Module: Data Visualisation

Problem Set 5

Topics Covered: Linear Regression

**Exercise 1.** A retailer wishes to determine the relationship between the amount it spends on advertising and the total sales revenue of the company. The data in this case are collected over 12 months and are given by the following data table:

| Month                | Revenue €1000 | Advertising €1000 |
|----------------------|---------------|-------------------|
| Jan                  | 75            | 2.1               |
| Feb                  | 81            | 2.4               |
| Mar                  | 65            | 1.5               |
| Apr                  | 67            | 1.5               |
| May                  | 71            | 2.3               |
| $\operatorname{Jun}$ | 73            | 2.3               |
| Jul                  | 79            | 2.7               |
| Aug                  | 84            | 3.1               |
| Sep                  | 86            | 3.3               |
| Oct                  | 74            | 3.2               |
| Nov                  | 88            | 4.1               |
| Dec                  | 92            | 4.5               |

Using this data set, answer the following

- (i) Identify the dependent and independent variables from this data set.
- (ii) Draw a scatter plot to represent this data set.
- (iii) From the scatter plot, is the linear relationship

$$y = a + bx$$

an appropriate relationship between these variables?

(iv) Use the least squares method to find the line of best fit.

- (v) Include this line of best fit in your scatter plot.
- (vi) Interpret the parameters a and b.

Exercise 2. A company wishes to determine how much money it should spend on Research & Development (R&D), if it wished to remain competitive. It performs a survey of 20 similar companies and tabulates the Price to Earnings Ratio (PER) and the Research to Sales Ratio (RSR) of these companies. The data is collected in the table below:

| Company | PER  | RSR   | Company | PER  | RSR   |
|---------|------|-------|---------|------|-------|
| 1       | 5.6  | 0.003 | 11      | 8.4  | 0.058 |
| 2       | 7.2  | 0.004 | 12      | 11.1 | 0.058 |
| 3       | 8.1  | 0.009 | 13      | 11.1 | 0.067 |
| 4       | 9.9  | 0.021 | 14      | 13.2 | 0.080 |
| 5       | 6.0  | 0.023 | 15      | 13.4 | 0.080 |
| 6       | 8.2  | 0.030 | 16      | 11.5 | 0.083 |
| 7       | 6.3  | 0.035 | 17      | 9.8  | 0.091 |
| 8       | 10.0 | 0.037 | 18      | 16.1 | 0.092 |
| 9       | 8.5  | 0.044 | 19      | 7.0  | 0.064 |
| 10      | 13.2 | 0.051 | 20      | 5.9  | 0.028 |

- (i) Identify the dependent and independent variables from this data set.
- (ii) Draw a scatter plot to represent this data set.
- (iii) From the scatter plot, is the linear relationship

$$y = a + bx$$

an appropriate relationship between these variables?

- (iv) Use the least squares method to find the line of best fit.
- (v) Include this line of best fit in your scatter plot.
- (vi) Interpret the parameters a and b.