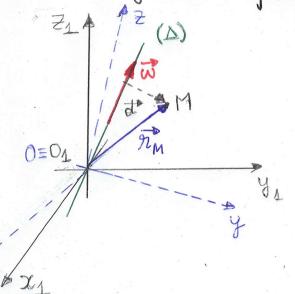
Kinematics of the rigid body

Rigid body with a fixed point:



$$\overrightarrow{a}_{M} = \overrightarrow{\omega} \times \overrightarrow{R}_{M}$$

$$\overrightarrow{a}_{M} = \overrightarrow{\omega} \times \overrightarrow{R} + \overrightarrow{\omega} \times (\overrightarrow{\omega} \times \overrightarrow{R}_{M})$$

$$= \overrightarrow{\omega} \times \overrightarrow{R} - \omega^{2} \cdot \overrightarrow{d}$$

△ - instantaneous axis of rotation

$$A \in (\Delta) \Rightarrow [\overline{v_A} = 0]$$

Thus:
$$\Delta: \frac{\chi}{P(t)} = \frac{4}{9(t)} = \frac{2}{72(t)}$$

where w = w(p,2,t).

1) Consider a rigid body with a fixed point 0. It is known that the velocity of a point M, (0,0,2) of the rigid is $V_{M_1}(1,2,0)$ and the direction's cosines of the velocity of the point M2(0,1,2) are (-23,2)-3). Find the angular velocity is and the equation of the instantaneous axis of rotation.

Rotation about a fined point = $\vec{v}_H = \vec{w} \times \vec{n}_H$, $\vec{w} (p_1 2_1 n)$. Solution:

$$|\nabla_{M_1} = |\nabla \times \vec{h}_{M_1}| =$$

$$\frac{11}{2,0}$$

$$\frac{1}{2,0}$$

$$\frac{1}{2,0}$$

$$\frac{1}{2}$$

Direction cosines:

$$\frac{1-2}{\sqrt{(1-2)^{2}+5}} = -\frac{2}{3}; \frac{2}{\sqrt{(1-2)^{2}+5}} = \frac{2}{3}; \frac{-1}{\sqrt{(1-2)^{2}+5}} = -\frac{1}{3}$$

$$9(1-2)^{2} = 4(1-2) + 20$$

$$(1-2)^{2} = 4 \implies 21 = 3$$

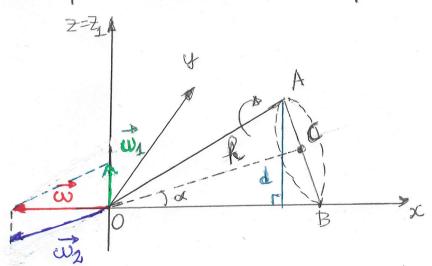
$$(1-2)^{2} = 4 \implies 22 = 4 \text{ (! mot ok, does mot verify (2a))}$$

Thus, we have: \(\overline{1}, \frac{1}{2}, 3\).

Instantaneous aris of rotation:

transport and of Notation:
(A):
$$\frac{\chi}{P} = \frac{4}{2} = \frac{7}{2} \implies (A): \frac{\chi}{-1} = \frac{4}{2} = \frac{2}{3}$$
.

(2) A circular cone of height h and with the vertex angle of 2d is rolling without slipping on a plane wich rotates around a fixed axis 071 perpendicular on the plane with a constant angular speed w1. Find the rotation and centripetal acceleration of a point A from the cone's base.



The rolling of the cone on the plane consists in a rotation about OC with the angular velocity wie and a rotation about OZI with the angular velocity wis.

On the other hand, the points from OB have no rotation. It means that the two rotations wis and wie combine in a unique rotation w, oriented on the instantaneous axis of

In order to find w, we calculate the velocity of the point C in two ways:

1. C rotates about OB => Ve = W1. d(C,OB) = W1. h. cosd)
2. C rotates about OB => Ve = W. d(C,OB) = W. h. sind) =>

=> w = w1. dg x => \vec{w} = -w1. dg x. i (1)

We have $\vec{w} = \vec{w}_1 + \vec{w}_2 = \vec{v}_c = \vec{w}_1 + \vec{w}_2) \times \vec{oc} = (\vec{w}_1 + \vec{w}_2$

= $\overrightarrow{\omega_1} \times \overrightarrow{oc}$ oc 11W2

Rotation acceleration of point A:

 $\vec{a}_{not} = \vec{\omega} \times \vec{r}_{A} = \vec{\omega} \times \vec{o} \vec{A}$ $\vec{\omega} = \frac{d\vec{\omega}}{dt} = -\omega_{1} \cdot dg \cdot d\vec{i} = -\omega_{1} \cdot dg \cdot \omega_{1} \cdot \vec{h} \times \vec{r} = -\omega_{1}^{2} \cdot dg \cdot \vec{d}$ $\vec{\omega} = \frac{d\vec{\omega}}{dt} = -\omega_{1} \cdot dg \cdot d\vec{i} = -\omega_{1} \cdot dg \cdot d\vec{i}$

Poisson. di = Wixi formulas dt = 4 angular relocity in the rolling rigid (0xyz).

 $\Delta OAC => OA = \frac{h}{cod} =>$ $=> OA \left(\frac{h}{cod}, cos 2d, o, \frac{h}{cos d}\right)$

 $\vec{a}_{rot} = \begin{vmatrix} \vec{i} & \vec{j} & \vec{k} \\ \vec{o} & -\omega_1 c dg d & 0 \end{vmatrix} = -\frac{h \omega_1^2 c dg d}{\cos d} \begin{vmatrix} \vec{i} & \vec{j} & \vec{k} \\ 0 & 1 & 0 \end{vmatrix} = \frac{h \omega_1 c dg d}{\cos d} \begin{vmatrix} \vec{i} & \vec{j} & \vec{k} \\ \cos d & 0 \end{vmatrix}$

 $= -\frac{h\omega_1^2}{\text{rind}} \left(\text{rin } 2 \times \vec{i} - 602 \times \vec{k} \right) = |\vec{a}_1 \cdot \vec{a}_2| = \frac{h\omega_1^2}{\text{rind}}$ 54 - page 3

Centripetal acceleration of point A:

(axipetal) $\vec{a}_{ax} = -\omega^2 \cdot \vec{d} = -\omega^2 \cdot d \cdot t \vec{n}$ $d = 0A \cdot \min_{x \to x} 2d = \frac{h \min_{x \to x} 2d}{\cos d} = 2h \min_{x \to x} d$ $\vec{a}_{ax} = -\omega_1^2 \cdot d_2^2 d \cdot 2h \min_{x \to x} d \cdot t \vec{n} = -\frac{2h \omega_1^2 \cos^2 d}{\min d} \cdot t \vec{n}$

 $|\vec{a}_{\alpha x}| = \frac{2h\omega_1^2\cos^2 d}{\sin d} = 2h\omega_1^2\cos d dg d$.