

Interpolation polynomials

A

1. Construct the interpolation polynomial P corresponding to the information below. Specify the type of interpolation.

$$\text{a) } \begin{array}{c|ccc} x_k & 0 & 1 & 2 \\ y_k & 0 & 1 & 0 \\ y'_k & 0 & 0 & 0 \end{array}$$

$$\text{b) } P(0) = f(0), \quad P'(1) = f'(1), \quad P''(2) = f''(2)$$

$$\text{c) } \begin{array}{c|cccc} x_k & 5 & 6 & 9 & 11 \\ y_k & 12 & 13 & 14 & 16 \end{array}$$

$$\text{d) } x_0 = 0 \text{ simple node, } x_1 = 1 \text{ triple node.}$$

B

1. Construct the interpolation polynomial P corresponding to the information below. Specify the type of interpolation.

$$\text{a) } \begin{array}{c|ccc} x_k & 0 & 1 & 2 \\ y_k & 1 & 3 & 21 \\ y'_k & 0 & 3 & 36 \end{array}$$

$$\text{b) } P''(-2) = f''(-2), \quad P'(-1) = f'(-1), \quad P(0) = f(0)$$

$$\text{c) } \begin{array}{c|cccc} x_k & 1 & 2 & 4 & 6 \\ y_k & 14 & 15 & 5 & 9 \end{array}$$

$$\text{d) } x_0 = 0 \text{ simple node, } x_1 = 1 \text{ triple node.}$$