IMPORTS

```
In [1]: import numpy as np
        import matplotlib.pyplot as plt
        from sklearn.model_selection import train_test_split
        from sklearn.linear_model import LogisticRegression
        from sklearn.model selection import KFold
        from sklearn.inspection import DecisionBoundaryDisplay
        import torch
        import torch.nn as nn
        import torch.optim as optim
        from torch_geometric.datasets import TUDataset
        from torch_geometric.utils import to_networkx
        import networkx as nx
        from torch_geometric.loader import DataLoader
        from torch_geometric.nn import GINConv, global_mean_pool
        from torch.utils.data import Subset
        from scipy.stats import binom_test # library for p-value
```

c:\Users\matsa\AppData\Local\Programs\Python\Python310\lib\site-packages\tqdm\auto.p
y:21: TqdmWarning: IProgress not found. Please update jupyter and ipywidgets. See ht
tps://ipywidgets.readthedocs.io/en/stable/user_install.html
from .autonotebook import tqdm as notebook_tqdm

LOAD THE DATA

```
In [2]: # https://www.edureka.co/community/72971/how-to-load-numpy-array-in-jupyter-noteboo

features = np.load("data/data/features.npy")
    labels = np.load("data/data/labels.npy")

    print(features.shape)
    print(labels.shape)

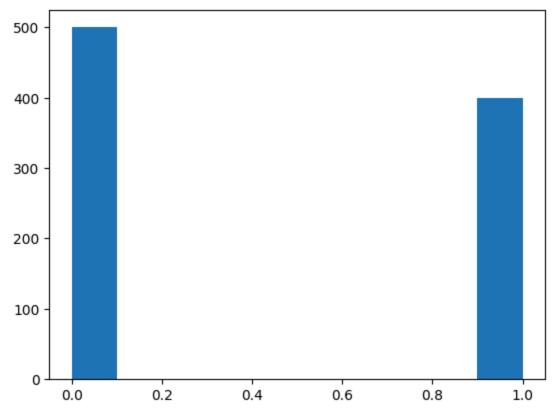
    print(set(labels))

(900, 2)
(900,)
{0.0, 1.0}
```

PART 1

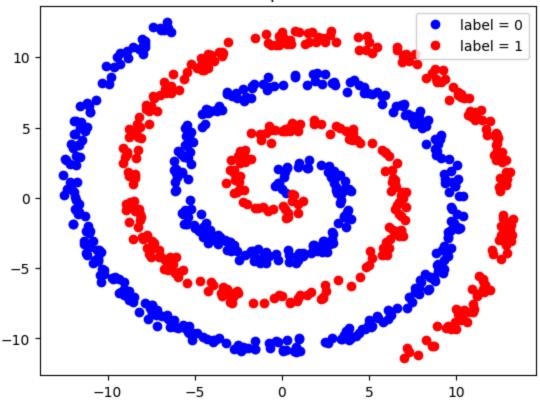
```
In [3]:
    """
1.
    a) 2 features, 900 samples
    b) binary classification since we only have 2 label values, 0 and 1
    c) we can infer that we have 500 0 samples and 400 1 samples
    """
```

```
# c:
plt.hist(labels)
```



```
In [4]: # Go through all the points, check ther label and plot them with the appropriate co
        label_1 = "label = 1"
        label 0 = "label = 0"
        for i in range(features.shape[0]):
            if labels[i] == 0:
                if label_0:
                    plt.plot(features[i][0], features[i][1], "bo", label=f"{label_0}")
                    label 0 = None
                else:
                    plt.plot(features[i][0], features[i][1], "bo")
            else:
                if label_1:
                    plt.plot(features[i][0], features[i][1], "ro", label=f"{label_1}")
                    label_1 = None
                else:
                    plt.plot(features[i][0], features[i][1], "ro")
        plt.title("2D scatter plot of the data")
        plt.legend()
        plt.show()
```

2D scatter plot of the data



```
In [5]:
"""
2.
a)...
b) the data does not look linearly speperable at first glance, since it has a spira
c) no since the data is not linearly seperable
d) the bayes optimal lassifier would follow the spiral pattern that we can observe
    It would be able to achieve an empirical risk of 0, since the data can
    be perfectly seperated due to the lack of noise (the only somewhat problematic p
    but since I am not completely sure I am making a bit of an assumption that we ha
"""
```

Out[5]: '\n2.\na)...\nb) the data does not look linearly speperable at first glance, since it has a spiral-like shape\nc) no since the data is not linearly seperable\nd) the bayes optimal lassifier would follow the spiral pattern that we can observe in the image.\n It would be able to achieve an empirical risk of 0, since the data can \n be perfectly seperated due to the lack of noise (the only somewhat problemati c part might be at the very middle\n but since I am not completely sure I am mak ing a bit of an assumption that we have 0 noise overall)\n'

```
In [5]: # Split data into train and test sets (80-20 split)
   X_train, X_test, y_train, y_test = train_test_split(features, labels, test_size=0.2
   print(X_train.shape)
   print(X_test.shape)

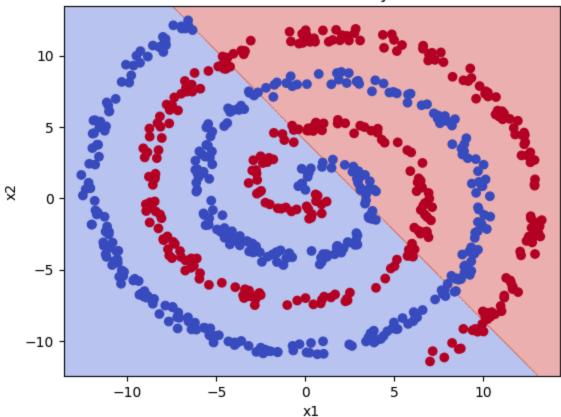
(720, 2)
   (180, 2)
```

```
In [ ]: """
3.
a) The split is neccesary, because you want to be abel to train on a part of the da
```

Out[]: '\n3.\na)...\nb) Well LDA is out of the question since it makes the assumption that we have Gaussian distributions\n as for the other 2, I would choose Logistic R egression, mainly because it is simplier and because\n it works with probabilities, which might be usefull in this case since a poor result is a given, considering all\n 3 classifiers are linear classifiers.\n'

```
In [8]: # Create a logistic classifier, train it and check the accuracy
#log_reg_classifier = LinearDiscriminantAnalysis()
#log_reg_classifier = SVC(kernel='linear', C=1.0)
log_reg_classifier = LogisticRegression()
log_reg_classifier.fit(X_train, y_train)
predictions = log_reg_classifier.predict(X_test)
print(calculate_accuracy(predictions, y_test))
```

Decision Boundary



```
4.

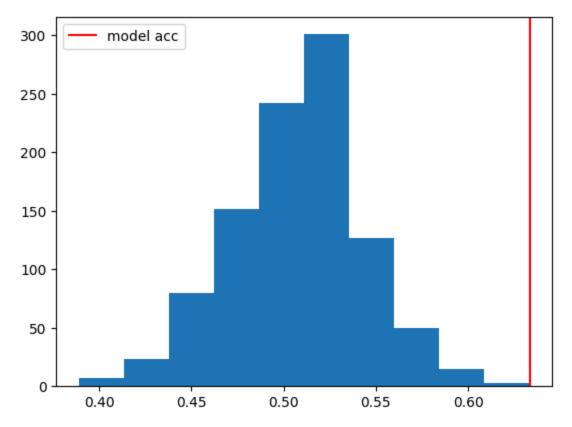
a) 0.6, almsost the same as the classifier
b) ...
c) the plot suggests that we are pretty much guessing. We are doing slightly better this accuracy could be reached.
d) well I repeated it 1000 times (as suggested in the pdf). I believe a 1000 is eno distributed. If we used less then there exists the possibility that outlier valu (when I say less, I mean considerably less, like 100 or 50. Obviously 900 would e) 0.65, so they are not the same which is to be expected. Afterall the chance accu of that cell, whereas this accuracy will always statys the same, since the numbe f) So from what we can observe guessing, picking the label that belongs to the majo because the classifier simply cant do that good of a job, because the data is no depends on the task and as I stated there is some accuracy benefit but it's mini
```

```
In [38]: # https://www.w3schools.com/python/numpy/numpy_random_permutation.asp
    y_test_random = np.random.permutation(y_test)
    print(calculate_accuracy(y_test_random, y_test))

0.6
```

```
In [17]: # Get 1000 accuracy scores and plot them into a histogram
    accuracies = []
    for i in range(1000):
        y_test_random = np.random.permutation(y_test)
        accuracies.append(calculate_accuracy(y_test_random, y_test))
```

Out[17]: <matplotlib.legend.Legend at 0x23bce1b9c90>



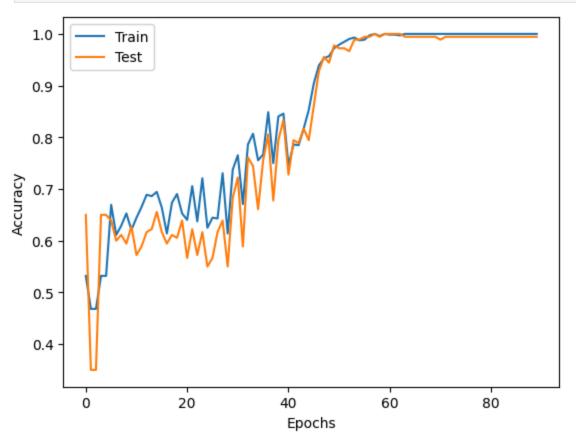
```
In [41]: # Count 0's, if it's greater than the half of the total in the test then 0, else 1
    count = 0
    choise = np.zeros_like(y_test)
    for value in y_test:
        if value == 0:
            count += 1
    if count <= len(y_test)/2:
        choise = np.ones_like(y_test)
    print(calculate_accuracy(choise, y_test))</pre>
```

```
In []:
"""
5.
a) ...
b) The learning curves suggest robustness and good generalization, due to both curv
c) Well my idea was to first find a good architecture, where with enough epochs we
    I did this by adding one layer at the time, while also increasing the number of
    you won't be able to get a better accuracy without adding another layer). After
    I used 10Fold cross validation to fine tune the learning rate (There are countle
    which show that just by tuning the learning rate, you should achieve the best re
d) ...
"""
```

```
In [ ]: # We need to convert to pytorch tensors
        X_train_nn = torch.FloatTensor(X_train)
        X_test_nn = torch.FloatTensor(X_test)
        y train nn = torch.LongTensor(y train)
        y_test_nn = torch.LongTensor(y_test)
        # NN architecture
        class Model(nn.Module):
            def __init__(self):
                super(Model, self).__init__()
                self.l1 = nn.Linear(2, 64)
                self.12 = nn.Linear(64, 128)
                self.13 = nn.Linear(128, 256)
                self.14 = nn.Linear(256, 512)
                self.15 = nn.Linear(512, 1024)
                self.16 = nn.Linear(1024, 2)
                self.relu = nn.ReLU()
            def forward(self, x):
                x = self.relu(self.l1(x))
                x = self.relu(self.12(x))
                x = self.relu(self.13(x))
                x = self.relu(self.14(x))
                x = self.relu(self.15(x))
                x = self.16(x)
                return x
        # Initialize some stuff
        model = Model()
        criterion = nn.CrossEntropyLoss()
        optimizer = optim.Adam(model.parameters(), lr=0.01)
        # Training Loop
        train_acc, test_acc = [], []
        for epoch in range(90):
            model.train()
            optimizer.zero_grad()
            outputs = model(X_train_nn)
            loss = criterion(outputs, y_train_nn)
            loss.backward()
            optimizer.step()
            with torch.no_grad():
                model.eval()
                # Train
                train_pred = model(X_train_nn).argmax(1)
                train_acc.append((train_pred == y_train_nn).float().mean())
                # Test
                test_pred = model(X_test_nn).argmax(1)
                test_acc.append((test_pred == y_test_nn).float().mean())
```

c:\Users\matsa\AppData\Local\Programs\Python\Python310\lib\site-packages\tqdm\auto.p
y:21: TqdmWarning: IProgress not found. Please update jupyter and ipywidgets. See ht
tps://ipywidgets.readthedocs.io/en/stable/user_install.html
from .autonotebook import tqdm as notebook_tqdm

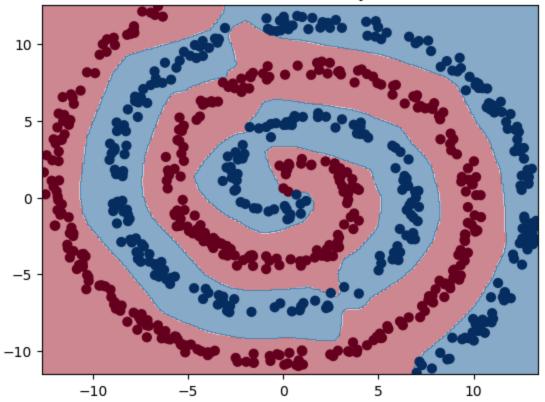
```
In [ ]: plt.plot(train_acc, label="Train")
    plt.plot(test_acc, label="Test")
    plt.xlabel("Epochs")
    plt.ylabel("Accuracy")
    plt.legend()
    plt.show()
```



```
In [ ]: # Learning rates
        learning_rates = [0.0001, 0.001, 0.005, 0.01, 0.05]
        kf = KFold(n_splits=k, shuffle=True)
        results = {}
        for lr in learning_rates:
            print(f"Testing learning rate: {lr}")
            fold_accuracies = []
            for train_index, val_index in kf.split(X_train_nn):
                # Split data
                X_train_cv, X_val_cv = X_train_nn[train_index], X_train_nn[val_index]
                y_train_cv, y_val_cv = y_train_nn[train_index], y_train_nn[val_index]
                model1 = Model()
                optimizer = optim.Adam(model1.parameters(), lr=lr)
                for epoch in range(90):
                    model1.train()
                    optimizer.zero_grad()
```

```
outputs = model1(X_train_nn)
                    loss = criterion(outputs, y_train_nn)
                    loss.backward()
                    optimizer.step()
                    with torch.no_grad():
                        model1.eval()
                        # Validation accuracy
                        val pred = model1(X val cv).argmax(1)
                        fold_accuracies.append((val_pred == y_val_cv).float().mean())
            avg_acc = np.mean(fold_accuracies)
            results[lr] = avg_acc
            print(f"Average validation accuracy: {avg_acc}")
        # Best Learning rate
        best_lr = max(results, key=results.get)
        print("\nBest learning rate:", best_lr)
In [ ]: # https://psrivasin.medium.com/plotting-decision-boundaries-using-numpy-and-matplot
        # Create mesh grid
        # Range for visualization
        x_{min}, x_{max} = X_{train}[:, 0].min() - 0.1, X_{train}[:, 0].max() + 0.1
        y_min, y_max = X_train[:, 1].min() - 0.1, X_train[:, 1].max() + 0.1
        # Create "points" (not yet points) that will use to draw the decision boundary
        xx, yy = np.meshgrid(np.linspace(x_min, x_max, 400), np.linspace(y_min, y_max, 400)
        # Create the actuall points
        x_in = np.c_[xx.ravel(), yy.ravel()]
        x_in_tensor = torch.FloatTensor(x_in)
        # Predict
        model.eval()
        with torch.no_grad():
            y_pred = model(x_in_tensor).argmax(1).reshape(xx.shape)
        # PLot
        plt.contourf(xx, yy, y_pred, cmap=plt.cm.RdBu, alpha=0.5)
        plt.scatter(X_train[:, 0], X_train[:, 1], c=y_train, s=40, cmap=plt.cm.RdBu)
        plt.title("Decision Boundary")
        plt.show()
```

Decision Boundary



PART 2

```
0.000
In [ ]:
         1.
         a) 188, 7, 2
         b) Per the ai model (prompt: Can you explain what the MUTAG dataset represents? Spe
            and google (https://paperswithcode.com/dataset/mutag)
            Sample: Chemical compound modeled as a graph
            Nodes: Atoms
            Edges: Bonds between the atoms
            Features: Features are one-hot encodings, so in essense the feature vector tells
            Labels: 1 if chemical compound is mutagenic, 0 if not
         c) The first sample has 17 nodes and 38 edges (prompt: how to get the nodes and edg
         d) ...
In [19]: # (https://medium.com/@james-coffey/gcn-with-neo4j-and-pytorch-using-mutag-dataset-
         dataset = TUDataset(root="data", name="MUTAG")
         samples = len(dataset)
         features = dataset.num_node_features
         classes = dataset.num_classes
         print(f"Samples: {samples}, Features: {features}, Classes: {classes}")
        Samples: 188, Features: 7, Classes: 2
```

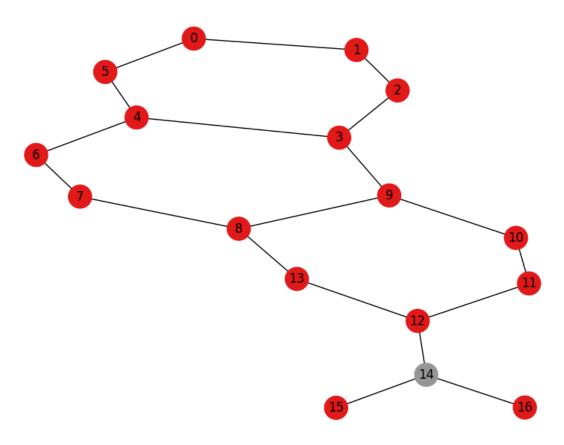
```
In [93]: # Nodes and edges in first graph
    sample = dataset[0]
    nodes = sample.x
    edges = sample.edge_index
    print(f"First sample has {nodes.shape[0]} nodes and {edges.shape[1]} edges")
```

First sample has 17 nodes and 38 edges

```
In [ ]: # Plot graph of the first sample with nodes colored by second feature (index 1)
graph = to_networkx(sample, to_undirected=True)
node_colors = sample.x[:, 1].tolist()

plt.figure(figsize=(8, 6))
nx.draw(graph, with_labels=True, node_color=node_colors, cmap=plt.cm.Set1, node_siz
plt.title("First graph from MUTAG")
plt.show()
```

First graph from MUTAG



In []: ""

We shall use the same linear modle as before, so Linear Regression.

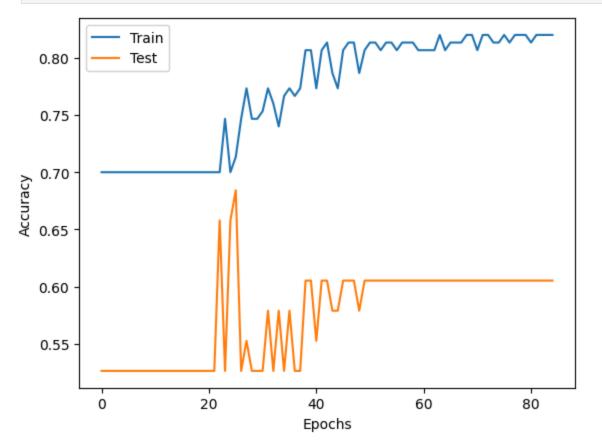
- a) After asking the AI "How can I prep the data so that I can train without using g add them together and then devide the whole vector by the number of nodes in tha
- b) ..., fairly poor results, we are learning just not all that much, peaking at aro
- c) Choosing most frequent label = 0.6648936170212766, Guessing = 0.4210526315789473 that even with the NN the accuracy remains low (plateauing at around 60%)

```
In [7]: # Prep the data
         features = []
         labels = []
         # Loop through each graph in the dataset
         for data in dataset:
             # data.x is a tensor that for each node in the graph, will have it's feature ve
             graph_features = data.x.mean(dim=0).numpy()
             features.append(graph_features)
             labels.append(data.y.item()) # Convert to a single number rather than a tensor
         # Split data into train and test sets (80-20 split)
         train_idx, test_idx = train_test_split(range(len(dataset)), test_size=0.2)
         # Split the training set further so that we can later use this for the validation p
         train_idx_val, val_idx = train_test_split(range(len(train_idx)), test_size=0.2)
         # Get the actual training splits
         X_train = np.array([features[i] for i in train_idx])
         X_test = np.array([features[i] for i in test_idx])
         y_train = np.array([labels[i] for i in train_idx])
         y_test = np.array([labels[i] for i in test_idx])
         #X_train, X_test, y_train, y_test =
         #X_train, X_test, y_train, y_test = train_test_split(features, labels, test_size=0.
         #print(len(X_train))
         #print(len(X_test))
In [8]: # GREAT DATA IMBALANCE NEEDS TO BE TAKEN INTO ACCOUNT!
         # What if we choose the most frequent class?
         count = 0
         for label in labels:
             if label == 1:
                 count += 1
         print(count/samples)
        0.6648936170212766
In [15]: # Guessing
         y_test_shuffled = np.random.permutation(y_test)
         print(calculate_accuracy(y_test_shuffled, y_test))
        0.42105263157894735
In [14]: # Linear model
         log_reg_classifier = LogisticRegression()
         log_reg_classifier.fit(X_train, y_train)
         predictions = log_reg_classifier.predict(X_test)
         print(calculate_accuracy(predictions, y_test))
```

```
In [ ]: # NN
        import torch
        import torch.nn as nn
        import torch.optim as optim
        import matplotlib.pyplot as plt
        # We need to convert to pytorch tensors
        X_train_nn = torch.FloatTensor(X_train)
        X_test_nn = torch.FloatTensor(X_test)
        y train nn = torch.LongTensor(y train)
        y_test_nn = torch.LongTensor(y_test)
        # NN architecture
        class Model(nn.Module):
            def __init__(self):
                super(Model, self).__init__()
                 self.l1 = nn.Linear(7, 64)
                self.12 = nn.Linear(64, 128)
                self.13 = nn.Linear(128, 256)
                self.14 = nn.Linear(256, 512)
                self.15 = nn.Linear(512, 512)
                self.16 = nn.Linear(512, 2)
                self.relu = nn.ReLU()
            def forward(self, x):
                x = self.relu(self.l1(x))
                x = self.relu(self.12(x))
                x = self.relu(self.13(x))
                x = self.relu(self.14(x))
                x = self.relu(self.15(x))
                x = self.16(x)
                return x
        # Initialize some stuff
        model = Model()
        criterion = nn.CrossEntropyLoss()
        optimizer = optim.Adam(model.parameters(), lr=0.01)
        # Training Loop
        train_acc, test_acc = [], []
        for epoch in range(85):
            model.train()
            optimizer.zero_grad()
            outputs = model(X_train_nn)
            loss = criterion(outputs, y_train_nn)
            loss.backward()
            optimizer.step()
            with torch.no_grad():
                model.eval()
                # Train
```

```
train_pred = model(X_train_nn).argmax(1)
train acc.append((train_pred == y_train_nn).float().mean())
# Test
test_pred = model(X_test_nn).argmax(1)
test_acc.append((test_pred == y_test_nn).float().mean())
```

```
In [ ]: plt.plot(train_acc, label="Train")
        plt.plot(test_acc, label="Test")
        plt.xlabel("Epochs")
        plt.ylabel("Accuracy")
        plt.legend()
        plt.show()
```



In [27]: print(test_acc[-1])

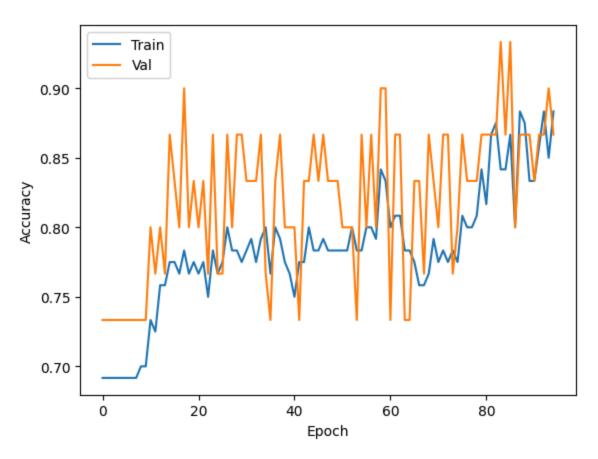
tensor(0.6053)

```
0.00
In [ ]:
```

- 3.
- a) ...
- b) AI prompt : "How does a GNN take into account graph info and what does the layer Per the ai and a bit of crossreferencing on google I understood that the high le is that each node doesn't just use it's own information but through message pass into account information of its surrounding/ neighboring nodes before updating i how far the neighbor you receive onfo from can be. Layer 1 -> immediate neighbor neighbor of neighor, etc.
- c) ..., in essense I just created a validation dataset from the training dataset an looked a bit on batch sizes but didn't get much of a change (even though I belie
- d) Accuracy = 0.79, P-value = 4.051328899727381e-06 (not exactly 0 probably but pre

```
In [ ]: # THIS PART IS USED FOR FINDING THE BEST HYPERPARAMETERS
        train_dataset = Subset(dataset, train_idx)
        # Create subsets for train and validation
        train_subdataset = Subset(train_dataset, train_idx_val)
        val_subdataset = Subset(train_dataset, val_idx)
        # DataLoaders for these subsets
        train_loader = DataLoader(train_subdataset, batch_size=32, shuffle=True)
        val_loader = DataLoader(val_subdataset, batch_size=32, shuffle=False)
        # Model with GINConv Layers
        class Model2(nn.Module):
            def __init__(self):
                super(Model2, self).__init__()
                part1 = nn.Sequential(
                    nn.Linear(7, 64),
                    nn.ReLU(),
                    nn.Linear(64, 128)
                self.l1 = GINConv(part1)
                part2 = nn.Sequential(
                    nn.Linear(128, 256),
                    nn.ReLU(),
                    nn.Linear(256, 256)
                self.12 = GINConv(part2)
                part3 = nn.Sequential(
                    nn.Linear(256, 512),
                    nn.ReLU(),
                    nn.Linear(512, 512)
                self.13 = GINConv(part3)
                self.14 = nn.Linear(512, 2)
                self.relu = nn.ReLU()
            def forward(self, x, edge_index, batch):
                x = self.relu(self.l1(x, edge_index))
                x = self.relu(self.12(x, edge_index))
                x = self.relu(self.13(x, edge_index))
                x = global_mean_pool(x, batch)
                x = self.14(x)
                return x
        model = Model2()
        criterion = nn.CrossEntropyLoss()
        optimizer = optim.Adam(model.parameters(), lr=0.01)
```

```
train_acc, val_acc = [], []
for epoch in range(95):
   model.train()
   for batch in train_loader:
        optimizer.zero_grad()
        outputs = model(batch.x, batch.edge_index, batch.batch)
        loss = criterion(outputs, batch.y)
        loss.backward()
        optimizer.step()
   with torch.no_grad():
       model.eval()
       # Train
       correct = 0
       total = 0
       for batch in train_loader:
            out = model(batch.x, batch.edge_index, batch.batch)
            pred = out.argmax(dim=1)
            correct += (pred == batch.y).sum().item()
            total += batch.y.size(0)
       train_acc.append(correct / total)
       # VaL
       correct = 0
       total = 0
       for batch in val_loader:
            out = model(batch.x, batch.edge_index, batch.batch)
            pred = out.argmax(dim=1)
            correct += (pred == batch.y).sum().item()
            total += batch.y.size(0)
        val_acc.append(correct / total)
# Plot results
plt.plot(train_acc, label="Train")
plt.plot(val_acc, label="Val")
plt.xlabel("Epoch")
plt.ylabel("Accuracy")
plt.legend()
plt.show()
```



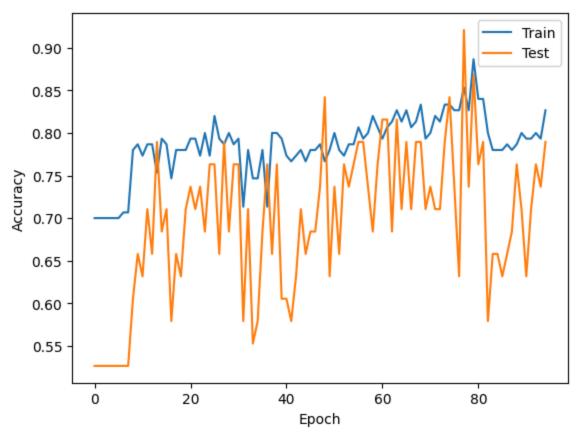
```
In [48]: print(train_acc[-1])
    print(val_acc[-1])
```

0.8833333333333333

```
In [ ]: train_dataset = Subset(dataset, train_idx)
        test_dataset = Subset(dataset, test_idx)
        train_loader = DataLoader(train_dataset, batch_size=32, shuffle=True)
        test_loader = DataLoader(test_dataset, batch_size=32, shuffle=False)
        # Model with GINConv layers
        class Model2(nn.Module):
            def __init__(self):
                super(Model2, self).__init__()
                 part1 = nn.Sequential(
                    nn.Linear(7, 64),
                    nn.ReLU(),
                    nn.Linear(64, 128)
                 self.l1 = GINConv(part1)
                 part2 = nn.Sequential(
                    nn.Linear(128, 256),
                    nn.ReLU(),
                    nn.Linear(256, 256)
                 self.12 = GINConv(part2)
```

```
part3 = nn.Sequential(
            nn.Linear(256, 512),
            nn.ReLU(),
            nn.Linear(512, 512)
        self.13 = GINConv(part3)
        self.14 = nn.Linear(512, 2)
        self.relu = nn.ReLU()
    def forward(self, x, edge_index, batch):
        x = self.relu(self.l1(x, edge_index))
        x = self.relu(self.l2(x, edge_index))
        x = self.relu(self.13(x, edge_index))
        x = global_mean_pool(x, batch)
        x = self.14(x)
        return x
model = Model2()
criterion = nn.CrossEntropyLoss()
optimizer = optim.Adam(model.parameters(), lr=0.01)
train_acc, test_acc = [], []
for epoch in range(95):
    model.train()
    for batch in train_loader:
        optimizer.zero_grad()
        outputs = model(batch.x, batch.edge_index, batch.batch)
        loss = criterion(outputs, batch.y)
        loss.backward()
        optimizer.step()
    with torch.no_grad():
        model.eval()
        # Train
        correct = 0
        total = 0
        for batch in train_loader:
            out = model(batch.x, batch.edge_index, batch.batch)
            pred = out.argmax(dim=1)
            correct += (pred == batch.y).sum().item()
            total += batch.y.size(0)
        train_acc.append(correct / total)
        # Test
        correct = 0
        total = 0
        for batch in test loader:
            out = model(batch.x, batch.edge_index, batch.batch)
            pred = out.argmax(dim=1)
            correct += (pred == batch.y).sum().item()
            total += batch.y.size(0)
        test_acc.append(correct / total)
```

```
# Plot results
plt.plot(train_acc, label="Train")
plt.plot(test_acc, label="Test")
plt.xlabel("Epoch")
plt.ylabel("Accuracy")
plt.legend()
plt.show()
```



```
In [50]: print(train_acc[-1])
    print(test_acc[-1])

0.8266666666666667
    0.7894736842105263

In []: # P-value calculation
    correct = int(len(test_idx)*test_acc[-1])
    total = len(test_idx)
    p_value = binom_test(correct, total, p=0.42105263157894735, alternative="greater")
    print(f"P-value: {p_value}")

P-value: 4.051328899727381e-06

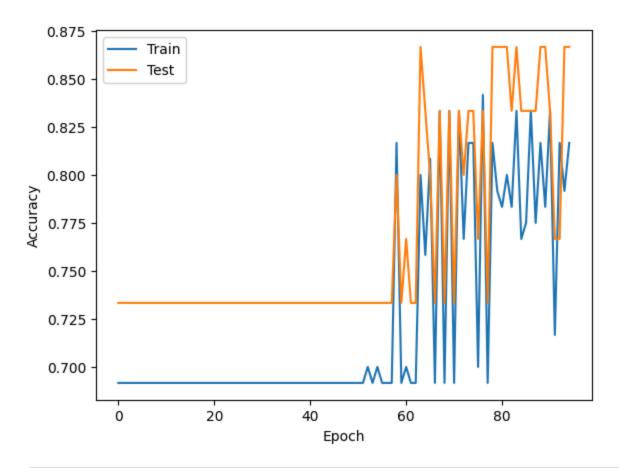
C:\Users\matsa\AppData\Local\Temp\ipykernel_20960\1323653989.py:8: DeprecationWarnin g: 'binom_test' is deprecated in favour of 'binomtest' from version 1.7.0 and will be removed in Scipy 1.12.0.
    p_value = binom_test(correct, total, p=0.42105263157894735, alternative='greater')
```

```
In []:
4.
a) ...
```

b) After some tests I found that using 2 + 16*2 (16 GIN layers with 2 linear layers and 2in 2out respectively) gave me pretty good results (around 80% accuracy) on c)

```
In [ ]: # THIS PART IS USED FOR FINDING THE BEST HYPERPARAMETERS
        train_dataset = Subset(dataset, train_idx)
        # Subsets for train and validation
        train_subdataset = Subset(train_dataset, train_idx_val)
        val_subdataset = Subset(train_dataset, val_idx)
        # DataLoaders for these subsets
        train_loader = DataLoader(train_subdataset, batch_size=32, shuffle=True)
        val_loader = DataLoader(val_subdataset, batch_size=32, shuffle=False)
        # Model with GINConv layers
        class Model2(nn.Module):
            def __init__(self):
                super(Model2, self).__init__()
                self.convs = nn.ModuleList()
                part1 = nn.Sequential(
                    nn.Linear(7, 6),
                    nn.ReLU(),
                    nn.Linear(6, 6)
                self.convs.append(GINConv(part1))
                for _ in range(15):
                    part = nn.Sequential(
                        nn.Linear(6, 6),
                        nn.ReLU(),
                        nn.Linear(6, 6)
                    self.convs.append(GINConv(part))
                self.em = nn.Linear(6, 2) # Embedding Layer
                self.fin = nn.Linear(2, 2)
                self.relu = nn.ReLU()
            def forward(self, x, edge_index, batch):
                for conv in self.convs:
                    x = self.relu(conv(x, edge_index))
                x = global_mean_pool(x, batch)
                embedding = self.em(x) # Embedding
                out = self.fin(embedding)
                return out, embedding
        model = Model2()
        criterion = nn.CrossEntropyLoss()
        optimizer = optim.Adam(model.parameters(), lr=0.01)
```

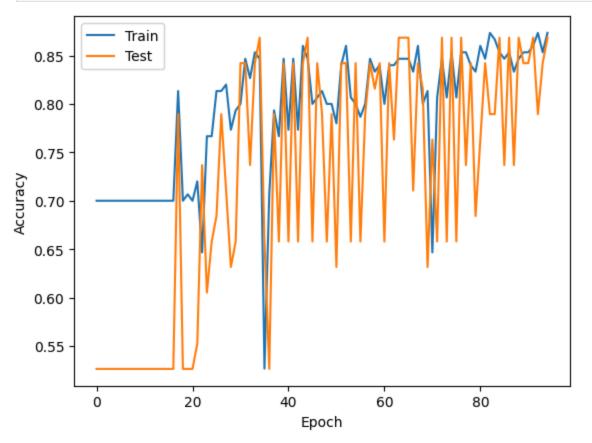
```
train_acc, val_acc = [], []
embeddings = []
predictions = []
true_labels = []
for epoch in range(95):
   model.train()
   for batch in train_loader:
        optimizer.zero_grad()
        outputs, embedding = model(batch.x, batch.edge_index, batch.batch)
        loss = criterion(outputs, batch.y)
        loss.backward()
        optimizer.step()
   with torch.no_grad():
       model.eval()
       # Train
       correct = 0
       total = 0
       for batch in train_loader:
            out, embedding = model(batch.x, batch.edge_index, batch.batch)
            pred = out.argmax(dim=1)
            correct += (pred == batch.y).sum().item()
            total += batch.y.size(0)
       train_acc.append(correct / total)
        # Val
        correct = 0
       total = 0
       for batch in val_loader:
            out, embedding = model(batch.x, batch.edge_index, batch.batch)
            pred = out.argmax(dim=1)
            embeddings.append(embedding)
            true_labels.append(batch.y)
            predictions.append(pred)
            correct += (pred == batch.y).sum().item()
            total += batch.y.size(0)
        val_acc.append(correct / total)
# Plot results
plt.plot(train_acc, label="Train")
plt.plot(val_acc, label="Test")
plt.xlabel("Epoch")
plt.ylabel("Accuracy")
plt.legend()
plt.show()
```



```
In [ ]: train_dataset = Subset(dataset, train_idx)
        test_dataset = Subset(dataset, test_idx)
        train_loader = DataLoader(train_dataset, batch_size=32, shuffle=True)
        test_loader = DataLoader(test_dataset, batch_size=32, shuffle=False)
        # Model with GINConv layers
        class Model2(nn.Module):
            def __init__(self):
                super(Model2, self).__init__()
                self.convs = nn.ModuleList()
                part1 = nn.Sequential(
                    nn.Linear(7, 6),
                    nn.ReLU(),
                    nn.Linear(6, 6)
                self.convs.append(GINConv(part1))
                for _ in range(15):
                    part = nn.Sequential(
                        nn.Linear(6, 6),
                         nn.ReLU(),
                         nn.Linear(6, 6)
                    self.convs.append(GINConv(part))
                self.em = nn.Linear(6, 2) # Embedding Layer
```

```
self.fin = nn.Linear(2, 2)
        self.relu = nn.ReLU()
    def forward(self, x, edge_index, batch):
        for conv in self.convs:
            x = self.relu(conv(x, edge_index))
        x = global_mean_pool(x, batch)
        embedding = self.em(x) # Embedding
        out = self.fin(embedding)
        return out, embedding
model = Model2()
criterion = nn.CrossEntropyLoss()
optimizer = optim.Adam(model.parameters(), lr=0.01)
train_acc, val_acc = [], []
embeddings = []
predictions = []
true_labels = []
for epoch in range(95):
    model.train()
    for batch in train_loader:
        optimizer.zero_grad()
        outputs, embedding = model(batch.x, batch.edge_index, batch.batch)
        loss = criterion(outputs, batch.y)
        loss.backward()
        optimizer.step()
    with torch.no_grad():
        model.eval()
        # Train
        correct = 0
        total = 0
        for batch in train loader:
            out, embedding = model(batch.x, batch.edge_index, batch.batch)
            pred = out.argmax(dim=1)
            correct += (pred == batch.y).sum().item()
            total += batch.y.size(0)
        train_acc.append(correct / total)
        # Test
        correct = 0
        total = 0
        for batch in test loader:
            out, embedding = model(batch.x, batch.edge_index, batch.batch)
            pred = out.argmax(dim=1)
            embeddings.append(embedding)
            true_labels.append(batch.y)
            predictions.append(pred)
            correct += (pred == batch.y).sum().item()
            total += batch.y.size(0)
        val_acc.append(correct / total)
# Plot results
```

```
plt.plot(train_acc, label="Train")
plt.plot(val_acc, label="Test")
plt.xlabel("Epoch")
plt.ylabel("Accuracy")
plt.legend()
plt.show()
```



```
In [ ]: # Lists to tensors
        embeddings_tensor = torch.cat(embeddings, dim=0)
        true_labels_tensor = torch.cat(true_labels, dim=0)
        predictions_tensor = torch.cat(predictions, dim=0)
        # Tensors to NumPy
        emb_np = embeddings_tensor.numpy()
        true_np = true_labels_tensor.numpy()
        pred_np = predictions_tensor.numpy()
        x_{min}, x_{max} = emb_{np}[:, 0].min() - 1, emb_{np}[:, 0].max() + 1
        y_{min}, y_{max} = emb_np[:, 1].min() - 1, <math>emb_np[:, 1].max() + 1
        xx, yy = np.meshgrid(np.linspace(x_min, x_max, 200), np.linspace(y_min, y_max, 200)
        grid_points = np.c_[xx.ravel(), yy.ravel()]
        grid_tensor = torch.from_numpy(grid_points.astype(np.float32))
        model.eval()
        with torch.no_grad():
            grid_outputs = model.fin(grid_tensor) # Using final classification layer
            grid_preds = torch.argmax(grid_outputs, dim=1).numpy()
        grid_preds = grid_preds.reshape(xx.shape)
```

```
plt.figure(figsize=(12, 5))

plt.subplot(1, 2, 1)

plt.scatter(emb_np[:, 0], emb_np[:, 1], c=true_np, cmap="plasma", edgecolor="k", al

plt.contourf(xx, yy, grid_preds, alpha=0.2, cmap="plasma")

plt.title("Samples Colored by True Labels + Decision Boundary")

plt.xlabel("Embedding dim 1")

plt.ylabel("Embedding dim 2")

plt.subplot(1, 2, 2)

plt.scatter(emb_np[:, 0], emb_np[:, 1], c=pred_np, cmap="plasma", edgecolor="k", al

plt.contourf(xx, yy, grid_preds, alpha=0.2, cmap="plasma")

plt.title("Samples Colored by Predicted Labels + Decision Boundary")

plt.xlabel("Embedding dim 1")

plt.ylabel("Embedding dim 2")

plt.tight_layout()

plt.show()
```

