

4. Let  $x$  = the number of nonzero digits in a randomly selected 4-digit PIN that has no restriction on the digits.

What are the possible values of  $x$ ? Give three possible outcomes and their associated  $x$  values?

Hence,  $x$  can be  $\{0, 1, 2, 3, 4\}$ .

$x = 1$   
0300,  $x = 1$ , only 3 is nonzero here.

$x = 2$   
1200,  $x = 2$ , only 1 and 2 are nonzero

2301,  $x = 3$ , 2, 3, 1 are nonzero.

6.

\* There are five possible outcomes and their values.

Sample Space  $S$ : L      AL      RRAL      RL      RAL

Number of cars  $X$ : 1      2      4      2      3

8.

$Y \rightarrow \{SSS\}$

$3 \rightarrow \{SSS\} \leftarrow 3 \text{ trials, 3 consecutive successes, in 3 trials}$

$4 \rightarrow \{FSSS\} \leftarrow 4 \text{ trials, 3 consecutive successes, in 4 trials}$

$5 \rightarrow \{FFSSS, SFSSS\} \leftarrow 5 \text{ trials, 3 consecutive successes in 5 trials}$

$6 \rightarrow \{FFFSSS, SSFSSS, SFFSSS, FSFSSS\} \leftarrow 6 \text{ trials, 3 consecutive successes in 6 trials}$

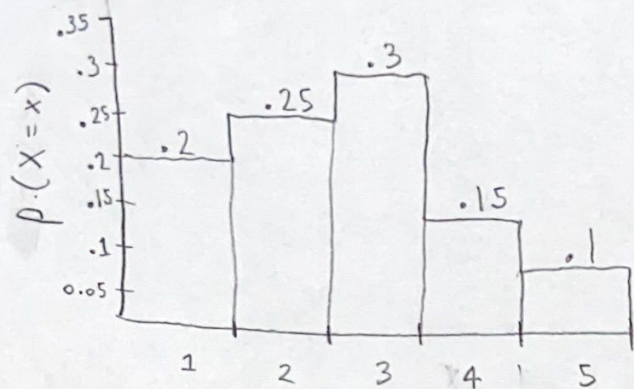
$7 \rightarrow \{FFFFSSS, FFSFSSS, FSFFSSS, SFFFSSS, FSSFSSS, SSFFSSS, SFSSFSSS\} \leftarrow 7 \text{ trials, 3 consecutive successes in 7 trials}$

$7 \rightarrow \{FFFFSSS, FFSFSSS, FSFFSSS, SFFFSSS, FSSFSSS, SSFFSSS, SFSSFSSS\}$



11.

a.



$$b. \quad P(X \geq 2) = P(X=2) + P(X=3) + P(X=4)$$

$$= 0.25 + 0.3 + 0.15 = 0.7$$

The probability that at least two students show up is 70%.

$$c. \quad P(X > 2) \rightarrow P(X > 2) = P(X=3) + P(X=4)$$

$$= 0.3 + 0.15 = 0.45$$

The probability that more than two students show up is 45%.

c.

$$P(1 \leq X \leq 3) = P(X=1) + P(X=2) + P(X=3)$$

$$0.2 + 0.25 + 0.3 = 0.75 \rightarrow$$

The probability that between one and three show up 75%.

D. we cannot find this value

14.

$$A. \sum p(y) = 1$$

$$\rightarrow 15k = 1$$

$$\rightarrow k = \frac{1}{15} \rightarrow \text{value of } k \text{ is } \frac{1}{15}$$

$$b. 1 - (p(y=4) + p(y=5))$$

$$= 1 - p(y=4) - p(y=5)$$

$$= 1 - 4k - 5k$$

$$= 1 - 9k$$

$$p(y < 3) = 1 - \frac{9}{15} = \frac{6}{15} = .4$$

The probability is

0.4 or 40%

$$c. \sum yp(y)$$

$$1 = 1 \times k + 2 \times 2k + 3 \times 3k + 4 \times 4k + 5 \times 5k$$

$$1 = k + 4k + 9k + 16k + 25k$$

$$1 = (1 + 4 + 9 + 16 + 25)k$$

$$= 55k$$

$$= 55 \times \frac{1}{15} \left( k = \frac{1}{15} \right) = 3.667$$

The expected number of forms required is

3.667

D.

$$E(y^2) - \mu_y^2$$

$$= 15 - 3.667^2$$

$$= 15 - 13.45$$

$$= 1.55$$

$$= \sqrt{1.55} = 1.24$$

The standard deviation of  
the number of forms  
required is

1.24



23.

a.  $p(2) = p(x=2)$

$$F(2) - F(1)$$

$$= .39 - .19$$

$$= .2 \rightarrow \text{value of } p(2) = \underline{.2}$$

b.  $p(x > 3) = 1 - p(x \leq 3)$

$$= 1 - F(3)$$

$$= 1 - 0.67$$

$$= .33 \rightarrow \text{The value of } p(x > 3) \text{ is } \underline{.33}$$

c.  $p(2 \leq x \leq 5) = p(x \leq 5) - p(x < 2)$

$$= p(x \leq 5) - p(x \leq 1)$$

$$= F(5) - F(1)$$

$$= .97 - 0.19$$

$$= .78 \rightarrow \text{The value of } p(2 \leq x \leq 5) \text{ is } \underline{.78}$$

d.  $p(2 < x < 5) = p(x=3) + p(x=4)$

$$.92 - .39$$

$$= .53$$

The value of  $p(2 < x < 5)$  is

$$\underline{.53}$$

$$= p(3) + p(4)$$

$$= [F(3) - F(2)] + [F(4) - F(3)]$$

$$= F(4) - F(2)$$