

### Cpt S 317 Homework #3

Please print your name!

1. Let  $L_1$  and  $L_2$  be two regular languages. They are specified by the following regular expressions:  $L_1 = 0(0 + 11)^*$  and  $L_2 = 0^*11^*$ .
  - (1). Draw a DFA accepting  $L_1$ .
  - (2). Draw a DFA accepting  $L_2$ .
  - (3). Draw a DFA accepting  $L_1 \cap L_2$ .
  - (4). What is the regular expression for  $L_1 \cap L_2$ ?
2. A natural number can be encoded as a unary string. For instance, 5 = the string of *aaaaa*. Therefore, we may treat a set of numbers as a language over a unary alphabet (that contains only one symbol, e.g., *a*). Write down the regular expression for the following sets of numbers: (1). all the  $n$  such that  $n \bmod 3 = 1$ . (2). all the  $n$  such that  $n \bmod 3 = 0$  or  $n \bmod 4 = 2$ .
3. Show that deterministic FAs are closed under complement. That is, for any deterministic FA  $M$ , there is a deterministic FA  $M'$  such that  $L(M') = \Sigma^* - L(M)$ , assuming that both  $M$  and  $M'$  have the same alphabet.
4. According to your proof of Problem 3, draw a deterministic finite automaton that accepts the complement of  $(00 + 1)^*$ . And also find a regular expression for the language accepted by  $M'$ .
5. Let  $L$  be a regular language on  $\Sigma$  and  $\Sigma' \subset \Sigma$ . The result of dropping symbols in  $\Sigma'$  from a word  $w$  is denoted by  $w^{-\Sigma'}$ . For instance,  $aaabacba^{-\{b\}}$  is  $aaaaca$ . Define  $L^{-\Sigma'} = \{w^{-\Sigma'} : w \in L\}$ . That is,  $L^{-\Sigma'}$  is the result of dropping symbols in  $\Sigma'$  from each word in  $L$ . Show that if  $L$  is a regular language, then  $L^{-\Sigma'}$  is also a regular language. (Hint: use structural induction)