

# RNN 24-hour Forecast Report - 西条

$$h_t = \sigma(W_h x_t + U_h h_{t-1} + b_h)$$

$$\hat{y}_t = W_y h_t + b_y$$

$$\mathcal{L} = \frac{1}{N} \sum_{t=1}^N (y_t - \hat{y}_t)^2$$

$x_t$ : input vector at time  $t$   
 $h_t$ : hidden state containing temporal information  
 $W_h, U_h, b_h$ : learnable parameters of the recurrent layer  
 $\sigma$ : non-linear activation function (usually tanh or ReLU)  
 $\hat{y}_t$ : predicted output for step  $t$   
 $\mathcal{L}$ : mean squared error minimized during training

The Recurrent Neural Network (RNN) is designed to handle sequential data, where each output depends not only on the current input but also on the previous hidden state.

At each time step, the hidden layer combines the current input  $x_t$  and the previous hidden state  $h_{(t-1)}$ , allowing the model to retain temporal information across steps.

The RNN is simpler than LSTM because it lacks explicit memory cells and gates. This makes it more sensitive to vanishing gradient problems but still effective for short-term dependencies.

The model is trained by minimizing the mean squared error between predicted and observed values.

|  |             |
|--|-------------|
| Prefecture code                        | 38          |
| Station code                           | 38206050    |
| Station name                           | 西条          |
| Target item                            | Ox(ppm)     |
| Number of data points in the train set | 15747       |
| Number of data points in the test set  | 6749        |
| Forecast horizon (hours)               | 24          |
| Model                                  | RNN         |
| Elapsed time                           | 0 min 3 sec |
| Number of features used                | 25          |
| Residuals mean                         | -0.003365   |
| Residuals median                       | -0.00324    |
| Residuals mode                         | -0.001746   |

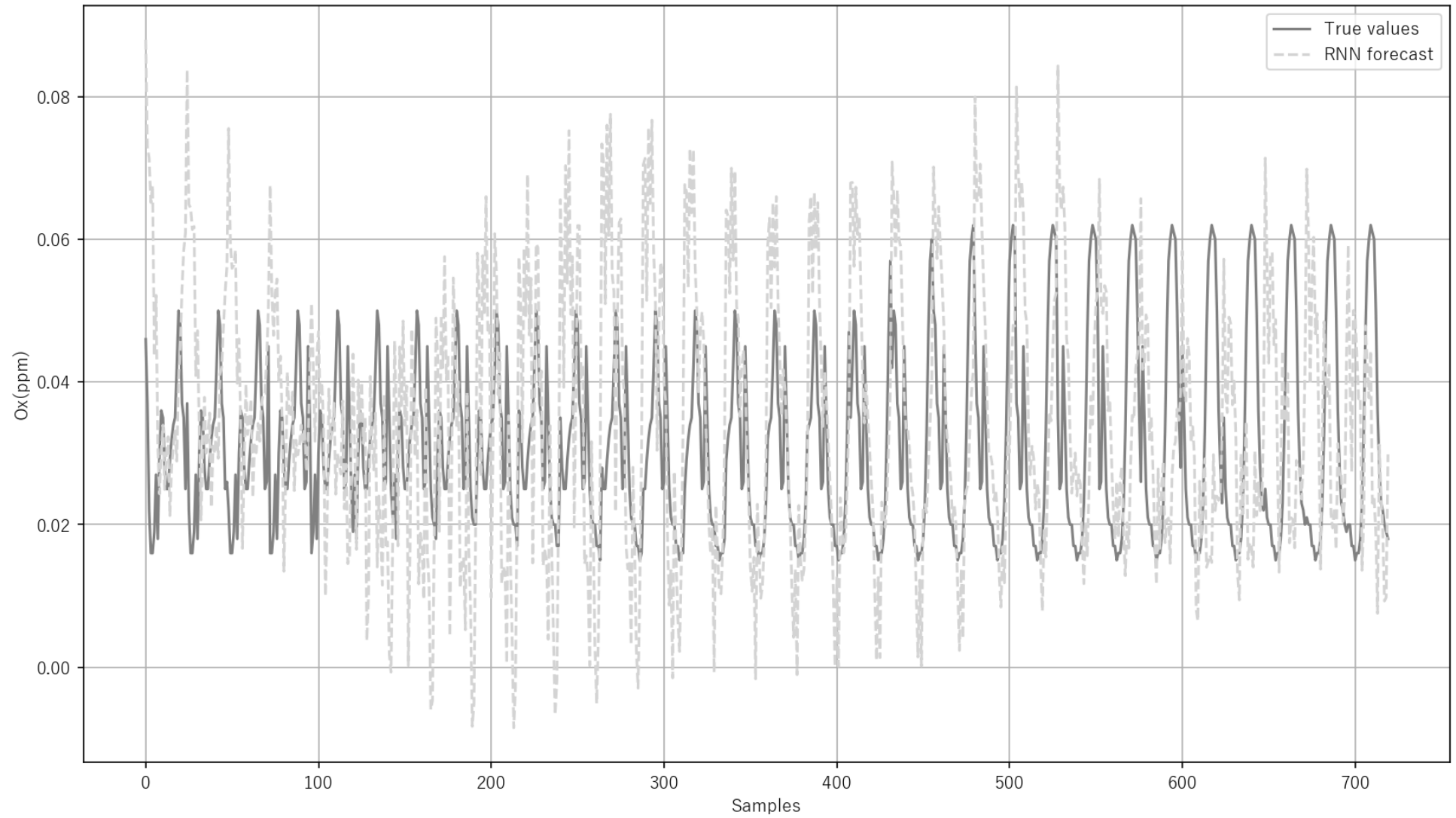
## Features used for prediction

|                    |                     |                    |                      |                     |
|--------------------|---------------------|--------------------|----------------------|---------------------|
| NO(ppm)            | NO2(ppm)            | U                  | V                    | Ox(ppm)_roll_mean_3 |
| Ox(ppm)_roll_std_6 | NO(ppm)_roll_mean_3 | NO(ppm)_roll_std_6 | NO2(ppm)_roll_mean_3 | NO2(ppm)_roll_std_6 |
| U_roll_mean_3      | U_roll_std_6        | V_roll_mean_3      | V_roll_std_6         | Ox(ppm)_diff_1      |
| Ox(ppm)_diff_2     | Ox(ppm)_diff_3      | NO(ppm)_diff_3     | NO2(ppm)_diff_3      | U_diff_3            |
| V_diff_3           | hour_sin            | hour_cos           | dayofweek            | is_weekend          |

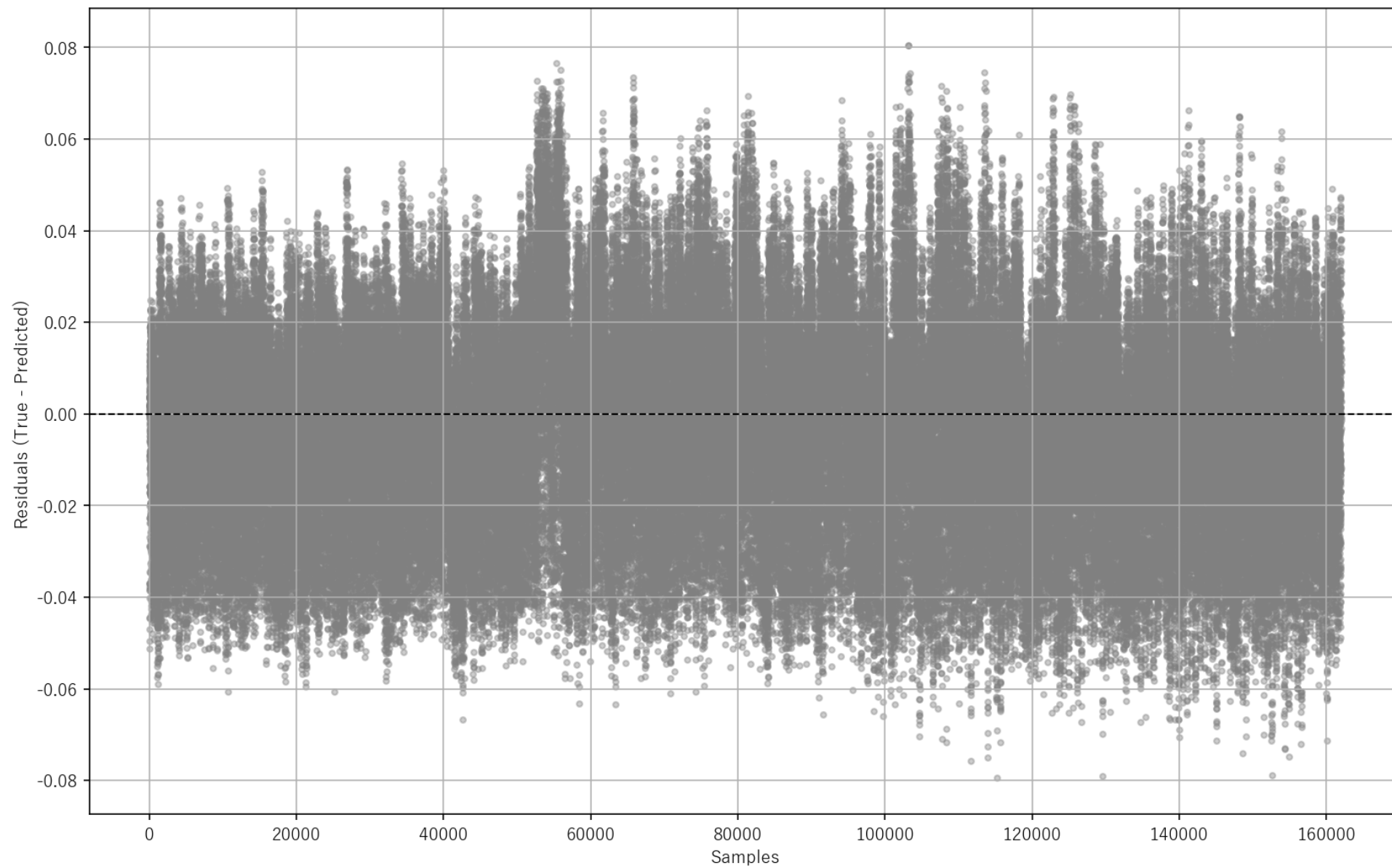
## Model accuracy

| Target       | R <sup>2</sup> | MAE    | RMSE   |
|--------------|----------------|--------|--------|
| Ox(ppm)_t+01 | -3.0883        | 0.0356 | 0.0369 |
| Ox(ppm)_t+02 | -1.7139        | 0.0280 | 0.0300 |
| Ox(ppm)_t+03 | -0.8162        | 0.0207 | 0.0246 |
| Ox(ppm)_t+04 | -2.0156        | 0.0295 | 0.0317 |
| Ox(ppm)_t+05 | -1.8350        | 0.0276 | 0.0307 |
| Ox(ppm)_t+06 | -1.0723        | 0.0231 | 0.0263 |
| Ox(ppm)_t+07 | -0.6667        | 0.0203 | 0.0236 |
| Ox(ppm)_t+08 | 0.2376         | 0.0132 | 0.0159 |
| Ox(ppm)_t+09 | -0.1592        | 0.0153 | 0.0196 |
| Ox(ppm)_t+10 | 0.1522         | 0.0138 | 0.0168 |
| Ox(ppm)_t+11 | 0.2040         | 0.0138 | 0.0163 |
| Ox(ppm)_t+12 | 0.2805         | 0.0127 | 0.0155 |
| Ox(ppm)_t+13 | 0.3140         | 0.0120 | 0.0151 |
| Ox(ppm)_t+14 | 0.3472         | 0.0115 | 0.0147 |
| Ox(ppm)_t+15 | -0.4246        | 0.0168 | 0.0218 |
| Ox(ppm)_t+16 | -0.3078        | 0.0169 | 0.0209 |
| Ox(ppm)_t+17 | -0.2766        | 0.0161 | 0.0206 |
| Ox(ppm)_t+18 | -0.8230        | 0.0204 | 0.0247 |
| Ox(ppm)_t+19 | -0.3263        | 0.0163 | 0.0210 |
| Ox(ppm)_t+20 | 0.0955         | 0.0133 | 0.0174 |
| Ox(ppm)_t+21 | -0.1580        | 0.0153 | 0.0196 |
| Ox(ppm)_t+22 | -0.2591        | 0.0167 | 0.0205 |
| Ox(ppm)_t+23 | 0.1254         | 0.0136 | 0.0171 |
| Ox(ppm)_t+24 | 0.3184         | 0.0118 | 0.0151 |

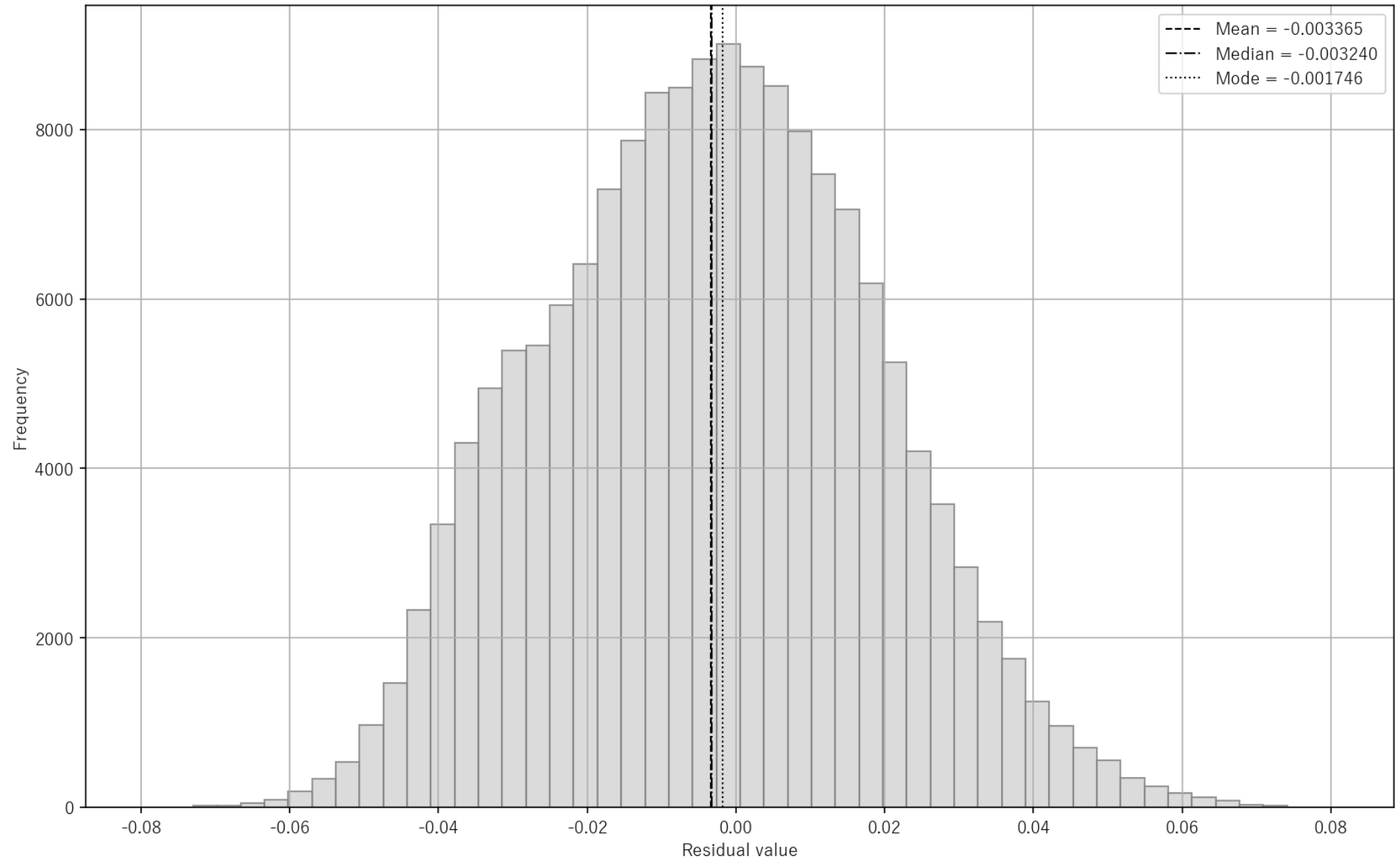
RNN Multi-step Forecast (24h)  
 $R^2$  (avg): -0.49450



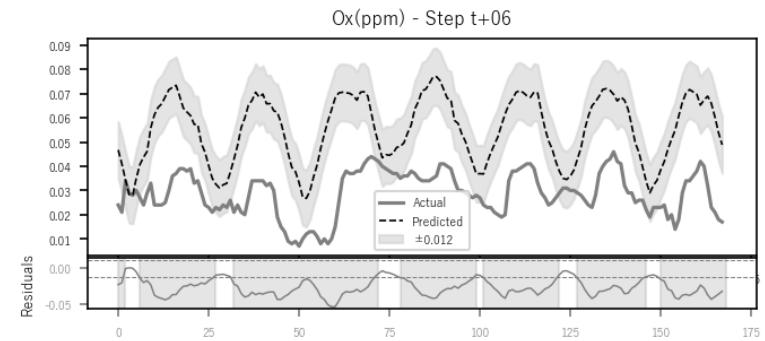
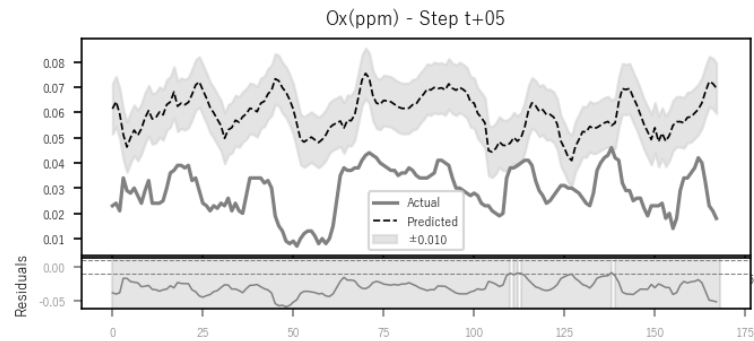
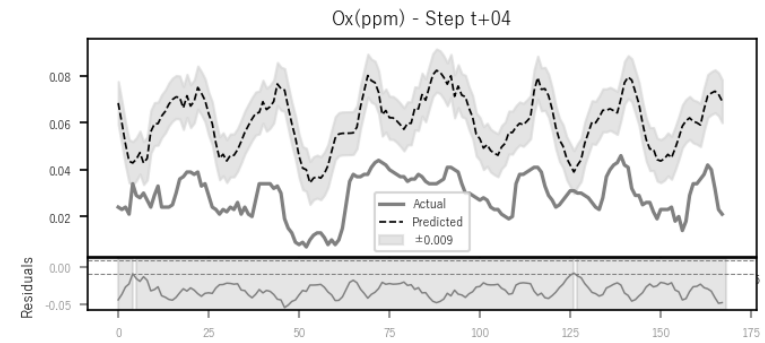
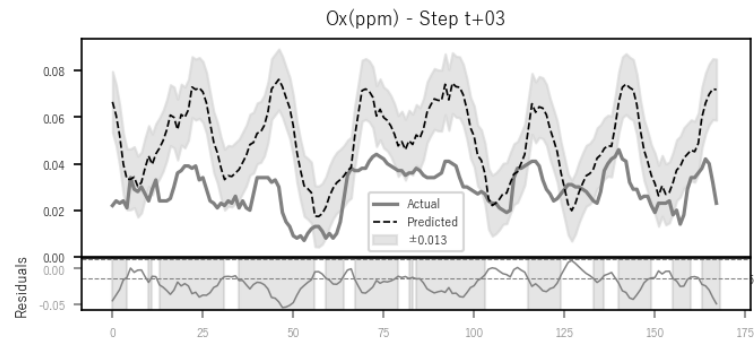
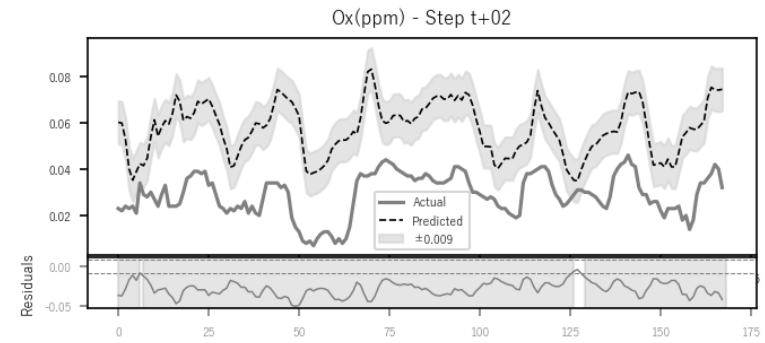
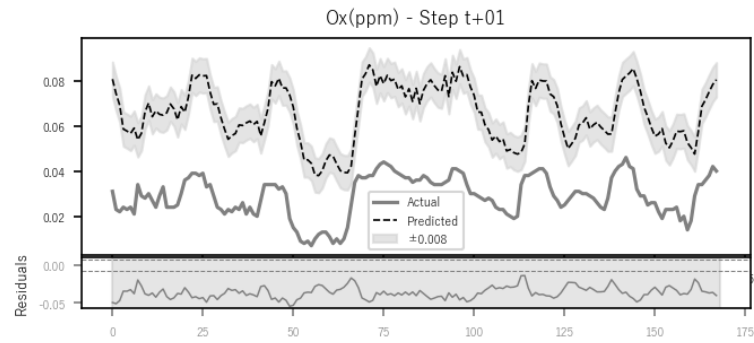
Distribution of Residual Errors



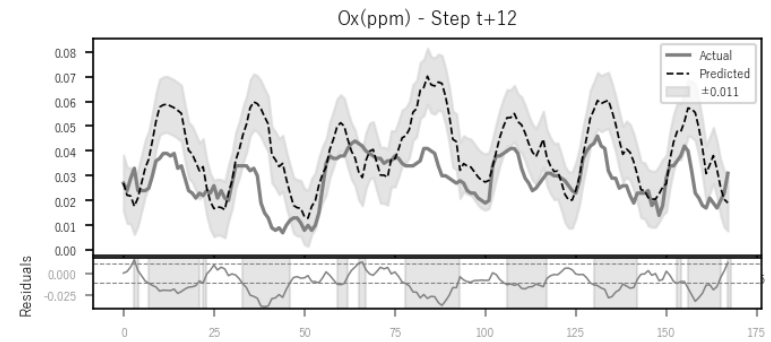
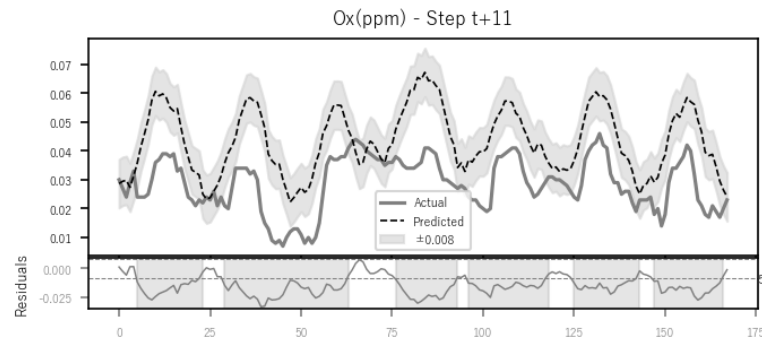
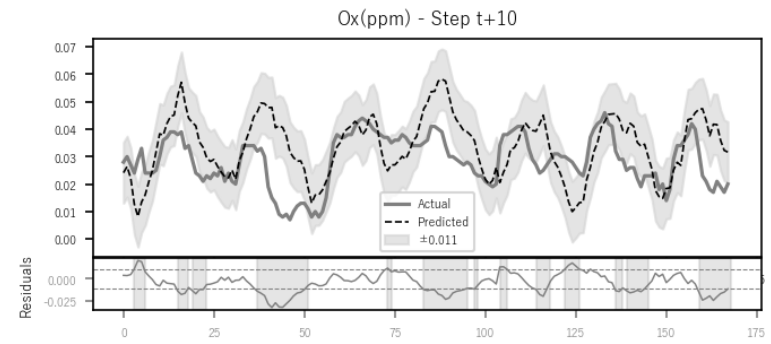
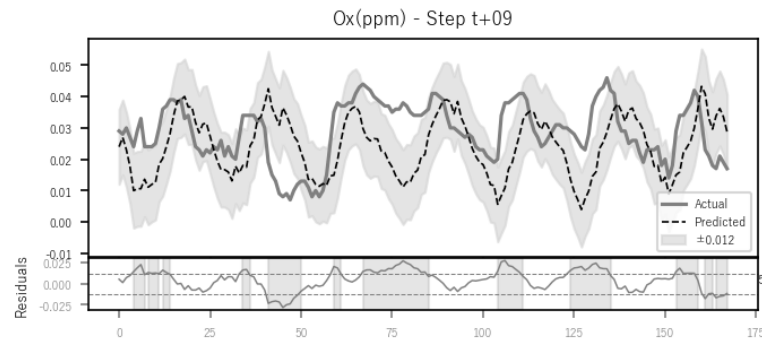
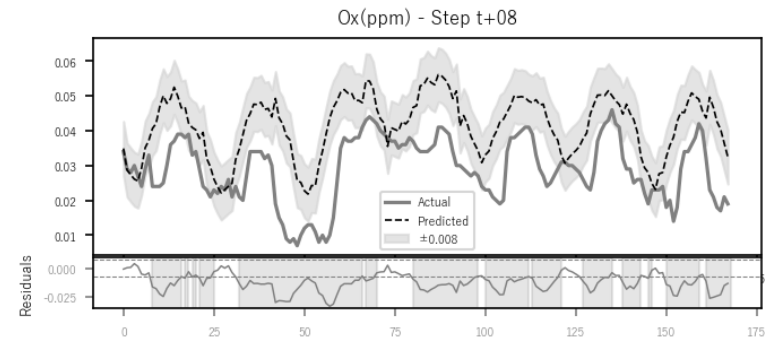
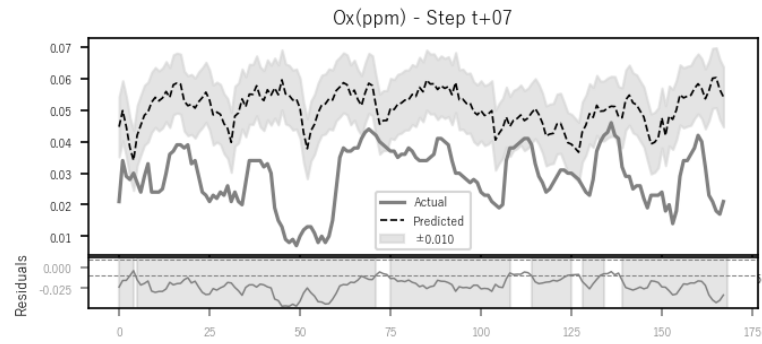
Histogram of Residuals – Distribution & Central Tendency



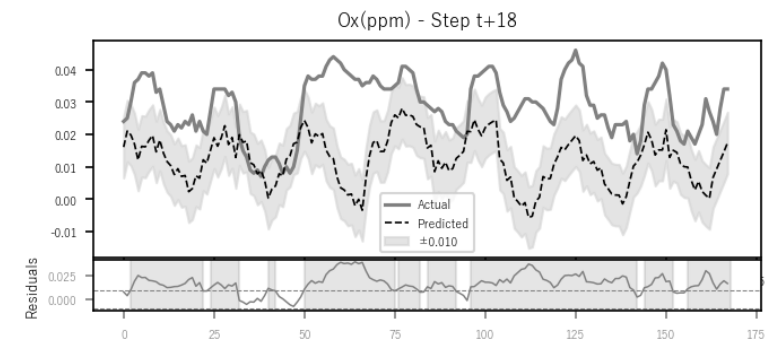
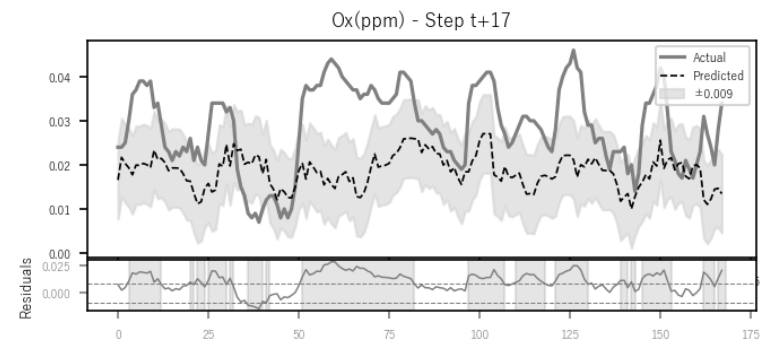
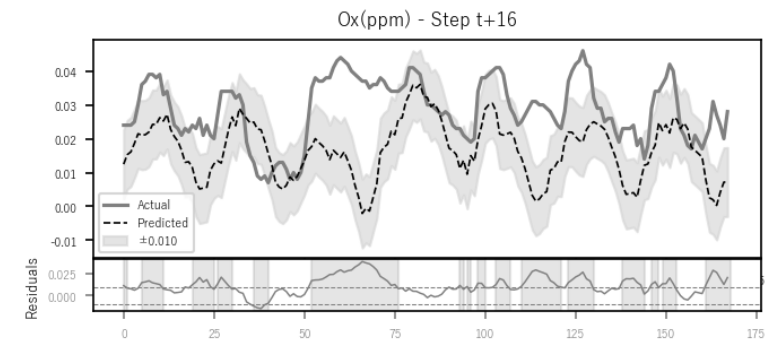
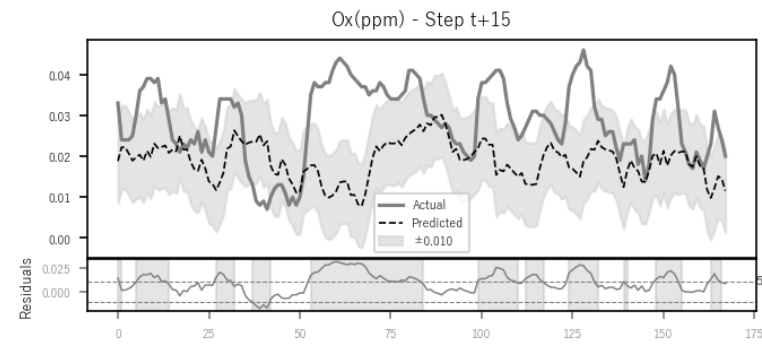
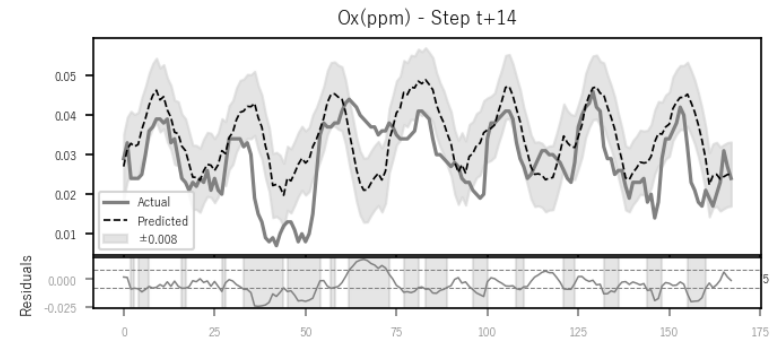
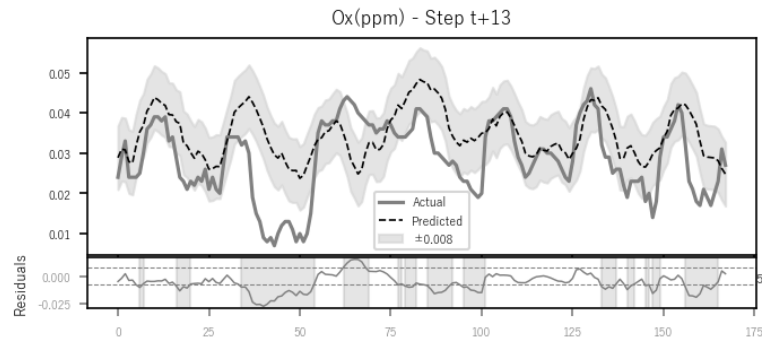
Comparison between actual and predicted values  
with  $\pm$  Standard Deviation Bands



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with  $\pm$  Standard Deviation Bands



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with  $\pm$  Standard Deviation Bands





Comparison between actual and predicted values  
with  $\pm$  Standard Deviation Bands

