



Programming languages – Haskell

Homework exercise (2024/25)

T. Goluch

1st exercise (1 pts.)

B-smooth numbers¹ are those whose prime divisors are less than or equal to B. Write a program calculating for a given B and n, how many B-smooth numbers are there that do not exceed n? For example, for B = 5 and n = 30, the initial 5-smooth numbers, also known as Hamming numbers, are: 1, 2, 3, 4, 5, 6, 8, 9, 10, 12, 15, 16, 18, 20, 24, 25, 27, 30... so the answer is: 18.

2nd exercise (6 pts.)

Write a program to solve propositional calculus² with: negation \neg (N), conjunction \wedge (C), alternative \vee (A) and implication \rightarrow (I) functors.

Sentence type: `data Sentence = S Char | ...` - i.e. the variable can be any variable S

Example sentence: `(I (N (S 'p')) (A (C (S 'p') (S 'q')) (S 'r')))`

Program should:

- 1) contains a function: `print_sentence` – (1 pts.)
for a given example `(I (N (S 'p')) (A (C (S 'p') (S 'q')) (S 'r')))`
the output should be `"(¬p => ((p ∧ q) ∨ r))"`
- 2) contains a function: `write_variables` sentence – (1 pts.)
for a given example `(I (N (S 'p')) (A (C (S 'p') (S 'q')) (S 'r')))`
the output should be `[p, q, r]` (not necessarily sorted, but unique)
- 3) contains a function: `check_sentence_values_map` – (1 pts.)
for a given example `(I (N (S 'p')) (A (C (S 'p') (S 'q')) (S 'r')))`
and values map fromList `[('p', False), ('q', True), ('r', False)]`
the output should be `False`
- 4) contains a function: `isTautology` – (1 pts.)
checking whether the sentence is true for any valuation of variables in the formula. Check if the following sentences are tautologies?:
 - a) $(\neg p \wedge p) \rightarrow q$
 - b) $((p \rightarrow q) \rightarrow p) \rightarrow p$
 - c) $(p \rightarrow (p \rightarrow q)) \rightarrow (p \rightarrow q)$

Extend the program to support Łukasiewicz's three-valued logic³ True/False/Nothing. Program should:

¹ https://en.wikipedia.org/wiki/Smooth_number

² https://en.wikipedia.org/wiki/Propositional_calculus

³ https://en.wikipedia.org/wiki/Three-valued_logic

- 5) contains a function: `check3val sentence values_map` – (1 pts.)
for a given example `(I (N (S 'p')) (A (C (S 'p') (S 'q')) (S 'r')))`
and values map `fromList [('p', LFalse), ('q', LTrue), ('r', LNothing)]`
the output should be `LFalse`
- 6) contains a function: `isTautology3val` – (1 pts.)
Check if the following sentences are tautologies?:
- a) $p \rightarrow (q \rightarrow q)$
 - b) $(p \rightarrow q) \rightarrow ((p \rightarrow r) \rightarrow (p \rightarrow (q \wedge r)))$
 - c) $(p \rightarrow r) \rightarrow ((q \rightarrow r) \rightarrow ((p \wedge q) \rightarrow r))$

Comments: all functions should have an appropriate header with the type of function,