

## Math 208H, Section 1

### Practice problems for Exam 2

9. Find the local extrema of the function

$$f(x, y) = 2x^4 - 2xy + y^2 ,$$

and determine, for each, if it is a local max. local min, or saddle point.

6. Find the point(s) on the ellipse  $g(x, y) = x^2 + 3y^2 = 4$

where the function  $f(x, y) = x - 3y + 4$  achieves its maximum value.

1. Evaluate the iterated integral  $\int_0^2 \int_x^2 x^2(y^4 + 1)^{1/3} dy dx$

by rewriting the integral to reverse the order of integration. (Note: the integral *cannot* be evaluated in the order given....)

4. Find the integral of the function  $f(x, y, z) = x + y + z$

over the region lying between the graph of  $z = x^2 + y^2 - 4$  and the  $x$ - $y$  plane.

3. Find the integral of the function  $f(x, y) = xy^2$  over the region lying in the first quadrant of the  $x$ - $y$  plane and lying inside of the circle  $x^2 + y^2 = 9$ .

5. Find the integral of the function  $f(x, y) = 6x + y^2$  over the region in the  $x$ - $y$  plane between the  $x$ -axis and the lines  $y = x$  and  $y = 6 - 2x$ .

4. Find the integral of the function  $f(x, y) = xy^2$  over the region in the plane lying between the graphs of  $a(x) = 2x$  and  $b(x) = 3 - x^2$ .

5. Evaluate the following double integrals:

$$(a): \int_0^1 \int_1^2 x^2 y - y^2 x dx dy \quad (b): \int_0^1 \int_{\sqrt{x}}^1 x\sqrt{y} dy dx$$

1. Find the integral of the function  $f(x, y) = x$  over the region  $R$  lying between the graphs of the curves

$$y = x - x^2 \text{ and } y = x - 1.$$

5. Use Lagrange multipliers to find the maximum value of the function  $f(x, y) = xy$  subject to the constraint  $g(x, y) = x^2 + 4y^2 - 1 = 0$ .

7. Find the area of the region  $S$  bounded by one loop of the curve described by

$$r = \sin(3\theta)$$

in polar coordinates. (Hint: to determine the limits of integration, when is  $r = 0$ ?)

4. A particle is moving through 3-space along the parametrized curve  $\vec{r}(t) = (\cos t, \sin t, t^{3/2})$ . Find:

(a) the velocity of the particle at time  $t$ ,

(b) the acceleration of the particle at time  $t$ , and

(c) the length of the curve traced out by the particle between  $t = 0$  and  $t = 2$ .