Homework 7: Lectures 13 & 14

CS 440: Programming Languages and Translators, Spring 2020

Due Mon Mar 16, 11:59 pm Fri Mar 13, 11:59 pm

3/8 p.1, 3/10, p.2, 3/12 p.1

What to submit

There's no programming assignment, so just submit your written work. Remember the new requirements: If you work alone, please say so in your submission. If you work in a group but aren't the person submitting the solution, then create a short file with the names of everyone in your group (including yourself), and submit that to Blackboard (in the HW 7 folder). These new requirements will make it easier for us to detect if someone forgot to put names down on the submission or didn't do the homework.

Problems [50 pts]: Lectures 13 & 14: LL(1) Parsing

- 1. [14 points] Below is a grammar for expressions with function calls and its *Predict* table for it. It uses x as a generic identifier name.
 - a. [7 points] Write out all the steps of a leftmost derivation of $[3/8] \times (\times \times \times, \times)$. If you want to abbreviate *Ttail*, *Ftail*, and *Atail* to something like *Tt*, *Ft*, and *At*, go ahead; just say you're doing that before you start.
 - b. [7 points] Write a trace of how the LL(1) parsing algorithm works on the input from part (a). (See Example 1 of Lecture 13 for an idea of the format to use.)

Rules

$ \begin{array}{cccc} 1 & S \rightarrow E \$ \\ 2 & E \rightarrow T T t a i l \\ 3 & T t a i l \rightarrow + T T t a i l \\ 4 & T t a i l \rightarrow \varepsilon \\ 5 & T \rightarrow F F t a i l \\ 6 & F t a i l \rightarrow * F F t a i l \\ 7 & F t a i l \rightarrow \varepsilon \\ 8 & F \rightarrow \times P A r g s \\ 9 & F \rightarrow (E) \\ 10 & P A r g s \rightarrow (A r g s) \\ 11 & P A r g s \rightarrow \varepsilon \\ 12 & A r g s \rightarrow \varepsilon \\ 14 & A t a i l \rightarrow , E A t a i l \end{array} $	Rule #	Rule
$3 Ttail \rightarrow + T Ttail$ $4 Ttail \rightarrow \varepsilon$ $5 T \rightarrow F Ftail$ $6 Ftail \rightarrow * F Ftail$ $7 Ftail \rightarrow \varepsilon$ $8 F \rightarrow \times PArgs$ $9 F \rightarrow (E)$ $10 PArgs \rightarrow (Args)$ $11 PArgs \rightarrow \varepsilon$ $12 Args \rightarrow E Atail$ $13 Args \rightarrow \varepsilon$	1	$S \to E $ \$
$4 \qquad Ttail \rightarrow \varepsilon$ $5 \qquad T \rightarrow F F tail$ $6 \qquad F tail \rightarrow \varepsilon$ $8 \qquad F \rightarrow x P A r g s$ $9 \qquad F \rightarrow (E)$ $10 \qquad P A r g s \rightarrow (A r g s)$ $11 \qquad P A r g s \rightarrow \varepsilon$ $12 \qquad A r g s \rightarrow \varepsilon A tail$ $13 \qquad A r g s \rightarrow \varepsilon$	2	$E \rightarrow T T tail$
5 $T \rightarrow F F t a i l$ 6 $F t a i l \rightarrow * F F t a i l$ 7 $F t a i l \rightarrow \varepsilon$ 8 $F \rightarrow * P A r g s$ 9 $F \rightarrow (E)$ 10 $P A r g s \rightarrow (A r g s)$ 11 $P A r g s \rightarrow \varepsilon$ 12 $A r g s \rightarrow \varepsilon$ 13 $A r g s \rightarrow \varepsilon$	3	$Ttail \rightarrow + T Ttail$
6 Ftail $\rightarrow * F$ Ftail 7 Ftail $\rightarrow \varepsilon$ 8 F $\rightarrow \times$ PArgs 9 F \rightarrow (E) 10 PArgs \rightarrow (Args) 11 PArgs $\rightarrow \varepsilon$ 12 Args $\rightarrow \varepsilon$ Atail 13 Args $\rightarrow \varepsilon$	4	$Ttail \rightarrow \varepsilon$
7 Ftail $\rightarrow \varepsilon$ 8 $F \rightarrow x PArgs$ 9 $F \rightarrow (E)$ 10 $PArgs \rightarrow (Args)$ 11 $PArgs \rightarrow \varepsilon$ 12 $Args \rightarrow E Atail$ 13 $Args \rightarrow \varepsilon$	5	$T \rightarrow F F tail$
8 $F \rightarrow x PArgs$ 9 $F \rightarrow (E)$ 10 $PArgs \rightarrow (Args)$ 11 $PArgs \rightarrow \varepsilon$ 12 $Args \rightarrow E Atail$ 13 $Args \rightarrow \varepsilon$	6	Ftail → * F Ftail
9 $F \rightarrow (E)$ 10 $PArgs \rightarrow (Args)$ 11 $PArgs \rightarrow \varepsilon$ 12 $Args \rightarrow E Atail$ 13 $Args \rightarrow \varepsilon$	7	$Ftail \rightarrow \varepsilon$
$ \begin{array}{ccc} 10 & PArgs \rightarrow (Args) \\ 11 & PArgs \rightarrow \varepsilon \\ 12 & Args \rightarrow EAtail \\ 13 & Args \rightarrow \varepsilon \end{array} $	8	$F \rightarrow x PArgs$
$ \begin{array}{ccc} 11 & PArgs \rightarrow \varepsilon \\ 12 & Args \rightarrow E Atail \\ 13 & Args \rightarrow \varepsilon \end{array} $	9	$F \rightarrow (E)$
$\begin{array}{ccc} 12 & Args \rightarrow E Atail \\ 13 & Args \rightarrow \varepsilon \end{array}$	10	$PArgs \rightarrow (Args)$
13 $Args \rightarrow \varepsilon$	11	$PArgs \rightarrow \varepsilon$
8	12	$Args \rightarrow E Atail$
14 $Atail \rightarrow , EAtail$	13	$Args \rightarrow \varepsilon$
	14	Atail → , E Atail
15 Atail $\rightarrow \varepsilon$	15	$Atail \rightarrow \varepsilon$

 $Predict(X, \mathbf{x})$

NonT	х	*	+	(\$,)
S	1			1			
E	2			2			
Ttail			3		4	4	4
T	5			5			
Ftail		6	7		7	7	7
F	8			9			
PArgs		11	11	10	11	11	11
Args	12			12			13
Atail						14	15

[3/12] Repaired Ftail row

- 2. [36 points] Study the grammar below.
 - a. [8 points] Write out the *First* set for the grammar.
 - b. [8 points] Write out the *Follow* set for the grammar.
 - c. [8 points] Write out the *Predict* table for the grammar. (You don't have to include your reasoning but if you do it might be worth partial credit.) You should find that the grammar is LL(1).
 - d. [12 points] Write out a trace of the LL(1) parsing algorithm for the input [3/8] s u v r s p s

(was uuvvsrrspstt)

Rules

Rule #	Rule
0	$S' \to S \$ [3/8]
1	$S \rightarrow P S [3/8] \neq$
2	$S \rightarrow \varepsilon [3/10] s$
3	$P \rightarrow p$
4	$P \rightarrow Q R s P$
5	$R \to r R$
6	$R \to \varepsilon$
7	$Q \rightarrow u Q v$
8	$Q \rightarrow \varepsilon$