

Task 1.1

$$i = 0; \text{while}(i < \text{size}(a))\{x = x + a[i]; i = i + 1\}$$
Task 2.1

- (a) $\langle s, n = 5 \rangle$
- $\rightarrow \langle b; s, n = 5 \rangle$
 - $\rightarrow \langle n = 3 * n + 1; s, n = 5 \rangle$
 - $\rightarrow \langle s, n = 16 \rangle$
 - $\rightarrow \langle b; s, n = 16 \rangle$
 - $\rightarrow \langle n = n/2; s, n = 16 \rangle$
 - $\rightarrow \langle s, n = 8 \rangle$
 - $\rightarrow \langle b; s, n = 8 \rangle$
 - $\rightarrow \langle n = n/2; s, n = 8 \rangle$
 - $\rightarrow \langle s, n = 4 \rangle$
 - $\rightarrow \langle b; s, n = 4 \rangle$
 - $\rightarrow \langle n = n/2; s, n = 4 \rangle$
 - $\rightarrow \langle s, n = 2 \rangle$
 - $\rightarrow \langle b; s, n = 2 \rangle$
 - $\rightarrow \langle n = n/2; s, n = 2 \rangle$
 - $\rightarrow \langle s, n = 1 \rangle$
 - $\rightarrow \langle \text{skip}, n = 1 \rangle$

- (b) $M(s, \sigma) = \{\{n = 1\}\}$

Task 2.2

- (a) $M(s, \sigma) = \{\perp_d\}$
- (b) $M(s, \sigma) = \{\{n = 0\}\}$
- (c) $M(s, \sigma) = \{\{n = -1\}\}$
- (d) $M(s, \sigma) = M(y := a[x], \sigma) = \{\{x = 1, a = [0, 3, 2, 1], y = 3\}\}$
- (e) $M(s, \sigma) = M(z := 0, \sigma) = \{\{x = -1, a = [0, 3, 2, 1], z = 0\}\}$
- (f) $M(s, \sigma) = M(y := a[x], \{x = 5, a = [0, 3, 2, 1], z = 0\}) = \{\perp_e\}$

Task 3.1

- (a) **Unsatisfied.** Post-condition is false, as i becomes 0.
- (b) **Satisfied.** Pre-condition and post-condition passes. $i = 0 \wedge i \geq 0$ and $x = 6 \wedge x \geq 1$.
- (c) **Satisfied.** Same reason as above. Program doesn't terminate and errors.
- (d) **Satisfied.** Pre-condition is false thus, the triple is satisfied.
- (e) **Satisfied.** Same reason as above.
- (f) **Unsatisfied.** Post-condition is false, as $x = 0$.
- (g) **Unsatisfied.** Post-condition is false, since i is updated throughout the program. At the end, $i = 0$, $x = 6$, and thus, $x \neq 0!$ or $x \neq 1$.
- (h) **Satisfied.** Fixes the previous problem by saving i in another variable, k . Precondition and post-condition passes. At the end, $i = 0 \wedge x = 6 \wedge k = 3$ and thus, $x = k!$.

Task 3.2

- (a) Valid. If $y = 0$ then causes an error which is fine for partial correctness. For all other states, they terminate in a state satisfying the post-condition.
- (b) Not valid since with $y = 0$ leads to runtime error, $x/0$. Fixed: $[x \geq 0 \wedge y > 0]z := x/y[z \geq 0]$
- (c) Valid
- (d) Not valid, since we don't know the contents of array, a . They can be negative which makes the post condition false. So, I changed the program and to make it use the absolute value instead. Fixed: $\{i \geq 0 \wedge i < |a|\}x := |a[i]| \{x \geq 0\}$

Task 3.3

Since $r := r * (-2)$, we need to make n be even so that it ends on a positive and passes the post-condition.
 $[r = 1 \wedge \exists k \in \mathbb{Z}. n = 2 * k]m := n; \text{ while } n \neq 0 \{r := r * (-2); n := n - 1\} [r = 2^m]$

Task 4.1

I spent about 3 hours on this.