/k}$$

$$\alpha^* = 1 - (1 - 0.05)^{1/17} = 0.003$$

| n   | 10 | 20  | 30  | 40  | 50  | 60  | 70  | 80  | 90  | 100 | 110 | 120 | 130 | 140 | 150 | 160 | 170 |
|-----|----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| 10  |    | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 000 |
| 20  |    |     | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 000 |
| 30  |    |     |     | 143 | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 000 |
| 40  |    |     |     |     | 001 | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 000 |
| 50  |    |     |     |     |     | 353 | 015 | 002 | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 000 |
| 60  |    |     |     |     |     |     | 123 | 011 | 003 | 000 | 000 | 000 | 000 | 000 | 000 | 000 | 000 |
| 70  |    |     |     |     |     |     |     | 218 | 089 | 009 | 003 | 000 | 000 | 000 | 000 | 000 | 000 |
| 80  |    |     |     |     |     |     |     |     | 353 | 105 | 105 | 005 | 001 | 000 | 000 | 000 | 000 |
| 90  |    |     |     |     |     |     |     |     |     | 393 | 315 | 035 | 015 | 009 | 002 | 001 | 002 |
| 100 |    |     |     |     |     |     |     |     |     |     | 912 | 280 | 190 | 089 | 035 | 029 | 023 |
| 110 |    |     |     |     |     |     |     |     |     |     |     | 280 | 165 | 105 | 035 | 029 | 009 |
| 120 |    |     |     |     |     |     |     |     |     |     |     |     | 631 | 481 | 190 | 075 | 023 |
| 130 |    |     |     |     |     |     |     |     |     |     |     |     |     | 912 | 579 | 123 | 043 |
| 140 |    |     |     |     |     |     |     |     |     |     |     |     |     |     | 436 | 218 | 063 |
| 150 |    |     |     |     |     |     |     |     |     |     |     |     |     |     |     | 481 | 165 |
| 160 |    |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     | 481 |
| 170 |    |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |     |

Table-4.14: Significance level (p values×  $10^{-3}$ ) in comparison of Ω reliability coefficients according to different sample sizes using Mann-Whitney U test for the scale with 39 items ( $\alpha$ \*=0.003)

#### Conclusion

The answer to the question of sample size in this context is important. The accuracy of reliability coefficients changes according to the sample size. There is high positive correlation between number of items and reliability coefficient as mentioned in Carmines and Zeller (1982). Also, the difference in number of items must be taken into account.

Significant differences are not observed due to the sample size in the commonly used Cronbach Alpha, and with the Theta coefficient which is based on principal components. However, with the Omega coefficient, based on factor analysis, large differences were observed due to the sample size. With an increase in item numbers, however, the Omega coefficient is stabilized even for smaller sample sizes.

Ozdamar (1999a) mentioned that the sample size should be more than 50 in reliability

analysis applications. According to the results of this study, that sample size is not important for the Cronbach alpha or theta coefficients, and is stable even for a small number of items (although of course an increase in the number of items will increase the magnitude.) However, in order to estimate the population parameter with Omega coefficient, the item number is important. With an increase in item number, either the consistency of estimation or the reliability level increases.

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