Math 107H Section 002

Some problems to set up (and evaluate) volumes/arclengths/surface areas

For each of the functions defined on the indicated intervals, set up but do not evaluate! the integrals which will compute:

- (a) the volume when the region between the graph and the x-axis is revolved around the x-axis (by slices)
- (b) the volume when the region between the graph and the x-axis is revolved around the line y = -2 (by slices)
- (c) the volume when the region between the graph and the x-axis is revolved around the y-axis (by shells)
- (d) the arclength of the graph
- (e) the area of the surface obtained by revolving the graph around the x-axis

A1.
$$y = f(x) = 2x - x^2$$
 from $x = 0$ to $x = 2$

A2.
$$y = f(x) = \ln x$$
 from $x = 1$ to $x = 3$

A3.
$$y = f(x) = \cos x$$
 from $x = \pi/2$ to $x = 3\pi/2$

A4.
$$y = f(x) = \sqrt{2x - x^2}$$
 from $x = 0$ to $x = 2$

A5.
$$y = f(x) = e^x$$
 from $x = 0$ to $x = 3$

A6.
$$y = f(x) = \frac{1}{x}$$
 for $x = 1$ to $x = 4$

Compute the integrals you have created!, for the problems

$$A1(a)$$
, $A1(c)$, $A1(d)$

$$A6(a)$$
, $A6(c)$, $A6(e)$

Write out and hand in your setup and evaluation for A2(c) , A3(e), A5(b), and A5(e)