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MACHINE Stable_Pendule
REFINES StableLassaleGeneric
SEES PenduleCtx
 VARIABLES
                             \mathbf{t}
                             \mathbf{x}
                              dx
                              \cos_{-}th
                             \sin_{-}th
                              dtheta
                             x_s
INVARIANTS
                              inv1: x \in RReal \rightarrow RReal
                              inv2: dx \in RReal \rightarrow RReal
                              inv3: cos\_th \in RReal \rightarrow RReal
                              inv4: sin\_th \in RReal \rightarrow RReal
                              inv5: dtheta \in RReal \rightarrow RReal
                              inv11: Closed2Closed(Rzero, t) \subseteq dom(x)
                              inv21: dom(x) = dom(dx)
                              inv31: dom(x) = dom(cos_th)
                              inv41: dom(x) = dom(sin\_th)
                              inv51: dom(x) = dom(dtheta)
                              inv7: x_p = bind(bind(bind(bind(x, dx), cos_th), sin_th), dtheta)
EVENTS
Initialisation
                         with
                                                    x_p': x_p' = bind(bind(bind(bind(x', dx'), cos_th'), sin_th'), dtheta')
                         begin
                                                    act1: t := Rzero
                                                   act2:
                                                                 x, dx, cos\_th, sin\_th, dtheta :=
                                                                 Rfcste(Rzero),
                                                                 Rfcste(Rzero),
                                                                 Rfcste(cos(angle\_init)),
                                                                 Rfcste(sin(angle\_init)),
                                                                  Rfcste(Rzero)
                                                    act3: x_s := etat
                         end
Event Transition (ordinary) \hat{=}
refines Transition
                         anv
                         where
                                                    grd2: s = \{etat\}
                         then
                                                   act1: x_s := etat
                         end
Event Sense ⟨ordinary⟩ =
refines Sense
                         with
                                                   p\colon\thinspace p = STATES \times RReal \times \{x_- \mapsto dx_- \mapsto cos_- \mapsto sin_- \mapsto dth_- | (x_- \mapsto dx_- \mapsto cos_- \mapsto sin_- \mapsto dth_-) \in STATES \times RReal \times \{x_- \mapsto dx_- \mapsto cos_- \mapsto sin_- \mapsto dth_- | (x_- \mapsto dx_- \mapsto cos_- \mapsto sin_- \mapsto dth_-) \in STATES \times RReal \times \{x_- \mapsto dx_- \mapsto cos_- \mapsto sin_- \mapsto dth_- | (x_- \mapsto dx_- \mapsto cos_- \mapsto sin_- \mapsto dth_-) \in STATES \times RReal \times \{x_- \mapsto dx_- \mapsto cos_- \mapsto sin_- \mapsto dth_- | (x_- \mapsto dx_- \mapsto cos_- \mapsto sin_- \mapsto dth_-) \in STATES \times RReal \times \{x_- \mapsto dx_- \mapsto cos_- \mapsto sin_- \mapsto dth_- | (x_- \mapsto dx_- \mapsto cos_- \mapsto sin_- \mapsto dth_-) \in STATES \times RReal \times \{x_- \mapsto dx_- \mapsto cos_- \mapsto sin_- \mapsto dth_- | (x_- \mapsto dx_- \mapsto cos_- \mapsto sin_- \mapsto dth_-) \in STATES \times RReal \times \{x_- \mapsto dx_- \mapsto cos_- \mapsto sin_- \mapsto dth_- | (x_- \mapsto dx_- \mapsto cos_- \mapsto sin_- \mapsto dth_-) \in STATES \times RReal \times \{x_- \mapsto dx_- \mapsto cos_- \mapsto sin_- \mapsto dth_- | (x_- \mapsto dx_- \mapsto cos_- \mapsto sin_- \mapsto dth_-) \in STATES \times RReal \times \{x_- \mapsto dx_- \mapsto cos_- \mapsto sin_- \mapsto dth_- | (x_- \mapsto dx_- \mapsto cos_- \mapsto sin_- \mapsto dth_-) \in STATES \times RReal \times \{x_- \mapsto dx_- \mapsto cos_- \mapsto sin_- \mapsto dth_- | (x_- \mapsto dx_- \mapsto cos_- \mapsto sin_- \mapsto dth_-) \in STATES \times RReal \times \{x_- \mapsto dx_- \mapsto cos_- \mapsto sin_- \mapsto dth_- \mid (x_- \mapsto dx_- \mapsto cos_- \mapsto sin_- \mapsto dth_-) \in STATES \times RReal \times \{x_- \mapsto dx_- \mapsto cos_- \mapsto cos
                         begin
                                                    act1: x\_s := etat
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end
 Event Actuate (ordinary) \hat{=}
 refines Actuate
                                                               any
                                                                 where
                                                                                                                                 grd0: tp \in RRealPlus \land t \mapsto tp \in lt
                                                                                                                                 grd2:
                                                                                                                                                                Solvable(Closed2Closed(t, tp), ode(F, tp))
                                                                                                                                                                bind(bind(bind(x, dx), cos\_th), sin\_th), dtheta)(Rzero), Rzero))
                                                                                                                                 grd4: x_s = etat
                                                                                                                                 grd7: tp \in RRealPlus \land t \mapsto tp \in lt
                                                               with
                                                                                                                                 e: e = ode(F, x_p(Rzero), Rzero)
                                                                                                                                 s: s = \{etat\}
                                                                                                                                 x_p': x_p' = bind(bind(bind(bind(x', dx'), cos_th'), sin_th'), dtheta')
                                                               then
                                                                                                                                                                t, x, dx, cos\_th, sin\_th, dtheta:
                                                                                                                                                                (t'=tp \land
                                                                                                                                                                x' \in RReal \rightarrow RReal \land Closed2Closed(Rzero, t') = dom(x') \land x'(t) = x(t) \land x'(t) 
                                                                                                                                                                dx' \in RReal \rightarrow RReal \land Closed2Closed(Rzero, t') = dom(dx') \land dx'(t) = dx(t) \land dx' \in RReal \rightarrow RReal \land Closed2Closed(Rzero, t') = dom(dx') \land dx'(t) = dx(t) \land dx' \in RReal \rightarrow RReal \land Closed2Closed(Rzero, t') = dom(dx') \land dx'(t) = dx(t) \land dx'(t) = dx'(t) \land dx'(t) = dx'
                                                                                                                                                                cos\_th' \in RReal \rightarrow RReal \land Closed2Closed(Rzero, t') = dom(cos\_th') \land cos\_th'(t) = cos\_th(t) \land cos\_th(t) \land cos\_th(t) = cos
                                                                                                                                                                sin\_th' \in RReal \rightarrow RReal \land Closed2Closed(Rzero, t') = dom(sin\_th') \land sin\_th'(t) = sin\_th(t) \land sin\_th'(t) = sin\_th'(t) \land sin\_th'(
                                                                                                                                                                dtheta' \in RReal \rightarrow RReal \land Closed 2Closed (Rzero, t') = dom(dtheta') \land dtheta'(t) = dtheta(t) \land dtheta'
                                                                                                                                                                CBAP solution Of (t, t^{\prime},
                                                                                                                                                                bind(bind(bind(bind(x,dx),cos\_th),sin\_th),dtheta),bind(bind(bind(bind(x',dx'),cos\_th'),sin\_th'),dtheta'),
                                                                                                                                                                ode(F, bind(bind(bind(x, dx), cos\_th), sin\_th), dtheta)(Rzero), Rzero),
                                                                                                                                                                Closed2Closed(t, t') \times S)
                                                                                                                                                                )
                                                               end
Event Behave \langle \text{ordinary} \rangle =
                                                               Refining Behave exactly as Actuate
   refines Behave
                                                               any
                                                                                                                               _{\mathrm{tp}}
                                                               where
                                                                                                                                 grd0: tp \in RRealPlus \land t \mapsto tp \in lt
                                                                                                                                 grd2:
                                                                                                                                                                  Solvable(Closed2Closed(t, tp), ode(F,
                                                                                                                                                                bind(bind(bind(bind(x, dx), cos\_th), sin\_th), dtheta)(Rzero), Rzero))
                                                               with
                                                                                                                                 e: e = ode(F, x p(Rzero), Rzero)
                                                                                                                                 Inv: Inv = Closed2Closed(t, t') \times S
                                                                                                                                 x_p': x_p' = bind(bind(bind(bind(x', dx'), cos_th'), sin_th'), dtheta')
                                                               then
                                                                                                                                 act1:
                                                                                                                                                                t, x, dx, cos\_th, sin\_th, dtheta:
                                                                                                                                                                (t'=tp \land
                                                                                                                                                                x' \in RReal \rightarrow RReal \land Closed2Closed(Rzero, t') = dom(x') \land x'(t) = x(t) \land x'(t) 
                                                                                                                                                                dx' \in RReal \rightarrow RReal \land Closed2Closed(Rzero, t') = dom(dx') \land dx'(t) = dx(t) \land dx'
                                                                                                                                                                cos\_th' \in RReal \rightarrow RReal \land Closed2Closed(Rzero, t') = dom(cos\_th') \land cos\_th'(t) = cos\_th(t) \land cos\_th(
                                                                                                                                                                sin\_th' \in RReal \rightarrow RReal \land Closed 2Closed (Rzero, t') = dom(sin\_th') \land sin\_th'(t) = sin\_th(t) \land sin\_th'(t) = sin\_th'(t) \land sin\_th'(t) =
                                                                                                                                                                dtheta' \in RReal \rightarrow RReal \land Closed \\ 2Closed \\ (Rzero,t') = dom(dtheta') \land dtheta'(t) = dtheta(t) \land dtheta' \\ (t) = dtheta(t) \land dtheta(t) \\ (t) = dtheta(t) \\ (t) = dtheta(t) \land dtheta(t) \\ (t) = dtheta(t) 
                                                                                                                                                                CBAP solution Of(t, t',
                                                                                                                                                                bind(bind(bind(bind(x,dx),cos\_th),sin\_th),dtheta),bind(bind(bind(bind(x',dx'),cos\_th'),sin\_th'),dtheta'),
                                                                                                                                                                ode(F, bind(bind(bind(x, dx), cos\_th), sin\_th), dtheta)(Rzero), Rzero),
                                                                                                                                                                Closed2Closed(t, t') \times S)
                                                                                                                                                                )
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 $\begin{array}{c} \text{end} \\ \textbf{END} \end{array}$

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