

AI Planning

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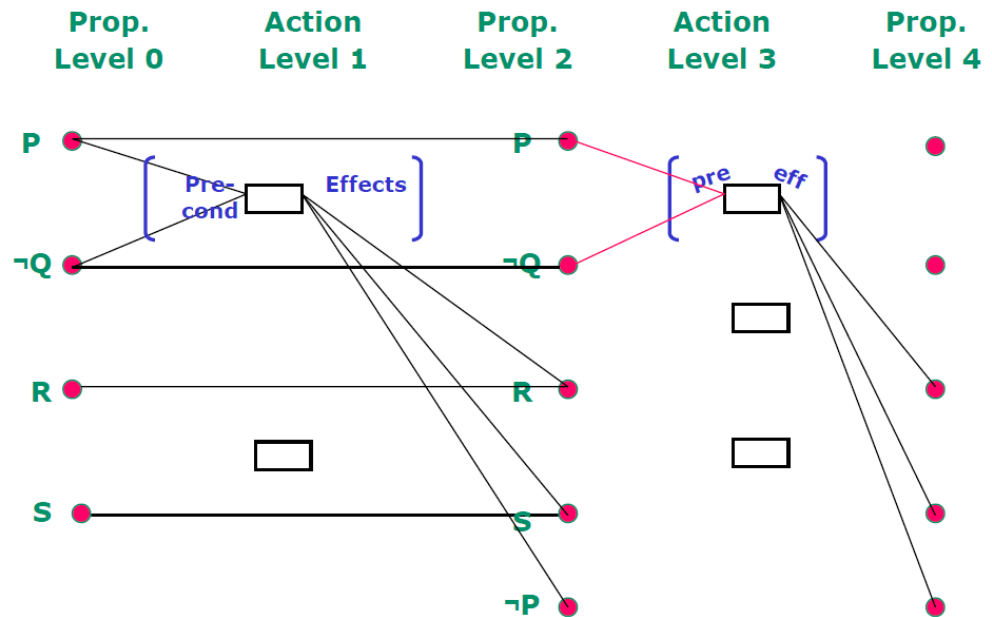
Graphplan and Advanced Heuristics

Graphplan

Graph Plan

- A propositional planner, that is, there are no variables
 - assertions Simpler – don't have to worry about matching
 - Bigger – if you have six blocks, you need 36 propositions to represent all $\text{On}(x,y)$

1. Make a plan graph of depth k
2. Search for a solution
3. If succeed, return a plan
4. Else $k=k+1$
5. Go to 1.

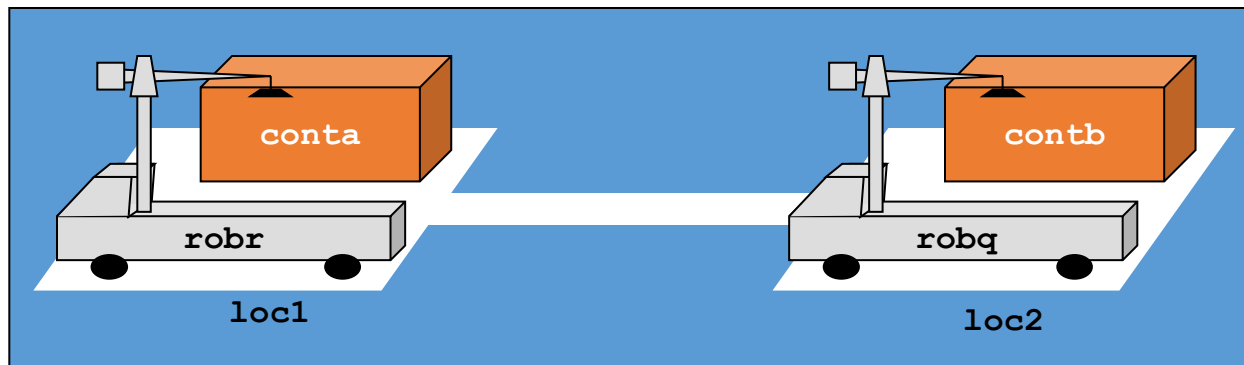


GraphPlan centres work on a [data structure](#) called a plan graph. A plan graph looks like this in the figure. You have a bunch of levels. [You start with level zero, level one, level two.](#)

Overview

- **A Propositional DWR Example**
- The Basic Planning Graph (No Mutex)
- Layered Plans
- Mutex Propositions and Actions
- Graphplan properties

Example: Simplified DWR Problem



- robots can load and unload autonomously
- locations may contain unlimited number of robots and containers
- problem: swap locations of containers

Simplified DWR Problem: STRIPS Operators

- **move(r, l, l')**
 - precondition: $\text{at}(r, l), \text{adjacent}(l, l')$
 - effects: $\text{at}(r, l'), \neg \text{at}(r, l)$
- **load(c, r, l)**
 - precondition: $\text{at}(r, l), \text{in}(c, l), \text{unloaded}(r)$
 - effects: $\text{loaded}(r, c), \neg \text{in}(c, l), \neg \text{unloaded}(r)$
- **unload(c, r, l)**
 - precondition: $\text{at}(r, l), \text{loaded}(r, c)$
 - effects: $\text{unloaded}(r), \text{in}(c, l), \neg \text{loaded}(r, c)$

Simplified DWR Problem: State Proposition Symbols

- robots:
 - *r1* and *r2*: at(robr,loc1) and at(robr,loc2)
 - *q1* and *q2*: at(robq,loc1) and at(robq,loc2)
 - *ur* and *uq*: unloaded(robr) and unloaded(robq)
- containers:
 - *a1*, *a2*, *ar*, and *aq*: in(conta,loc1), in(conta,loc2), loaded(conta,robr), and loaded(conta,robq)
 - *b1*, *b2*, *br*, and *bq*: in(contb,loc1), in(contb,loc2), loaded(contb,robr), and loaded(contb,robq)

Initial state: {*r1*, *q2*, *a1*, *b2*, *ur*, *uq*}

Simplified DWR Problem:

Propositions Action Symbols

- move actions:
 - Mr12: move(robr,loc1,loc2), Mr21: move(robr,loc2,loc1), Mq12: move(robq,loc1,loc2), Mq21: move(robq,loc2,loc1)
- load actions:
 - Lar1: load(conta,robr,loc1); Lar2, Laq1, Laq2, Lbr1, Lbr2, Lbq1, and Lbq2 correspondingly
- unload actions:
 - Uar1: unload(conta,robr,loc1); Uar2, Uaq1, Uaq2, Ubr1, Ubr2, Ubq1, and Ubq2 correspondingly

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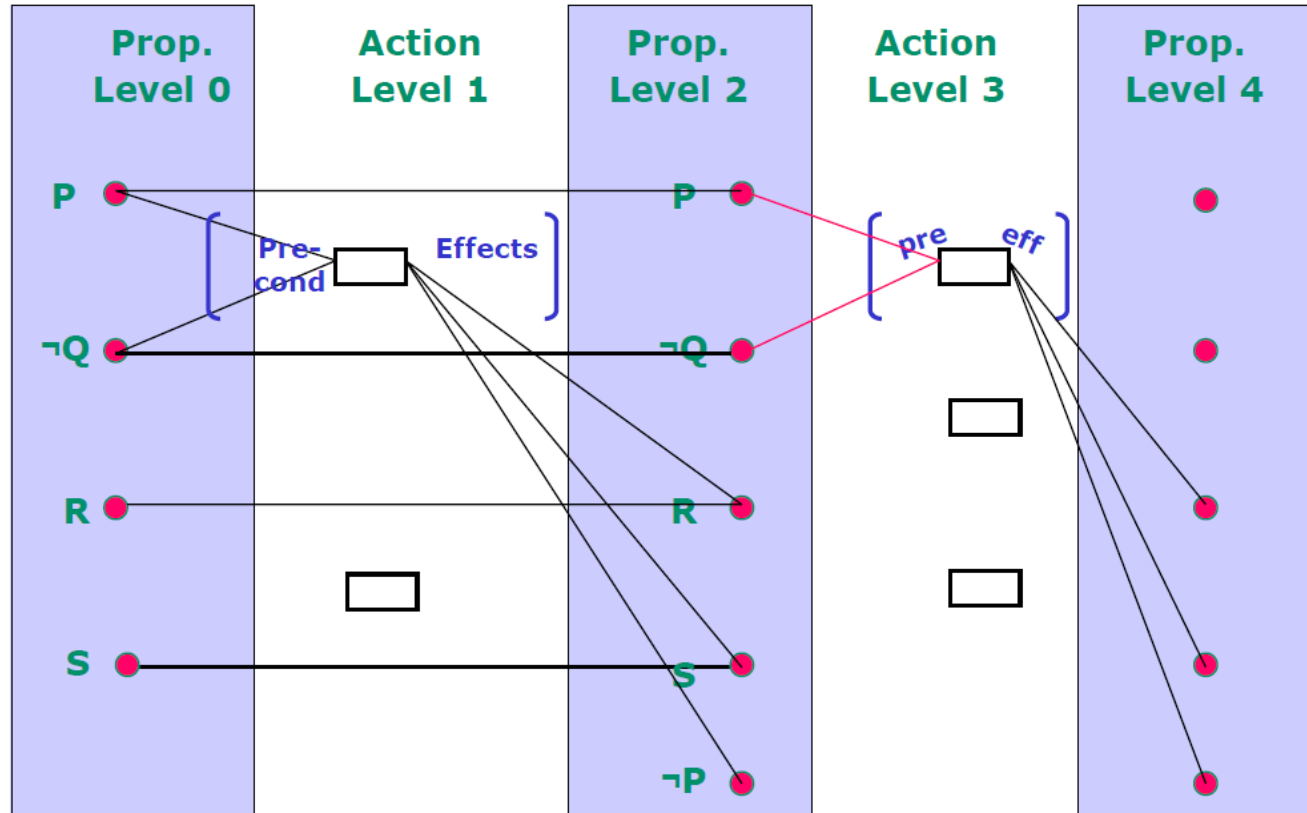
Planning Graph: Nodes

- layered directed graph $G=(N,E)$:
 - $N = P_0 \cup A_1 \cup P_1 \cup A_2 \cup P_2 \cup \dots$
 - state proposition layers: P_0, P_1, \dots
 - action layers: A_1, A_2, \dots
- first proposition layer P_0 :
 - propositions in initial state s_i : $P_0 = s_i$
- action layer A_j :
 - all actions a where: $\text{precond}(a) \subseteq P_{j-1}$
- proposition layer P_j :
 - all propositions p where: $p \in P_{j-1}$ or $\exists a \in A_j: p \in \text{effects}(a)$

Planning Graph: Edges

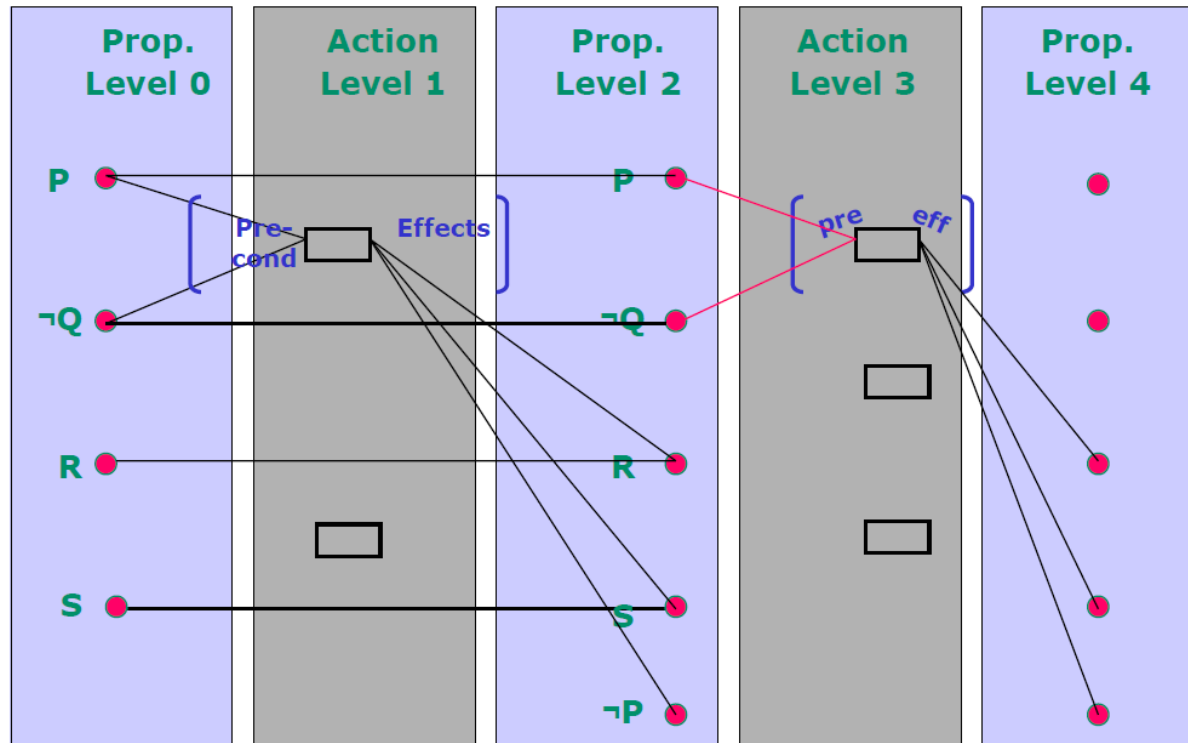
- from proposition $p \in P_{j-1}$ to action $a \in A_j$:
 - if: $p \in \text{precond}(a)$
- from action $a \in A_j$ to layer $p \in P_j$:
 - positive arc if: $p \in \text{effects}^+(a)$
 - negative arc if: $p \in \text{effects}^-(a)$

Graph Plan Example



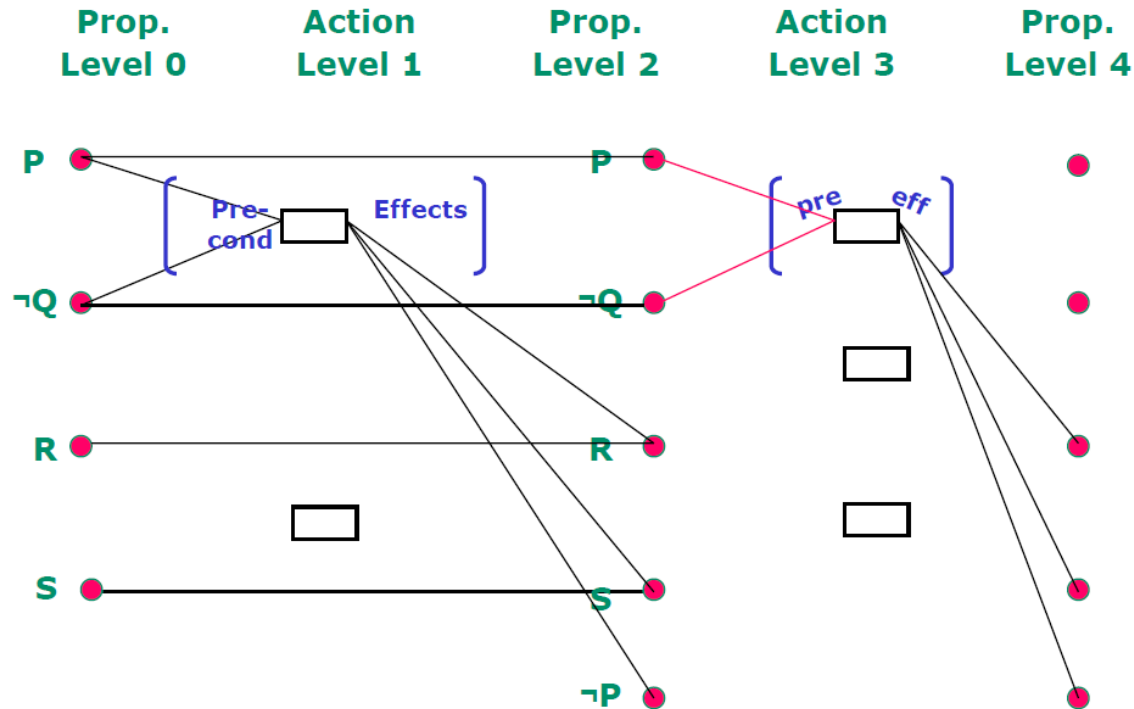
At the even- numbered levels you have propositions, which they draw as a little dot.

Graph Plan Example



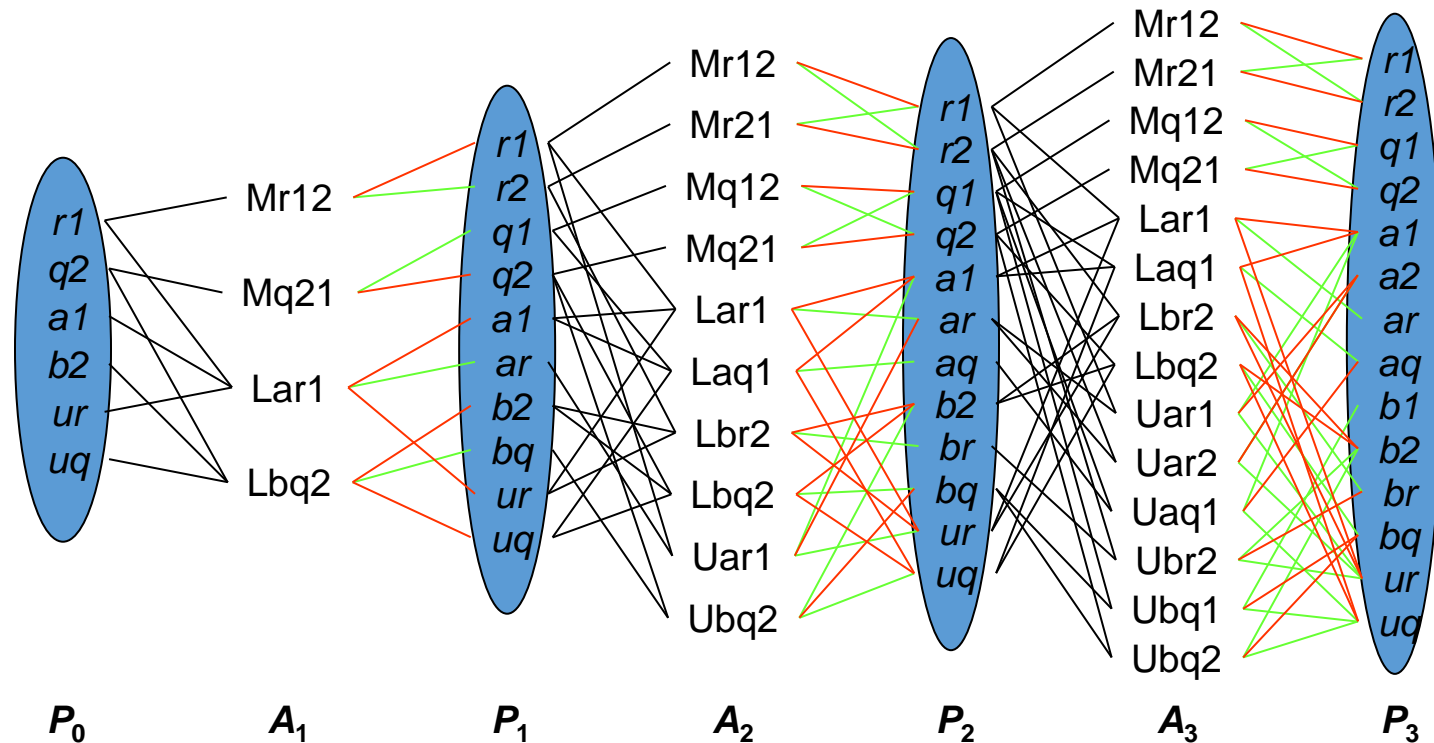
- Three proposition levels (levels 0, 2, and 4) and two action levels (levels 1 and 3).
- To encode depth-two plans (because there are two layers of actions).
 - Action level 1 has the actions that we might choose to do on the first step,
 - Action level 3 has the actions we might choose to do on the second step.

Graph Plan Example



- Start by making a graph with levels 0 through 2, corresponding to a depth 1 plan,
- Search for a satisfactory plan within that graph. If we can't find one,
- Extend the graph out by two more layers (an action layer and a proposition layer),
- Then find a depth 2 plan.

Planning Graph Example



The goal is to swap the containers: $\{a2, q1\}$

Reachability in the Planning Graph

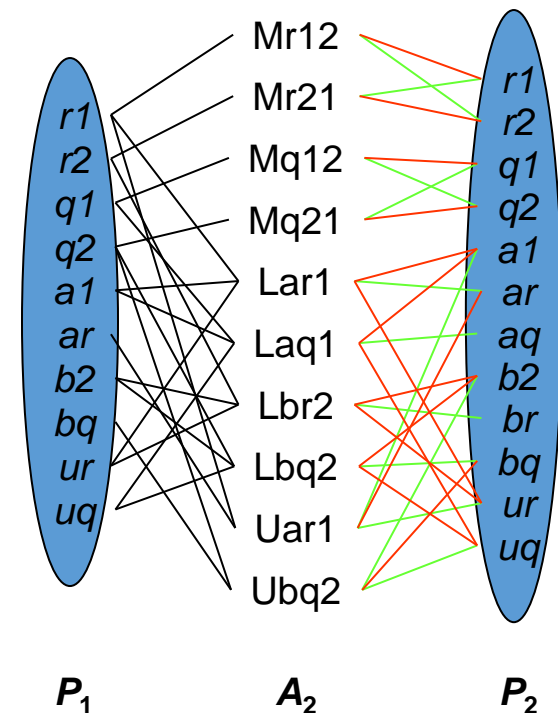
- reachability analysis:
 - if a goal g is reachable from initial state s_i
 - then there will be a proposition layer P_g in the planning graph such that $g \subseteq P_g$
- necessary condition, but not sufficient
- low complexity:
 - planning graph is of polynomial size and
 - can be computed in polynomial time

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- **Layered Plans**
- Mutex Propositions and Actions
- Graphplan properties

Independent Actions: Examples

- Mr12 and Lar1:
 - cannot occur together
 - Mr12 deletes precondition *r1* of Lar1
- Mr12 and Mr21:
 - cannot occur together
 - Mr12 deletes positive effect *r1* of Mr21
- Mr12 and Mq21:
 - may occur in same action layer



Independent Actions

- Two actions a_1 and a_2 are independent iff:
 - $\text{effects}^-(a_1) \cap (\text{precond}(a_2) \cup \text{effects}^+(a_2)) = \{\}$
and
 - $\text{effects}^-(a_2) \cap (\text{precond}(a_1) \cup \text{effects}^+(a_1)) = \{\}$.
- A set of actions π is independent iff every pair of actions $a_1, a_2 \in \pi$ is independent.
- The final solution Π is $\{\pi_1, \pi_2, \pi_3, \dots, \pi_k\}$

Pseudo Code: independent

```
function independent( $a_1, a_2$ )  
  for all  $p \in \text{effects}^-(a_1)$   
    if  $p \in \text{precond}(a_2)$  or  $p \in \text{effects}^+(a_2)$  then  
      return false  
  for all  $p \in \text{effects}^-(a_2)$   
    if  $p \in \text{precond}(a_1)$  or  $p \in \text{effects}^+(a_1)$  then  
      return false  
  return true
```

Layered Plans

- Let $P = (A, s_i, g)$ be a statement of a propositional planning problem and $G = (N, E)$, $N = P_0 \cup A_1 \cup P_1 \cup A_2 \cup P_2 \cup \dots$, the corresponding planning graph.
- A layered plan over G is a sequence of sets of actions: $\prod = \langle \pi_1, \dots, \pi_k \rangle$ where, k is the graph depth, and:
 - $\pi_i \subseteq A_i \subseteq A$,
 - π_i is applicable in state P_{i-1} , and
 - the actions in π_i are independent.

Layered Solution Plan

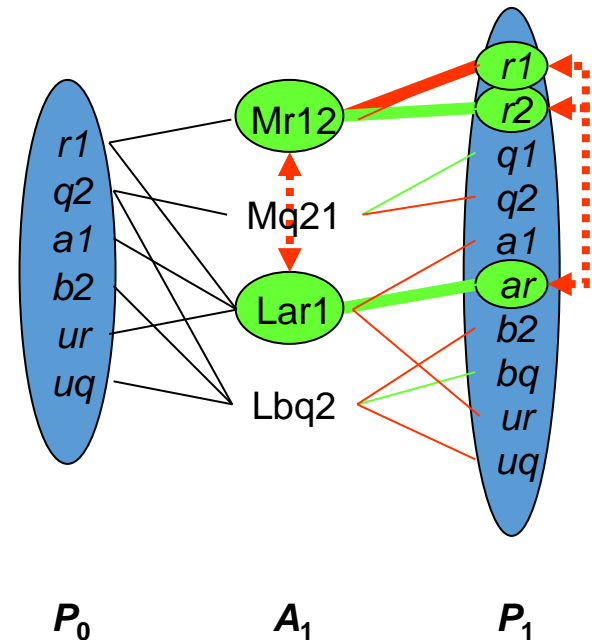
- A layered plan $\Pi = \langle \pi_1, \dots, \pi_k \rangle$ is a solution to a planning problem $P = (A, s_i, g)$ iff:
 - π_1 is applicable in s_i ,
 - for $j \in \{2 \dots k\}$, π_j is applicable in state $\gamma(\dots \gamma(\gamma(s_i, \pi_1), \pi_2), \dots \pi_{j-1})$, and
 - $g \subseteq \gamma(\dots \gamma(\gamma(s_i, \pi_1), \pi_2), \dots, \pi_k)$.

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- **Mutex Propositions and Actions**
- Graphplan properties

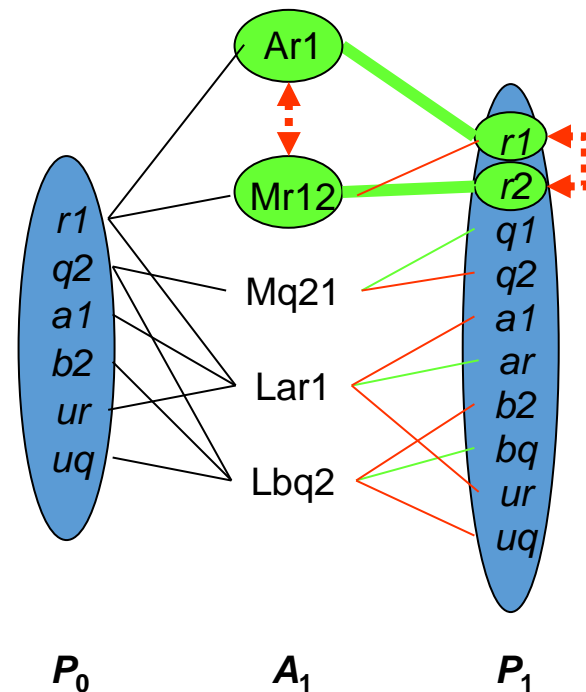
Problem: Dependent Propositions: Example

- $r2$ and ar :
 - $r2$: positive effect of Mr12
 - ar : positive effect of Lar1
 - but: Mr12 and Lar1 not independent
 - hence: $r2$ and ar incompatible in P_1
- $r1$ and $r2$:
 - positive and negative effects of same action: Mr12
 - hence: $r1$ and $r2$ incompatible in P_1



No-Operation Actions

- No-Op for proposition p :
 - name: A_p
 - precondition: p
 - effect: p
- $r1$ and $r2$:
 - $r1$: positive effect of $Ar1$
 - $r2$: positive effect of $Mr12$
 - but: $Ar1$ and $Mr12$ not independent
 - hence: $r1$ and $r2$ incompatible in P_1



Mutex Propositions

- Two propositions p and q in proposition layer P_j are mutex (mutually exclusive) if:
 - every action in the preceding action layer A_j that has p as a positive effect (incl. no-op actions) **is mutex** with every action in A_j that has q as a positive effect, and
 - there is no single action in A_j that has both, p and q , as positive effects.
- notation: $\mu P_j = \{ (p, q) \mid p, q \in P_j \text{ are mutex} \}$

Pseudo Code: mutex for Propositions

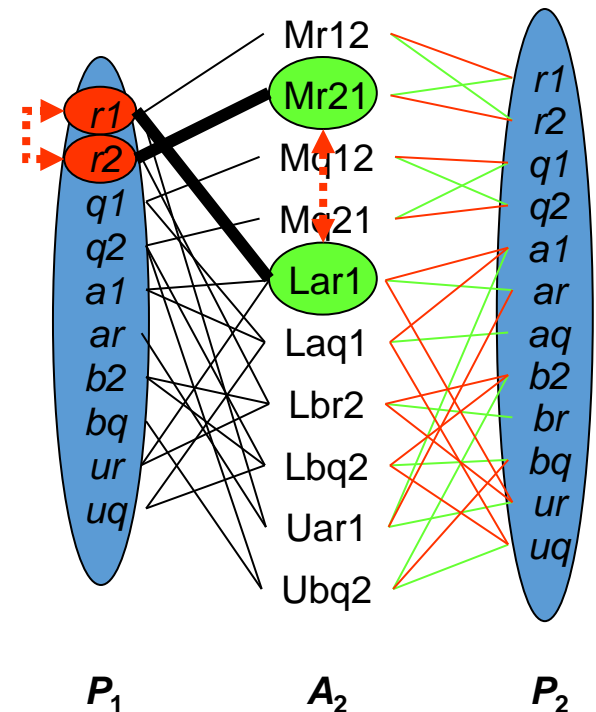
```
function mutex( $p_1, p_2, \mu A_j$ )  
  for all  $a_1 \in p_1.\text{producers}()$   
    for all  $a_2 \in p_2.\text{producers}()$   
      if  $(a_1, a_2) \notin \mu A_j$  then  
        return false  
  return true
```

Mutex Actions

- Two actions a_1 and a_2 in action layer A_j are mutex if:
 - a_1 and a_2 are dependent, or
 - a precondition of a_1 is mutex with a precondition of a_2 .
- notation: $\mu A_j = \{ (a_1, a_2) \mid a_1, a_2 \in A_j \text{ are mutex} \}$

Mutex Actions: Example

- $r1$ and $r2$ are mutex in P_1
- $r1$ is precondition for Lar1 in A_2
- $r2$ is precondition for Mr21 in A_2
- hence: Lar1 and Mr21 are mutex in A_2



Pseudo Code: mutex for Actions

```
function mutex( $a_1, a_2, \mu P$ )  
  if  $\neg$ independent( $a_1, a_2$ ) then  
    return true  
  for all  $p_1 \in \text{precond}(a_1)$   
    for all  $p_2 \in \text{precond}(a_2)$   
      if  $(p_1, p_2) \in \mu P$  then return true  
  return false
```

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Graphplan Properties

- **Proposition:** The Graphplan algorithm is sound, complete, and always terminates.
 - It returns failure iff the given planning problem has no solution;
 - otherwise, it returns a layered plan Π that is a solution to the given planning problem.
- Graphplan is orders of magnitude faster than previous techniques!

Advanced Heuristics

Overview

- **Simple Planning Graph Heuristics**
- The FF Planner

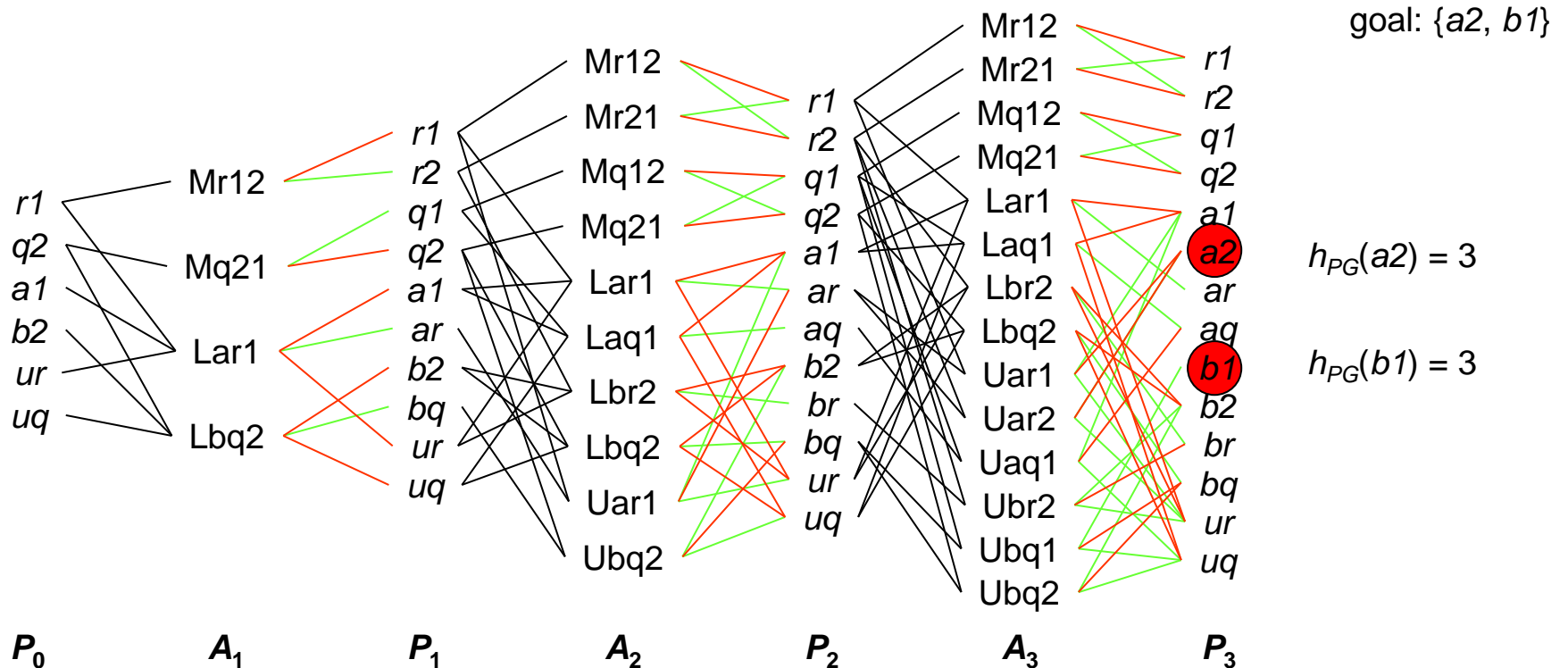
Forward State-Space Search with A*

- A* is optimally efficient: For a given heuristic function, no other algorithm is guaranteed to expand fewer nodes than A*.
- room for improvement: use better heuristic function!

Planning Graph Heuristics

- basic idea: use reachability graph analysis as a heuristic for forward search
 - $P = (A, s_i, g)$ be a propositional planning problem and $G = (N, E)$ the corresponding planning graph
 - $g = \{g_1, \dots, g_n\}$
 - $g_k, k \in [1, n]$, is reachable from s_i if there is a proposition layer P_g such that $g_k \in P_g$
 - in proposition layer P_m : if g_k not in P_m then g_k not reachable in m steps
- define (admissible) $h_{PG}(g_k) = m$ for reachable $\{g_k\}$

Graphplan: Heuristic



Overview

- Simple Planning Graph Heuristics
- **The FF (Fast Forward) Planner**

The FF Planner

- performs forward state-space search (A^*)
- relaxed problem heuristic (h^{FF})
 - construct relaxed problem: ignore delete lists
 - solve relaxed problem (in polynomial time)
 - chain forward to build a relaxed planning graph
 - chain backward to extract a relaxed plan from the graph
 - use length of relaxed plan as heuristic value

Relaxed Planning Problem: Example

- $\text{move}(r, l, l')$
 - precondition: $\text{at}(r, l), \text{adjacent}(l, l')$
 - effects: $\text{at}(r, l'), \text{-at}(r, l)$
- $\text{load}(c, r, l)$
 - precondition: $\text{at}(r, l), \text{in}(c, l), \text{unloaded}(r)$
 - effects: $\text{loaded}(r, c), \text{-in}(c, l), \text{-unloaded}(r)$
- $\text{unload}(c, r, l)$
 - precondition: $\text{at}(r, l), \text{loaded}(r, c)$
 - effects: $\text{unloaded}(r), \text{in}(c, l), \text{-loaded}(r, c)$

Computing h^{FF} : Relaxed Planning Graph

```
function computeRPG( $A, s_i, g$ )  
   $F_0 \leftarrow s_i; t \leftarrow 0$   
  while  $g \not\subseteq F_t$  do  
     $t \leftarrow t+1$   
     $A_t \leftarrow \{a \in A \mid \text{precond}(a) \subseteq F_{t-1}\}$   
     $F_t \leftarrow F_{t-1}$   
    for all  $a \in A_t$  do  
       $F_t \leftarrow F_t \cup \text{effects}^+(a)$   
    if  $F_t = F_{t-1}$  then return failure  
  return [ $F_0, A_1, F_1, \dots, A_t, F_t$ ]
```

Computing h^{FF} : Extracting a Relaxed Plan

```
function extractRPSize( $[F_0, A_1, F_1, \dots, A_k, F_k]$ ,  $g$ )  
  if  $g \not\subseteq F_k$  then return failure  
   $M \leftarrow \max\{\text{firstlevel}(g_i, [F_0, \dots, F_k]) \mid g_i \in g\}$   
  for  $t \leftarrow 0$  to  $M$  do  
     $G_t \leftarrow \{g_i \in g \mid \text{firstlevel}(g_i, [F_0, \dots, F_k]) = t\}$   
    for  $t \leftarrow M$  to  $1$  do  
      for all  $g_t \in G_t$  do  
        select  $a : \text{firstlevel}(a, [A_1, \dots, A_t]) = t$  and  $g_t \in \text{effects}^+(a)$   
        for all  $p \in \text{precond}(a)$  do  
           $G_{\text{firstlevel}(p, [F_0, \dots, F_k])} \leftarrow G_{\text{firstlevel}(p, [F_0, \dots, F_k])} \cup \{p\}$   
  return number of selected actions
```

End

