

# Big Data Computing

Master's Degree in Computer Science

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UNIVERSITÀ DI ROMA

# Recap from Last Lecture(s)

2 unsupervised learning techniques to extract "structural" patterns from raw data

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- Formalized as an NP-hard optimization problem
- K-means and its variants as effective heuristics that work in practice

## Principal Component Analysis (PCA)

- Reduce data dimensionality
- Automatically extract features from raw data
- Resort to computing the eigenvectors and eigenvalues of the covariance matrix

# SUPERVISED LEARNING

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  - **Task/Problem**: Find the maximum element of a list of 1 million unsorted numbers
  - **Solution/Algorithm**: Scan all the numbers in the set and keep track of the largest found "so far"
  - **Code/Program**: Encode the algorithm above into one specific programming language (e.g., C/C++, Java, Python)

# Programming a Computer



Problem

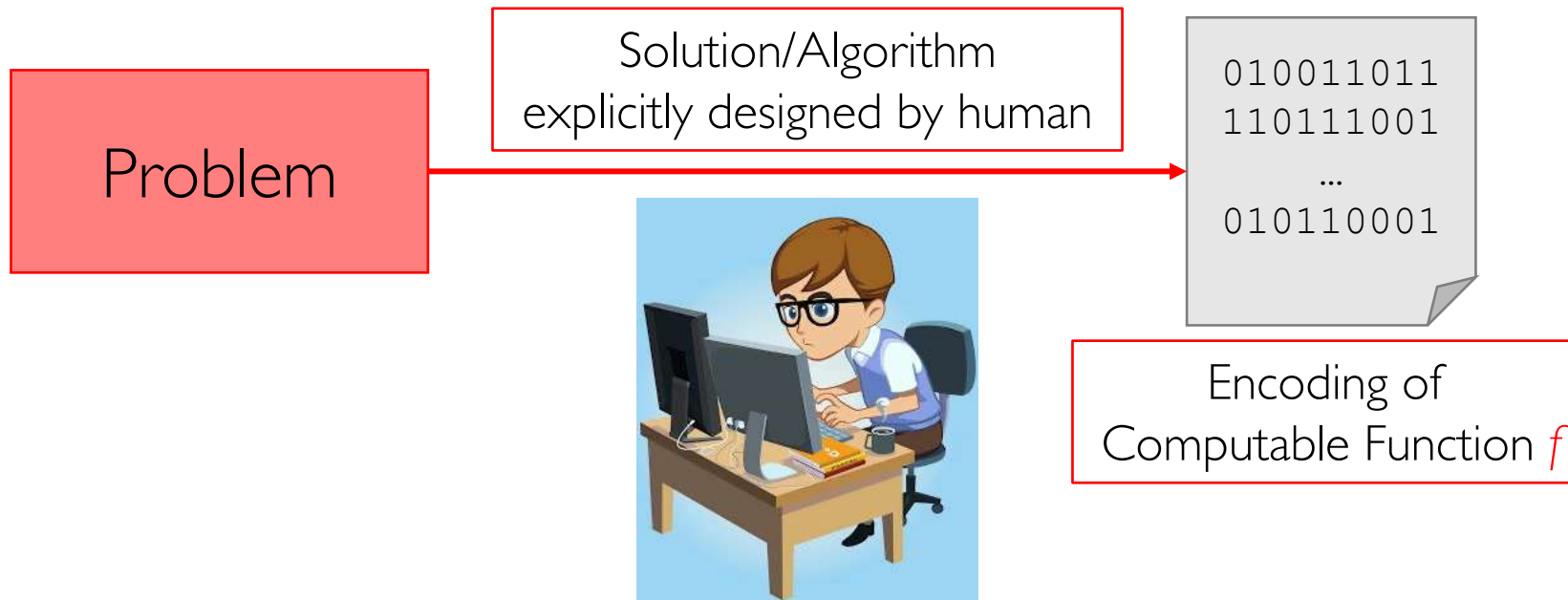
# Programming a Computer

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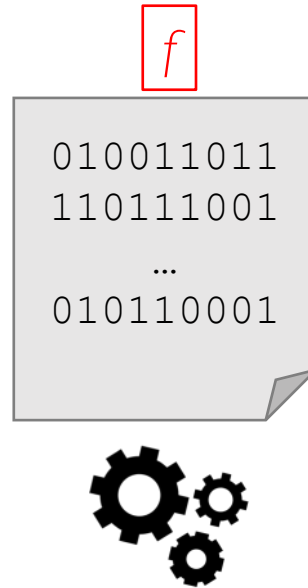
Solution/Algorithm  
explicitly designed by human



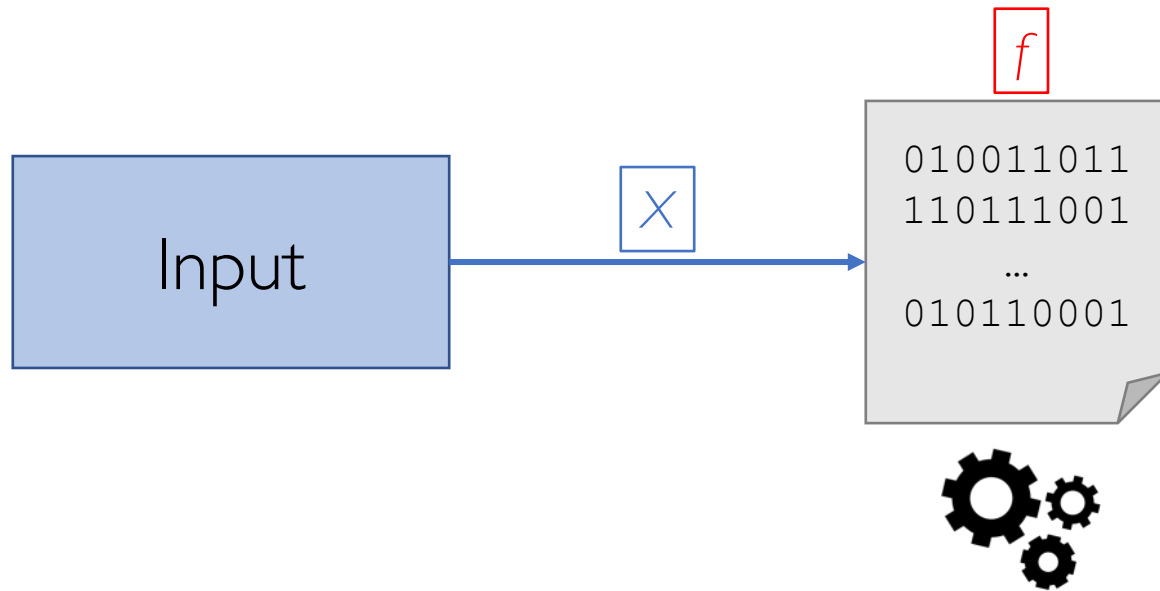
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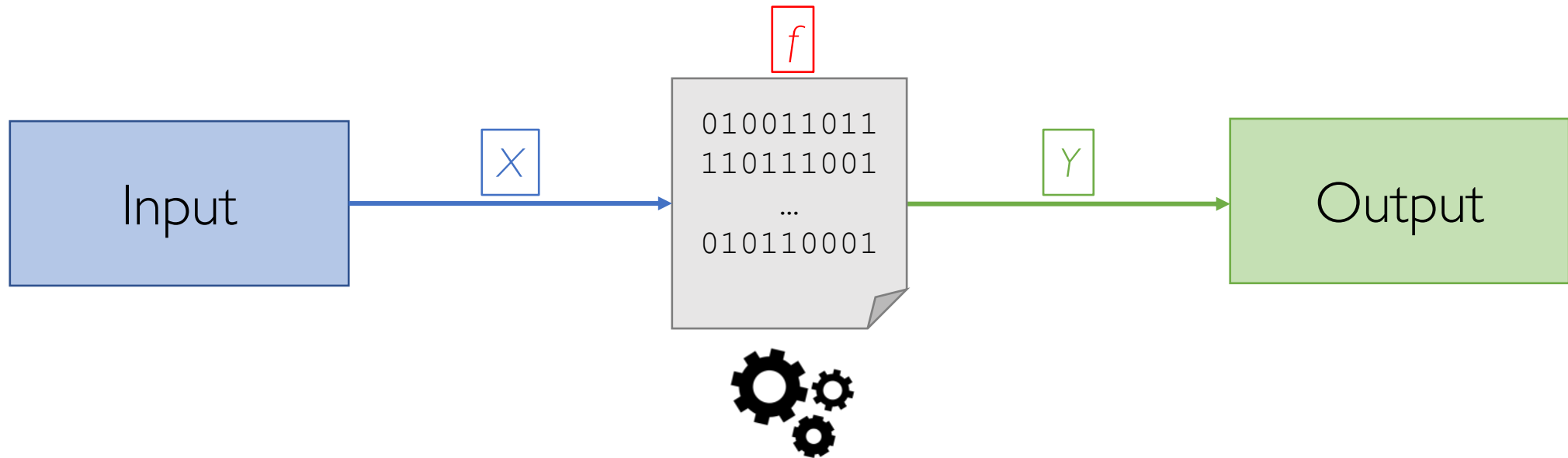
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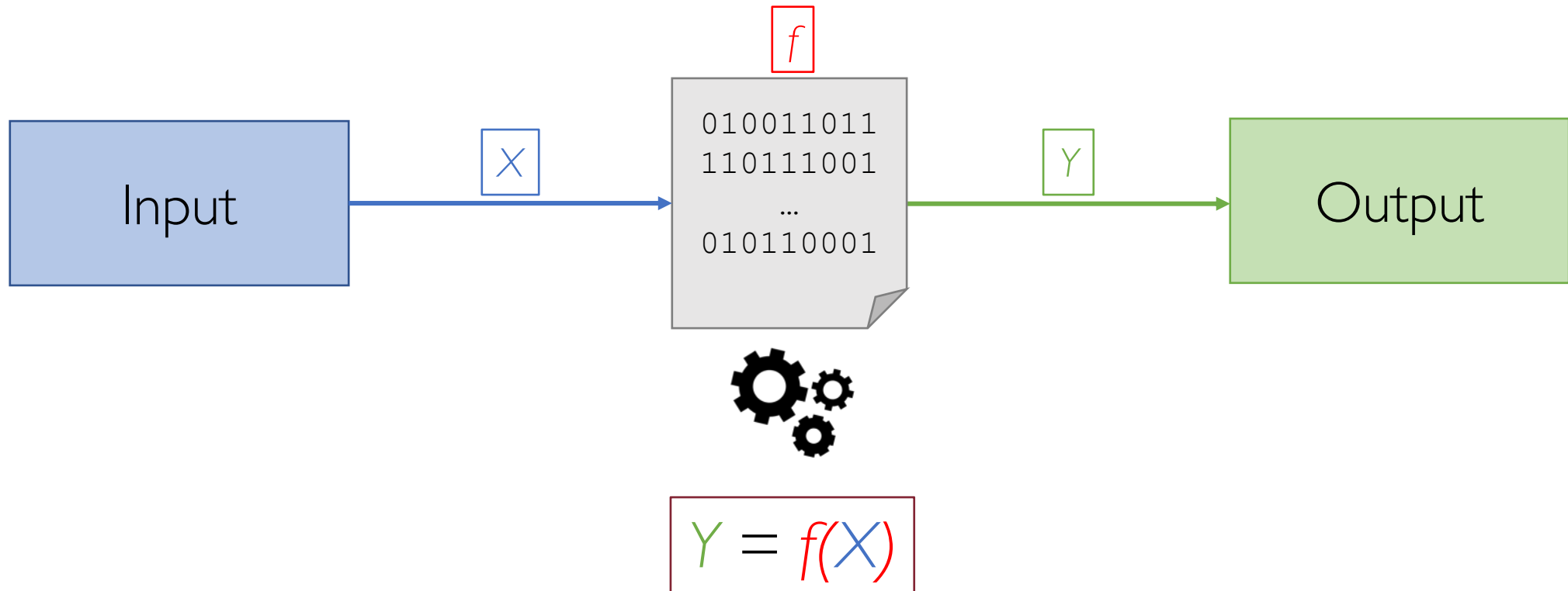
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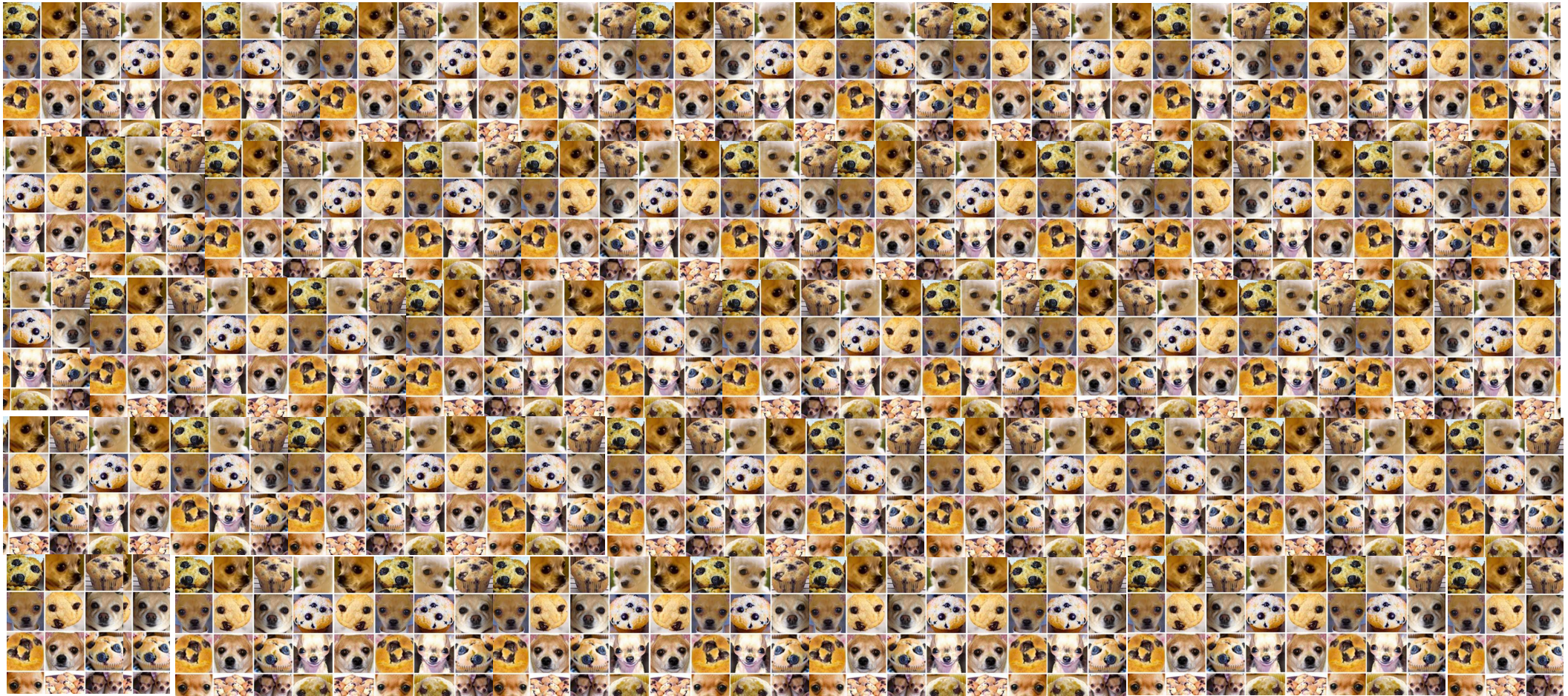
# Programming a Computer





Can We Always Do That?

# Chihuahua or Muffin?



[Copyright @teenybiscuit]



# Chihuahua



# Muffin



# Programming vs. "Training" a Computer

- There exist some problems like the **chihuahua** vs. **muffin** above which are too hard to be solved directly

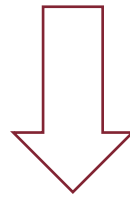
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# "Training" a Computer

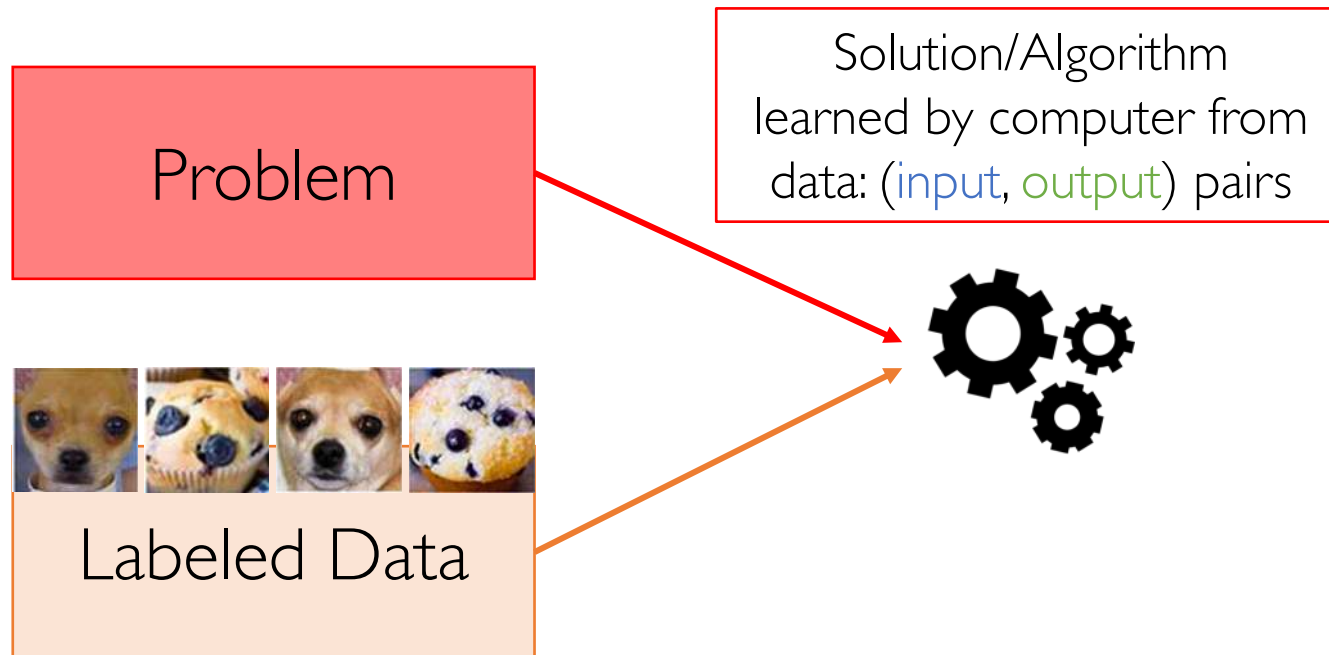
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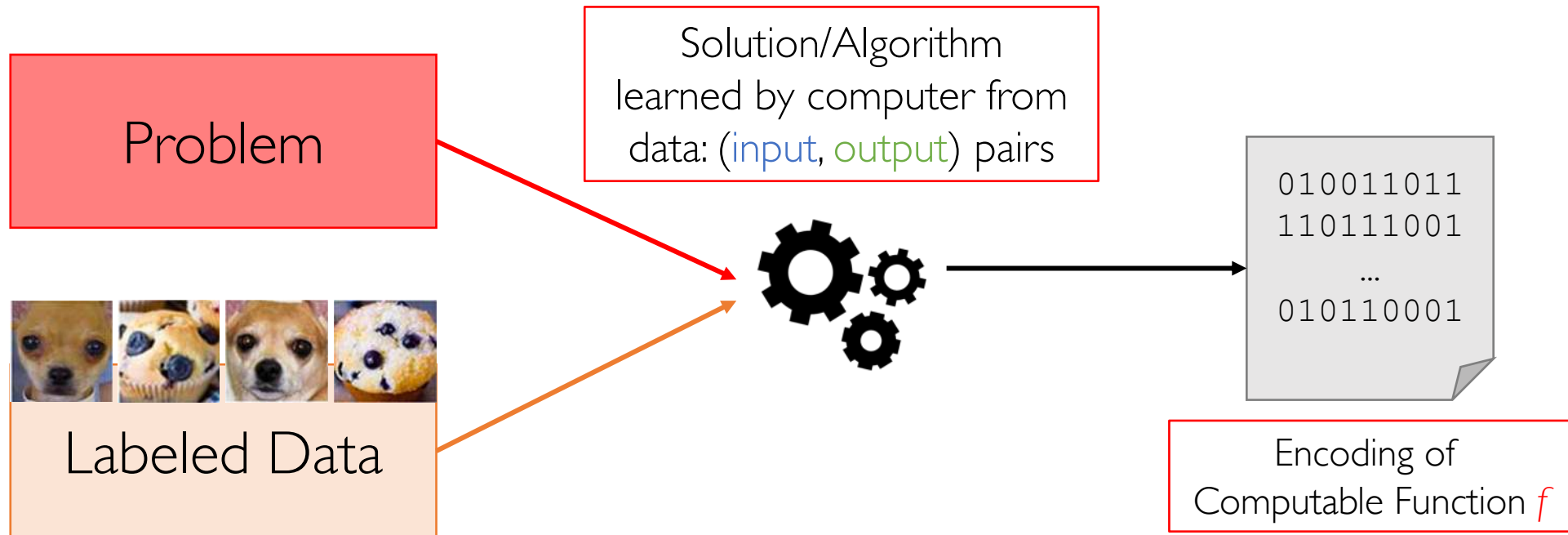
Labeled Data



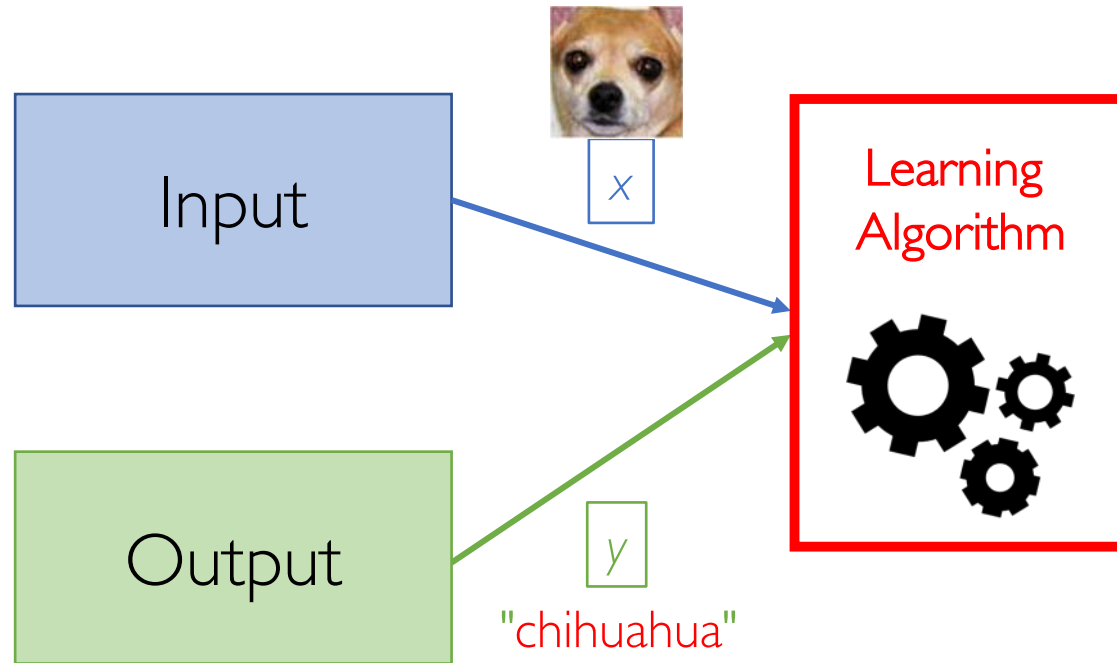
# "Training" a Computer



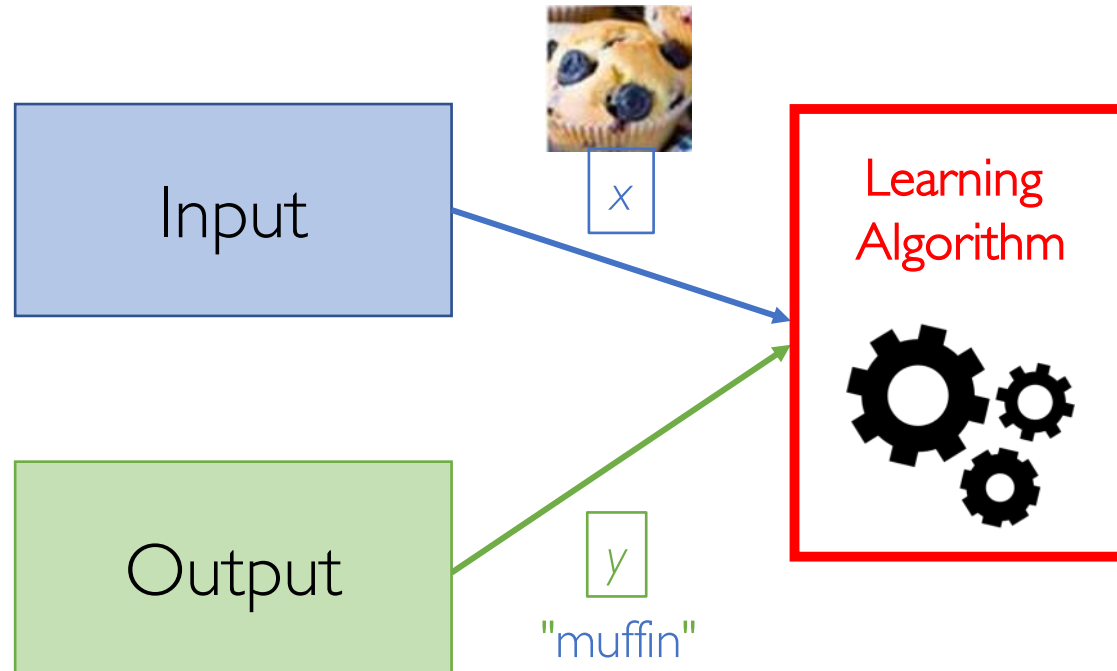
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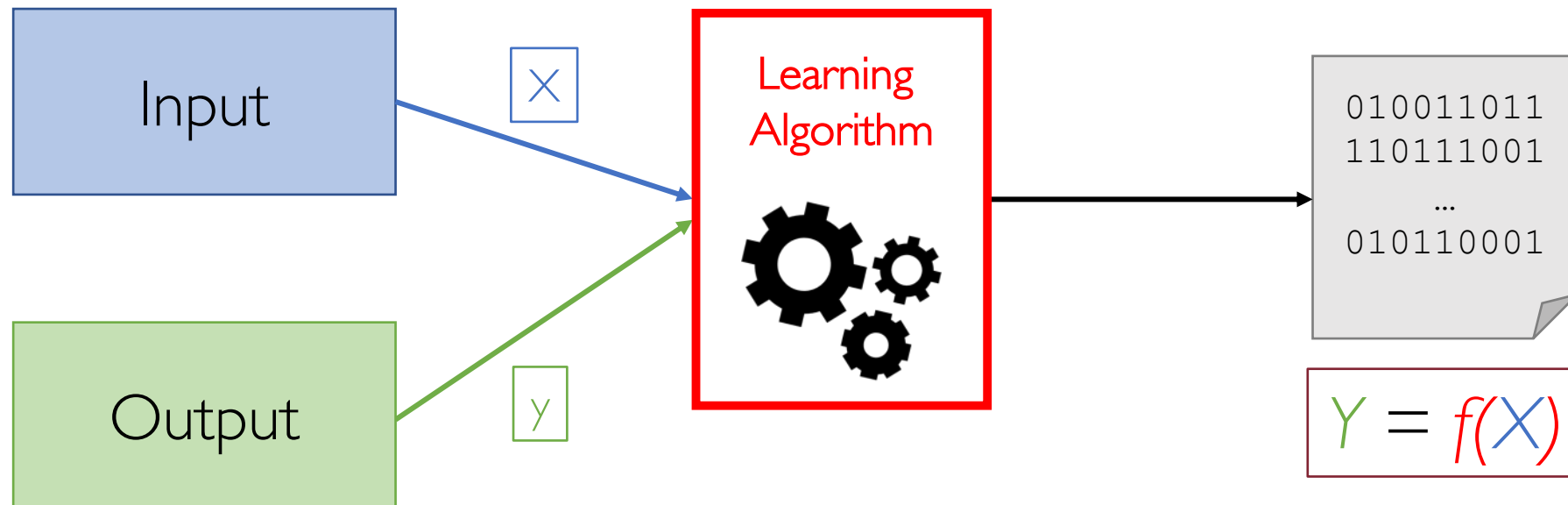
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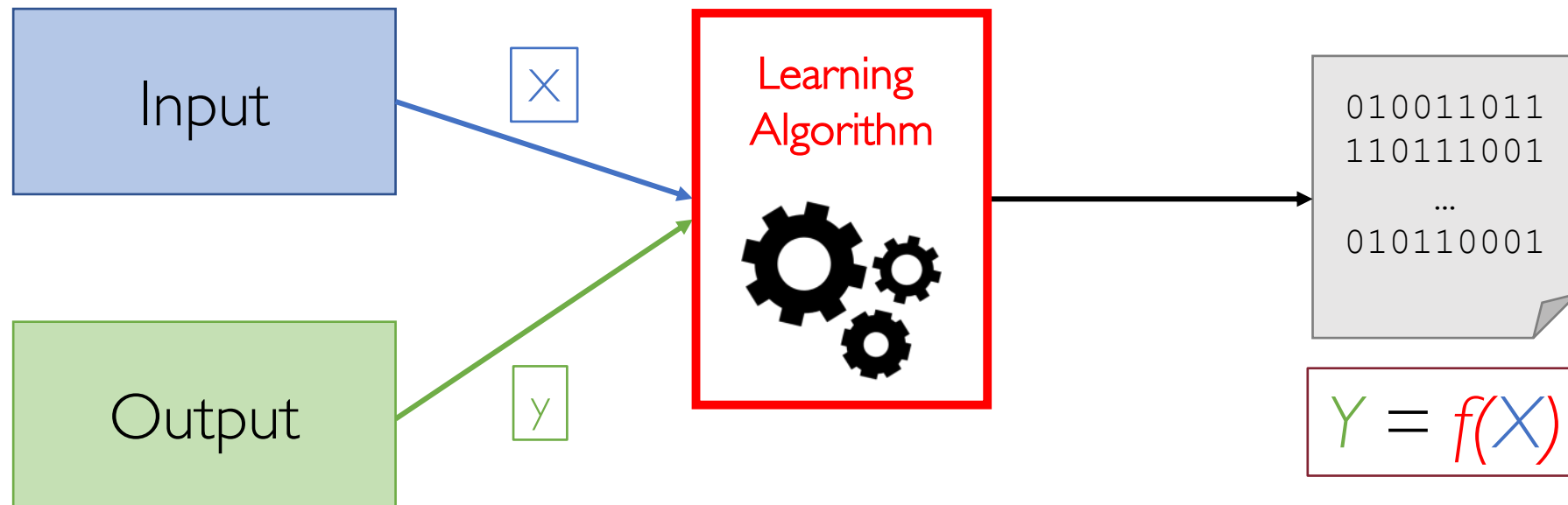
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Eventually, the function  $f$  is **learned** by the learning algorithm from a (large) set of **labeled data**

# Machine Learning

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*"A computer program is said to learn from experience  $E$  with respect to some class of tasks  $T$  and performance measure  $P$ , if its performance at tasks in  $T$ , as measured by  $P$ , improves with experience  $E$ "*

Tom Mitchell

# Machine Learning: Taxonomy

Machine Learning

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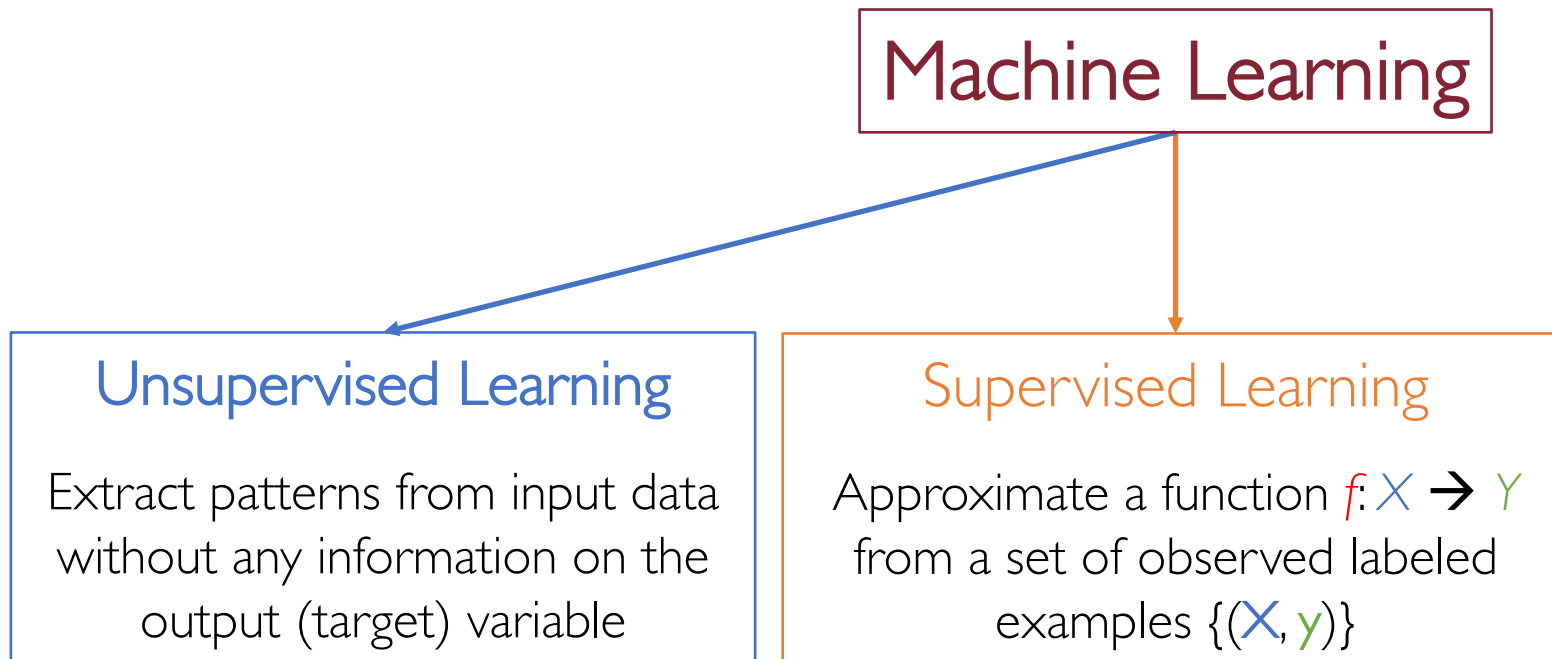
Machine Learning



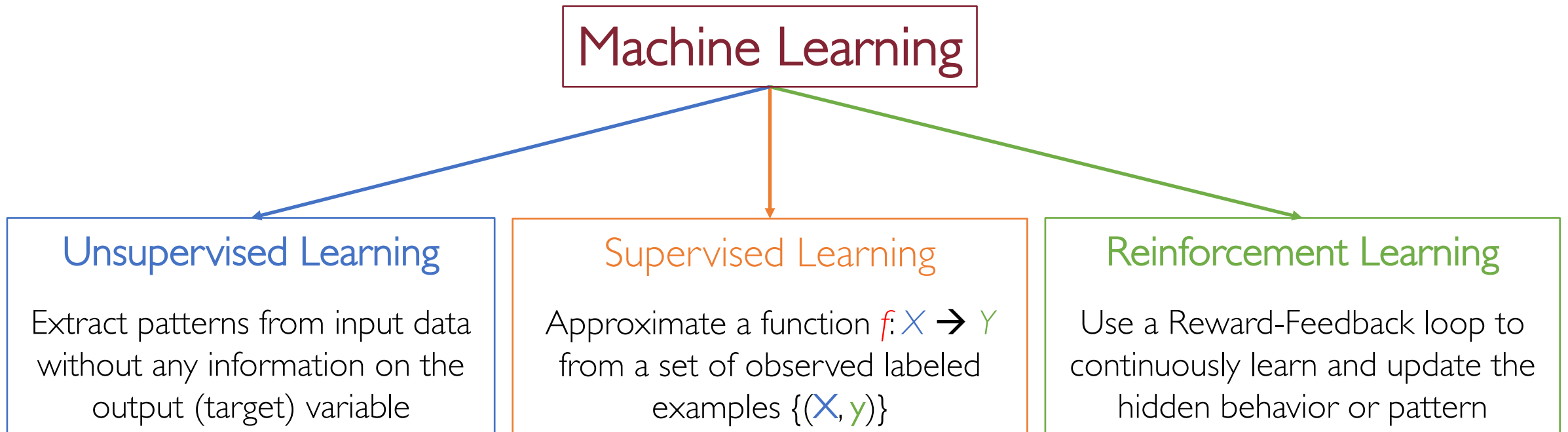
## Unsupervised Learning

Extract patterns from input data without any information on the output (target) variable

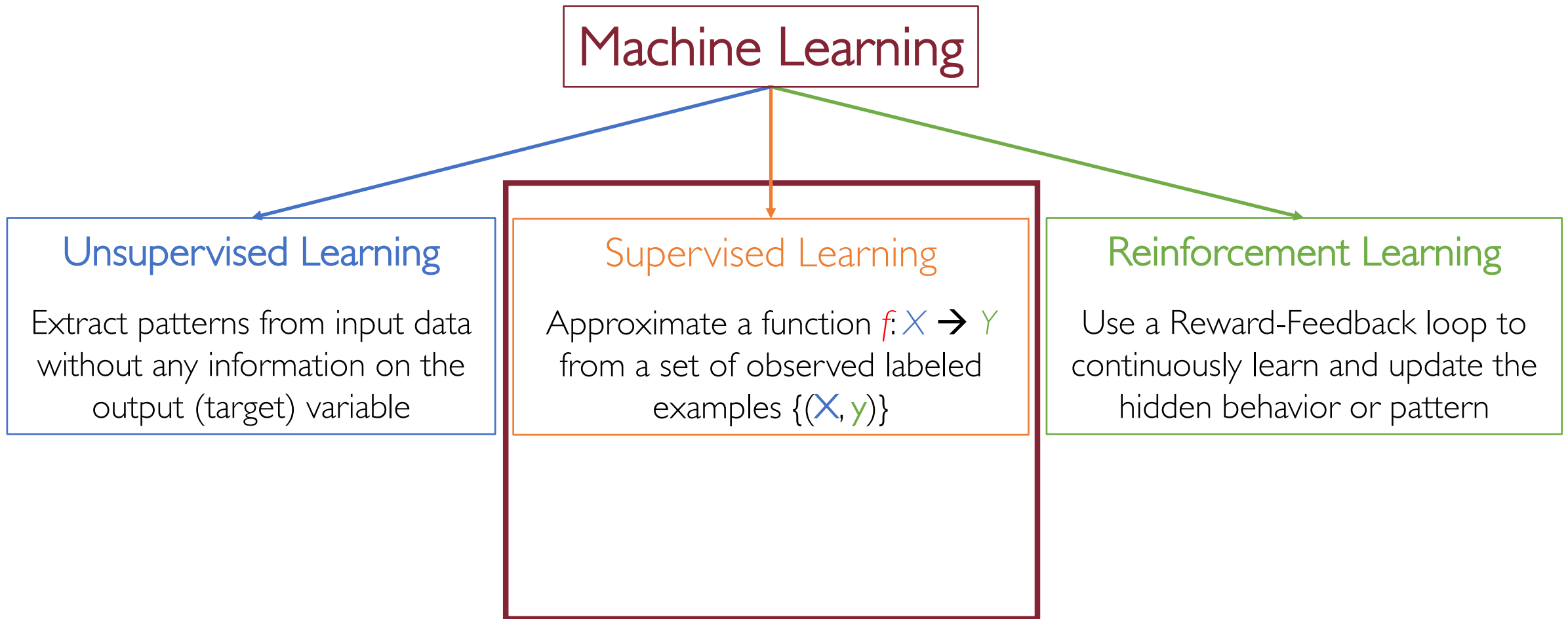
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# Supervised Learning: What Do We Predict?

Supervised Learning



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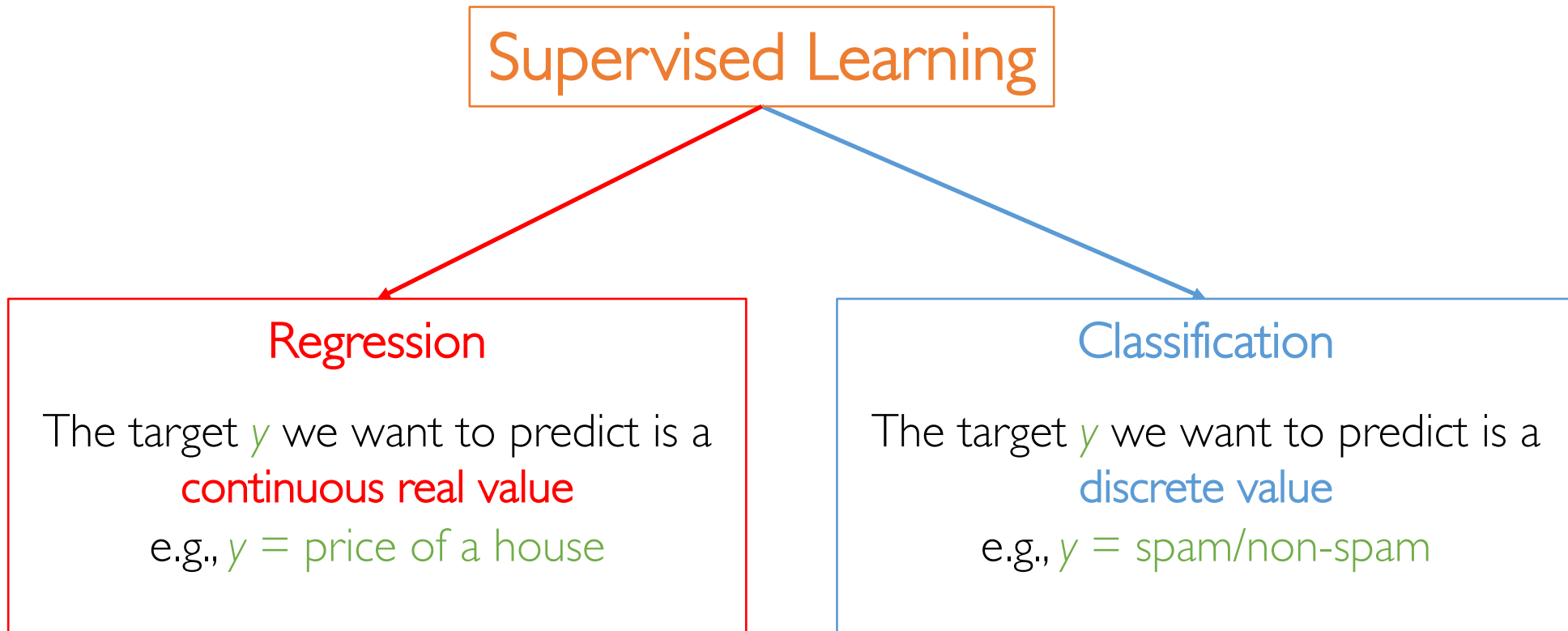
Supervised Learning



Regression

The target  $y$  we want to predict is a  
**continuous real value**  
e.g.,  $y = \text{price of a house}$

# Supervised Learning: What Do We Predict?



# The Supervised Learning Pipeline

# The Stages of Supervised Learning

0. Be sure your problem needs actually to be tackled using Machine Learning techniques

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3. **Model training:** “build” one (or more) learning models

**4. Model selection/evaluation:** pick the best-performing model according to some quality metrics



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- Supervised Learning requires **labeled data** which may be even harder to get
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- Might involve combining multiple and heterogeneous data sources

# Feature Engineering



Domain Objects

# Feature Engineering

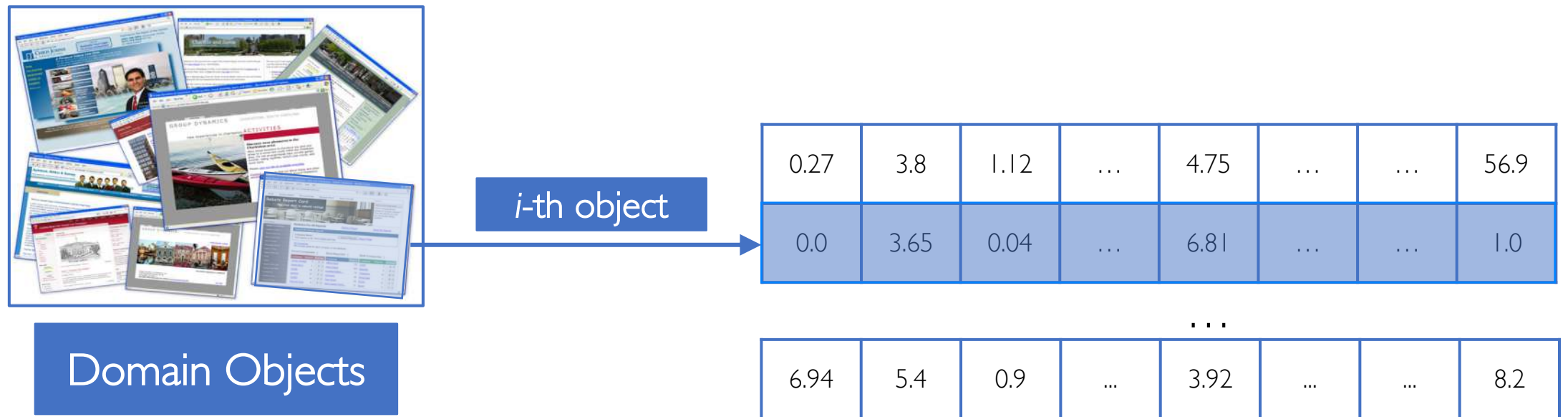
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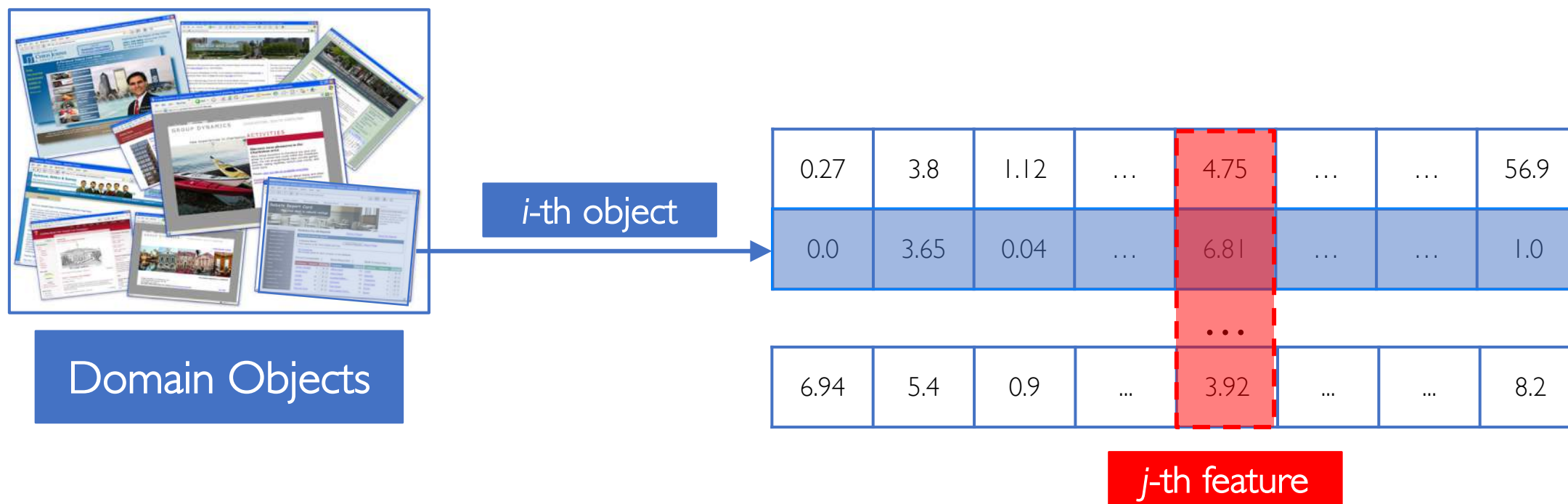
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- Each feature can be either derived locally from an instance
  - e.g., **annual\_income** of a person
- Or it can be the result of more complex computation involving the whole data collection
  - e.g., **tf-idf** of a word of a document w.r.t. a corpus

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- Require in-depth knowledge of the specific domain of application
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- Tedious and time-consuming process
- Techniques to **automatically** learn data representation (i.e., features):
  - K-means clustering, PCA, autoencoders (**unsupervised**)
  - Neural Networks (**supervised**)

# Feature Engineering: Challenges and Solutions

Collected (raw) data is far from being perfect!

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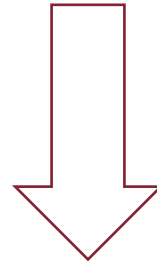
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Data Preprocessing

# Feature Engineering: Challenges and Solutions

Challenge	Description	
Missing values	A feature value may not be available for one or more instances	

# Feature Engineering: Challenges and Solutions

Challenge	Description	Solution
Missing values	A feature value may not be available for one or more instances	Replace missing values with the <b>median</b> (continuous) or the <b>mode</b> (categorical) of the existing values

# Feature Engineering: Challenges and Solutions

Challenge	Description	
Sparsity	Most of the instances contain just a small subset of the features	

# Feature Engineering: Challenges and Solutions

Challenge	Description	Solution
Sparsity	Most of the instances contain just a small subset of the features	Use “sparse-friendly” data structures (e.g., DOK)

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# Feature Engineering: Challenges and Solutions

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Outliers	One or more instances have out-of-range values for one or more features	Retention vs. Exclusion ( <i>trimming</i> or <i>winsorising</i> )

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Multiple feature magnitudes	Feature set contains very wide range of values	

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Challenge	Description	Solution
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Strong multicollinearity	Linear relationship between one or more features	Dimensionality reduction (PCA)

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input feature space



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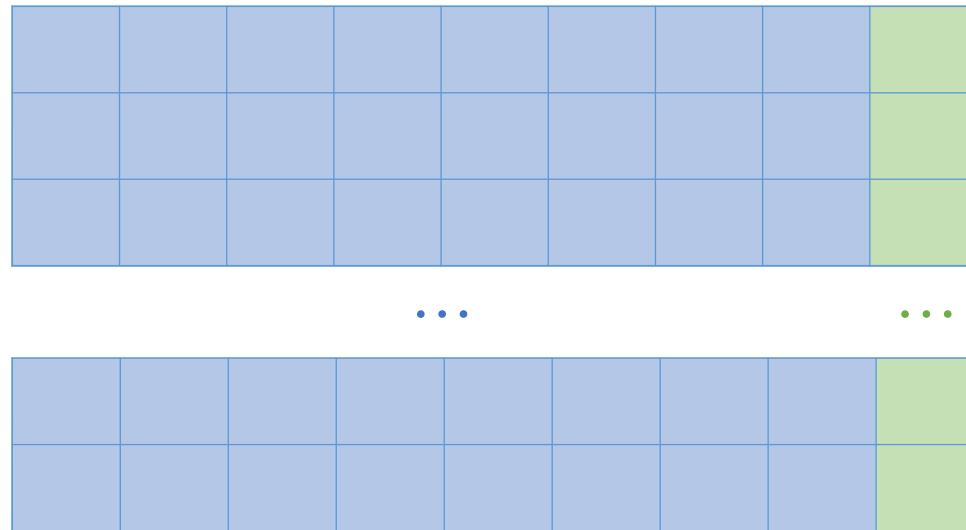
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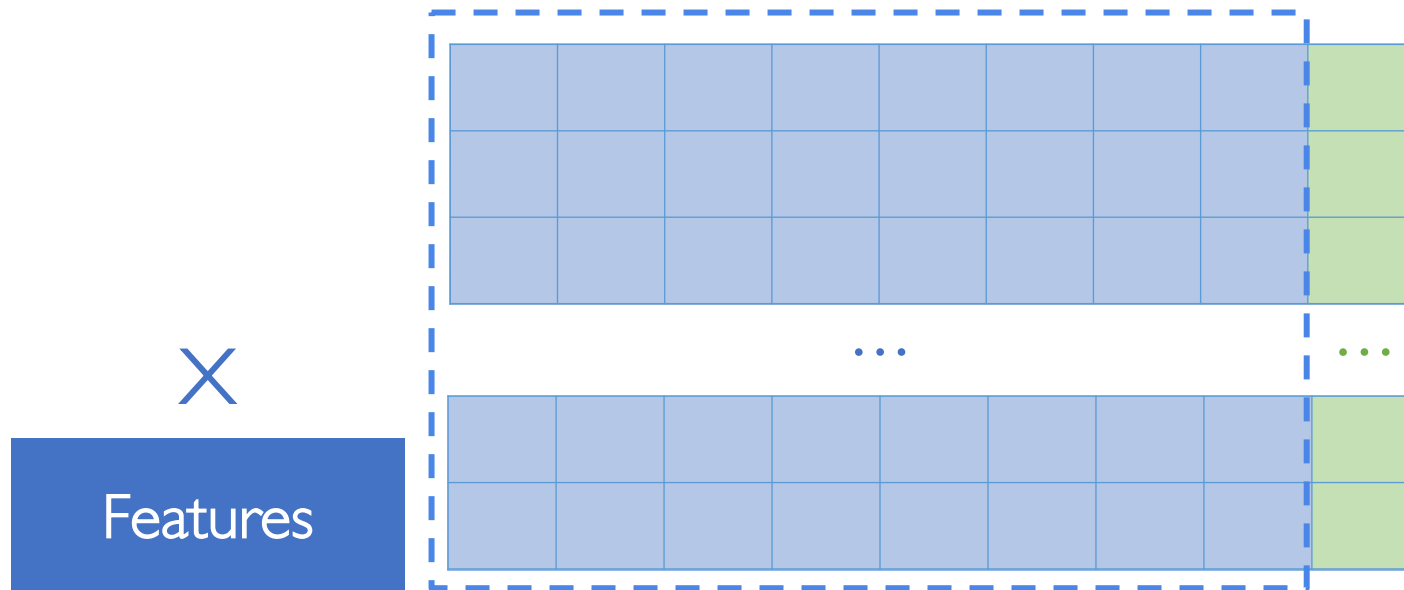
$$\mathcal{D} = \{(\mathbf{x}_1, y_1), \dots, (\mathbf{x}_m, y_m)\}$$

dataset of  $m$  **i.i.d.** labeled instances

# Model Training: Labeled Dataset

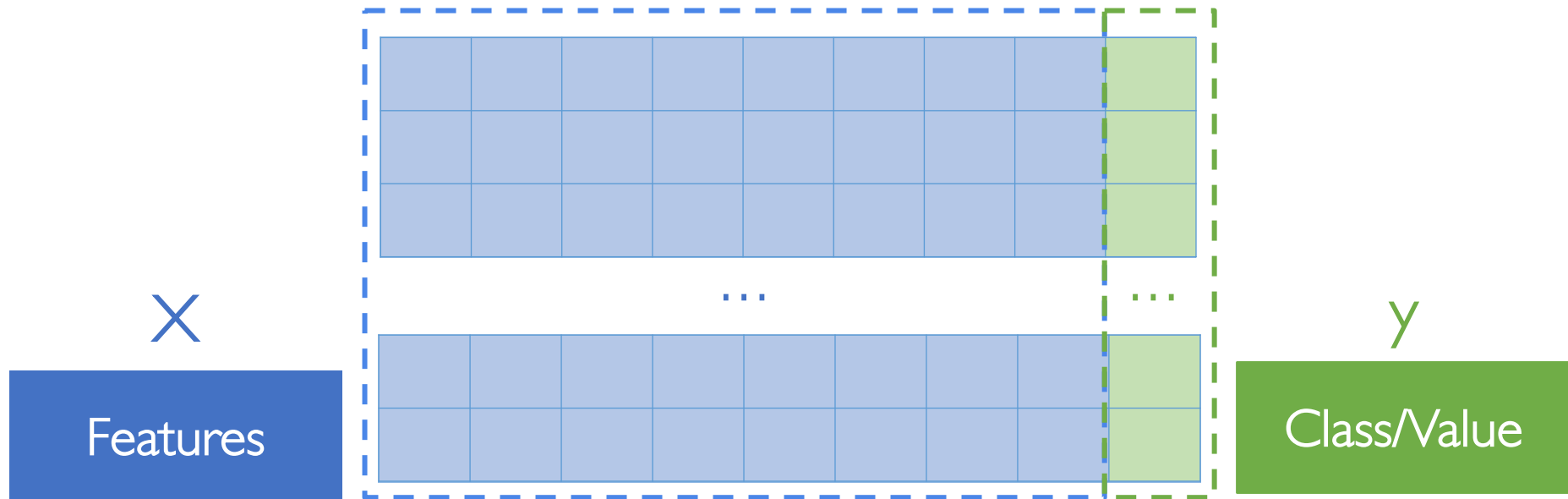


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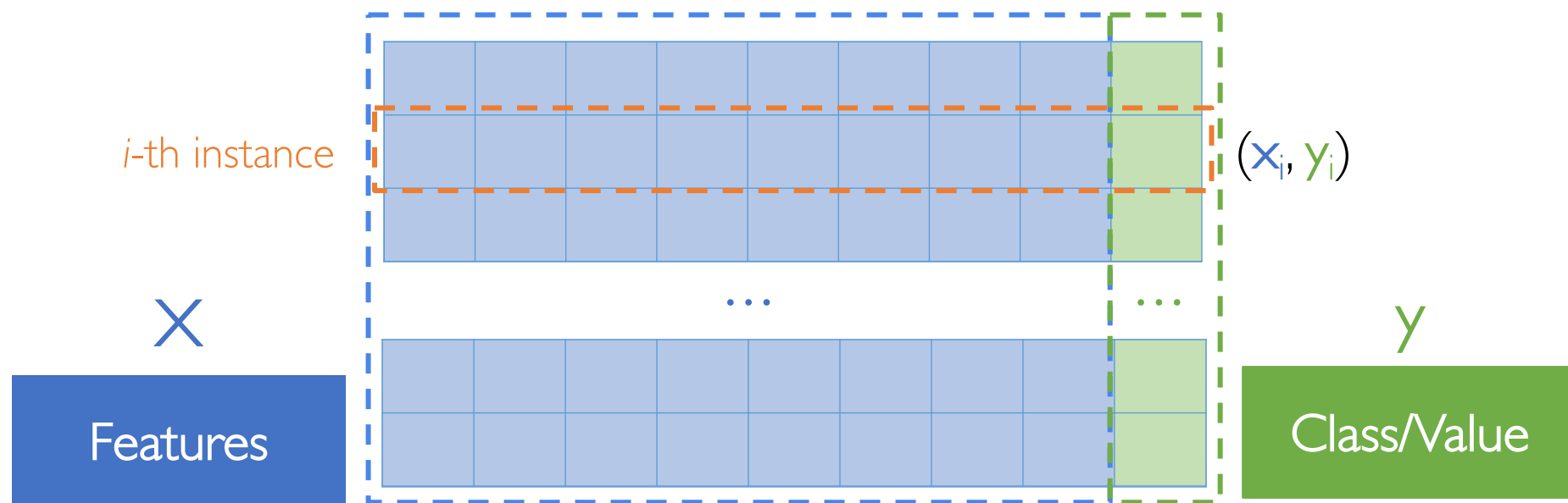


# Model Training: Labeled Dataset



# Model Training: Labeled Dataset

Each instance comes with the **class label** (**classification**) or the **value** (**regression**) we want to predict



# Model Training: Intuition

## Idea

There is an **unknown target function**  $f$  which puts in a relationship elements of  $X$  with elements of  $Y$

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## Problem

We cannot write down an algorithm which just implements  $f$

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  - **learning algorithm**: explores the hypothesis space to pick the function which minimizes the loss on the observed data

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## Trade-off

Put some constraints on  $H$ , e.g., limit the search space only to **linear functions**

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- This **in-sample error** (a.k.a. empirical loss) is an estimate of the **out-of-sample error** (a.k.a. expected loss or risk)



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$$h^* = \operatorname{argmin}_{h \in \mathcal{H}} L(h, \mathcal{D})$$

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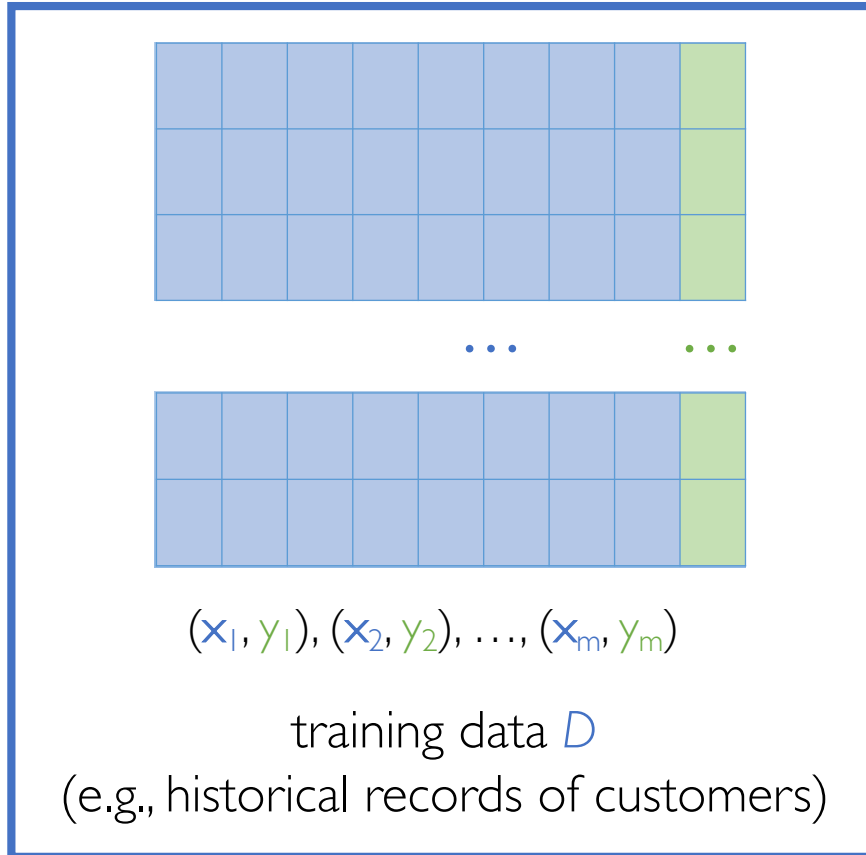
A diagram showing training data D as a grid of feature-target pairs. It consists of two rows of blue boxes (features) and one column of green boxes (targets). The first row has 8 blue boxes followed by 1 green box. The second row has 8 blue boxes followed by 1 green box. Below the first row, there are three blue dots and three green dots, indicating continuation of the data.

$(x_1, y_1), (x_2, y_2), \dots, (x_m, y_m)$

training data  $D$   
(e.g., historical records of customers)

unknown target  
(e.g., ideal credit approval function)

$$f = X \rightarrow Y$$



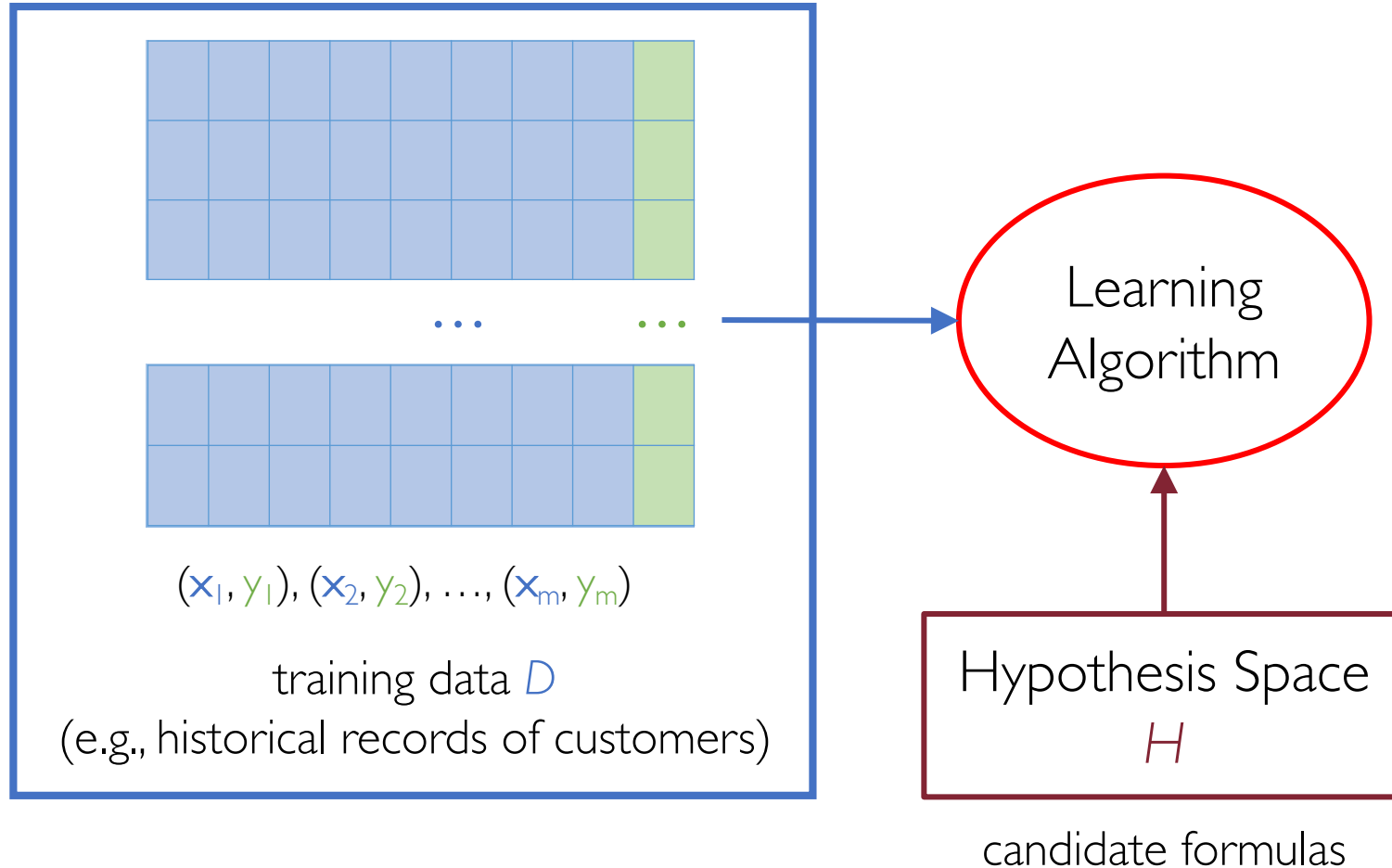
Hypothesis Space

$H$

candidate formulas

unknown target  
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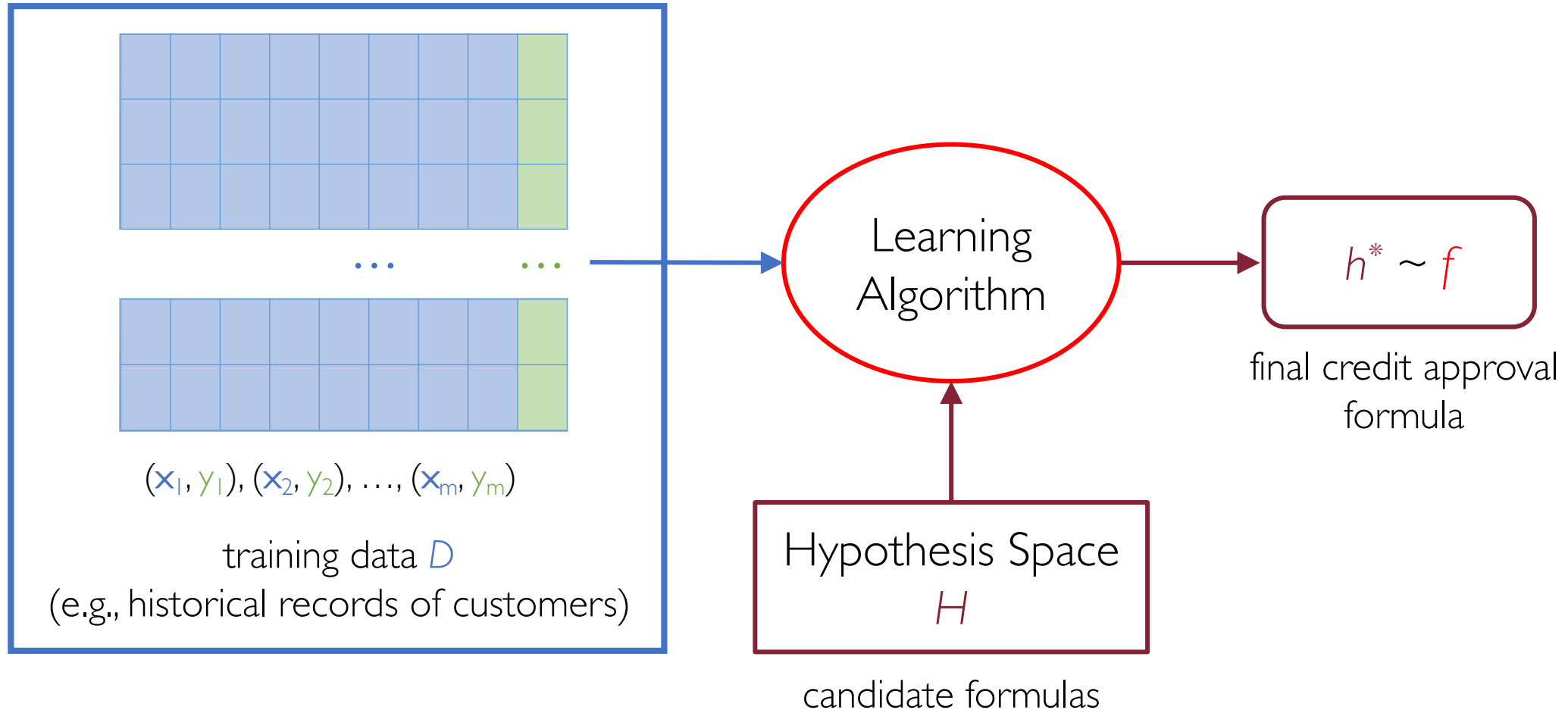
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# Learning $f$ as an Optimization Problem

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- Those choices are usually "mathematically convenient": e.g., **convex objective functions** are guaranteed to have a unique global minimum
- Even though closed-form solutions to the optimization problem rarely exist, there are numerical methods which work: e.g., **gradient descent**

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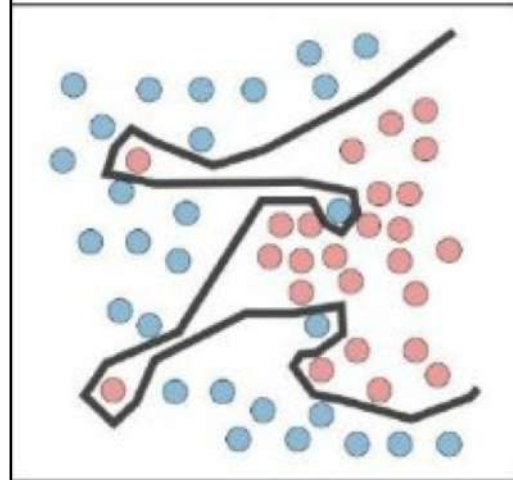
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- At the same time we do not want  $h^*$  to perform poorly on  $D$

# Overfitting (High Variance)

Regression



Classification



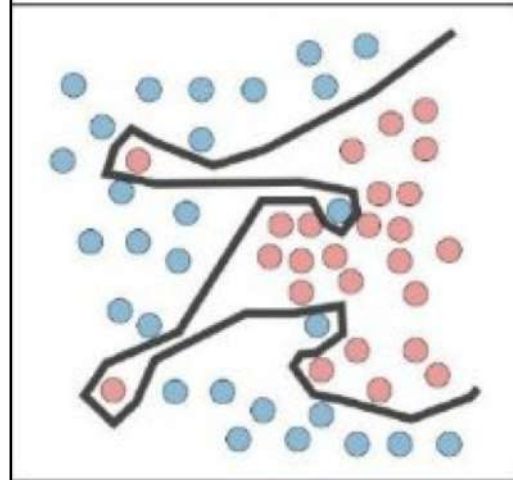
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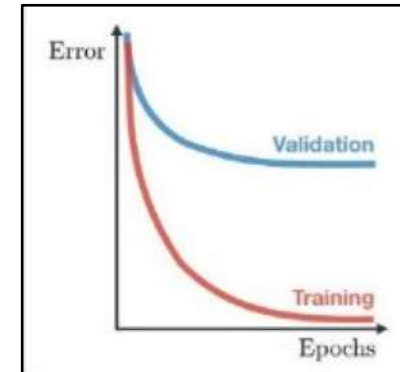
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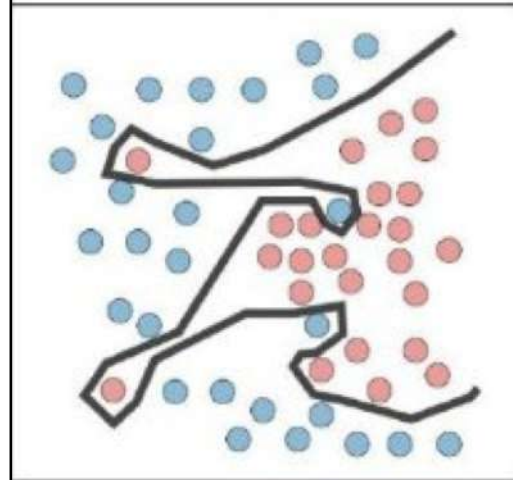
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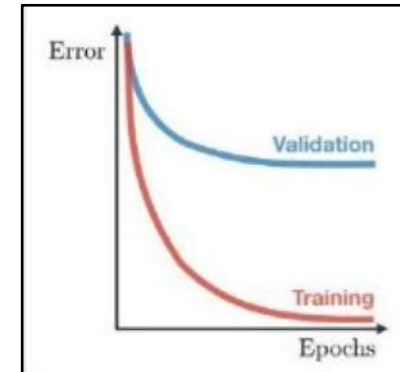
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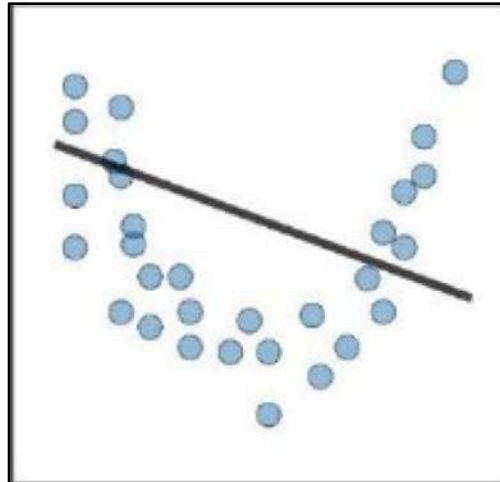


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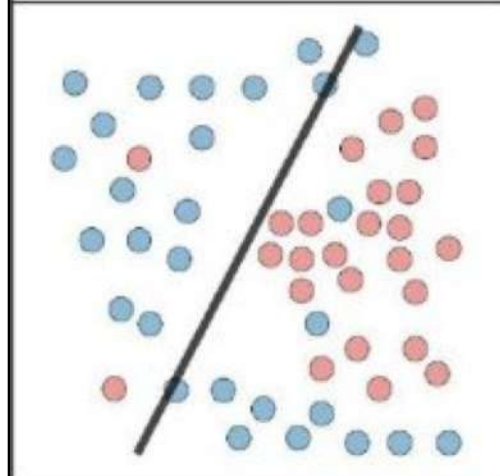
- Regularization
- Get more data

# Underfitting (High Bias)

Regression



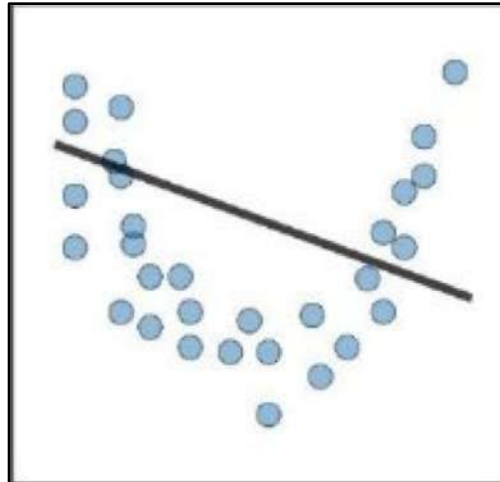
Classification



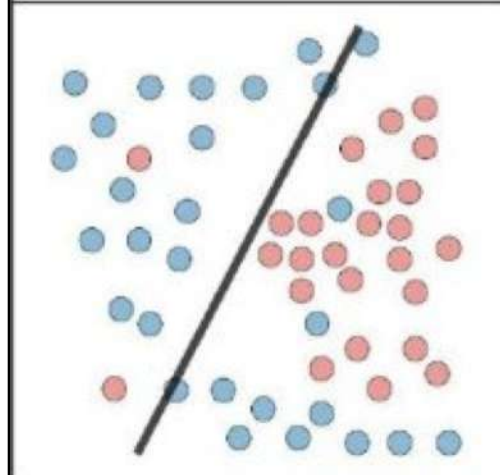
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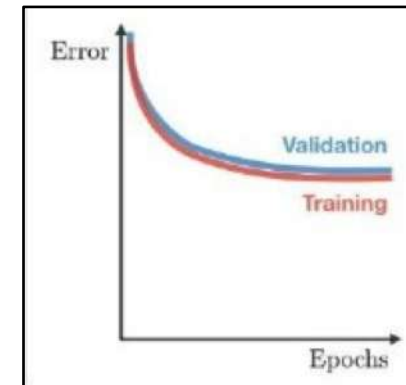
Regression



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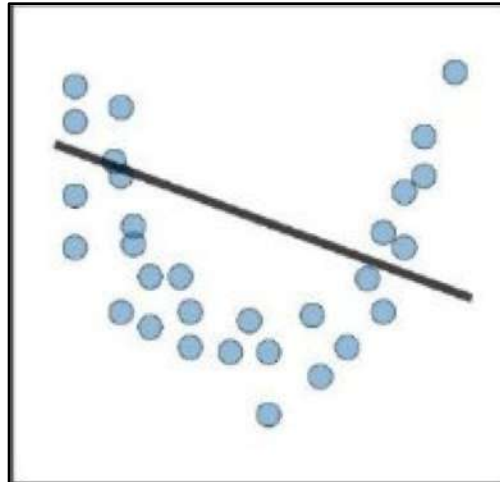
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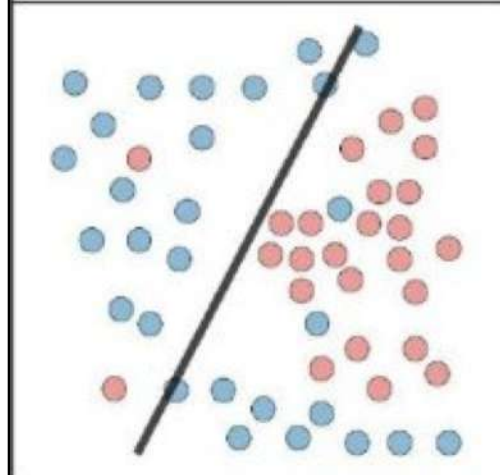
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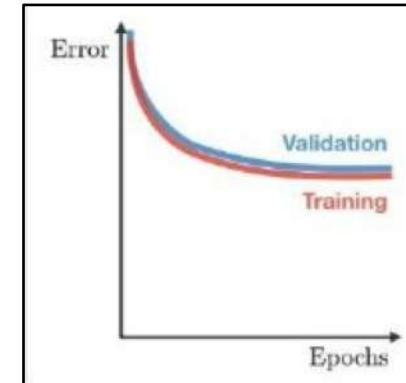
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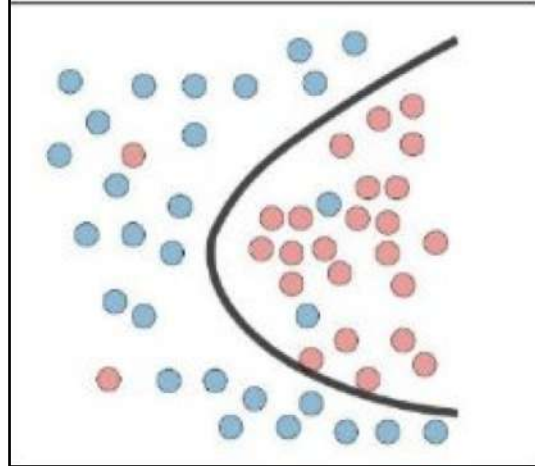
- Increase model complexity
- Add more features

# Bias-Variance Tradeoff

Regression



Classification



The hypothesis  $h^*$  is just right:  
the simplest one explaining the data

Occam's razor

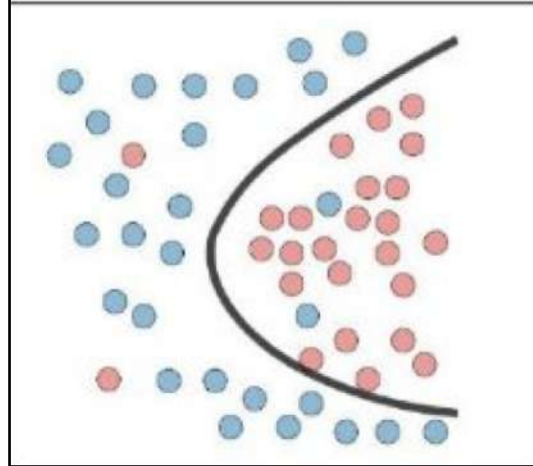


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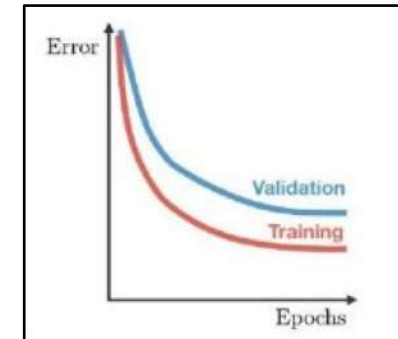


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# Estimating Generalization Performance

- Measuring the generalization (i.e., out-of-sample) performance online may be too risky

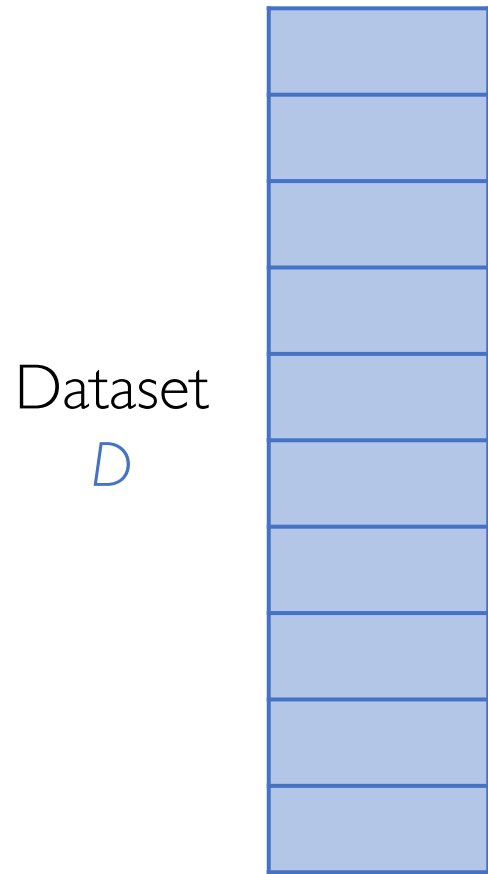
# Estimating Generalization Performance

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- **Example:** Don't want to deploy your new spam classifier in production knowing only its training (i.e., in-sample) performance

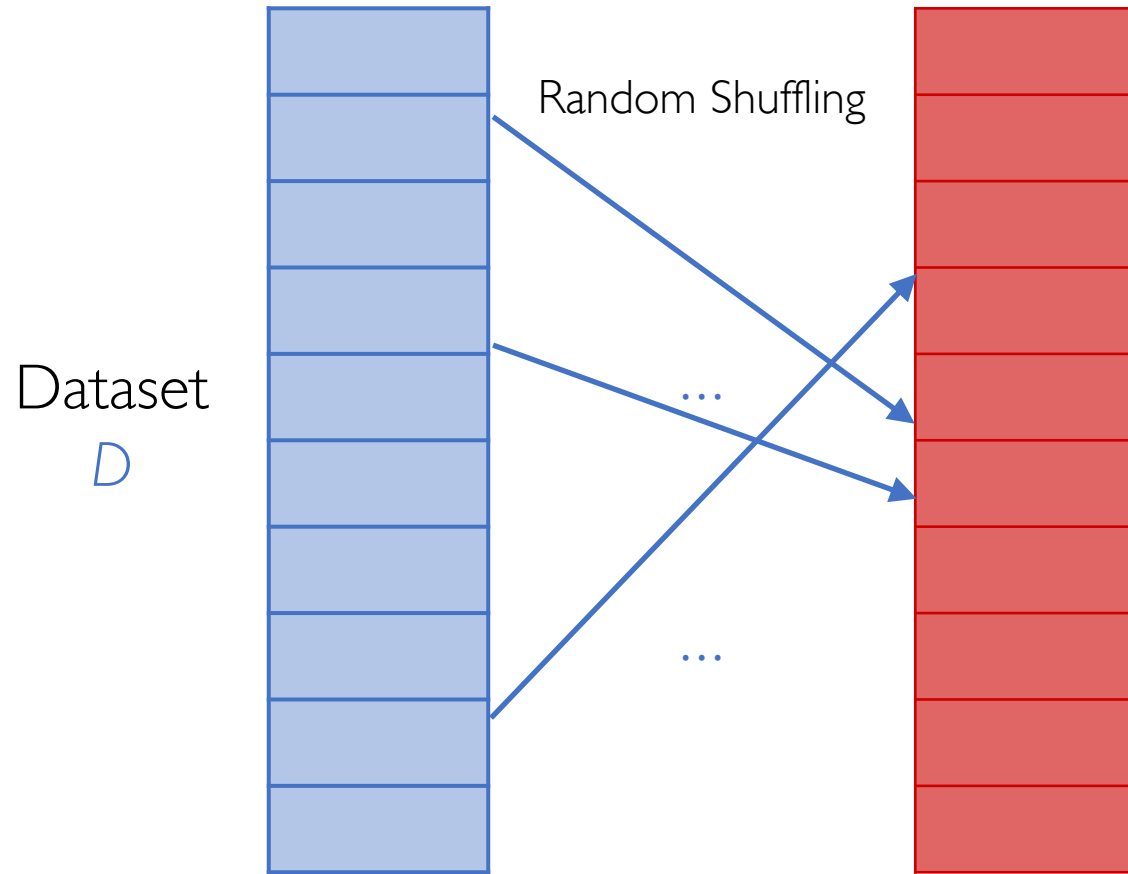
# Estimating Generalization Performance

- Measuring the generalization (i.e., out-of-sample) performance online may be too risky
- **Example:** Don't want to deploy your new spam classifier in production knowing only its training (i.e., in-sample) performance
- **Solution:** Estimate the generalization performance using training set
  - As long as it holds true the assumption that training and test instances are both drawn from the same probability distribution (**i.i.d. assumption**)

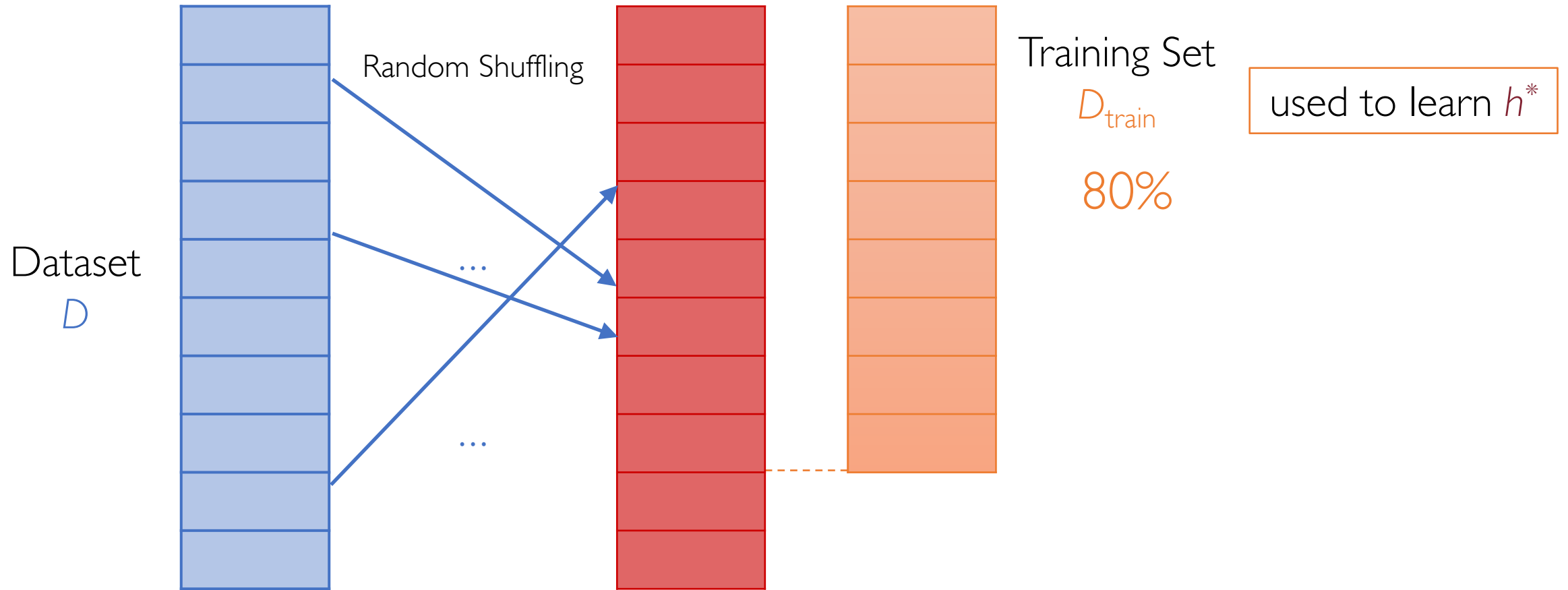
# Dataset Splitting



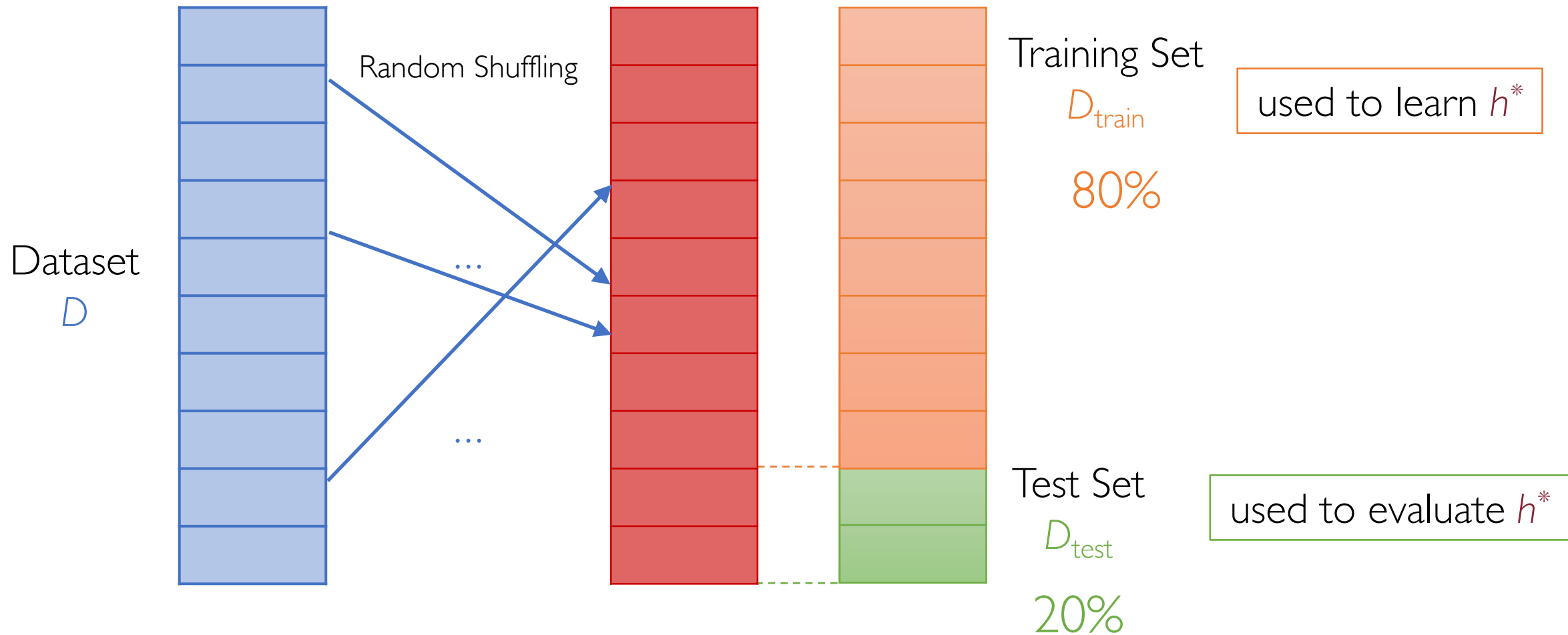
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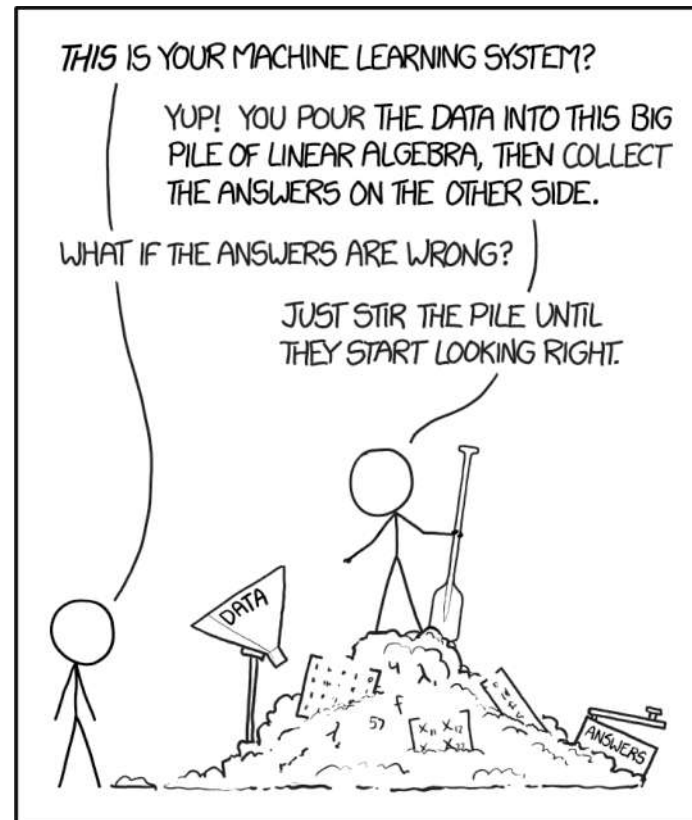
# Dataset Splitting





# How Much Data Do We Need?

In general, the more data we have the better we learn



# K-Fold Cross Validation

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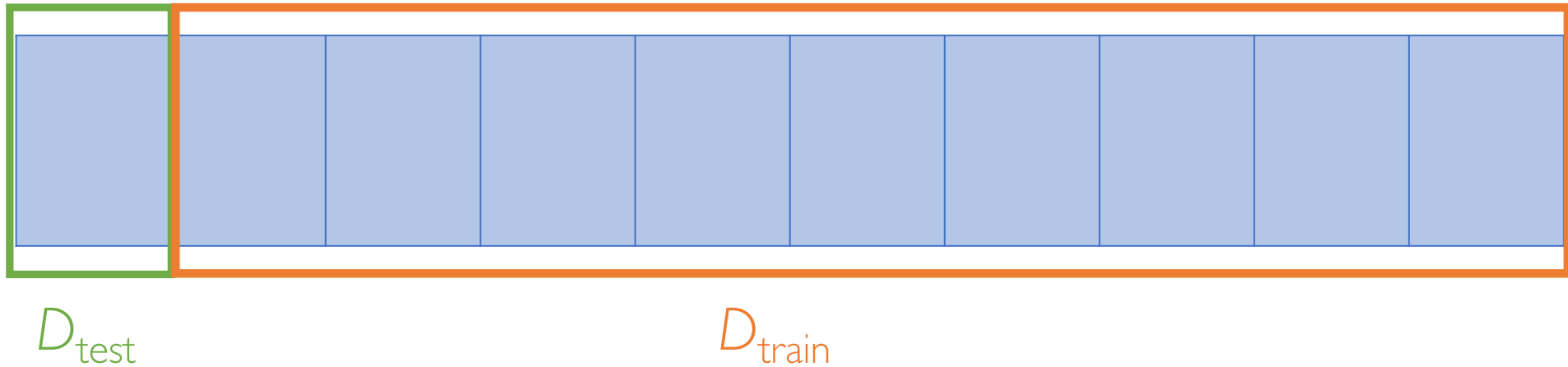
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- The estimate of generalization error is the average across the  $K$  test folds of all the  $K$  rounds

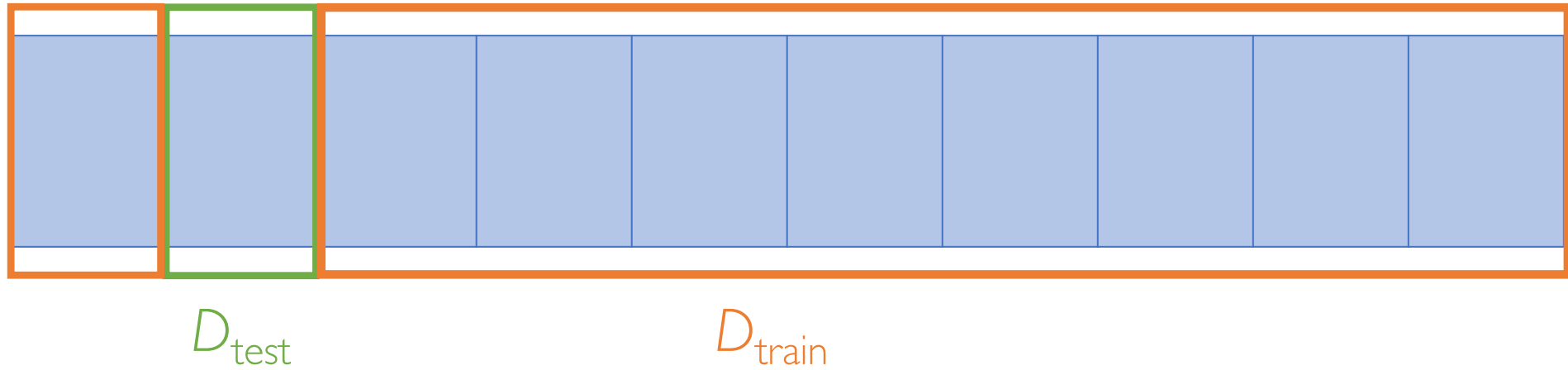
# K-Fold Cross Validation

Round  $k = 1$



# K-Fold Cross Validation

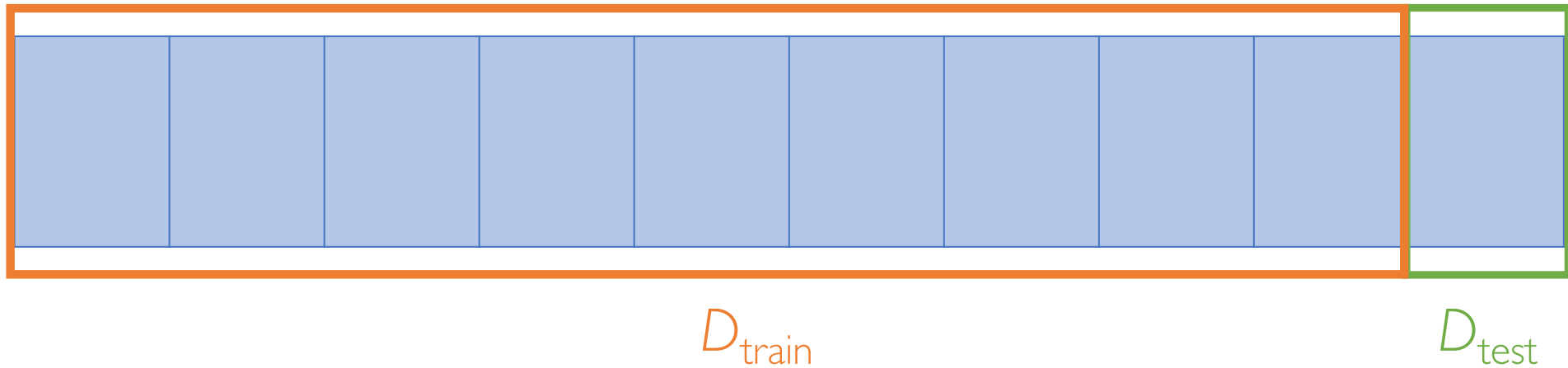
Round  $k = 2$





# K-Fold Cross Validation

Round  $k = 10$



# Model Selection/Evaluation

Several different learning models to achieve the same task



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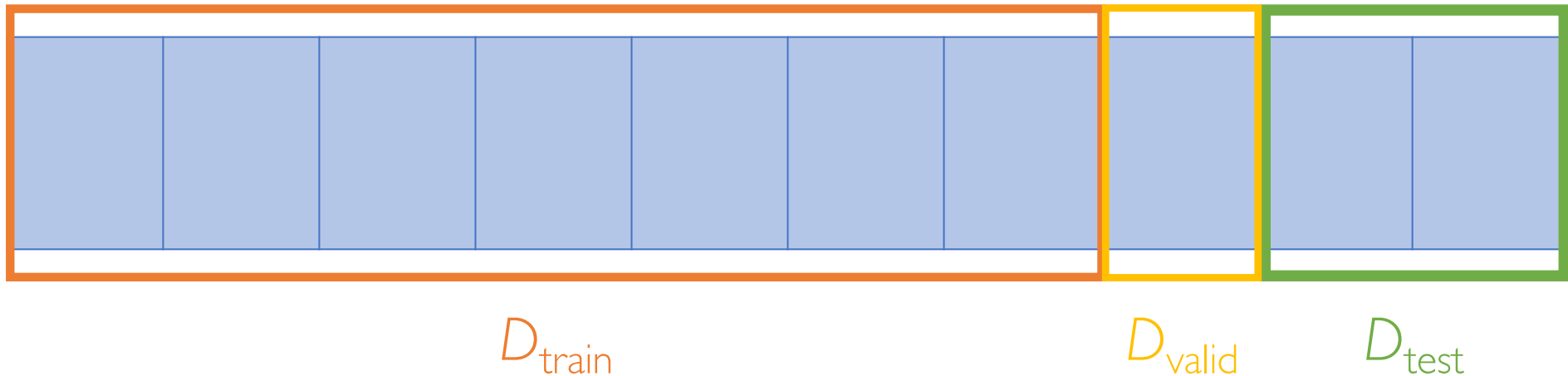
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How do we select the best model?

# Model Selection/Evaluation: Validation Set

Separate hyperparameter selection from model evaluation

$D_{\text{valid}}$  is used to validate hyperparameters



# Model Selection/Evaluation: Example

Select which value of  $k = \{2, 5, 10\}$  of a  $k$ NN gives the best performance

- 1) Train a separate model for each value of  $k$  on the training set (e.g., 70%)
- 2) Measure the error of each model on the validation set (e.g., 10%)
- 3) Select the model whose value of  $k$  gives the best performance on the validation set (e.g.,  $k = 5$ )
- 4) Re-train only this model on the training + validation set
- 5) Measure the performance on the test set (e.g., 20%)

## Note:

The strategy above can also be extended to K-fold Cross Validation

# Take-Home Message of Today

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  - Hypothesis space (assumption)
  - Loss Function (objective)
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Suggested reading: <https://homes.cs.washington.edu/~pedrod/papers/cacml2.pdf>