factors and tables III in R

Factors are data type in R that resembles that of nominal (categorical) variables in statistics. Factors are nonnumeric in nature, even if coded to numerical values in practice. Factors are viewed in R as vectors with some additional information attached; the extra information being a record of distinct values in a vector, referred to as *levels*. The illustration below displays the results of a factor coercion:

```
1 > x <- c(5,12,13,12)

2 > xf <- factor(x)

3 > xf

4 [1] 5 12 13 12

5 Levels: 5 12 13
```

The *levels* in the above illustration represent the distinct values in vector **xf—5**, **12**, **13**.

In additional to the behavior in the above illustration, the **length()** of a factor is still represented as the length of the data, opposed to a count of levels, etc.

```
1 > length(xf)
2 [1] 4
```

Anticipated levels can be added into the factor's construction. For example, the current data represents 3 separate levels (categories, labels, classes, etc.) and a fourth is anticipated to exist in a new dataset:

```
#four-element vector x
   > X
   [1] 5 12 13 12
   > xf
                                                 #factor xf with 3 levels (5, 12, 13)
   [1] 5 12 13 12
   Levels: 5 12 13
   > xff <- factor(x, levels = c(5,12,13,88)) #factor xf with 4 levels (5, 12, 13, 88)</pre>
   > xff
  [1] 5 12 13 12
11 Levels: 5 12 13 88
12
                                                 #example assignment of additional factor
13 > xff[2] < 88
  > xff
14
   [1] 5 88 13 12
  Levels: 5 12 13 88
```

Conversely, undefined levels within a factor cannot be added if the level within the factor does not exist:

```
1 > xff[2] <- 28
2 Warning message:
3 In `[<-.factor`(`*tmp*`, 2, value = 28) :
4 invalid factor level, NA generated</pre>
```

factors and functions $f(\mathbb{H})$ in R

In the context of factors, the **tapply()** function is leveraged to apply functions against factor elements.

```
1 tapply(X, INDEX< FUN = NULL, ..., simplify = TRUE)</pre>
```

The call **tapply(x, f, g)** has vector \mathbf{x} , factor (or list of multiple factors) \mathbf{f} , and function \mathbf{g} .

The motivating example illustration is vector \mathbf{x} of ages of voters and factor \mathbf{f} of voter party affiliation. Each factor in \mathbf{f} must consists of equal lengths to \mathbf{x} . If a component of \mathbf{f} is a vector, it is coerced into a factor by application of function **as.factor()** to the vector in \mathbf{f} .

The operation performed by **tapply()** temporarily splits \mathbf{x} into groups, each corresponding to a level (or combination of levels) in factor \mathbf{f} , finally applying $\mathbf{g}()$ to the resulting subvectors of \mathbf{x} (illustrated below):

The example illustration is expanded to break down groups by both gender and age. When 2 or more factors are applied, each produces a set of groups computed against each other under **AND** logic. The **mean()** function will then be applied to return the each of the four subgroups inclusive of the operation:

1) Male < 25; **2)** Male > 25; **3)** Female < 25; **4)** Female > 25

```
> d <- data.frame(list(gender = c("M","M","F","M","F","F"),</pre>
2
                         age = c(47,59,21,32,33,24),
3
                         income = c(55000,8800,32450,76500,123000,45650))
   > d
     gender age income
   1
          M 47 55000
7
          M 59 8800
   3
          F 21 32450
   4
          M 32 76500
10 5
          F
            33 123000
11 6
          F 24 45650
12
13 > d$over25 <- ifelse(d$age > 25, 1,0)
14 > d
15
   gender age income over25
16 1
          M 47
                55000
17 2
          M 59
                 8800
                           1
18 3
          F 21 32450
                           0
19 4
          M 32 76500
                           1
20 5
          F 33 123000
                           1
21 6
          F 24 45650
22
23
  > tapply(d$income, list(d$gender, d$over25),mean)
24
         0
25
   F 39050 123000.00
26
        NA 46766.67
```

The two specified factors (Age < OR > 25 and Gender) each contain two levels. Therefore, **tapply()** split (partitioned) the data into four groups; each group representative of each possible permutation of gender and age. Lastly, the **mean()** function was applied to each group individually.

Using the **split()** function simply forms the vector into groups, opposed to splitting a vector into groups and **then** apply a function against each group; seen in the **tapply()** function.

```
1 split(x, f, drop = FALSE, ...)
```

The vector \mathbf{x} and factor \mathbf{f} serve similar roles in the **split()** function as they did in the **tapply()** function. Note that in the **split()** function, \mathbf{x} is allowed to be a dataframe; the latter is not true with **tapply()**.

```
> d
      gender age income over25
3 1 M 47 55000
4 2 M 59 8800
5 3 F 21 32450
6 4 M 32 76500
7 5 F 33 123000
8 6 F 24 45650
                                   0
                                 1
10 > split(d$income, list(d$gender, d$over25)) #list output denoted by $
11 $F.0
12 [1] 32450 45650
13
14 $M.0
15 numeric(0)
16
17 $F.1
18 [1] 123000
19
20 $M.1
21 [1] 55000 8800 76500
```

Note that the output is a list with components denoted by \$; the vectors are represented by the combination of factors that make up the results (e.g. \$F.0 = Female < 25, \$M.1 = Male > 25).

The example below determines the indices of which vector elements correspond to Male, Female, or Infants:

```
1  > g <- c("M","F","F","I","M","M","F")
2  > split(1:7,g)
3  $F
4  [1] 2 3 7
5
6  $I
7  [1] 4
8
9  $M
10  [1] 1 5 6
```

The **by()** function operates similar to that of **tapply()**, which is internally called within **by()**. The difference is how the **by()** function is applied to **objects**, rather than vectors. This is useful for performing certain operations against dataframes and matrices.

```
1 split(x, f, drop = FALSE, ...)
```

Calls to the **by()** function are similar to those of the **tapply()** function. The first argument **x** specifies the data, the second argument **f** specifies the grouping factor(s), and the third argument specifies the function to be applied to each factor group individually. Just as **tapply()** forms groups of indices of a vector corresponding to each factor level, **by()** finds groups of row numbers of a dataframe, creating sub dataframes for each corresponding factor level. The specified function is then called against each of the identified factor groups defined in the problem.

working with tables III in R

Given the following example:

```
1  > u <- c(22,8,33,6,8,29,-2)
2  > fl <- list(c(5,12,13,12,13,5,13),c("a","bc","a","a","bc","a","a"))
3  > tapply(u,fl,length)
4     a bc
5     5     2 NA
6     12     1     1
7     13     2     1
```

Again, **tapply()** partitions vector **u** into subvectors and applies the **length()** function to each subvector. Note that the latter operation is independent of the contents of vector **u**; the focus is strictly on the factors. The resulting **contingency table** illustrates the frequency of factors occurring in the data. Note the occurrence of **NA** representing that **5** occurred with "**bc**" in no observations from the function. The problem with the above illustration is the misrepresentation of **0** occurrences as an **NA** value; use **table()** instead:

```
1 > table(fl)  #applying the table() function to appropriately represent all cases
2    fl.2
3    fl.1 a bc
4    5    2   0
5    12   1   1
6    13   2   1
```

The first argument in the **table()** function is either a factor or a list of factors (two factors in above).

Typically, a dataframe serves as the **table()** argument. Consider the following example of polling-data:

The **table()** function computes the **contingency table** for the above dataset.

One-dimensional counts are equally available; counts on a single factor:

```
1  > table(c(5,12,13,12,8,5))
2
3    5  8 12 13
4    2  1  2  1
```

matrix/array-like operations on tables ABC in R

Considering that nonmathematical operators can be used on dataframes, the same applies to tables—the cell counts component of a table object is an array. Table cell counts can be accessed with matrix notation:

```
1  > class(cttab)
2  [1] "table"
3
4  > cttab[1,1]
5  [1] 2
6
7  > cttab[1,]
8  No Yes
9  2 0
```

Below illustrates multiplicative properties of table operations by converting cell counts to proportions:

The *marginal values* (statistical method are the values of a variable when the variable itself is held constant while other variables are summed) are computed with the **apply()** function below:

```
1 > apply(cttab, 1, sum)
2     No Not Sure    Yes
3     2    1    2
```

The above illustration computes that marginal values of the polling data (1+1=2, 1+0=1, 1+1=2).

The *marginal values* both dimensions can be computed simultaneously with the **addmargins()** function.

The dimension names of a table can be accessed through the **dimnames()** function as follows:

```
1 > dimnames(cttab)
2 $Vote.for.X
3 [1] "No" "Not Sure" "Yes"
4
5 $Voted.for.X.Last.Time
6 [1] "No" "Yes"
```

other factor- and table-related functions ≡ in R

the aggregate() function calls tapply() once for each variable in a group.

```
1 aggregate(x, ...)
```

The **cut()** function is a common way to generate factors (particularly with tables) by providing data vector \mathbf{x} and a set of bins defined by vector \mathbf{b} . The functions determines the bins each element of \mathbf{x} falls into.

```
1 cut(x, b, labels = FALSE, ...)
```