Old First solutions

 $\int \frac{2x+3}{x^3+x^2-2} dx = \int \frac{1}{x-1} - \frac{x+1}{x^3+2x+2} dx = \ln|x-1| - \int \frac{x+1}{(x+1)^2+1} dx$ = ln(x-1) - \(\frac{u}{a^2+1} \du \| \(\text{LEXT} \) = \(\lambda \lambda \) \(\text{LEXT} \) = ln|x-1|-\$\ln|v=u+1|uex+1 = h/x-1/- h/(x+13+1/+c) 2. f(x) = g(x): $2x-1 = x^4 + x-1$, $x^4 - x = 0 = (x^3 - 1)x$ =) x=0 or x3-1=0 -) x3=1 -) x=1 an [0,1], $2x-1 \ge x^{4}+x-1$ (check $x=\pm : 0=1-1 > \frac{1}{16} + \frac{1}{2}-1$) Area = $\int_0^1 (2x^1) - (x^0 + x - 1) dx = \int_0^1 - x^0 + x dx$ $= \frac{x^2 - \frac{x^2}{5}}{|s|^2} = (\frac{1}{5} - \frac{1}{5}) - (1 - 0) = \frac{1}{5} - \frac{1}{5} = \frac{3}{10} + \frac{3}{10}$ $x^3+7x-22=0:(x-2)(x^2+2x+11)=0$ X=2. By shells! (width) (height)

-2

Volume = $\int_{0}^{2} 2\pi(x-(-2))(x^3+7x-22) dx$ $= \int_{0}^{2} 2\pi(x+2)(x^{3}+7x-22) dx = 2\pi \int_{0}^{2} x^{4}+2x^{5}+7x^{2}+14x-22x-44 dx$ $=2\pi \left(\frac{x^{4}+2x^{3}+7x^{2}-8x-44}{5}\right)\left(\frac{x^{5}+\frac{x^{4}}{2}+\frac{7x^{3}}{3}-4x^{2}-44x}{5}\right)\left(\frac{x^{5}+\frac{x^{4}}{2}+\frac{7x^{3}}{3}-4x^{2}-44x}{5}\right)\left(\frac{x^{5}+\frac{x^{4}}{2}+\frac{7x^{3}}{3}-4x^{2}-44x}{5}\right)\left(\frac{x^{5}+\frac{x^{4}}{2}+\frac{7x^{3}}{3}-4x^{2}-44x}{5}\right)\left(\frac{x^{5}+\frac{x^{4}}{2}+\frac{7x^{3}}{3}-4x^{2}-44x}{5}\right)\left(\frac{x^{5}+\frac{x^{4}}{2}+\frac{7x^{3}}{3}-4x^{2}-44x}{5}\right)\left(\frac{x^{5}+\frac{x^{4}}{2}+\frac{7x^{3}}{3}-4x^{2}-44x}{5}\right)\left(\frac{x^{5}+\frac{x^{4}}{2}+\frac{7x^{3}}{3}-4x^{2}-44x}{5}\right)\left(\frac{x^{5}+\frac{x^{4}}{2}+\frac{7x^{3}}{3}-4x^{2}-44x}{5}\right)\left(\frac{x^{5}+\frac{x^{4}}{2}+\frac{7x^{3}}{3}-4x^{2}-44x}{5}\right)\left(\frac{x^{5}+\frac{x^{4}}{2}+\frac{x^{4}}{3}-4x^{2}-44x}{5}\right)\left(\frac{x^{5}+\frac{x^{4}}{2}+\frac{x^{4}}{3}-4x^{2}-44x}{5}\right)\left(\frac{x^{5}+\frac{x^{4}}{2}+\frac{x^{4}}{3}-4x^{2}-44x}{5}\right)\left(\frac{x^{5}+\frac{x^{4}}{2}+\frac{x^{4}}{3}-4x^{2}-44x}{5}\right)\left(\frac{x^{5}+\frac{x^{4}}{2}+\frac{x^{4}}{3}-4x^{2}-4x}{5}\right)\left(\frac{x^{5}+\frac{x^{4}}{2}+\frac{x^{4}}{3}-4x^{2}-4x}{5}\right)\left(\frac{x^{5}+\frac{x^{4}}{2}+\frac{x^{4}}{3}-4x}{5}\right)\left(\frac{x^{5}+\frac{x^{4}}{2}+\frac{x^{4}}{3}-4x}{5}\right)\left(\frac{x^{5}+\frac{x^{4}}{2}+\frac{x^{4}}{3}-4x}{5}\right)\left(\frac{x^{5}+\frac{x^{4}}{2}+\frac{x^{4}}{3}-4x}{5}\right)\left(\frac{x^{5}+\frac{x^{4}}{2}+\frac{x^{4}}{3}-4x}{5}\right)\left(\frac{x^{5}+\frac{x^{4}}{2}+\frac{x^{4}}{3}-4x}{5}\right)\left(\frac{x^{5}+\frac{x^{4}}{2}+\frac{x^{4}}{3}-\frac{x^{4}}{2}+\frac{x^{4}}{3}-\frac{x^{4}}{2}\right)\left(\frac{x^{5}+\frac{x^{4}}{2}+\frac{x^{4}}{3}-\frac{x^{4}}{2}+\frac{x^{4}}{3}-\frac{x^{4}}{2}+\frac{x^{4}}{3}-\frac{x^{4}}{2}\right)\left(\frac{x^{5}+\frac{x^{4}}{2}+\frac{x^{4}}{3}-\frac{x^{4}}{2}+\frac{x^{4}}{2}+\frac{x^{4}}{3}-\frac{x^{4}}{2}+\frac{x^{4}}{2}+\frac{x^{4}}{2}+\frac{x^{4}}{2}+\frac{x^{4}}{2}+\frac{x^{4}}{2}+\frac{x^{4}}{2}+\frac{x^{4}}{2}+\frac{x^{4}}{2}+\frac{x^{4}}{2}+\frac{x^{4}}{2}+\frac{x^{4}}{2}+\frac{x^{4}}{2}+\frac$ $= 2\pi \left(\left(\frac{2^{5}}{5} + \frac{24}{2} + \frac{7.8}{3} - 4.4 - 44.2 \right) - (0) \right)$

Area = A(x) = T(x2 = T(144-y2) Je x2+y2=122 work = (-y) fr (144-y) dy) $= 30\pi \left(\frac{0}{-144y + y^3} \right) = 300\pi \left(-72y^3 + \frac{y^4}{4} \right) \Big|_{12}$ $=300\pi\left((0+0)-\left(-72(-12)^{2}+\frac{(-12)^{4}}{4}\right)\right)$ = 30T (72.12 × 12.12) = 300T.122 (72-36) 5 (a) $l_{x} = \frac{x^{2} - 3x^{3} + 9}{4x^{2} - 6x + 1} = l_{x} = l_{x}$ (b) lu (x3+1) = 2 lul = lu x lu(x3+1) - 2x lu(x+1) =hx(In(x3+1)-2h(x+1)) = hxxxx(1x+1) 7 An In(1x+1x) $= \ln \times \ln \left(\frac{x^{2+1}}{(x+1)^2} \right) = \ln \times \ln \left(\frac{1+(x)^2}{(1+(x)^2)} \right) = \lim_{x \to \infty} \ln \left(\frac{1+(x)^2}{(1+(x)^2)} \right)$ $= h + h \left(\frac{1+h^2}{(1+h)^2}\right) = f(b), f(x) = h \left(\frac{1+x^2}{1+x^2}\right)$ Bh: $F(x) = \left(\frac{1}{1+x^2}\right)\left(\frac{1+x^2(2x)-(1+x^2)(2(1+x))}{(1+x)^2}\right)$; at x=0, $f'(0) = \frac{1}{(1)} \left(\frac{(1)(0) - (1)(2)}{1^2} \right) = -2$. Since $L = e^2$.

6-1:
$$\frac{1}{1} \frac{(n+1)^{1/2}}{n^2} = \frac{1}{1} \frac$$

$$f''(x) = \frac{5}{2} \left(\frac{3}{4} (2x)^{\frac{1}{2}} (2x) (4x) + \frac{3}{8} (x) (x^{2} - 5)^{\frac{1}{2}} \right) + 2(\frac{3}{2}) (x^{2} - 5)^{\frac{1}{2}} (2x)$$

$$f''(x) = \frac{5}{2} \left(\frac{3}{2} \left(\frac{1}{2} (4x)^{\frac{1}{2}} (6x) (4x^{2} + 4x^{2}) + \frac{3}{2} (4x) (4x)^{\frac{1}{2}} \right) + 3(4x)^{\frac{1}{2}} (6x)$$

$$= \frac{5}{2} \left(\frac{3}{2} \left(\frac{1}{2} (2x^{2} + 4x^{2}) + 36 \right) = \frac{5}{2} \left(\frac{3}{2} (3x^{2} + 36) \right) = \frac{5}{2} (432) = 1080$$

$$= \frac{32}{32} + 120 (x - 3) + 155 (x - 3)^{\frac{3}{2}} + \frac{180}{6} (x - 3)^{\frac{3}{2}}$$

$$= \frac{32}{32} + 120 (x - 3) + 155 (x - 3)^{\frac{3}{2}} + 180 (x - 3)^{\frac{3}{2}}$$

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$$= \frac{3}{12} + 120 (x - 3)^{\frac{3}{2}} + 165 (x -$$

6. (15 pts.) Find the area lying between the polar curves r=4 and $r=\frac{2}{\sin(\theta)}$ (see figure).

$$y = \frac{3}{\sqrt{3}} \quad \text{sid} = \frac{3}{4} = \frac{1}{2}$$

$$\partial = \overline{A}, \ \overline{A} - \overline{A} = \overline{A}$$

Anea =
$$\int_{6}^{15} \frac{1}{2}(4)^{2} - \frac{1}{2}(\frac{2}{500})^{2} d0 = \int_{6}^{6} 8 - \frac{2}{500} d0$$

$$= \int_{\frac{\pi}{6}}^{\frac{\pi}{6}} 8 - 2 \cos^2 \theta \, d\theta = 8\theta - 2(-\cot \theta) \Big|_{\frac{\pi}{6}}^{\frac{\pi}{6}}$$

$$=8\theta+2\cot\theta\Big|_{\overline{A}}^{\overline{ST}}=\left(8\frac{\overline{ST}}{6}+2\cot(\frac{\overline{ST}}{6})\right)-\left(8\frac{\overline{T}}{6}\right)+2\cot(\frac{\overline{T}}{6})$$

$$= \left(\frac{207}{3} + 2(-\sqrt{3})\right) - \left(\frac{4\pi}{3} + 2(\sqrt{3})\right)$$

$$= \frac{167}{3} - 4\sqrt{3}$$

$$= \frac{16\pi}{3} - 4\sqrt{3}$$

21:
$$\left((2x3)^{\frac{1}{2}} \frac{1}{4x} \right) \left| \frac{1}{4x^{2}} \frac{1}{4x} \right| = \left(\frac{1}{4x} \frac{1}{2} \frac{1}{4x} \right) \left| \frac{1}{4x^{2}} \frac{1}{4x} \right| = \left(\frac{1}{4x^{2}} \frac{1}{4x} \right) \left| \frac{1}{4x^{2}} \frac{1}{4x^{2}} \right| = \left(\frac{1}{4x^{2}} \frac{1}{4x^{2}} \frac{1}{4x^{2}} \right) \left| \frac{1}{4x^{2}} \frac{1}{4x^{2}} \frac{1}{4x^{2}} \right| = \left(\frac{1}{4x^{2}} \frac{1}$$

by the Ratio Test, I an diverges-2-8(b) = (4) 1/241 = 5(4) 1/20 | by=full for f(x)=x+1 and $f(x)=\frac{x(x^2+1)^2-x(2x)}{(x^2+1)^2}=\frac{1-x^2}{(x^2+1)^2}<0$ (for x>1) Efic Jiso as by is decrease, and The moting sense test, E Girly converses. 2-9 60= I (x+1) = I an(x+1) for an=3"1/2" an = 3 n2 = 1 (2) = 1 = 3 (2) = 3 = 6 dius

(2) = 3 n+1 (2) = 3 (2) = 3 = 6 dius

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(5) = 6 dius

(6) = 6 dius

(7) = 6 dius

(7) = 6 dius

(8) = 6 dius when x+1=3, $dx=\sum_{3}^{3}n^{2}=\sum_{m=2}^{1}$ which converges (p-senes) when (x=2) when (x=2) which canverges (cabolitely.) (x=4)(x) converges for -45x52. 2-10! $f(x) = x \in X$ $F_{S}(x)$ continued at $\alpha = 1$: $f(x) = e^{-x} - xe^{x}$, $f'(x) = -e^{x} - (e^{x} - xe^{x}) = 2xe^{x} - 7e^{-x}$ $f''(x) = e^{-x} - xe^{x} + 2e^{-x} = 3e^{x} - xe^{-x}$ s f(ι)= |·e'=e' , f(ι)= e'- |·e'=0 p'(ι)=(μe'-2e'=-e') f"(1) = 3€ '-(1)e+ = 2€ , 80

$$P_3(x) = f(0) + f(0)(x_1) + \frac{f'(1)}{2}(x_1)^2 + \frac{f''(1)}{3!}(x_1)^3$$

$$= e' + o(x_1) + \frac{e}{2}(x_1)^2 + \frac{2e'(x_1)^3}{6}$$

$$= e' + \frac{1}{2}e'(x_1)^2 + \frac{1}{3}e'(x_1)^3.$$