World Health Organization Life Expectancy

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Introduction:

In the past, there have been many studies that show the factors that affect an individual's life expectancy. In these studies researchers have considered demographic variables, income composition and mortality rates. While conducting these studies researcher found that the effect of immunization and human development was not taken into account. Using one year's worth of data for all countries, some research was done considering multiple linear regression. The data from the Global Health Organization (GHO) under World Health Organization (WHO) contains data from all countries health status.

Purpose

Taking into account both of the affects that where described above we have found enough reason to formulate a regression model by using WHO data. We will focus on mixed effects model and multiple linear regression. We will also use data from the time period of 2000 to 2015 for all countries to model our regression. These models help countries determine where to invest more resources if they seek to improve overall Life Expectancy.

Multiple Linear Regression Overview

- y = Life Expectancy in age
- x1 = Adult Mortality
- x2 = Alcohol, recorded per capita (15+) consumption (in litres of pure alcohol)
- x3 = Measles number of reported cases per 1000 population
- x4 = Number of under-five deaths per 1000 population
- x5 = Polio (Pol3) immunization coverage among 1-year-olds (
- x6 = General Government Expenditure on health as a percentage of total government expenditure (
- x7 = Diphtheria tetanus toxoid and pertussis (DTP3) immunization coverage among 1-year-olds (
- x8 = HIV/AIDSDeaths per 1 000 live births HIV/AIDS (0-4 years)
- x9 = GDPGross Domestic Product per capita (in USD)
- x10 = Population of the country
- x11 = thinness 1-19 yearsPrevalence of thinness among children
- x12 = Number of years of Schooling

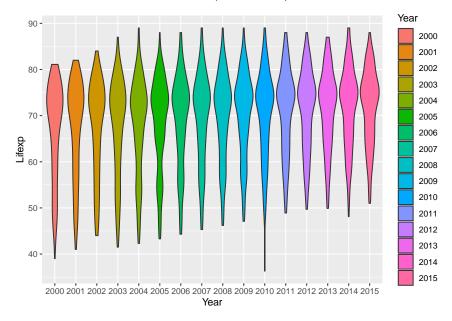
Data

Let us take a look at randomly selected rows

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	Country	Year	Lifexp	Admort	Alcohol	Measles	U5deaths	Polio	Totexp	Diphtheria	HIV	GDP	Population	Thinness	Schooling
342	Botswana	2010	61.10	349	5.99	853	3	96	5.64	95	6.20	6434.82	2014866.00	8.00	12.30
1802	Namibia	2009	62.40	36	7.99	4076	4	83	8.50	83	8.70	5112.64	2137040.00	1.90	11.40
347	Botswana	2005	51.70	566	6.37	5	3	96	5.62	96	20.60	5686.78	1855852.00	1.00	11.90
177	Bahrain	2015	76.90	69		0		98		98	0.10	22435.73	1371855.00	6.20	14.50
1605	Maldives	2012	77.60	65	0.01	0		99	9.16	99	0.10	7251.68	386203.00	13.80	12.10
1504	Liberia	2001	51.50	333	4.40	1379	20	54	6.41	42	3.10	609.68	2991132.00	9.00	10.50
2223	Sao Tome and Principe	2008	65.40	215	4.36	0		99	5.66	99	0.90	1056.10	166913.00	6.50	10.40
589	Colombia	2003	72.40	15	4.25	0	19	92	5.92	92	0.10	5026.24	42152151.00	2.50	11.60
496	Cameroon	2000	51.40	394	3.91	14629	100	57	4.48	62	7.70	1145.45	15274234.00	7.70	6.90
1321	Japan	2008	82.70	66	7.11	11015	4	98	8.60	98	0.10	45165.79	128063000.00	1.80	15.00
1956	Pakistan	2000	62.80	19	0.02	2064	495	65	2.79	62	0.10	824.73	138523285.00	22.20	5.30
2567	Tajikistan	2000	63.70	198	0.37	192	17	86	4.64	83	0.30	415.46	6216205.00	4.20	9.60
1731	Mongolia	2000	62.80	274	2.79	925	3	94	4.92	94	0.10	1600.49	2397436.00	2.60	8.90
1432	Lao People's Democratic Republic	2009	63.10	223	5.18	78	14	67	3.77	67	0.20	1068.17	6152036.00	9.40	9.40
288	Benin	2000	55.40	279	1.34	4244	40	78	4.34	78	2.00	694.92	6865951.00	9.70	6.40

Data Visualization with Years (2000-2015)



Fitting Model

```
summary(who.lm)
```

```
##
## Call:
## lm(formula = who_dat$Lifexp ~ . - Country - Year, data = who_dat)
##
## Residuals:
##
                       Median
                                            Max
        Min
                  1Q
##
   -20.0800
            -2.2788
                       0.0658
                                2.5038
                                        12.2611
##
## Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
## (Intercept) 4.986e+01
                          6.364e-01
                                     78.346 < 2e-16 ***
## Admort
               -1.453e-02 9.369e-04 -15.513 < 2e-16 ***
## Alcohol
               -1.573e-01 3.269e-02
                                     -4.811 1.63e-06 ***
               -3.772e-05 9.161e-06 -4.117 4.02e-05 ***
## Measles
```

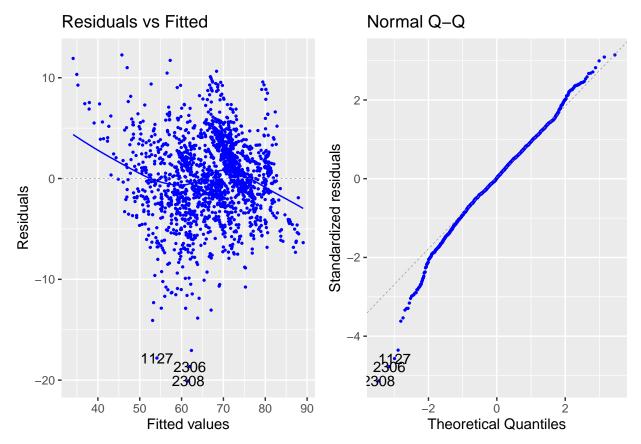
```
## U5deaths
              -3.214e-03 7.555e-04 -4.254 2.21e-05 ***
## Polio
               9.985e-03 5.417e-03
                                      1.843
                                              0.0654 .
                         4.413e-02
## Totexp
               1.765e-02
                                      0.400
                                              0.6893
## Diphtheria
               3.830e-02 5.692e-03
                                      6.729 2.29e-11 ***
## HIV
              -5.524e-01
                          2.180e-02 -25.345
                                             < 2e-16 ***
## GDP
               9.468e-05
                          1.008e-05
                                             < 2e-16 ***
                                      9.396
               7.156e-09
                          8.912e-10
                                      8.030 1.75e-15 ***
## Population
## Thinness
              -5.691e-02
                          2.523e-02
                                     -2.256
                                              0.0242 *
## Schooling
               1.518e+00 5.008e-02
                                     30.311 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 3.929 on 1791 degrees of freedom
##
     (1076 observations deleted due to missingness)
## Multiple R-squared: 0.8338, Adjusted R-squared: 0.8327
## F-statistic: 748.6 on 12 and 1791 DF, p-value: < 2.2e-16
```

Our p-value: 2.2e-16 is significant at $\alpha = .05$. Therefore, we conclude that the model is significant. Hence, there is a linear relationship between the response y and any of the other of the regressor variables.

According to our t-tests the p values .0654,.6893 are greater than our significance level of $\alpha = .05$. Therefore the regressors Polio, Totexp are not contributing significantly to the model.

```
\hat{y} = 49.86 - .01453x_1 - .1573x_2 - .00003772x_3 - .003214x_4 + .00935x_5 + .01765x_6 + .03830x_7 - .5524x_8 + 00009468x_9 + .000000007156x_{10} - .05691x_{11} + 1.518x_{12}
```

Model Adequacy Checking



In our residuals vs \hat{y} there is not obvious pattern. Therefore, we satisfy Linearity assumption. However, our probability plot of the residuals may show issues with normality. Thus, we proceed with the normality test.

ols_test_normality(who.lm)

##			
##	Test	Statistic	pvalue
##			
##	Shapiro-Wilk	0.9865	0.0000
##	Kolmogorov-Smirnov	0.0382	0.0105
##	Cramer-von Mises	124.3553	0.0000
##	Anderson-Darling	3.3569	0.0000
##			

According to the Shapiro-Wilk, Kolmogorov-Smirnov, Cramer-von Mises and Anderson-Darling normality tests, because of our small p value, we reject the null and conclude that our residuals are not normal. This may be due to influential observations

We proceed to find some influential observations and potential outliers

```
inflm.fit <- influence.measures(who.lm)
inflm_obs <- which(apply(inflm.fit$is.inf, 1, any))
length(inflm_obs)</pre>
```

[1] 158

There are 158 influential observations.

```
##
## Shapiro-Wilk normality test
##
## data: who.lm2$residuals
## W = 0.79906, p-value < 2.2e-16</pre>
```

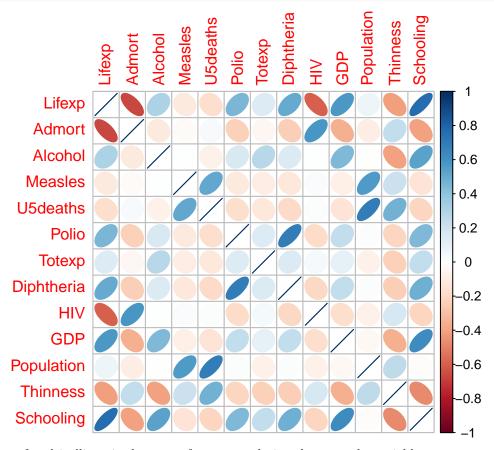
Removing influential observations with the largest residuals did not improve the adequacy of our model. Our normality assumptions were still not met. After some data exploratory analysis, these observations seem valid.

Examine correlation plot for any suspect of multicoliinearity

```
who_dat <- na.omit(who_dat) #Omit Na Values
who_dat <- select_if(who_dat, is.numeric) #Select only numeric Columns
row.names(who_dat) <- NULL #Resetting Index
#install.packages('corrplot')
library(corrplot)</pre>
```

corrplot 0.84 loaded

corrplot(cor(who_dat), method = "ellipse")



There is suspect of multicollinearity because of some correlations between the variables

Thus we proceed to check Variance Inflation Factors

```
vif(who.lm)
```

##	Admort	Alcohol	Measles	U5deaths	Polio	Totexp	Diphtheria
##	1.828499	1.679334	1.585609	2.592436	2.031997	1.141177	2.152803

```
## HIV GDP Population Thinness Schooling
## 1.583458 1.781839 2.422343 1.758080 2.728819
```

Our Variance Inflation Factors are all less than 5. We can conclude there is no multicollinearity issues.

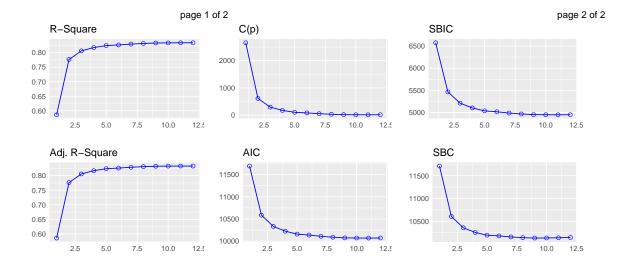
Variable Selection and Model Building

APC: Amemiya Prediction Criteria

plot(ols_step_best_subset(lm(Lifexp~., data=who_dat)))

```
ols_step_best_subset(lm(Lifexp~., data=who_dat))
```

```
##
                                              Best Subsets Regression
##
## Model Index
                  Predictors
##
##
        1
                  Schooling
##
        2
                  HIV Schooling
##
        3
                  Admort HIV Schooling
##
        4
                  Admort Diphtheria HIV Schooling
##
        5
                  Admort Diphtheria HIV GDP Schooling
##
        6
                  Admort Alcohol Diphtheria HIV GDP Schooling
        7
##
                  Admort U5deaths Diphtheria HIV GDP Population Schooling
##
        8
                  Admort Alcohol U5deaths Diphtheria HIV GDP Population Schooling
                  Admort Alcohol Measles U5deaths Diphtheria HIV GDP Population Schooling
        9
##
##
                  Admort Alcohol Measles U5deaths Diphtheria HIV GDP Population Thinness Schooling
       10
##
                  Admort Alcohol Measles U5deaths Polio Diphtheria HIV GDP Population Thinness Schooling
       11
##
                  Admort Alcohol Measles U5deaths Polio Totexp Diphtheria HIV GDP Population Thinness Schooling
       12
##
##
##
                                                              Subsets Regression Summary
##
##
                          Adj.
                                       Pred
## Model
            R-Square
                        R-Square
                                     R-Square
                                                   C(p)
                                                                  AIC
                                                                                SBTC
                                                                                              SBC
                                                                                                            MSEP
##
##
    1
              0.5863
                          0.5861
                                       0.5855
                                                 2656.8036
                                                               11693.9090
                                                                             6571.2893
                                                                                           11710.4023
                                                                                                          68863.3339
##
    2
              0.7764
                                       0.7754
                                                               10586.3261
                                                                             5465.1620
                                                                                           10608.3171
                          0.7761
                                                  611.3661
                                                                                                          37248.4796
##
    3
              0.8060
                          0.8057
                                       0.8045
                                                  294.3199
                                                               10332.0740
                                                                             5211.4105
                                                                                           10359.5628
                                                                                                          32334.0308
##
    4
                                                                             5105.0341
                                                                                           10258.3987
              0.8173
                          0.8169
                                       0.8157
                                                  174.1288
                                                               10225.4121
                                                                                                          30460.8548
##
                                                  102.5433
                                                               10158.6699
                                                                                           10197.1543
                                                                                                          29338.2848
    5
              0.8242
                          0.8237
                                       0.8224
                                                                             5038.5617
##
     6
                                                               10137.7085
                                                                             5017.6775
                                                                                           10181.6906
                                                                                                          28983.3608
              0.8264
                          0.8258
                                       0.8245
                                                   80.5823
    7
##
              0.8293
                          0.8286
                                       0.8272
                                                   51.5288
                                                               10109.5091
                                                                             4989.6691
                                                                                           10158.9889
                                                                                                          28518.0880
##
    8
              0.8314
                          0.8306
                                       0.8293
                                                   30.5897
                                                               10088.8716
                                                                             4969.2165
                                                                                           10143.8492
                                                                                                          28178.1633
##
     9
              0.8330
                          0.8321
                                       0.8308
                                                   15.5713
                                                               10073.8914
                                                                             4954.4104
                                                                                           10134.3668
                                                                                                          27929.7492
##
    10
              0.8334
                          0.8325
                                       0.8311
                                                   12.5915
                                                               10070.8925
                                                                             4951.4775
                                                                                           10136.8656
                                                                                                          27868.0040
##
    11
              0.8338
                          0.8327
                                       0.8312
                                                   11.1599
                                                               10069.4396
                                                                             4950.0813
                                                                                           10140.9105
                                                                                                          27830.2457
##
    12
              0.8338
                          0.8327
                                       0.8308
                                                   13.0000
                                                               10071.2785
                                                                             4951.9369
                                                                                           10148.2472
                                                                                                          27843.3071
##
## AIC: Akaike Information Criteria
  SBIC: Sawa's Bayesian Information Criteria
  SBC: Schwarz Bayesian Criteria
  MSEP: Estimated error of prediction, assuming multivariate normality
  FPE: Final Prediction Error
##
##
   HSP: Hocking's Sp
```



We will select the top 5 models and compare them

$$Model1: \hat{y} = 49.86 + 1.518x_{12}$$

$$Model2: \hat{y} = 49.86 + 1.518x_{12} + .5524x_{8}$$

$$Model3: \hat{y} = 49.86 + 1.518x_{12} + .5524x_{8} + .01453x_{1}$$

$$Model4: \hat{y} = 49.86 + 1.518x_{12} + .5524x_{8} + .01453x_{1} + .03830x_{7}$$

 $Model5: \hat{y} = 49.86 + 1.518x_{12} + .5524x_8 + .01453x_1 + .03830x_7 + 00009468x_9$

PRESS Statistics for Models

[1] "Our PRESS statistic for the First model is: 68925.9735616238"
[1] "Our PRESS statistic for the Second model is: 37352.9349138681"
[1] "Our PRESS statistic for the Third model is: 32501.8275243135"
[1] "Our PRESS statistic for the Fourth model is: 30641.8984253618"
[1] "Our PRESS statistic for the Fifth model is: 29526.8361755966"

Variance Inflation Factors for Models

```
## Schooling
##
    1.048654
               1.048654
   Schooling
                    HIV
                            Admort
##
    1.195352
               1.525211
                          1.737160
##
    Schooling
                       HIV
                               Admort Diphtheria
                 1.542060
##
     1.477598
                             1.737327
                                         1.321474
##
                       HIV
                               Admort Diphtheria
                                                           GDP
    Schooling
##
     2.108629
                 1.544047
                             1.776499
                                         1.331262
                                                     1.699836
```

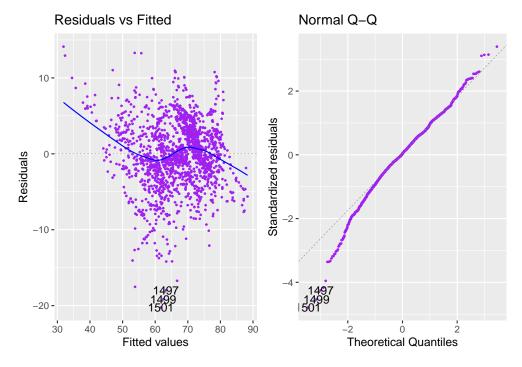
None of our models have issues with Multicollinearity. We proceed to select two models to compare. Parsimonious models are simple models with great explanatory predictive power. They explain data with a minimum number of parameters, or predictor variables. Therefore we picked models:

$$Model3: \hat{y} = 49.86 + 1.518x_{12} + .5524x_8 + .01453x_1$$

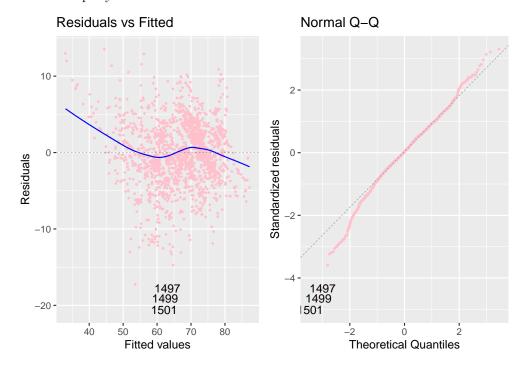
$$Model4: \hat{y} = 49.86 + 1.518x_{12} + .5524x_8 + .01453x_1 + .03830x_7$$

Due to their lower PRESS statistics compared to Models 1 and 2. They also have a high Pred \mathbb{R}^2 values. .8045 and ,8157 respectively.

Model Adequacy of Model 3



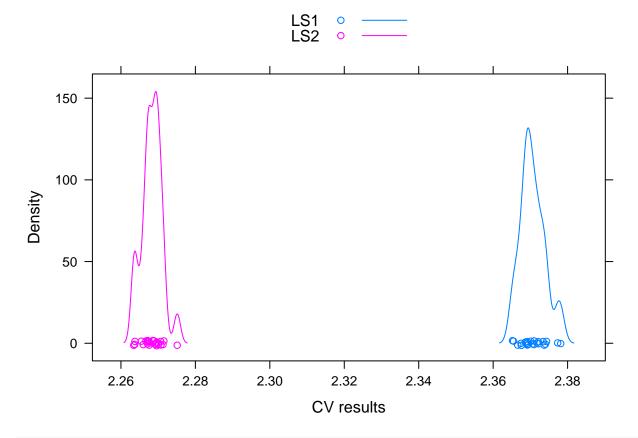
Model Adequacy of Model 4



For both our models, in our residuals vs \hat{y} there is not obvious patterns. Therefore, we satisfy Linearity assumption.

Cross Validation

```
##
## 5-fold CV results:
## Fit CV
## 1 LS1 2.370626
## 2 LS2 2.268312
##
## Best model:
## CV
## "LS2"
```



summary(fit4)

```
##
## Call:
## lm(formula = Lifexp ~ Schooling + HIV + Admort + Diphtheria,
##
       data = who_dat)
##
## Residuals:
##
       Min
                1Q Median
                                ЗQ
                                       Max
## -20.585 -2.314
                    0.116
                            2.624 13.545
##
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
## (Intercept) 47.7536642 0.5216962
                                       91.53
                                               <2e-16 ***
## Schooling 1.7216144 0.0385466
                                       44.66
                                               <2e-16 ***
```

```
## HIV
               -0.5641439
                           0.0224969
                                      -25.08
                                                <2e-16 ***
## Admort
               -0.0164102
                           0.0009552
                                      -17.18
                                                <2e-16 ***
## Diphtheria
                0.0492997
                           0.0046648
                                       10.57
                                                <2e-16 ***
## ---
## Signif. codes:
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 4.109 on 1799 degrees of freedom
## Multiple R-squared: 0.8173, Adjusted R-squared: 0.8169
## F-statistic: 2012 on 4 and 1799 DF, p-value: < 2.2e-16
```

Conclusion:

We prefer $Model4: \hat{y} = 49.86 + 1.518x_{12} + .5524x_8 + .01453x_1 + .03830x_7$ because it performed better in cross validation testing and because the principle of parsimony. The porportion of variation of the dependent variable (Life Expectancy) explained by this model is $R_{adj} = .8169$. It is interesting to note that the variables $x_{12} = Schooling, x_8 = HIV, x_1 = AdultMort, x_7 = Diptheria$ are significant variables in explaining Life Expectancy. Here, increasing Schooling by 1 unit(year) while holding all other variables constant, results an increase of 1.722 in Life Expectancy. We can also expect an imporvement in Life expectancy if we increase Diphtheria(immunization coverage) by one unit while holding other variables constant by 0.0493 years. Increasing HIV by 1 unit while holding all other constant results in a decrease of Life Expectancy(years) by -0.564. Similarly, a unit increase in Adult Mortalities while holding all other variables constant results in a decrease in Life Expectancy by -0.0164. These variables agree with our intuition. If countries provide education and immuzation, there is an overall increase in life expectancy. However, other variables like HIV and Adult mortalities negatively affect Life Expectancy. This is why HIV is a largely researched field and similarly overall adult health.

References

Data: https://www.kaggle.com/fahmadi96/life-expectancy-who-revised Montgomery, D., Peck, E., & Vining, G. (2012). Introduction to Linear Regression Analysis, 5th Edition. John Wiley & Sons.