

Big Data Computing

Master's Degree in Computer Science
2024-2025



SAPIENZA
UNIVERSITÀ DI ROMA

Gabriele Tolomei

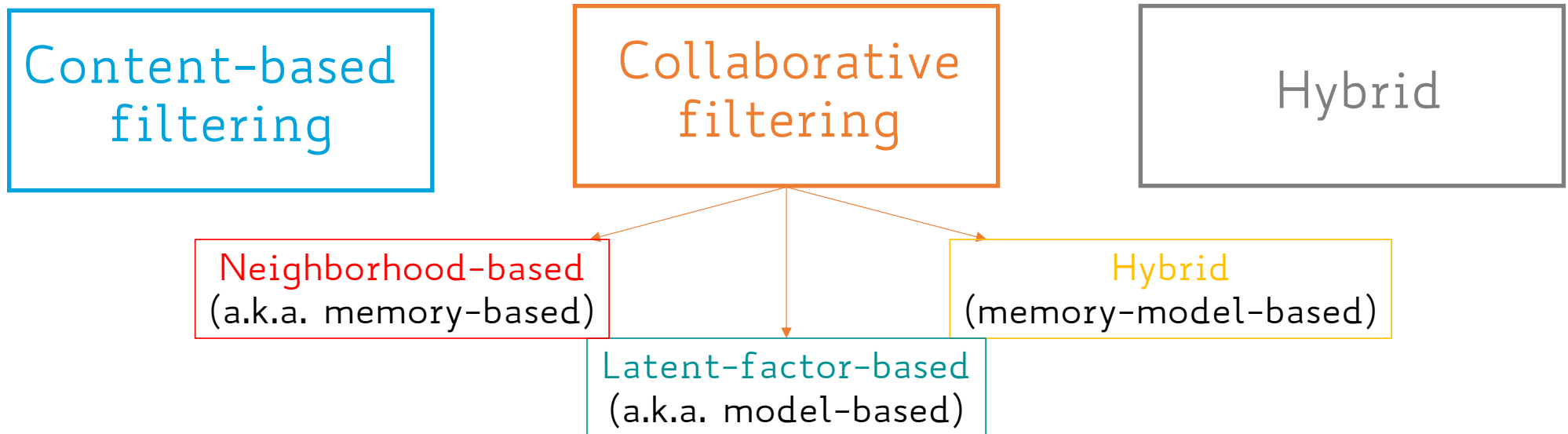
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Recommendation Strategies

3 approaches to recommender systems



COLLABORATIVE FILTERING

Collaborative Filtering (CF)

Idea

Recommend items to user u based on preferences of other users similar to u

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Core concept:

User-to-User or Item-to-Item similarity

Collaborative Filtering (CF)

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Recommend items to user u based on preferences of other users similar to u

Core concept:

User-to-User or Item-to-Item similarity

No need for explicit creation of user/item profiles

Collaborative Filtering: Approaches

3 main approaches to collaborative filtering

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Neighborhood-based
(a.k.a. memory-based)

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3 main approaches to collaborative filtering

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Latent-factor-based
(a.k.a. model-based)

Collaborative Filtering: Approaches

3 main approaches to collaborative filtering

Neighborhood-based
(a.k.a. memory-based)

Hybrid
(memory-model-based)

Latent-factor-based
(a.k.a. model-based)

Neighborhood-based (Memory-based) CF

Compute the relationship between **users** or **items**

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User-based

Evaluates a user's preference for an item based on ratings of "neighboring" users for that item

Neighborhood-based (Memory-based) CF

Compute the relationship between **users** or **items**

User-based

Evaluates a user's preference for an item based on ratings of "neighboring" users for that item

Item-based

Evaluates a user's preference for an item based on ratings of "neighboring" items by the same user

USER-BASED COLLABORATIVE FILTERING

User-based Neighborhood

Given a user u and an item i not rated by u , we want to estimate $r(u, i)$

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Estimate $r(u, i)$ based on the ratings of users in the
 k -neighborhood of u

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In theory, rating prediction $r(u,i)$ could be defined on
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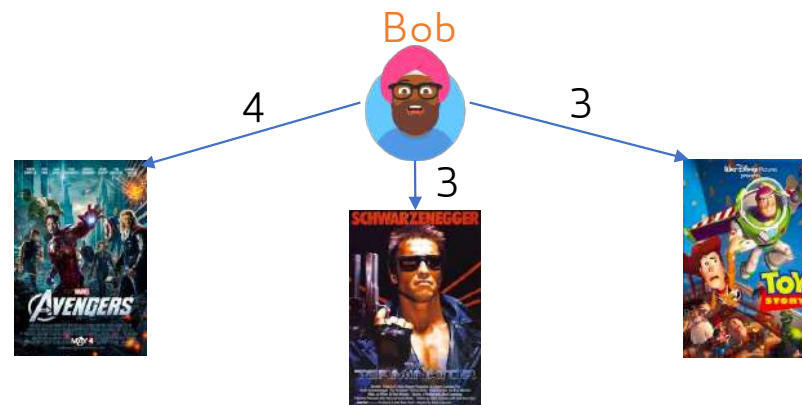
In other words, the u 's k -neighborhood must be
computed first to narrow down the set of items which
we must predict the rating of

User-based Neighborhood: Example

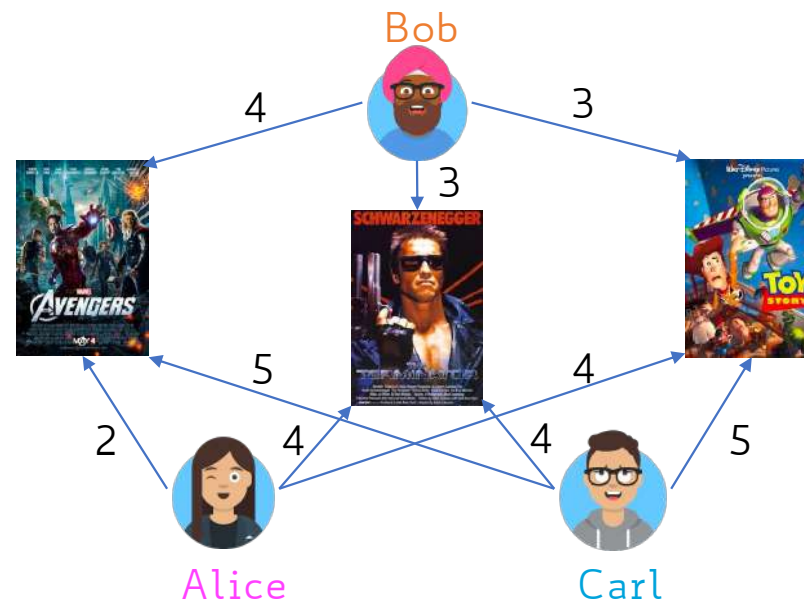
		MOVIES							
									
USERS	 Alice	2		5	4	5	4		4
	 Bob	4					3		3
	 Carl	5	5	3	4	5	4		5

	 Zoe		1	3				5	4

User-based Neighborhood: Example

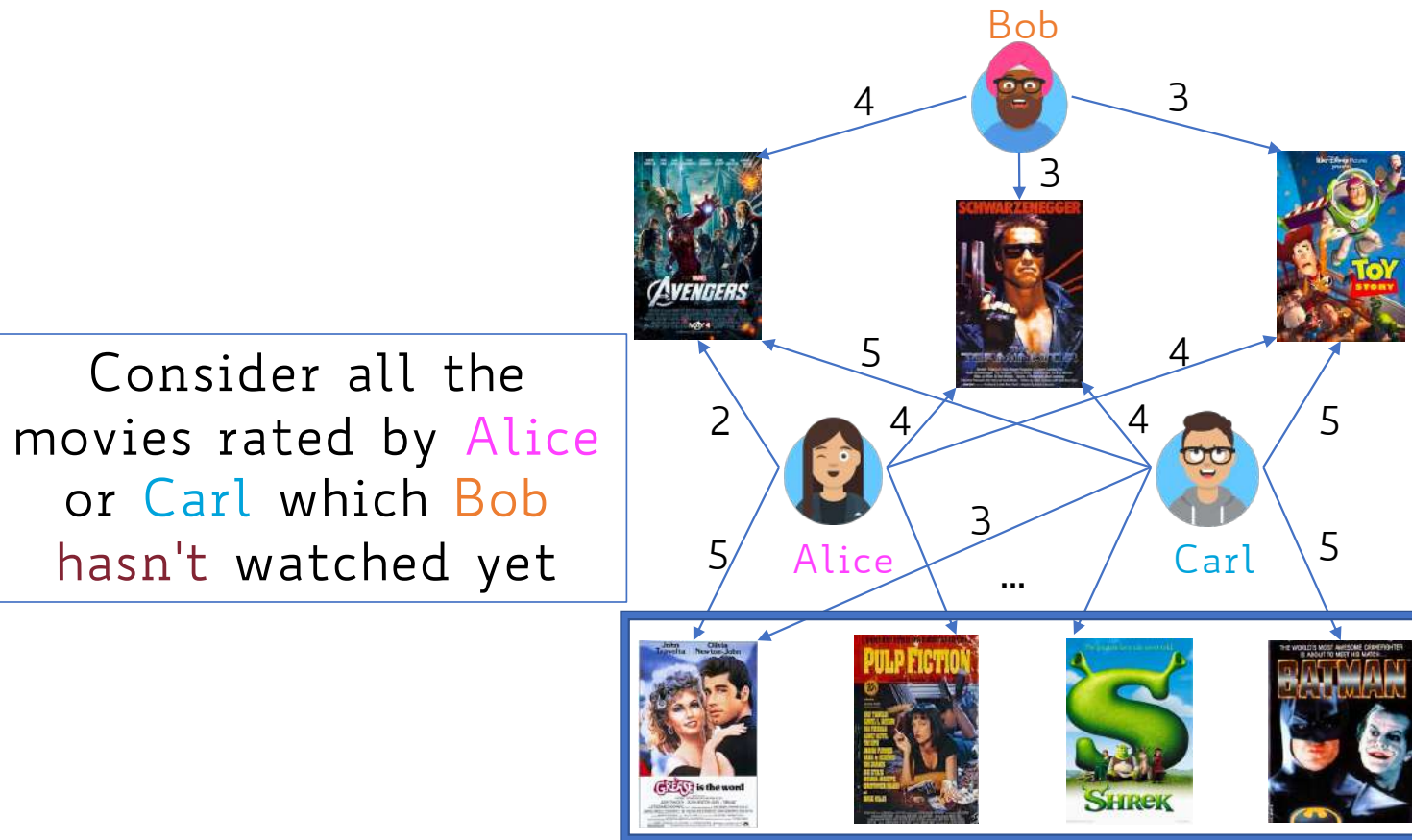


User-based Neighborhood: Example



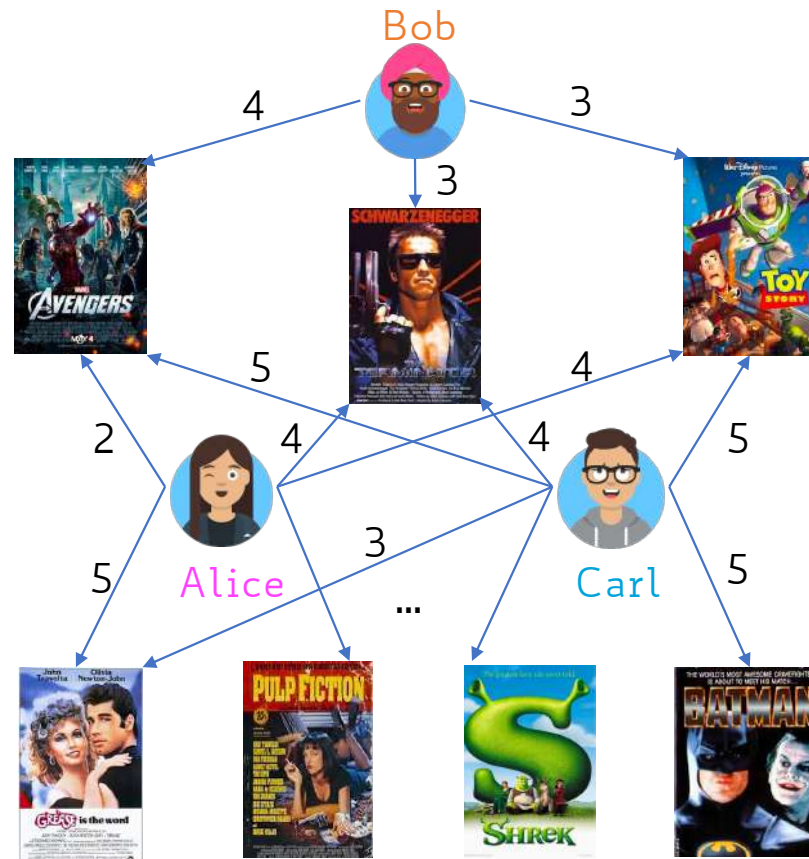
Alice and Carl are the 2-nearest neighbours of Bob if we look at their rating behaviours

User-based Neighborhood: Example



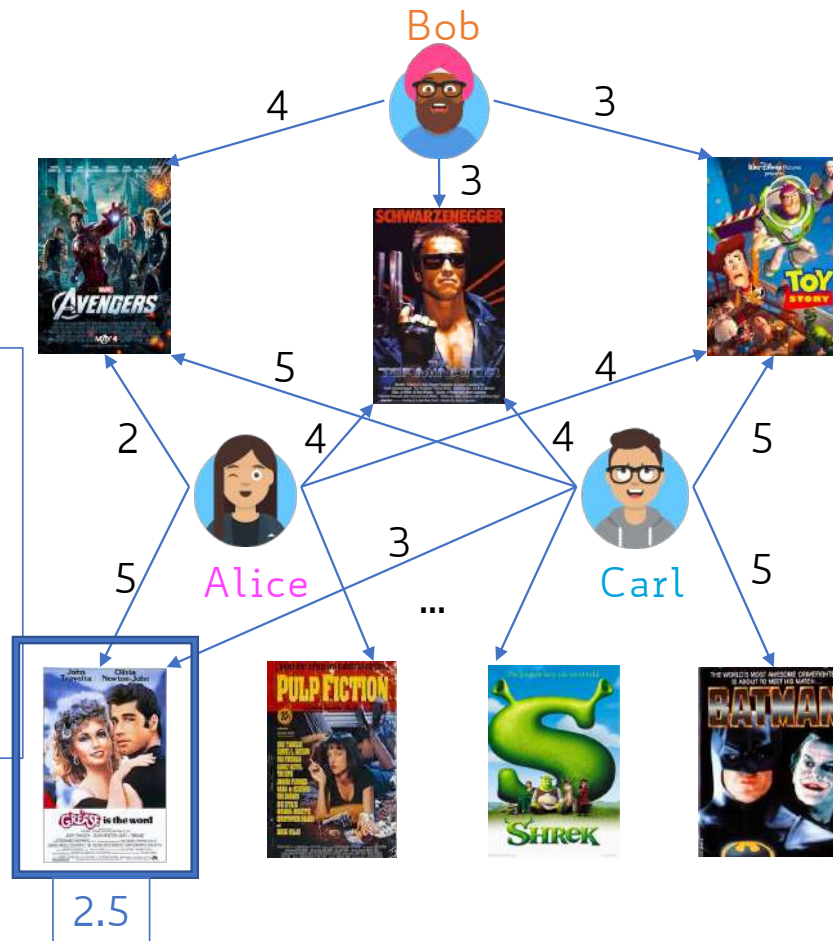
User-based Neighborhood: Example

Predict the rating that **Bob** would give to each of those movies on the basis of **Alice's** and **Carl's** ratings



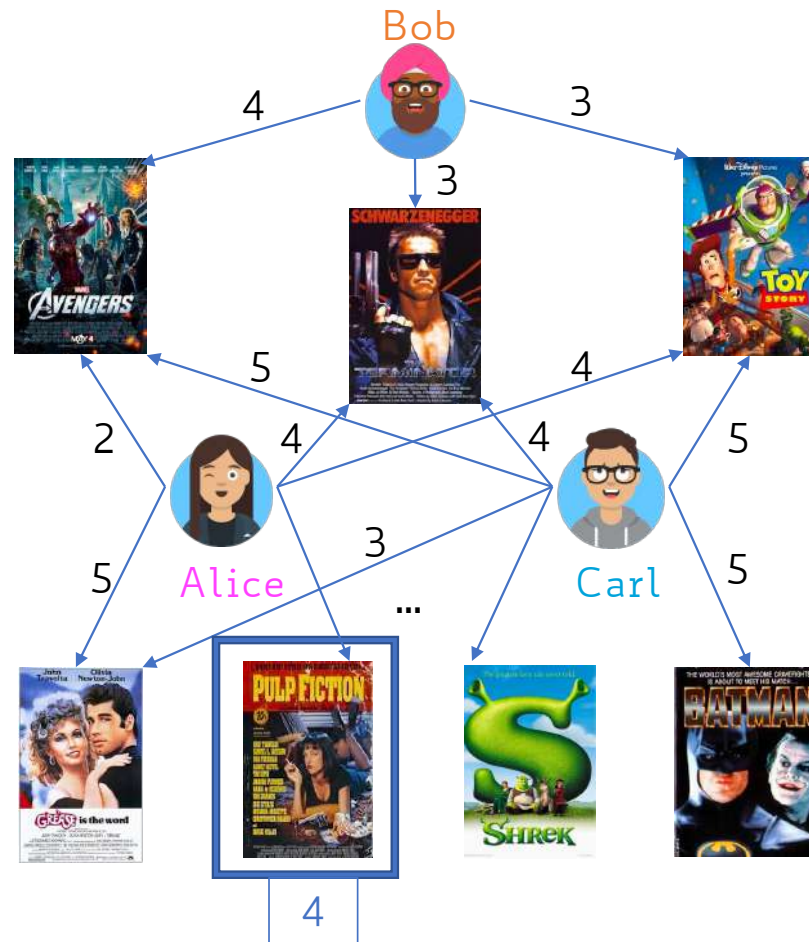
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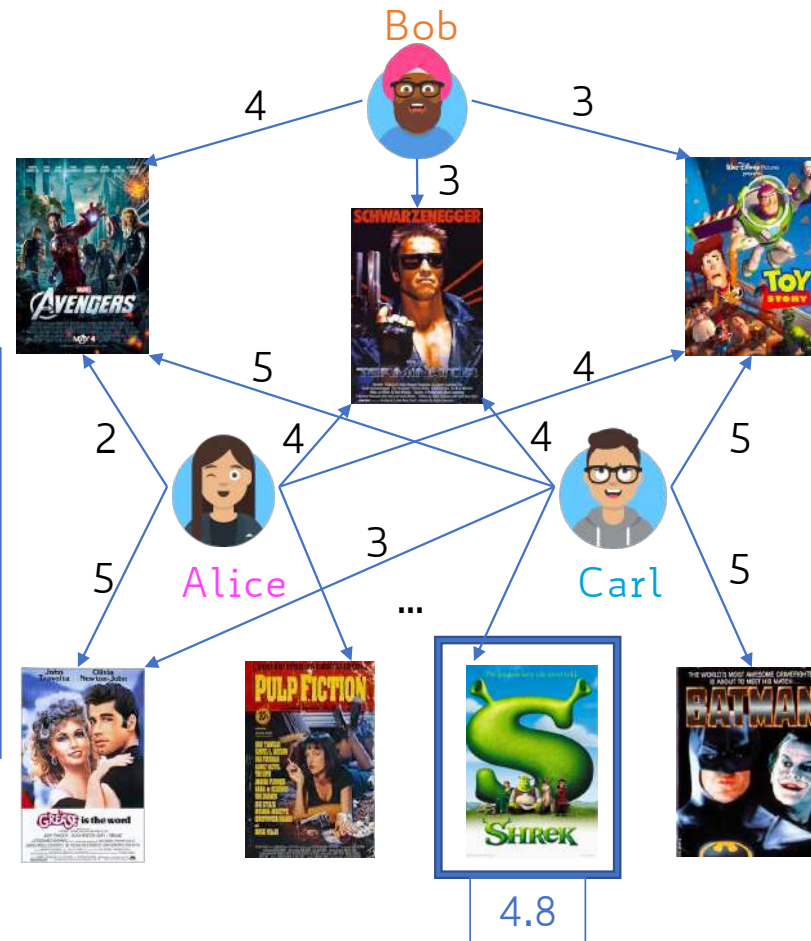
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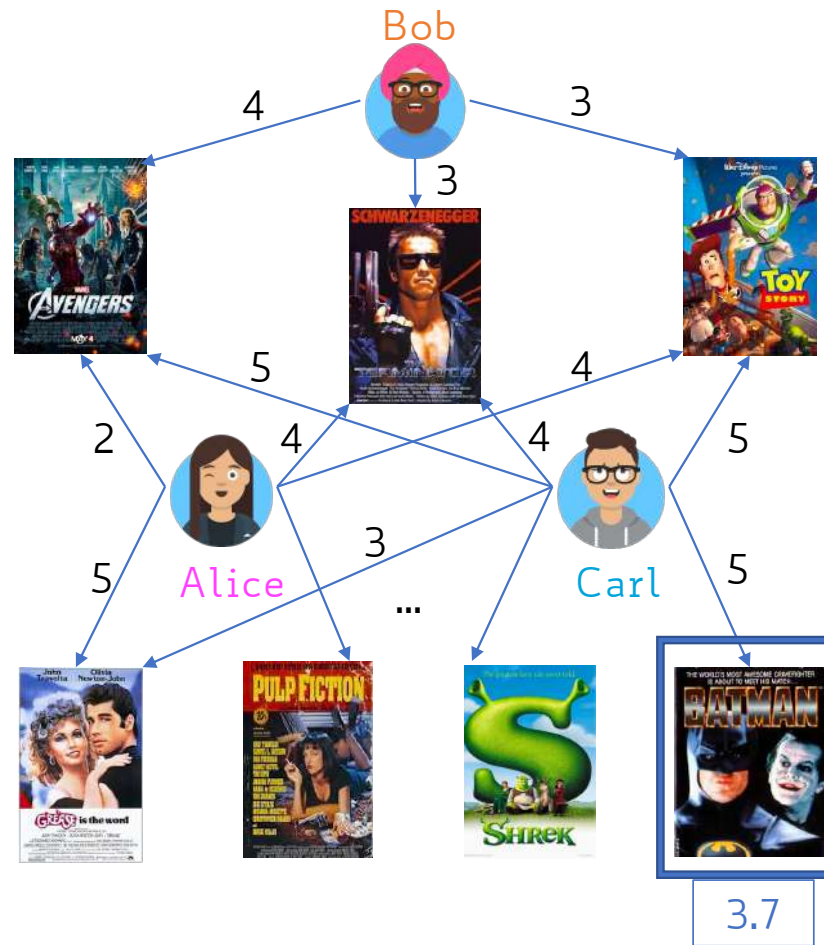
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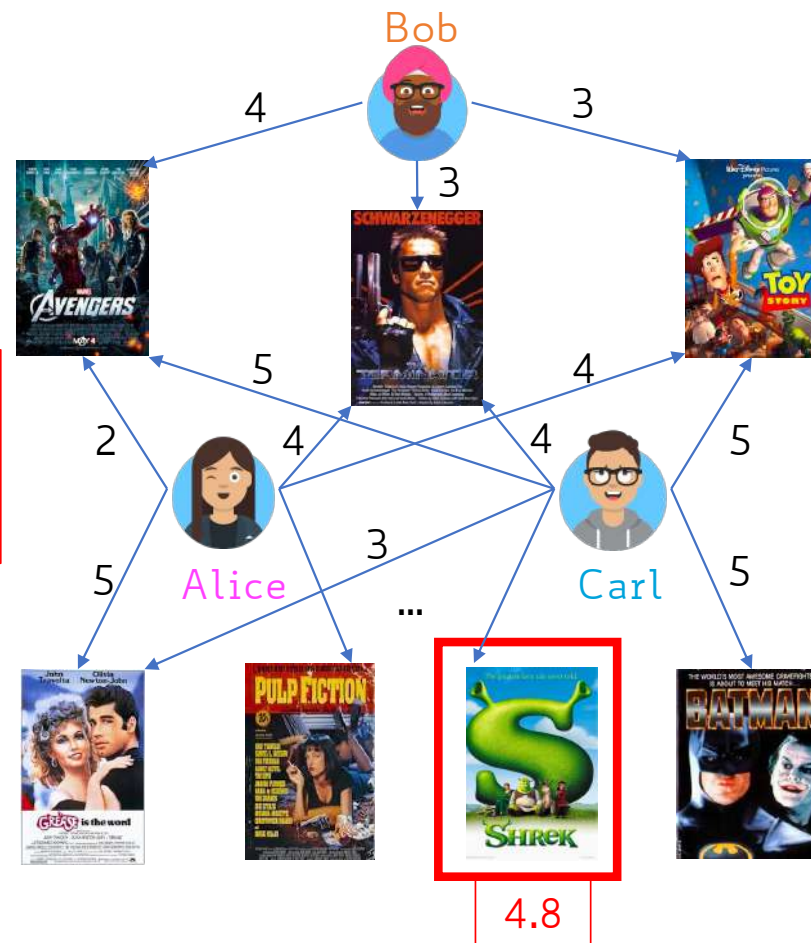
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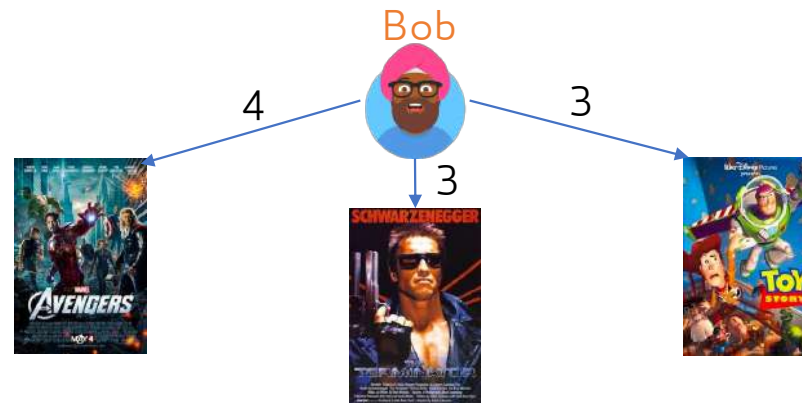


User-based Neighborhood: Example

Recommend the
highest rated
movie(s) to **Bob**!



User-based Neighborhood: Example



There is no point in predicting the rating of a movie which has only been rated by a user (Zoe) who is not in the Bob's neighborhood



User-to-User Similarity

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- Each user represented by her/his rating vector and similarity between them is measured in the item (rating) space

User-to-User Similarity





$\text{sim}(u, v)$ Similarity metric between any pair of users

		MOVIES							
									
USERS	 Alice	2		5	4	5	4		4
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Must capture the intuition: $\text{sim}(\text{Alice}, \text{Carl}) > \text{sim}(\text{Alice}, \text{Bob})$

User-to-User Similarity












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\mathbf{r}_{Bob}

User-to-User Similarity: Jaccard Similarity












$$\text{sim}(u, v) = J(\mathbf{r}_u, \mathbf{r}_v) = \frac{|\mathbf{r}_u \cap \mathbf{r}_v|}{|\mathbf{r}_u \cup \mathbf{r}_v|}$$


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$$\begin{aligned} \text{sim}(\text{Alice}, \text{Bob}) &= \frac{|\mathbf{r}_{\text{Alice}} \cap \mathbf{r}_{\text{Bob}}|}{|\mathbf{r}_{\text{Alice}} \cup \mathbf{r}_{\text{Bob}}|} \\ &= \frac{3}{6} = 0.5 \end{aligned}$$

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Problem!
Jaccard ignores
rating values

User-to-User Similarity: Cosine Similarity

$$\text{sim}(u, v) = \text{cosine}(\mathbf{r}_u, \mathbf{r}_v) = \frac{\mathbf{r}_u \cdot \mathbf{r}_v}{\|\mathbf{r}_u\| \|\mathbf{r}_v\|}$$

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$$\text{sim}(\text{Alice}, \text{Bob}) = \frac{\mathbf{r}_{\text{Alice}} \cdot \mathbf{r}_{\text{Bob}}}{\|\mathbf{r}_{\text{Alice}}\| \|\mathbf{r}_{\text{Bob}}\|}$$

$$= \frac{32}{\sqrt{102}\sqrt{44}} \approx 0.48$$

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$$= \frac{102}{\sqrt{102} \sqrt{141}} \approx 0.85$$

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Problem!
Missing rating values
are treated as 0s
and have a negative
effect

User-to-User Similarity: Pearson Correlation

$$\text{sim}(u, v) = \text{Pearson}(\mathbf{r}_u, \mathbf{r}_v) = \frac{(\mathbf{r}_u - \bar{\mathbf{r}}_u) \cdot (\mathbf{r}_v - \bar{\mathbf{r}}_v)}{\sqrt{(\mathbf{r}_u - \bar{\mathbf{r}}_u)^T \cdot (\mathbf{r}_u - \bar{\mathbf{r}}_u)} \times \sqrt{(\mathbf{r}_v - \bar{\mathbf{r}}_v)^T \cdot (\mathbf{r}_v - \bar{\mathbf{r}}_v)}}$$

		MOVIES							
									
USERS	 Alice	-2		1	0	1	0		0
	 Bob	2/3				-1/3		-1/3	
	 Carl	4/7	4/7	-10/7	-3/7	4/7	-3/7		4/7

	 Zoe		-9/4	-1/4				7/4	-1/4

Solution:
Normalize ratings by subtracting the mean rating

Now 0 means neutral, and if we treat missing ratings as 0, it doesn't mean it's negative

User-to-User Similarity: Pearson Correlation

$\mathbf{r}'_u = \mathbf{r}_u - \bar{\mathbf{r}}_u$ mean-scaled rating vector of u

$\mathbf{r}'_v = \mathbf{r}_v - \bar{\mathbf{r}}_v$ mean-scaled rating vector of v

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$$= \frac{(\mathbf{r}_u - \bar{\mathbf{r}}_u) \cdot (\mathbf{r}_v - \bar{\mathbf{r}}_v)}{\sqrt{(\mathbf{r}_u - \bar{\mathbf{r}}_u)^T \cdot (\mathbf{r}_u - \bar{\mathbf{r}}_u)} \times \sqrt{(\mathbf{r}_v - \bar{\mathbf{r}}_v)^T \cdot (\mathbf{r}_v - \bar{\mathbf{r}}_v)}} = \text{Pearson}(\mathbf{r}_u, \mathbf{r}_v)$$

User-based Neighborhood: Predictions

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$$\mathcal{U}^k = \operatorname{argmax}_{\mathcal{U}' \subseteq \mathcal{U} \setminus u, |\mathcal{U}'|=k} \sum_{u' \in \mathcal{U}'} \operatorname{sim}(u, u') \quad \begin{array}{l} \text{Top-}k \text{ most "similar" users to } u \\ \text{u's } k\text{-neighborhood} \end{array}$$

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Set of items rated by u 's neighbors

$$\mathcal{I}^k = \{i \in \mathcal{I} : \mathbf{r}_{u',i} = \downarrow \wedge u' \in \mathcal{U}^k\}$$

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Predicted rating given by user u to item i

$$\mathbf{r}_u[i] = r(u, i) = r_{u,i}$$

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plain average

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plain average

$$r_{u,i} = \frac{1}{k} \sum_{u' \in \mathcal{U}^k} \text{sim}(u, u') \cdot r_{u',i}$$

weighted average

User-based CF: Drawbacks

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computing similarities between all pairs of users is expensive

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computing similarities between all pairs of users is expensive

Aging

user profiles changed quickly and the entire system model had to be recomputed

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- The model doesn't suffer from aging and therefore it does not need to be recomputed frequently

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Estimate $r(u, i)$ based on the ratings of items in the
 k -neighborhood of i

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$\mathbf{r}_{\text{Shrek}}$

Item-based Neighborhood: Example

Let's consider again Bob!

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Item-based Neighborhood: Example


Suppose we want to predict the rating **Bob** would give to **Shrek**

		MOVIES							
									
USERS	Alice	2		5	4	5	4		4
	Bob	4				?	3		3
	Carl	5	5	3	4	5	4		5

	Zoe		1	3				5	4

Item-based Neighborhood: Example

We first extract the subset of k most similar items to Shrek which have been rated by Bob












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r_{Shrek}

Item-based Neighborhood: Example

Suppose those are: The Avengers and The Terminator








		MOVIES							
									
USERS	 Alice	2		5	4	5	4		4
	 Bob	4					3		3
	 Carl	5	5	3	4	5	4		5

	 Zoe		1	3				5	4

For example, item similarity is measured using Pearson's correlation

Item-based Neighborhood: Example

The predicted rating is computed as an aggregating function of the ratings that **Bob** gave to the k most similar movies to Shrek

		MOVIES							
									
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Item-based Neighborhood: Predictions

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Predicted rating given by user u to item i

$$\mathbf{r}_u[i] = r(u, i) = r_{u,i}$$

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$$r_{u,i} = \frac{1}{k} \sum_{i' \in \mathcal{I}_u^k} \text{sim}(i, i') \cdot r_{u,i'}$$

weighted average

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- Item similarity can be computed from rating vectors (in user space)
- Analogous to user similarity of rating vectors (in item space):
 - Jaccard index
 - Cosine similarity (normalized = Pearson's correlation)
- Rating prediction using the same methods proposed for user-based CF
 - Plain average of ratings
 - Weighted average of ratings (taking item similarity into account)

Item-to-Item Collaborative Filtering

In general, **item-based** works better than **user-based** CF

Memory-based CF: Implementation

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- Finding the k most similar users/items should be pre-computed (offline)
- k -nearest neighbors search in high dimensions (i.e., quickly find the set of k nearest data points)

Memory-based CF: Implementation

The curse of dimensionality (again!)



Memory-based CF: Implementation

Locality-Sensitive Hashing (LSH) approximation



Take-Home Message of Today

- Recommender systems as tools for dealing with information overload

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- 2 main approaches:
 - Content-based (explicitly creating user and item profiles)
 - Collaborative-filtering (extract patterns from past observed ratings)

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- Collaborative-filtering may require computing the all-pair user/item similarity
- In large scale systems, this must be pre-computed offline
- At inference time, make use of ad hoc data structures (e.g., k-d trees) to efficiently compute the set of (approximated) nearest neighbors for a query user/item