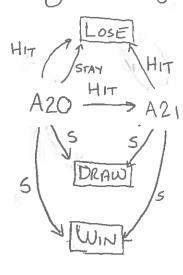
D Consider the following MDP for blackjack:



$$R_{t}(W_{IN}) = 1$$

$$R_{t}(L_{OSE}) = -1$$

$$R_{t}(D_{RAW}) = 0$$

$$R_{t}(A_{20}) = R_{t}(A_{21}) = 0$$

$$P(L_{OSE}|A_{20}, S_{TAY}) = 0.12$$

Can we still compute the expected utility of a particular policy, e.g. Tr(A20)=1+1+7
Tr(A21)=5TAY

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3) Well, not without more information. However, suppose we play several games using this policy:

(i) A20 $\xrightarrow{\text{HiT}}$ Lose (utility = -1)

(ii) AZO HIT LOSE (utility = -1)

(iii) A20 HIT A21 STAY WIN (utility = 1)

(iv) A20 HIT LOSE (utility = -1)

(v) A20 HIT A21 STAY DRAW (utility = 0)

4) The simplest strategy is to estimate the expected utility directly:

$$U^{T}(A20) = (-1)+(-1)+1+(-1)+0$$

$$= -2$$
5

=-0.4

This is just the average utility I've experienced over the 5 times I've been in state A20.

3) The main downside to this strategy (called direct utility estimation) is that it treats each state independently, e.g. U" (A20) and U" (A21) are estimated as if they have nothing to do with each other.

Throther strategy is to estimate the transition probabilities of the MDP by keeping track of how many times we experience each transition < q, o, q'>.

These counts allow us to estimate the transition probabilities in a straightforward way

$$P(Lose | A20, HiT) = count(A20 \xrightarrow{HiT} Lose)$$

$$= 3$$

$$P(A21 | A20, HiT) = count(A20 \xrightarrow{HiT} A21)$$

$$= count(A20 \xrightarrow{HiT} Lose) + count(A20 \xrightarrow{HiT} A21)$$

$$=\frac{2}{5}$$

etc.

This technique is called Adaptive Dynamic Programming (ADP).

- F) Once we know the transition probabilities, we can estimate the utilities using the standard techniques (e.g. value iteration) for filly-specified MDPs.
- Both of bese methods (direct utility estimation and ADP) require us to stream games and their results in memory. These are called offline methods.

Can we play a game, update our utilities online, and then forget about the game (i.e. don't store the results, except via our updated utilities)?

9 Consider the task of computing the mean of a sequence of numbers:
15, 3, 10, 4, 3

Everybordy probably knows the offline method:

mean = 15 + 3 + 12 + 2 + 3

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10 But there's also a convenient online method:

conic	next num xr	internear my
1	15	15
2	3	$m_1 + \frac{1}{2} \cdot (x_2 - m_1) = 9$
3	12	$m_z + \frac{1}{3}(x_3 - m_2) = 10$
4	2	$m_3 + \frac{1}{4}(x_4 - m_3) = 8$
5	3	$m_4 + \frac{1}{5}(x_5 - m_4) = 7$

IIIn pseudocode:

$$m=0$$
for $n=1$ to N :
$$m=m+1.(x_n-m)$$

Note that we only need to ever have 3 numbers in memory at one time: m, n, and xn.

This is true regardless of how many numbers we are averaging.

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Now consider applying this to compute expected utility of a state, given a policy of. As we play the game according to our policy, we get a sequence of utilities, e.g.

A21 STAY WIN (utility = U"(WIN)=1)

A21 STAY WIN (utility = U"(WIN)=1)

A21 STAY DRAW (utility = U"(DRAW)=0)

The expected utility of state A21 is the average of these utilities as our number of observations goes to infinity.

So we can compute this using our online technique: $U^{\pi}(q) = 0$ for n = 1 to ∞ : $U^{\pi}(q) = U^{\pi}(q) + \frac{1}{n} \cdot \left(\left[R(q) + \delta U^{\pi}(q') \right] - U^{\pi}(q') \right)$

(4) Turns at this works even when we compute the expected utility of each state simultaneously: TOLEARNING (Q, Z, R, T): set U"(g)=0, ng=1 for all gEQ observe transition q = q'. update U"(g) = U"(g) + 1 ([R(g) + VU"(g')] - U"(g)) n += 1 if we keep taking observations forever, then this can be replaced with $\sqrt[n]{x} \propto (n_q) = O(\frac{1}{n_0})$ and it will converge to the mean as. no > 00

This is called temporal difference (TD) learning.