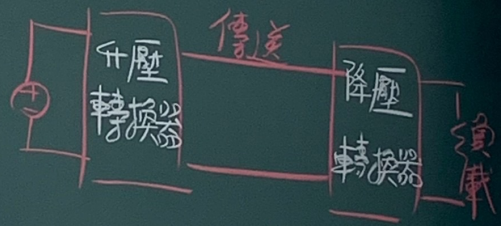
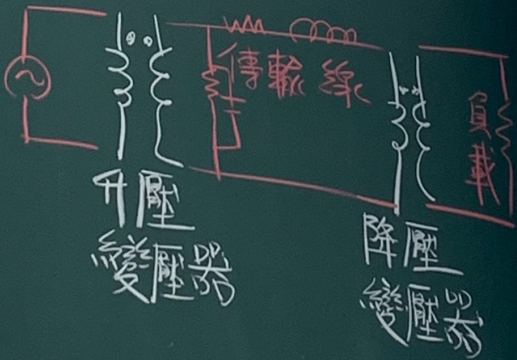


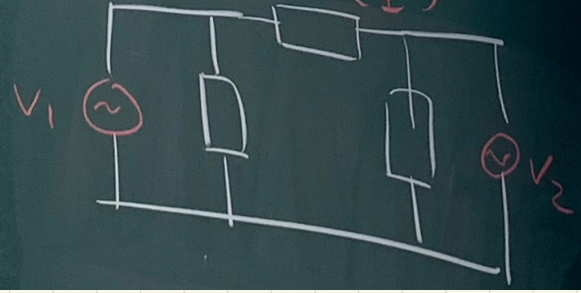
DC power system



AC power system (60Hz)



AC power system (60Hz) 近似 (留意誤差)



4.3 傳輸矩陣(Transmission Matrix)

Steady-state terminal voltage and currents.

$$V_1 = AV_2 + BI_2 ; I_1 = CV_2 + DI_2 ,$$

where $A = \cosh \gamma l$, $B = Z_c \sinh \gamma l$, $C = (1/Z_c) \sinh \gamma l$, $D = \cosh \gamma l$,

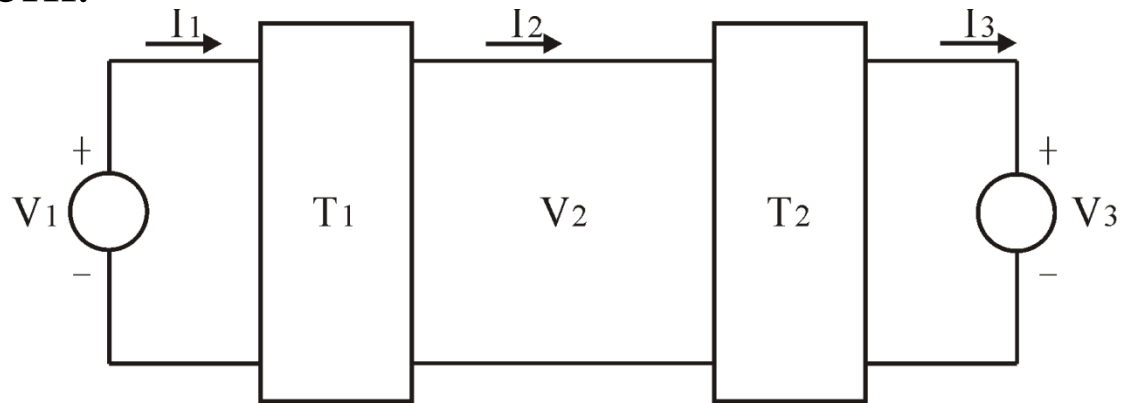
Transmission matrix (chain matrix) $T = \begin{bmatrix} A & B \\ C & D \end{bmatrix}$, $T^{-1} = \begin{bmatrix} D & -B \\ -C & A \end{bmatrix}$

$$\det T = AD - BC = (\cosh \gamma l)^2 - (\sinh \gamma l)^2 = 1$$

$$[V_1 \ I_1] = T_1 [V_2 \ I_2] = T_1 T_2 [V_3 \ I_3] = T [V_3 \ I_3]$$

That $\det T = 1$, holds in general for two-port networks composed of (linear time-invariant) resistors, capacitors, inductors, coupled inductors, and transformers. This provides a useful check of analytical or numerical work.

CH3 傳輸線 有 R, L, C , $\gamma = \sqrt{yz}$, $y = g + j\omega C$
 CH4 傳輸線模型
 $V_1 = V_2 \cosh \gamma l + Z_c I_2 \sinh \gamma l$
 $I_1 = I_2 \cosh \gamma l + \left(\frac{V_2}{Z_c}\right) \sinh \gamma l$
 $\begin{bmatrix} V_1 \\ I_1 \end{bmatrix} = \begin{bmatrix} \cosh \gamma l & Z_c \sinh \gamma l \\ \frac{\sinh \gamma l}{Z_c} & \cosh \gamma l \end{bmatrix} \begin{bmatrix} V_2 \\ I_2 \end{bmatrix} = T_1 \begin{bmatrix} V_2 \\ I_2 \end{bmatrix} = T_1 T_2 \begin{bmatrix} V_3 \\ I_3 \end{bmatrix}$



4.4 等效集總電路(Lumped-Circuit Equivalent), $\gamma = (y z)^{0.5}$

$$V_1 = AV_2 + BI_2 ; I_1 = CV_2 + DI_2 ,$$

Find a **Π equivalent circuit** that has the same A, B, C, D parameters as the transmission line. We note that a T equivalent circuit may also be derived.

$$V_1 = V_2 \cosh \gamma l + Z_c I_2 \sinh \gamma l ; I_1 = I_2 \cosh \gamma l + (V_2 / Z_c) \sinh \gamma l$$

$$V_1 = V_2 + Z' [I_2 + (Y'/2)V_2] = (1 + Z'Y'/2)V_2 + Z'I_2$$

$$I_1 = (Y'/2)V_1 + (Y'/2)V_2 + I_2 = Y'(1 + Z'Y'/4)V_2 + (1 + Z'Y'/2)I_2$$

$$A = \cosh \gamma l = 1 + Z'Y'/2 , B = Z_c \sinh \gamma l = Z' ,$$

$$C = (1/Z_c) \sinh \gamma l = Y'(1 + Z'Y'/4), D = \cosh \gamma l = 1 + Z'Y'/2 ,$$

$$Z' = Z_c \sinh \gamma l = (z/y)^{0.5} \sinh \gamma l = zl \sinh \gamma l / l(zy)^{0.5} = Z \sinh \gamma l / \gamma l = Z$$

Assume $|\gamma l| \ll 1 \Rightarrow \sinh \gamma l / \gamma l = 1 ; Z = zl$ is the total series impedance of line

$$1 + Z'Y'/2 = \cosh \gamma l \Rightarrow Y'/2 = (\cosh \gamma l - 1)/Z' = (\cosh \gamma l - 1)/(Z_c \sinh \gamma l)$$

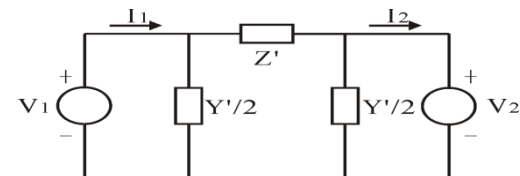
$$= (1/Z_c)(e^{\gamma l} + e^{-\gamma l} - 2)/(e^{\gamma l} - e^{-\gamma l}) = (1/Z_c)(e^{\gamma l/2} - e^{-\gamma l/2})^2 / (e^{\gamma l/2} + e^{-\gamma l/2})(e^{\gamma l/2} - e^{-\gamma l/2})$$

$$= (1/Z_c) \tanh(\gamma l/2) = (y/z)^{0.5} \tanh(\gamma l/2) = (yl/\gamma l) \tanh(\gamma l/2) = (Y/2) \tanh(\gamma l/2) / (\gamma l/2)$$

Assume $|\gamma l| \ll 1 \Rightarrow \tanh(\gamma l/2) / (\gamma l/2) = 1 ; Y = yl$ is the total line-neutral admittance of line

$$Z_c = (z/y)^{0.5} = (zl/yl)^{0.5} = (Z/Y)^{0.5}$$

$$\gamma l = (zy)^{0.5} l = (zl/yl)^{0.5} = (Z/Y)^{0.5}$$



Ex4.4 Find the Π equivalent circuit in Ex4.1 A **60-Hz** 138-kV 3 Φ transmission line is 225mile long. The distributed line parameters are $r = 0.169 \Omega/\text{mile}$, $l = 2.093 \text{ mH}/\text{mile}$, $c = 0.01427 \mu\text{F}/\text{mile}$, $g = 0$.

$$z = r + j\omega l = 0.169 + j0.789 = 0.807 \angle 77.9^\circ \Omega/\text{mile}$$

$$y = g + j\omega c = j5.38 \times 10^{-6} = 5.38 \times 10^{-6} \angle 90^\circ \text{ mho}/\text{mile}$$

$$\Rightarrow Z_c = (z/y)^{0.5} = 387.3 \angle -6.05^\circ \Omega$$

$$\Rightarrow \gamma l = 225 (y z)^{0.5} = 0.4688 \angle 83.95^\circ = 0.0494 + j0.466$$

$$2 \sinh \gamma l = e^{\gamma l} - e^{-\gamma l} = e^{0.0494} e^{j0.466} - e^{-0.0494} e^{-j0.466} = 1.051 \angle 0.466 \text{ rad} - 0.952 \angle -0.466 \text{ rad}$$

$$\sinh \gamma l = 0.452 \angle 84.4^\circ$$

$$Z' = Z_c \sinh \gamma l = 387.3 \angle -6.05^\circ \Omega \times 0.452 \angle 84.4^\circ = 175.06 \angle 78.35^\circ$$

$$Z' = Z \sinh \gamma l / \gamma l = 225 \times 0.807 \angle 77.9^\circ \times 0.452 \angle 84.4^\circ / (0.4688 \angle 83.95^\circ)$$

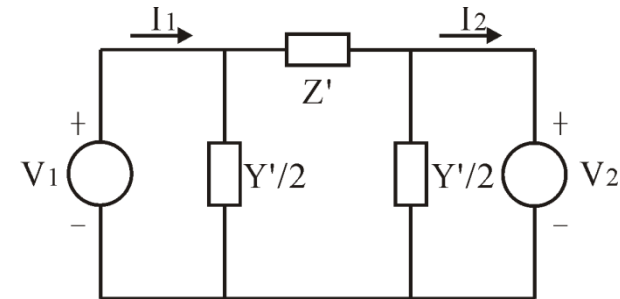
$$= 181.57 \angle 77.9^\circ \times 0.9642 \angle 0.45^\circ = 175.07 \angle 78.35^\circ$$

$$2 \cosh \gamma l = e^{\gamma l} + e^{-\gamma l} = 1.051 \angle 0.466 \text{ rad} + 0.952 \angle -0.466 \text{ rad} = 1.790 \angle 1.42^\circ$$

$$\cosh \gamma l = 0.895 \angle 1.42^\circ$$

$$Y'/2 = (\cosh \gamma l - 1)/Z' = (0.895 \angle 1.42^\circ - 1) / 175.06 \angle 78.35^\circ = 614.57 \times 10^{-6} \angle 89.8^\circ \text{ mho}$$

$$Y/2 = (yl)/2 = (225 \times 5.38 \times 10^{-6} \angle 90^\circ) / 2 = 605.25 \times 10^{-6} \angle 90^\circ \text{ mho}$$



4.5 簡化模型(Simplified Models)

Long line ($l > 150\text{mile} = 241.4\text{ km}$): Use the Π equivalent circuit model with Z' and $Y'/2$.

Medium length line ($50\text{mile} < l < 150\text{mile} = 241.4\text{ km}$): Use the Π equivalent circuit model with Z and $Y/2$ instead of Z' and $Y'/2$.

Short line ($l < 50\text{mile} = 80.5\text{ km}$): Same as the medium length line except that we neglect $Y/2$.

$$z = r + j\omega l \Rightarrow Z = zl,$$

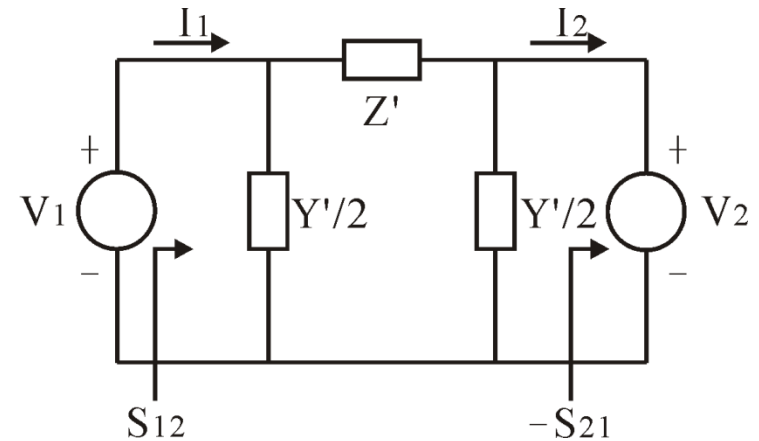
$$y = g + j\omega c \Rightarrow Y = yl,$$

$$Z' = Z_c \sinh \gamma l$$

$$Y'/2 = (\cosh \gamma l - 1)/Z'$$

$$\gamma = (yz)^{0.5}, Z_c = (z/y)^{0.5}$$

$$\sinh \gamma l = (e^{\gamma l} - e^{-\gamma l})/2, \cosh \gamma l = (e^{\gamma l} + e^{-\gamma l})/2$$



Ex 4.5 Consider the receiving-end voltage of a **lossless open-circuited** line and compare the results by use of the three models. V_1 is fixed.

Open circuited $\Rightarrow I_2 = 0$, lossless $\Rightarrow \alpha = 0$, $\gamma = j\beta$, assume $\beta = 0.002$ rad/mile

M1: Long line ($l > 150$ mile):

$$V_1 = V_2 \cosh \gamma l + Z_c I_2 \sinh \gamma l = V_2 \cosh \gamma l = V_2 (e^{\gamma l} + e^{-\gamma l})/2 = V_2 \cos \beta l$$

$$I_1 = I_2 \cosh \gamma l + (V_2 / Z_c) \sinh \gamma l = (V_2 / Z_c) \sinh \gamma l$$

M2: Medium length line: Use the Π model with Z and $Y/2$ instead of Z' and $Y'/2$.

$$\begin{aligned} V_1 &= V_2 + Z' [I_2 + (Y'/2)V_2] = (1 + Z'Y'/2)V_2 + Z'I_2 \\ &= (1 + ZY/2)V_2 = [1 + (\gamma l)^2 / 2] V_2 = [1 - (\beta l)^2 / 2] V_2 \end{aligned}$$

This is the first two terms in the Taylor series expansion of $\cos \beta l$.

M3: Short line ($l < 50$ mile = 80.5 km): Same as the medium length line ($Y/2 = 0$).

$$V_1 = V_2 + Z' [I_2 + (Y'/2)V_2] = V_2$$

This is the first term in the Taylor series expansion of $\cos \beta l$.

(1) 50 miles $\Rightarrow \beta l = 0.1$ rad,

$$\text{M1: } V_1 = 0.995004 V_2, \text{ M2: } V_1 = 0.995000 V_2, \text{ M3: } V_1 = V_2,$$

(2) 200 miles $\Rightarrow \beta l = 0.4$ rad,

$$\text{M1: } V_1 = 0.921 V_2, \text{ M2: } V_1 = 0.920 V_2, \text{ M3: } V_1 = V_2,$$

(1) 600 miles $\Rightarrow \beta l = 1.2$ rad,

$$\text{M1: } V_1 = 0.362 V_2, \text{ M2: } V_1 = 0.280 V_2 \text{ (error ?), M3: } V_1 = V_2 \text{ (inaccurate),}$$

4.6 複數功率傳輸(長程或中程線路)(Complex Power Transmission: Long or Medium Lines)

Z between voltages V_1 and V_2

$$S_{12} = V_1 I_1^* = V_1 [(V_1 - V_2)/Z]^* = |V_1|^2 / Z^* - V_1 V_2^* / Z^*$$

$$= (|V_1|^2 / |Z|) e^{j\angle Z} - (|V_1| |V_2| / |Z|) e^{j\angle Z} e^{j\theta_{12}}$$

$$S_{21} = V_2 I_2^* = V_2 [(V_2 - V_1)/Z]^* = |V_2|^2 / Z^* - V_2 V_1^* / Z^*$$

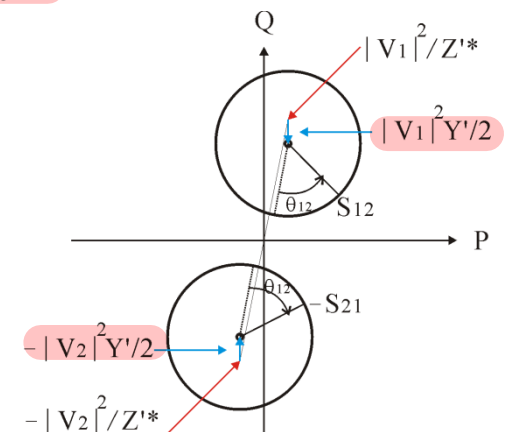
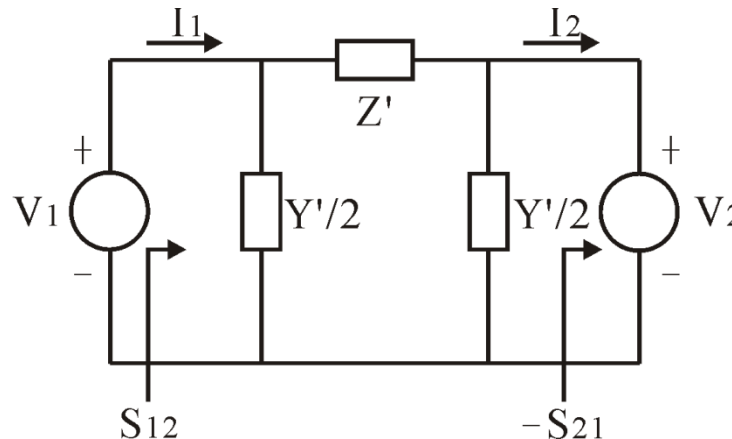
$$= (|V_2|^2 / |Z|) e^{j\angle Z} - (|V_2| |V_1| / |Z|) e^{j\angle Z} e^{-j\theta_{12}}$$

$$-S_{21} = -(|V_2|^2 / |Z|) e^{j\angle Z} + (|V_2| |V_1| / |Z|) e^{j\angle Z} e^{-j\theta_{12}}$$

Z' and $Y'/2$ between voltages V_1 and V_2

$$S_{12} = (Y'^*/2) |V_1|^2 + (|V_1|^2 / Z'^*) - (|V_1| |V_2| / Z'^*) e^{j\theta_{12}}$$

$$-S_{21} = -(Y'^*/2) |V_2|^2 - (|V_2|^2 / Z'^*) + (|V_1| |V_2| / Z'^*) e^{-j\theta_{12}}$$



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$742.7 \times 2 + 724.7 \times 4 + 600 \times 1 = 4,984.2 \text{ MW}$

桃 2,270,971

(大潭 7 部 燃氣)

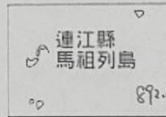
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基隆市

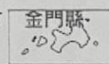
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13,403



140,325



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中 K 550×10

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1,262,673

彰化縣

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南投縣

489,148

嘉義縣

嘉義市

縣 497,691

臺南市

1,871,224

高雄縣

高雄市

臺東縣

214,599

屏東縣

809,765

核 = 951×2

(1,902 MW)

興達 燃氣 5 部

4 部 運轉

445.2×4

$= 1,780.8 \text{ MW}$

大林 燃氣 2 部

1 部 運轉

500 MW

高雄興達加大林共 6,080.8 MW

嘉義以南到屏東共 6,204,074

台中 K 力 5,500 MW

中彰投共 4,572,800

雲林麥寮 1,200 MW, 雲林人 674,622

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桃園大潭 4,984.2 MW, 桃園人 2,270,971

4.7 線路的功率處理容量(Power-Handling Capability of Lines)

Power line are limited in their ability to deliver power. The two most important limits can be understood by considering thermal effects and stability.

When current flows in conductors, there are I^2R losses and heat is generated (T increased, T is limited 100°C). This loss of power reduces transmission efficiency.

If the cable gets too hot, the insulation will begin to deteriorate and may fail in time.

With limitations on maximum current and voltage there is a corresponding limitation on the MVA that can safely be transmitted.

The maximum angle θ_{12} is 90° , for stability, the maximum angle θ_{12} is $40^\circ \sim 50^\circ$,

A lossless line with equal voltage magnitudes at each end as Ex 4.3.

$$z = r + j\omega l = j\omega l \text{ series impedance per meter}$$

$$y = g + j\omega c = j\omega c \text{ shunt admittance per meter to neutral}$$

$$Z_c = (z/y)^{0.5} = (j\omega l / j\omega c)^{0.5} = (l / c)^{0.5} = (L/C)^{0.5} ,$$

$$\gamma = (z y)^{0.5} = \alpha + j\beta = j\beta = (j\omega l j\omega c)^{0.5} = j\omega (l c)^{0.5}$$

$$\sinh \gamma l = (e^{\gamma l} - e^{-\gamma l})/2 = (e^{j\beta l} - e^{-j\beta l})/2 = j \sin \beta l$$

$$\cosh \gamma l = (e^{\gamma l} + e^{-\gamma l})/2 = (e^{j\beta l} + e^{-j\beta l})/2 = \cos \beta l$$

$$Z' = Z_c \sinh \gamma l = jZ_c \sin \beta l$$

$$Y'/2 = (\cosh \gamma l - 1)/Z' = (\text{Y/2}) \tanh(\gamma l/2)/(\gamma l/2) = (j\omega C/2) \tan(\beta l/2)/(\beta l/2)$$

$$\text{Assume } |V_1| = |V_2| , P_{\text{SIL}} = |V_1|^2 / Z_c$$

$$S_{12} = (Y'^*/2)|V_1|^2 + (|V_1|^2 / Z'^*) - (|V_1||V_2|/Z'^*) e^{j\theta_{12}}$$

$$P_{12} = - [|V_1||V_2| / (-jZ_c \sin \beta l)] (j \sin \theta_{12}) = (|V_1|^2 / Z_c) (\sin \theta_{12} / \sin \beta l)$$

$$P_{12} = P_{\text{SIL}} (\sin \theta_{12} / \sin \beta l)$$

$$-S_{21} = -(Y'^*/2)|V_2|^2 - (|V_2|^2 / Z'^*) + (|V_1||V_2|/Z'^*) e^{-j\theta_{12}}$$

Ex 4.6 Assume that $\beta = 0.002$ rad/mile and $\theta_{12} = 45^\circ$. Find P_{12}/P_{SIL} as a function of line length.

Assume $|V_1| = |V_2|$, $P_{SIL} = |V_1|^2 / Z_c$

$$S_{12} = (Y'^*/2)|V_1|^2 + (|V_1|^2 / Z'^*) - (|V_1||V_2|/Z'^*) e^{j\theta_{12}}$$

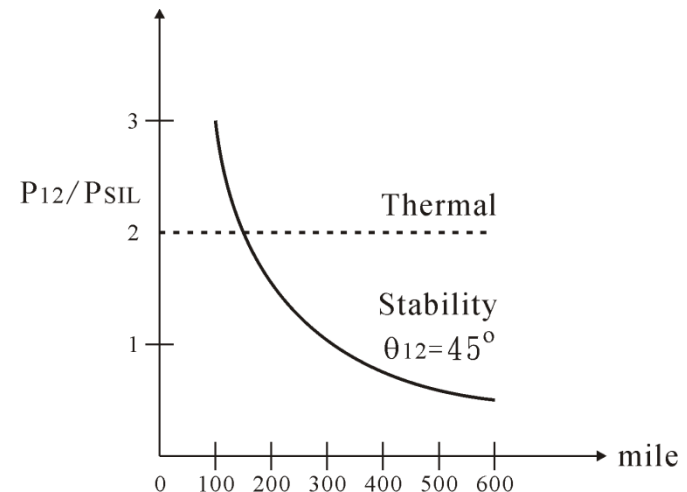
$$P_{12} = - [|V_1||V_2| / (-jZ_c \sin \beta l)] (j \sin \theta_{12}) = (|V_1|^2 / Z_c) (\sin \theta_{12} / \sin \beta l)$$

$$P_{12} = P_{SIL} (\sin \theta_{12} / \sin \beta l) \Rightarrow P_{12} / P_{SIL} = (\sin \theta_{12} / \sin \beta l)$$

$$\theta_{12} = 45^\circ, \beta l = 0.002 \text{ rad/mile} \times l = 0.1146^\circ/\text{mile} \times l$$

$$P_{12} / P_{SIL} = 0.707 / \sin (0.1146^\circ/\text{mile} \times l)$$

We see that for short lines the **thermal** limit governs, where as for long lines the **stability** limit prevails.



4.8 結論與習題(Summary)

The long line equation is frequently used.

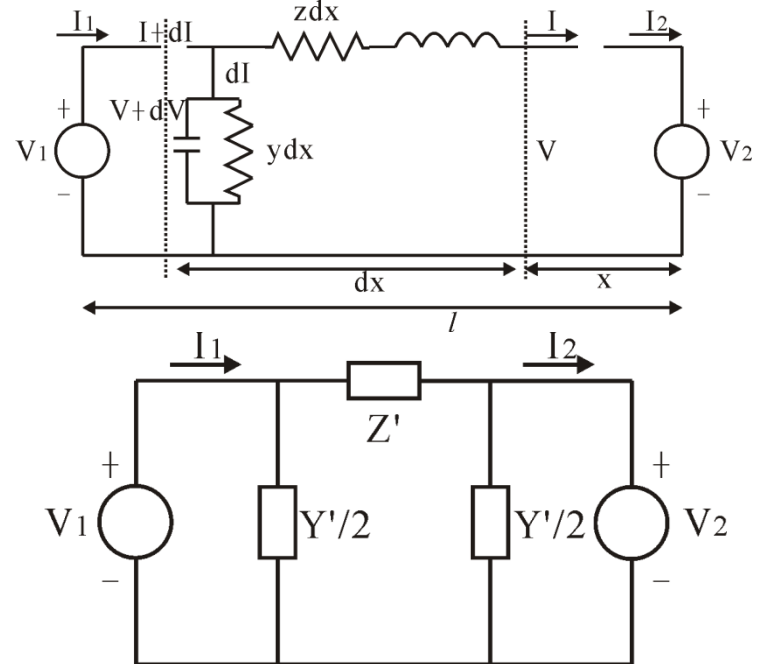
$$V_1 = V_2 \cosh \gamma l + Z_c I_2 \sinh \gamma l$$

$$I_1 = I_2 \cosh \gamma l + (V_2 / Z_c) \sinh \gamma l$$

The Π equivalent circuit

$$Z' = Z_c \sinh \gamma l$$

$$Y'/2 = (\cosh \gamma l - 1) / Z'$$



Finally, we note that **thermal** effects limit the power handling capability of short and medium length lines, whereas **stability** requirements impose the limitations on long lines.

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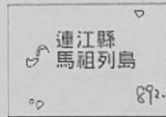
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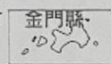
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