

MSc - Data Mining

Topic 03 : Exploratory Data Analysis

Part 01 : Exploratory Data Analysis

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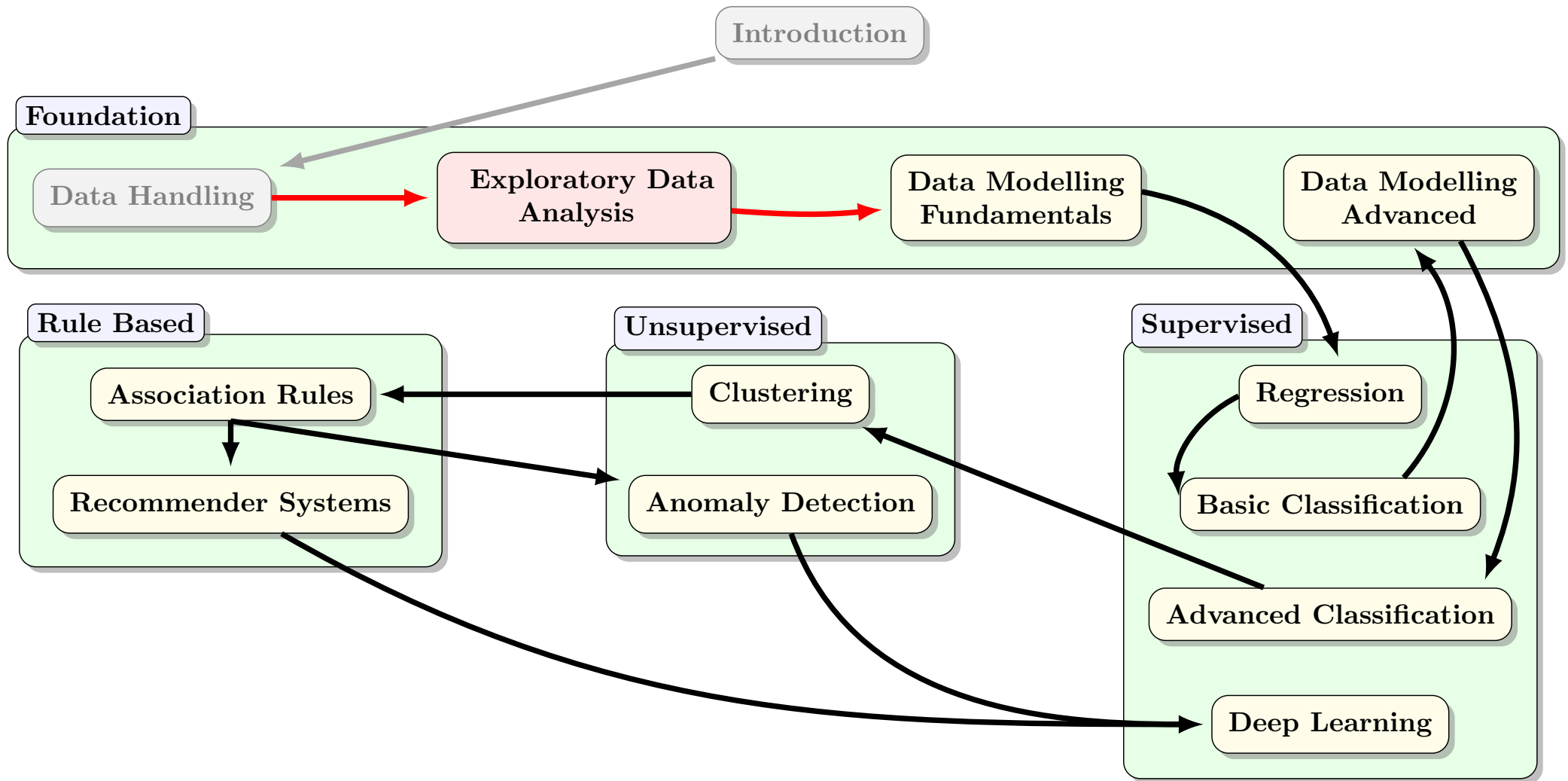
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Outline

- EDA Process
- Datasets = Tips, Titanic and Algae Blooms
- Identifying and resolving issues (missing value, outliers)
- Generating ToDo list for Feature Engineering/Transformation/Selection

Data Mining (Week 3)



Exploratory Data Analysis — Summary

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Introduction

Exploratory Data Analysis (EDA)

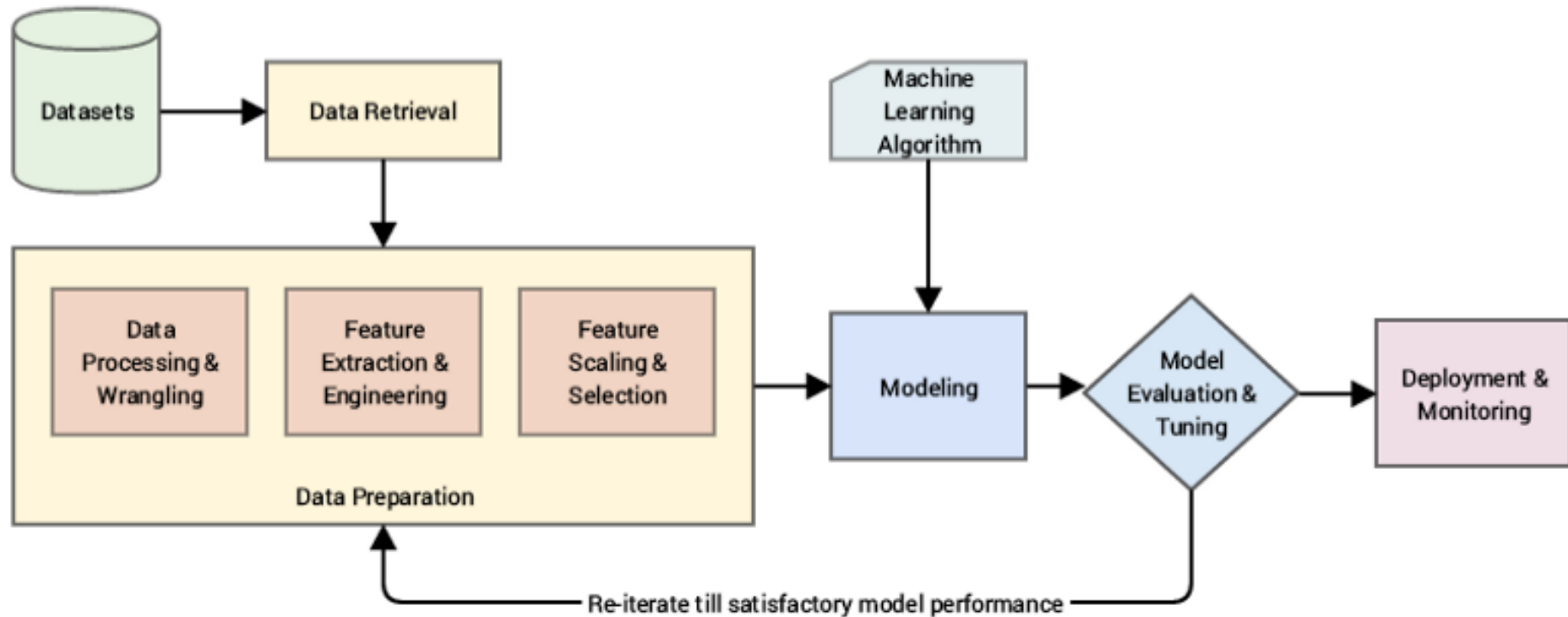
Aim

To understand and summarise a dataset to ensure that the features which are feed to machine learning algorithms are refined and that the results are valid and can correctly interpreted.

Benefits

- Develop insight about the dataset and understanding of the underlying structure.
- Extract important parameters and relationships that hold between them.
- Test underlying assumptions.
- Identify issues that affect model performance — outliers, missing values.

Data Pipeline



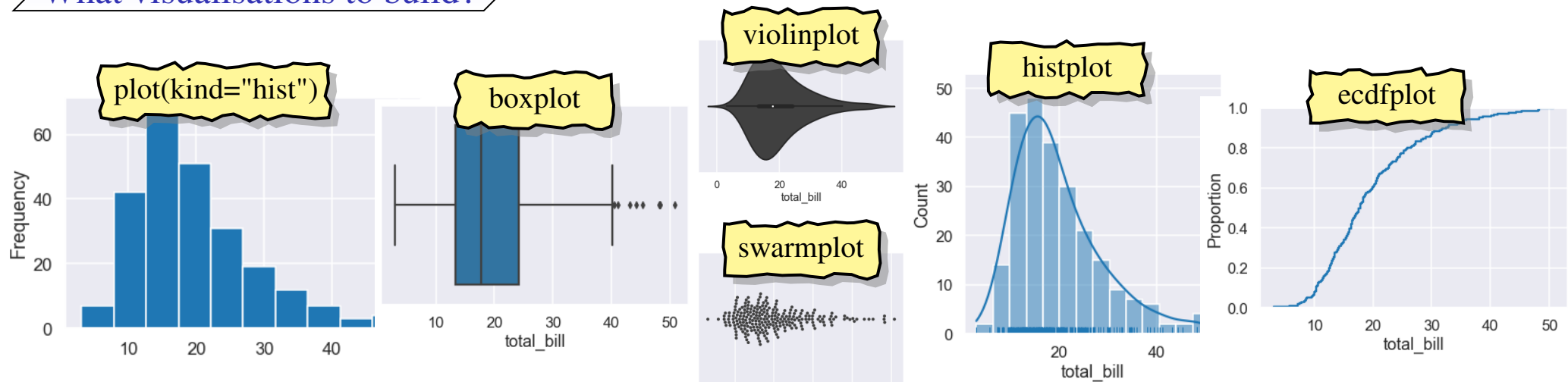
- Data preparation is the core of the data mining pipeline (typical estimates >50% of the time/effort).
- EDA is the data processing and wrangling.
- EDA informs the feature extraction, engineering, transformation and selection.

The Bad News — ‘The curse of choice’

What questions to ask?

Dataset global questions: How many features? How many observations? What is the data type of each feature? Any null values? ... Feature specific questions: What is the distribution of each variable? Do there appear to be outliers? What features are related? ... Missing value questions: Are null value a result of the way data was recorded? Can we drop the rows with null values without it significantly affecting your analysis? Can we justify filling in the missing values with the mean or median for that variable? If the data is time-series data, can we fill the missing values with interpolation? Are there so many missing values for a variable that we should drop that variable from the dataset? ... Outlier questions: Why are outliers present? Do the outliers represent real observations (i.e. not errors)? Should we exclude these observations? If not, should we winsorise the values? ... Correlations/Relationships questions: Which variables are most correlated with your target variable? (If applicable) Is there multicollinearity? (Two features that have a correlation > 0.8) How will this affect your model? Do you have variables that represent the same information? Can one be dropped? ...

What visualisations to build?



Have a plan, be selective, understand strengths/weaknesses of metrics/visualisations

Terminology / Notation

$n + 1$ columns / variables

X

n features / attributes / dimensions

y
target

$\mathbf{x}^{(i)}$

\mathbf{x}_j

m observations /
instances /
cases / rows

PassengerId	Pclass	Name	Sex	Age	SibSp	Parch	Ticket	Fare	Cabin	Embarked	Survived
1	3	Braund, Mr. Owen Harris	male	22.0	1	0	A/5 21171	7.2500	NaN	S	0
2	1	Cumings, Mrs. John Bradley (Florence Briggs Th...	female	38.0	1	0	PC 17599	71.2833	C85	C	1
3	3	Heikkinen, Miss. Laina	female	26.0	0	0	STON/O2. 3101282	7.9250	NaN	S	1
4	1	Futrelle, Mrs. Jacques Heath (Lily May Peel)	female	35.0	1	0	113803	53.1000	C123	S	1
5	3	Allen, Mr. William Henry	male	35.0	0	0	373450	8.0500	NaN	S	0
6	3	Moran, Mr. James	male	NaN	0	0	330877	8.4583	NaN	Q	0
7	1	McCarthy, Mr. Timothy J	male	54.0	0	0	17463	51.8625	E46	S	0
8	3	Palsson, Master. Gosta Leonard	male	2.0	3	1	349909	21.0750	NaN	S	0
9	3	Johnson, Mrs. Oscar W (Elisabeth Vilhelmina Berg)	female	27.0	0	2	347742	11.1333	NaN	S	1
10	2	Nasser, Mrs. Nicholas (Adele Achem)	female	14.0	1	0	237736	30.0708	NaN	C	1
11	3	Sandstrom, Miss. Marguerite Rut	female	4.0	1	1	PP 9549	16.7000	G6	S	1

- A labeled dataset consists of m rows \times $(n + 1)$ columns / variables.
- Use bold to represent vectors and matrices.
- Use subscripts to indicate particular **feature / attribute / column** \mathbf{x}_j
- Use superscript in parenthesis to indicate particular **observation / instance/ case / row** $\mathbf{x}^{(i)}$
- So $x_j^{(i)}$ (or $x_{i,j}$) is the i -th observation in the j -th feature $x_j^{(i)}$

Example Datasets

We will use a few datasets today to illustrate the various features:

Tips

- Small dataset of total bills, and tips for different servers with gender, day, time and group size.
- Clean, no missing values, some outliers.
- Task: exploratory data analysis

Titanic

- Classic dataset with passenger information for the Titanic's fatal voyage, and whether they survived.
- Has missing values and information rich text fields (Name, ticket number).
- Task: classification — predict whether a passenger survived.

Algae Blooms

- Water quality study where samples were taken from different rivers over time.
- Recorded levels of (seven) chemical substances and population of (six) algae species and other information on the sample conditions.
- Task: regression — predict algae population level (7 separate populations).

Tips **dataset**

	total_bill	tip	sex	smoker	day	time	size
0	16.99	1.01	Female	No	Sun	Dinner	2
1	10.34	1.66	Male	No	Sun	Dinner	3
2	21.01	3.50	Male	No	Sun	Dinner	3
3	23.68	3.31	Male	No	Sun	Dinner	2
4	24.59	3.61	Female	No	Sun	Dinner	4
5	25.29	4.71	Male	No	Sun	Dinner	4
6	8.77	2.00	Male	No	Sun	Dinner	2
7	26.88	3.12	Male	No	Sun	Dinner	4
8	15.04	1.96	Male	No	Sun	Dinner	2
9	14.78	3.23	Male	No	Sun	Dinner	2

No target column, so mainly just an exploratory data analysis problem. But questions of interest:

- How do factors **sex**, **smoker**, **day**, **time**, or **size** affect tip / percentage tip?
- Does **size** vary with **day**, **time**, **smoker**?

But some questions don't make sense

- What is the relationship between **sex** and **smoker**? — why should they be related?

This is the downside of automatic EDA tools such as **pandas-profiling** — you will drowned in statistics / charts.

Algae Blooms dataset

	Season	Size	Speed	max_pH	min_O2	mean_Cl	mean_NO3	mean_NH4	mean_oPO4	mean_PO4	mean_Chlor	a1	a2	a3	a4	a5	a6	a7
0	winter	small	medium	8.00	9.8	60.800	6.238	578.00000	105.00000	170.00000	50.000	0.0	0.0	0.0	0.0	34.2	8.3	0.0
1	spring	small	medium	8.35	8.0	57.750	1.288	370.00000	428.75000	558.75000	1.300	1.4	7.6	4.8	1.9	6.7	0.0	2.1
2	autumn	small	medium	8.10	11.4	40.020	5.330	346.66699	125.66700	187.05701	15.600	3.3	53.6	1.9	0.0	0.0	0.0	9.7
3	spring	small	medium	8.07	4.8	77.364	2.302	98.18200	61.18200	138.70000	1.400	3.1	41.0	18.9	0.0	1.4	0.0	1.4
4	autumn	small	medium	8.06	9.0	55.350	10.416	233.70000	58.22200	97.58000	10.500	9.2	2.9	7.5	0.0	7.5	4.1	1.0
5	winter	small	high	8.25	13.1	65.750	9.248	430.00000	18.25000	56.66700	28.400	15.1	14.6	1.4	0.0	22.5	12.6	2.9
6	summer	small	high	8.15	10.3	73.250	1.535	110.00000	61.25000	111.75000	3.200	2.4	1.2	3.2	3.9	5.8	6.8	0.0
7	autumn	small	high	8.05	10.6	59.067	4.990	205.66701	44.66700	77.43400	6.900	18.2	1.6	0.0	0.0	5.5	8.7	0.0
8	winter	small	medium	8.70	3.4	21.950	0.886	102.75000	36.30000	71.00000	5.544	25.4	5.4	2.5	0.0	0.0	0.0	0.0
9	winter	small	medium	8.70	3.4	21.950	0.886	102.75000	36.30000	71.00000	5.544	25.4	5.4	2.5	0.0	0.0	0.0	0.0
10	spring	small	high	7.70	10.2	8.000	1.527	21.57100	12.75000	20.75000	0.800	16.6	0.0	0.0	0.0	1.2	0.0	6.0
11	summer	small	high	7.45	11.7	8.690	1.588	18.42900	10.66700	19.00000	0.600	32.1	0.0	0.0	0.0	0.0	0.0	1.5
12	winter	small	high	7.74	9.6	5.000	1.223	27.28600	12.00000	17.00000	41.000	43.5	0.0	2.1	0.0	1.2	0.0	2.1
13	summer	small	high	7.72	11.8	6.300	1.470	8.00000	16.00000	15.00000	0.500	31.1	1.0	3.4	0.0	1.9	0.0	4.1
14	winter	small	high	7.90	9.6	3.000	1.448	46.20000	13.00000	61.60000	0.300	52.2	5.0	7.8	0.0	4.0	0.0	0.0
15	autumn	small	high	7.55	11.5	4.700	1.320	14.75000	4.25000	98.25000	1.100	69.9	0.0	1.7	0.0	0.0	0.0	0.0
16	winter	small	high	7.78	12.0	7.000	1.420	34.33300	18.66700	50.00000	1.100	46.2	0.0	0.0	1.2	0.0	0.0	0.0
17	spring	small	high	7.61	9.8	7.000	1.443	31.33300	20.00000	57.83300	0.400	31.8	0.0	3.1	4.8	7.7	1.4	7.2
18	summer	small	high	7.35	10.4	7.000	1.718	49.00000	41.50000	61.50000	0.800	50.6	0.0	9.9	4.3	3.6	8.2	2.2
19	spring	small	medium	7.79	3.2	64.000	2.822	8777.59961	564.59998	771.59998	4.500	0.0	0.0	0.0	44.6	0.0	0.0	1.4

How well can we predict the (7) different algae population levels using water sample information?

Titanic dataset

PassengerId	Survived	Pclass	Name	Sex	Age	SibSp	Parch	Ticket	Fare	Cabin	Embarked		
0	1	0	3	Braund, Mr. Owen Harris	male	22.0	1	0	A/5 21171	7.2500	NaN	S	
1	2	1	1	Cumings, Mrs. John Bradley (Florence Briggs Th...	female	38.0	1	0	PC 17599	71.2833	C85	C	
2	3	1	3	Heikkinen, Miss. Laina	female	26.0	0	0	STON/O2. 3101282	7.9250	NaN	S	
3	4	1	1	Futrelle, Mrs. Jacques Heath (Lily May Peel)	female	35.0	1	0	113803	53.1000	C123	S	
4	5	0	3	Allen, Mr. William Henry	male	35.0	0	0	373450	8.0500	NaN	S	
5	6	0	3	Moran, Mr. James	male	NaN	0	0	330877	8.4583	NaN	Q	
6	7	0	1	McCarthy, Mr. Timothy J	male	54.0	0	0	17463	51.8625	E46	S	
7	8	0	3	Palsson, Master. Gosta Leonard	male	2.0	3	1	349909	21.0750	NaN	S	
8	9	1	3	Johnson, Mrs. Oscar W (Elisabeth Vilhelmina Berg)	female	27.0	0	2	347742	11.1333	NaN	S	
9	10	1	2	Nasser, Mrs. Nicholas (Adele Achem)	female	14.0	1	0	237736	30.0708	NaN	C	
10	11	1	3	Sandstrom, Miss. Marguerite Rut	female	4.0	1	1	PP 9549	16.7000	G6	S	
11	12	1	How well can we predict a passenger's survival using information at time of departure?									C103	S
12	13	0								NaN	S		
13	14	0	3	Andersson, Mr. Anders Johan	male	39.0	1	5	347082	31.2750	NaN	S	
14	15	0	3	Vestrom, Miss. Hulda Amanda Adolfina	female	14.0	0	0	350406	7.8542	NaN	S	
15	16	1	2	Hewlett, Mrs. (Mary D Kingcome)	female	55.0	0	0	248706	16.0000	NaN	S	
16	17	0	3	Rice, Master. Eugene	male	2.0	4	1	382652	29.1250	NaN	Q	
17	18	1	2	Williams, Mr. Charles Eugene	male	NaN	0	0	244373	13.0000	NaN	S	
18	19	0	3	Vander Planke, Mrs. Julius (Emelia Maria Vande...	female	31.0	1	0	345763	18.0000	NaN	S	
19	20	1	3	Masselmani, Mrs. Fatima	female	NaN	0	0	2649	7.2250	NaN	C	
20	21	0	2	Fynney, Mr. Joseph J	male	35.0	0	0	239865	26.0000	NaN	S	
21	22	1	2	Beesley, Mr. Lawrence	male	34.0	0	0	248698	13.0000	D56	S	
22	23	1	3	McGowan, Miss. Anna "Annie"	female	15.0	0	0	330923	8.0292	NaN	Q	
23	24	1	1	Sloper, Mr. William Thompson	male	28.0	0	0	113788	35.5000	A6	S	

How well can we predict a passenger's survival using information at time of departure?

Before we start ... Loading libraries

We start by loading in the core data science modules...

```
import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
```

matplotlib is an excellent visualisation library but some plots need additional configuration. seaborn sits above matplotlib and has a collection of visualisations optimised for statistical analysis. ...

```
import seaborn as sns
```

Next, we import some statistical modules ...

```
import scipy.stats as stats
import statsmodels.api as sm
import pingouin as pg
```

`scipy.stats` has a large number of distributions, parametric and nonparametric statistical tests, and descriptive statistics.
`statsmodels` is more focused on estimating statistical models.
`pingouin` overlaps with bits of `scipy.stats` and `statsmodels` but generates more details and nicer visualisations.

Finally we set options ...

```
plt.style.use("seaborn-darkgrid")
```

Before we start ... auto EDA using pandas — profiling

```
from pandas_profiling import ProfileReport
profile = ProfileReport(df, title="Tips Report", html={"style": {"full_width": True}}, sort="None")
profile
```

Summarize dataset: 100%  21/21 [00:05<00:00, 4.00it/s, Completed]

Generate report structure: 100%  1/1 [00:02<00:00, 2.78s/it]

Render HTML: 100%  1/1 [00:00<00:00, 1.72it/s]

pandas-profiling is nice, but see how slow it is on this tiny dataset. What would happen if we had 100K rows x 100 columns?

Tips Report

Overview Variables Interactions Correlations Missing values Sample Duplicate rows

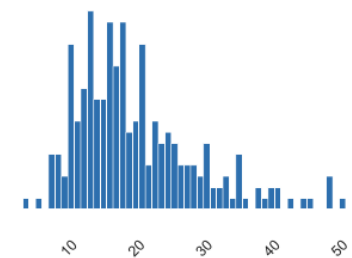
Variables

total_bill

Real number ($\mathbb{R}_{\geq 0}$)

Distinct	229
Distinct (%)	93.9%
Missing	0
Missing (%)	0.0%
Infinite	0
Infinite (%)	0.0%

Mean	19.78594262
Minimum	3.07
Maximum	50.81
Zeros	0
Zeros (%)	0.0%
Memory size	1.9 KiB



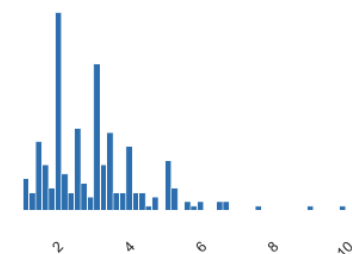
Toggle details

tip

Real number ($\mathbb{R}_{\geq 0}$)

Distinct	123
Distinct (%)	50.4%
Missing	0
Missing (%)	0.0%
Infinite	0
Infinite (%)	0.0%

Mean	2.998278689
Minimum	1
Maximum	10
Zeros	0
Zeros (%)	0.0%
Memory size	1.9 KiB



Before we start ... zero-code EDA using dtale

Using dtale will help you explore data sets while you are building up your python data science skills.

total_bill (float64)

#	Visible	Column Name	Data Type
0	<input checked="" type="checkbox"/>	total_bill	float64
1	<input checked="" type="checkbox"/>	tip	float64
2	<input checked="" type="checkbox"/>	sex	string
3	<input checked="" type="checkbox"/>	smoker	string
4	<input checked="" type="checkbox"/>	day	string
5	<input checked="" type="checkbox"/>	time	string
6	<input checked="" type="checkbox"/>	size	int64

total_bill (float64)

Describe Histogram Categories

Bins (Please edit) 20

total_bill (float64)

Describe Histogram Categories

Code Export

total_bill (float64)

Describe Histogram Categories

Code Export

- Total Rows: 244
 - Count (non-nan): 244
 - Count (missing): 0
 - % Missing: 0
- top: 13.42
 - Frequency: 3
- 25%: 13.3475
- 50%: 17.795
- 75%: 24.1275
- kurt: 1.22 (platykurtic)
- max: 50.81
- mean: 19.7859
- median: 17.795
- min: 3.07
- mode: 13.42
- sem: 0.5699
- skew: 1.13 (highly skewed)
- std: 8.9024
- sum: 4,827.77
- unique: 229
- var: 79.2529
- Sequential Diffs
 - Min: -35.06
 - Average: 0.007366
 - Max: 40.18

values (top 100 most common):

16.69 (2), 10.34 (2), 10.07 (2), 20.69 (2), 13 (2), 15.98 (2), 7.25 (2), 13.81 (2), 17.92 (1), 20.29 (2), 10.33 (2), 21.01 (2), 21.16 (1), 26.86 (1), 20.92 (1), 24.71 (1), 11.02 (1), 13 (1), 21.5 (1), 16 (1), 14.26 (1), 12.9 (1), 8.52 (1), 15.04 (1), 12.46 (1), 15.36 (1), 10.06 (1), 7.51 (1), 22.75 (1), 23.68 (1), 18.24 (1), 32.68 (1), 27.18 (1), 14 (1), 16.47 (1), 13.51 (1), 20.41 (1), 11.01 (1), 25.03 (1), 12.03 (1), 24.03 (1), 24.01 (1), 17.01 (1)

Update Grid

First Pass — Load Dataset and Initial Clean

- Load dataset
- Check variables names
- Verify variable types
- Identify (and possibly address) missing values

Tips — Load

```
df = pd.read_csv("tips.csv")
print(df.shape)
df.head(10)
```

(244, 7)

	total_bill	tip	sex	smoker	day	time	size
0	16.99	1.01	Female	No	Sun	Dinner	2
1	10.34	1.66	Male	No	Sun	Dinner	3
2	21.01	3.50	Male	No	Sun	Dinner	3
3	23.68	3.31	Male	No	Sun	Dinner	2
4	24.59	3.61	Female	No	Sun	Dinner	4
5	25.29	4.71	Male	No	Sun	Dinner	4
6	8.77	2.00	Male	No	Sun	Dinner	2
7	26.88	3.12	Male	No	Sun	Dinner	4
8	15.04	1.96	Male	No	Sun	Dinner	2
9	14.78	3.23	Male	No	Sun	Dinner	2

```
df.info()
```

```
<class 'pandas.core.frame.DataFrame'>
```

```
RangeIndex: 244 entries, 0 to 243
```

```
Data columns (total 7 columns):
```

```
#      Column      Non-Null Count  Dtype
```

```
0      total_bill  244 non-null    float64
```

```
1      tip        244 non-null    float64
```

```
2      sex        244 non-null    object
```

```
3      smoker     244 non-null    object
```

```
4      day        244 non-null    object
```

```
5      time       244 non-null    object
```

```
6      size       244 non-null    int64
```

```
dtypes: float64(2), int64(1), object(4)
```

```
memory usage: 13.5+ KB
```

Issue: categorical data treated as object (string).

Tips — Fix Data Types

I

```
df.sex.unique()
```

```
array(['Female', 'Male'], dtype=object)
```

```
df.sex = pd.Categorical(df.sex)  
df.sex.unique()
```

```
['Female', 'Male']  
Categories (2, object): ['Female', 'Male']
```

```
df.smoker.unique()
```

```
array(['No', 'Yes'], dtype=object)
```

```
df.smoker = pd.Categorical(df.smoker)  
df.smoker.unique()
```

```
['No', 'Yes']  
Categories (2, object): ['No', 'Yes']
```

```
df.day.unique()
```

```
array(['Sun', 'Sat', 'Thur', 'Fri'], dtype=object)
```

```
df.day = pd.Categorical(df.day, categories=['Thur', 'Fri', 'Sun', 'Sat'], ordered=True)  
df.day.unique()
```

```
['Sun', 'Sat', 'Thur', 'Fri']  
Categories (4, object): ['Thur' < 'Fri' < 'Sun' < 'Sat']
```

Tips — fix datatypes

```
df.time = pd.Categorical(df.time, categories=['Lunch', 'Dinner'], ordered=True)
df.time.unique()
```

```
['Dinner', 'Lunch']
Categories (2, object): ['Lunch' < 'Dinner']
```

```
df.info()
```

Converting to category will:

- Simplify visualisation (order can be preserved).
 - Reduce memory usage (not that big a deal for us).
 - Speed up I/O (depending on file format).
- ⇒ Convert to category is a bigger deal for features where the levels have an order.

```
<class 'pandas.core.frame.DataFrame'>
```

```
RangeIndex: 244 entries, 0 to 243
```

```
Data columns (total 7 columns):
```

#	Column	Non-Null Count	Dtype
0	total_bill	244 non-null	float64
1	tip	244 non-null	float64
2	sex	244 non-null	category
3	smoker	244 non-null	category
4	day	244 non-null	category
5	time	244 non-null	category
6	size	244 non-null	int64

```
dtypes: category(4), float64(2), int64(1)
```

```
memory usage: 7.3 KB
```

Titanic — load

- Dataset is split into two parts:
 - `train.csv` — 891 rows with Survived column, used in EDA and model training.
 - `test.csv` — 418 rows without the Survived column, used in competition scoring.

```
df = pd.read_csv("train.csv")
print(df.shape)
df.head(25)
```

	PassengerId	Survived	Pclass	Name	Sex	Age	SibSp	Parch	Ticket	Fare	Cabin	Embarked
0	1	0	3	Braund, Mr. Owen Harris	male	22.0	1	0	A/5 21171	7.2500	NaN	S
1	2	1	1	Cumings, Mrs. John Bradley (Florence Briggs Th...	female	38.0	1	0	PC 17599	71.2833	C85	C
2	3	1	3	Heikkinen, Miss. Laina	female	26.0	0	0	STON/O2. 3101282	7.9250	NaN	S
3	4	1	1	Futrelle, Mrs. Jacques Heath (Lily May Peel)	female	35.0	1	0	113803	53.1000	C123	S
4	5	0	3	Allen, Mr. William Henry	male	35.0	0	0	373450	8.0500	NaN	S

- We could convert `Sex` or `Embarked`, to a category, but since their levels are not ordered there is no big advantage.
- We don't want to convert `Name`, `Ticket` and `Cabin` since we want to perform further text processing on these columns. For example, extracting title (Capt, Mr, Miss, etc.) out of `Name`.
- We have missing values (**that are plausibly linked to target**) that we need to deal with.

```
df.info()
```

```
<class 'pandas.core.frame.DataFrame'>
```

```
RangeIndex: 891 entries, 0 to 890
```

```
Data columns (total 12 columns):
```

```
#      Column      Non-Null Count  Dtype
```

```
-----
```

0	PassengerId	891 non-null	int64
1	Survived	891 non-null	int64
2	Pclass	891 non-null	int64
3	Name	891 non-null	object
4	Sex	891 non-null	object
5	Age	714 non-null	float64
6	SibSp	891 non-null	int64
7	Parch	891 non-null	int64
8	Ticket	891 non-null	object
9	Fare	891 non-null	float64
10	Cabin	204 non-null	object
11	Embarked	889 non-null	object

```
dtypes: float64(2), int64(5), object(5)
```

```
memory usage: 83.7+ KB
```

Algae_Blooms – load

<https://archive.ics.uci.edu/ml/datasets/Coil+1999+Competition+Data>

Read `instructions.txt`, and download the `*.data` files.

UCI Machine Learning Repository: Coil 1999 Competition Data Data Set

UCI Machine Learning Repository
Center for Machine Learning and Intelligent Systems

Coil 1999 Competition Data Data Set
Download: [Data Folder](#), [Data Set Description](#)

Abstract: This data set is from the 1999 Computational Intelligence and Learning (COIL) competition. The data contains measurements of river chemical concentrations and algae densities.

Data Set Characteristics:	Multivariate	Number of Instances:	340	Area:	Physical
Attribute Characteristics:	Categorical, Real	Number of Attributes:	17	Date Donated	1999-09-09
Associated Tasks:	N/A	Missing Values?	No	Number of Web Hits:	52986

Source:

Original Owner:

ERUDIT
European Network for Fuzzy Logic and Uncertainty Modelling
<http://www.erudit.de/>

Donor:

Jens Strackeljan
Technical University Clausthal
Institute of Applied Mechanics
Graupenstr. 3, 38678 Clausthal-Zellerfeld, Germany
tmjs '@' itm.tu-clausthal.de

Data Set Information:

This data comes from a water quality study where samples were taken from rivers. The data includes measurements of chemical substances including: nitrogen in the form of nitrates, nitrites, and ammonia.

The competition involved the prediction of algal frequency distribution when the sample was taken, the river size and its flow velocity.

archive.ics.uci.edu

Index of /ml/machine-learning-databases/coil-mld

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- [analysis.data](#)
- [coil.data.html](#)
- [coil.html](#)
- [eval.data](#)
- [instructions.txt](#)
- [r2](#)
- [results.data](#)
- [results.htm](#)
- [results.txt](#)

Apache/2.4.6 (CentOS) OpenSSL/1.0.2k-fips SVN/1.7.14 Phusion_Passenger/4.0.53 mod_perl/2.0.11 Perl/v5.16.3 Server at archive.ics.uci.edu Port 443

Algae_Blooms — load (1st attempt)

Pandas function `pd.read_table`, is a more general function than `read_csv`.

```
df = pd.read_table('src/Analysis.txt')
print(df.shape)
df.head()
```

(199, 1)

	winter	small	medium	8.00000	9.80000	60.80000	6.23800	578.00000	105.00000	170.00000	50.00000	0.00000	0.00000	0.00000	0.00000	34.20000	8.30000	0.00000
0	spring	small	medium	8.35000	...													
1	autumn	small	medium	8.10000	1...													
2	spring	small	medium	8.07000	...													
3	autumn	small	medium	8.06000	...													
4	winter	small	high	8.25000	13...													

Two problems, first row was treated as column headers, and we need to specify the character(s) used to separate columns

Algae_Blooms — load (2nd attempt)

```
df = pd.read_table('src/Analysis.txt', sep='\s+', header=None)
print(df.shape)
df.head()
```

(200, 18)

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17
0	winter	small	medium	8.00000	9.80000	60.80000	6.23800	578.00000	105.00000	170.00000	50.00000	0.0	0.0	0.0	0.0	34.2	8.3	0.0
1	spring	small	medium	8.35000	8.00000	57.75000	1.28800	370.00000	428.75000	558.75000	1.30000	1.4	7.6	4.8	1.9	6.7	0.0	2.1
2	autumn	small	medium	8.10000	11.40000	40.02000	5.33000	346.66699	125.66700	187.05701	15.60000	3.3	53.6	1.9	0.0	0.0	0.0	9.7
3	spring	small	medium	8.07000	4.80000	77.36400	2.30200	98.18200	61.18200	138.70000	1.40000	3.1	41.0	18.9	0.0	1.4	0.0	1.4
4	autumn	small	medium	8.06000	9.00000	55.35000	10.41600	233.70000	58.22200	97.58000	10.50000	9.2	2.9	7.5	0.0	7.5	4.1	1.0

- Now, notice that the number of data row changed from 199 to 200 since the first row is now counted as a data row. And now we are using default columns names.
- The "\s+" matches one or more spaces. This is an example of a regex.
- We need to name the columns.

Algae_Blooms — load (3rd attempt)

IV

```
names = ('Season', 'Size', 'Speed', 'max_pH', 'min_O2', 'mean_Cl', 'mean_NO3', 'mean_NH4', 'mean_oPO4',
         'mean_PO4', 'mean_Chlor', 'a1', 'a2', 'a3', 'a4', 'a5', 'a6', 'a7')
```

```
df = pd.read_table('src/Analysis.txt', sep='\s+', names=names)
```

```
print(df.shape)
```

```
df.head()
```

(200, 18)

	Season	Size	Speed	max_pH	min_O2	mean_Cl	mean_NO3	mean_NH4	mean_oPO4	mean_PO4	mean_Chlor	a1	a2	a3	a4	a5	a6	a7
0	winter	small	medium	8.00000	9.80000	60.80000	6.23800	578.00000	105.00000	170.00000	50.00000	0.0	0.0	0.0	0.0	34.2	8.3	0.0
1	spring	small	medium	8.35000	8.00000	57.75000	1.28800	370.00000										
2	autumn	small	medium	8.10000	11.40000	40.02000	5.33000	346.6669										
3	spring	small	medium	8.07000	4.80000	77.36400	2.30200	98.18200										
4	autumn	small	medium	8.06000	9.00000	55.35000	10.41600	233.7000										

```
<class 'pandas.core.frame.DataFrame'>
```

```
RangeIndex: 200 entries, 0 to 199
```

```
Data columns (total 18 columns):
```

#	Column	Non-Null Count	Dtype
0	Season	200 non-null	object
1	Size	200 non-null	object
2	Speed	200 non-null	object
3	max_pH	200 non-null	object
4	min_O2	200 non-null	object
5	mean_Cl	200 non-null	object
6	mean_NO3	200 non-null	object
7	mean_NH4	200 non-null	object
8	mean_oPO4	200 non-null	object
9	mean_PO4	200 non-null	object
10	mean_Chlor	200 non-null	object
11	a1	200 non-null	float64
12	a2	200 non-null	float64

Dataframe looks a bit better, but why are numeric columns converted as **object**?
Reading instructions.txt we see that missing values are indicated by XXXXXX.

Algae_Blooms — load (4th attempt)

V

```
names = ('Season', 'Size', 'Speed', 'max_pH', 'min_O2', 'mean_Cl', 'mean_NO3', 'mean_NH4', 'mean_oP04',
         'mean_P04', 'mean_Chlor', 'a1', 'a2', 'a3', 'a4', 'a5', 'a6', 'a7')
```

```
df = pd.read_table('src/Analysis.txt', sep='\s+', names=names, na_values='XXXXXXX')
```

```
print(df.shape)
```

```
df.head()
```

(200, 18)

	Season	Size	Speed	max_pH	min_O2	mean_Cl	mean_NO3	mean_NH4	mean_oP04	mean_P04	mean_Chlor	a1	a2	a3	a4	a5	a6	a7
0	winter	small	medium	8.00	9.8	60.800	6.238	578.00000	105.000	170.00000	50.0	0.0	0.0	0.0	0.0	34.2	8.3	0.0
1	spring	small	medium	8.35	8.0	57.750	1.288	370.0000										
2	autumn	small	medium	8.10	11.4	40.020	5.330	346.6669										
3	spring	small	medium	8.07	4.8	77.364	2.302	98.18200										
4	autumn	small	medium	8.06	9.0	55.350	10.416	233.7000										

Now some variables have missing values

Also we should convert Season, Size and Speed to category and ensure the levels are ordered.

```
<class 'pandas.core.frame.DataFrame'>
```

```
RangeIndex: 200 entries, 0 to 199
```

```
Data columns (total 18 columns):
```

```
#    Column    Non-Null Count  Dtype
```

```

0    Season    200 non-null    object
1    Size      200 non-null    object
2    Speed     200 non-null    object
3    max_pH    199 non-null    float64
4    min_O2    198 non-null    float64
5    mean_Cl   190 non-null    float64
6    mean_NO3  198 non-null    float64
7    mean_NH4  198 non-null    float64
8    mean_oP04 198 non-null    float64
9    mean_P04  198 non-null    float64
10   mean_Chlor 188 non-null    float64
11   a1         200 non-null    float64
12   a2         200 non-null    float64
13   a3         200 non-null    float64
14   a4         200 non-null    float64
15   a5         200 non-null    float64
16   a6         200 non-null    float64
17   a7         200 non-null    float64
```

Algae_Blooms — Fix Data Types

II

The three categorical variables have levels with a natural order \Rightarrow convert to category and specify order:

```
df.Season = pd.Categorical(df.Season, categories=['spring', 'summer', 'autumn', 'winter'], ordered=True)
print(df.Season.unique())
```

```
['winter', 'spring', 'autumn', 'summer']
Categories (4, object): ['spring' < 'summer' < 'autumn' < 'winter']
```

```
df.Size = pd.Categorical(df.Size, categories=['small', 'medium', 'large'], ordered=True)
print(df.Size.unique())
```

```
['small', 'medium', 'large']
Categories (3, object): ['small' < 'medium' < 'large']
```

```
df.Speed = pd.Categorical(df.Speed, categories=['low', 'medium', 'high'], ordered=True)
print(df.Speed.unique())
```

```
['medium', 'high', 'low']
Categories (3, object): ['low' < 'medium' < 'high']
```

Algae_Blooms — Identification of Missing Values (NA)

1 Which columns have missing values?

```
df.isna().sum()
```

```
Season      0
Size        0
Speed       0
max_pH      1
min_O2      2
mean_Cl     10
mean_NO3    2
mean_NH4    2
mean_oPO4   2
mean_PO4    2
mean_Chlor  12
a1          0
a2          0
a3          0
a4          0
a5          0
a6          0
a7          0
dtype: int64
```

- Two columns (features) account for 22 NAs, but cannot just drop them as will lose a lot of information.
- Two rows (observations) account for 12 NAs \Rightarrow remove.
- Removing other rows with a NA will result in a loss of 14 rows (7% of the data), instead will impute later.

2 Which rows have missing values?
How many NAs per row?

```
df.isna().sum(axis=1).value_counts()
```

```
0      184
2        7
1        7
6         2
dtype: int64
```

4 Rows / Cols to drop?

```
df.loc[df.isna().sum(axis=1)==6]
```

	Season	Size	Speed	max_pH	min_O2	mean_Cl	mean_NO3	mean_NH4	mean_oPO4	mean_PO4	mean_Chlor	a1	a2	a3	a4
61	summer	small	medium	6.4	NaN	NaN	NaN	NaN	NaN	14.0	NaN	19.4	0.0	0.0	2.0
198	winter	large	medium	8.0	7.6	NaN	NaN	NaN	NaN	NaN	NaN	0.0	12.5	3.7	1.0

```
df = df.loc[df.isna().sum(axis=1)<6].copy()
print(df.shape)
```

```
(198, 18)
```

After Loading and Initial Clean — Where are we?

Tips

- ✓ Loaded data, corrected dtypes (categorical with order levels)
- ✓ Sanitised column names — not needed, but note column name size shadows pandas dataframe function size \Rightarrow so use `df["size"]` instead of `df.size`.
- ✓ No missing values

Titanic

- ✓ Loaded data — no conversion of dtypes needed (but if you don't plots/crosstab order won't agree)
- ✓ Sanitised column names — not needed,
 - Missing values in Age (177/891=20%), Cabin (687/891=77%), and Embarked (2/891=0.2%).
 - A feature with 77% missing values should be considered for deletion, but what if the presence of a missing value actually tells us something? \Rightarrow convert to a boolean feature.

Algae Blooms

- ✓ Loaded data, corrected dtypes (categorical with ordered levels)
- ✓ Sanitised column names.
 - Missing values
 - Removed two rows with 6 NA each, accounted for 12/33=36% of the missing values.
 - Remaining, 21 NAs are concentrated in mean_CL (8) and mean_Chlor (10). EDA will suggest options.

After Loading and Initial Clean — Where are we?

II

Next we might

- Save result of initial clean:
 - To either a CSV (if we don't mind losing dtype metadata)

```
df.to_csv('data/Analysis.csv', index=False)
```

- To (say) pickle format (to keep dtype metadata)

```
df.to_pickle('data/Analysis.pkl')
```

Later can read dataframe back in using

```
df = pd.read_pickle('data/Analysis.pkl')  
print(df.shape)  
df.head(1)
```

- If the dataset is large (>100K rows), save a (reproducible) sample of the dataset for later EDA to speed up calculations (especially visualisations).

```
df.sample(frac=.25, random_state=42).to_pickle('data/Analysis_sample.pkl')
```

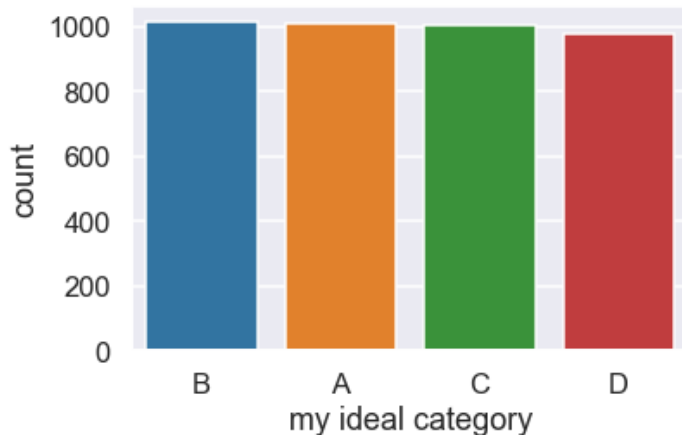
A Selection of Statistical Visualisations and Metrics

Relationship to Target			
	Feature	Categorical	Numerical
Categorical	nunique, unique, describe, value_counts, ...	crosstab, ...	boxplot, ...
	countplot, ...	countplot, ...	catplot, boxplot, ...
Numerical	describe, ...	groupby+describe, ...	correlations, ...
	histplot, boxplot, displot, qqplot, ...	catplot, boxplot, ...	lmpplot, ...

Categorical Variables

The Ideal

- Each level equally likely.
- Not too many levels: 2–12(ish).



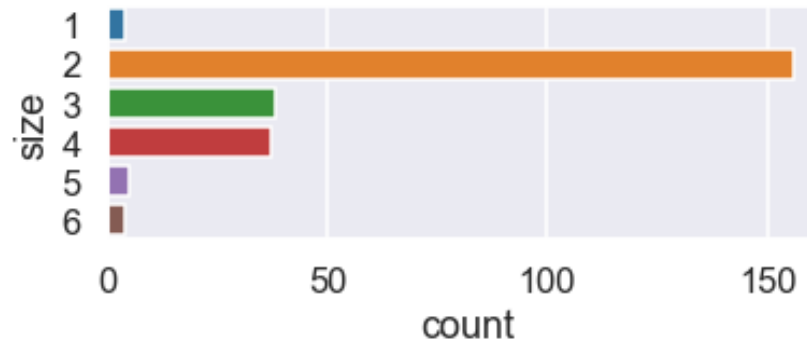
Tools

- `nunique`, `unique`, `value_counts`.
- `sns.countplot` — shows the counts of observations in each categorical level using bars.

Reality

```
sns.countplot(y="size", data=df);
```

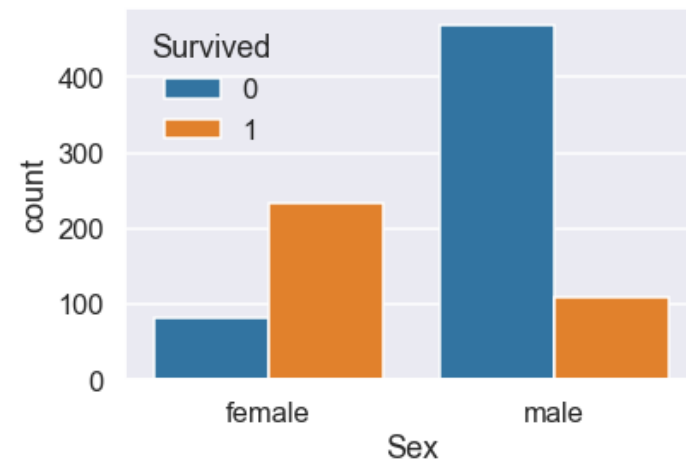
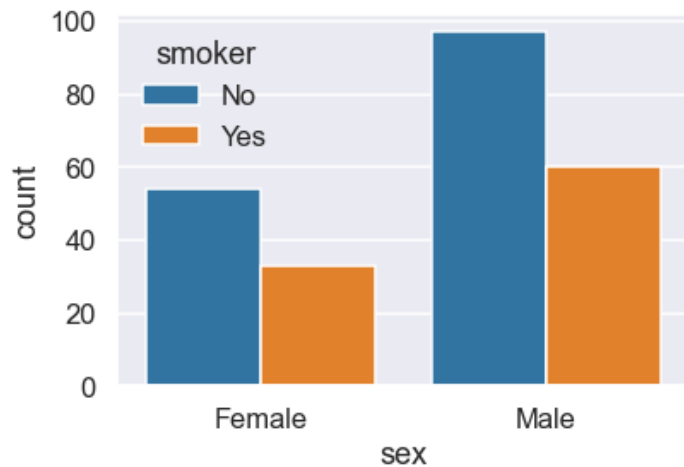
Tips



- If size was the target, then most models will train towards the majority class (`size=2`).
- If size was a feature, then quality of predictor could vary greatly depending on the feature categorical level.
- Consider merge/drop rare category levels.

Categorical Variables — Relationship with (Categorical) Target

`sns.countplot(x="Sex", hue="Survived", data=df);`



`pd.crosstab(columns=df.Sex, index=df.Survived, margins=True, normalize='columns') \`
`.style.format("{:.2%}).background_gradient(cmap='summer_r')`

sex	Female	Male	All
smoker			
No	62.07%	61.78%	61.89%
Yes	37.93%	38.22%	38.11%

No relationship between sex and smoker

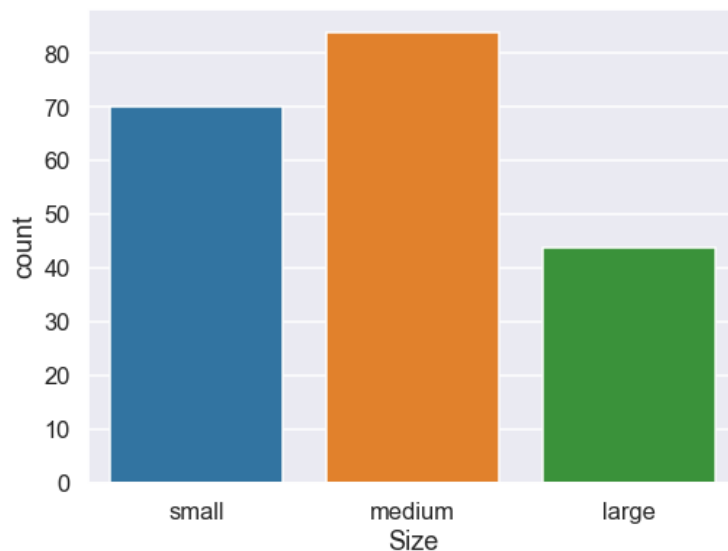
Sex	female	male	All
Survived			
0	25.80%	81.11%	61.62%
1	74.20%	18.89%	38.38%

Strong relationship between Sex and Survived

Categorical Variables — Relationship with (Numerical) Target

I

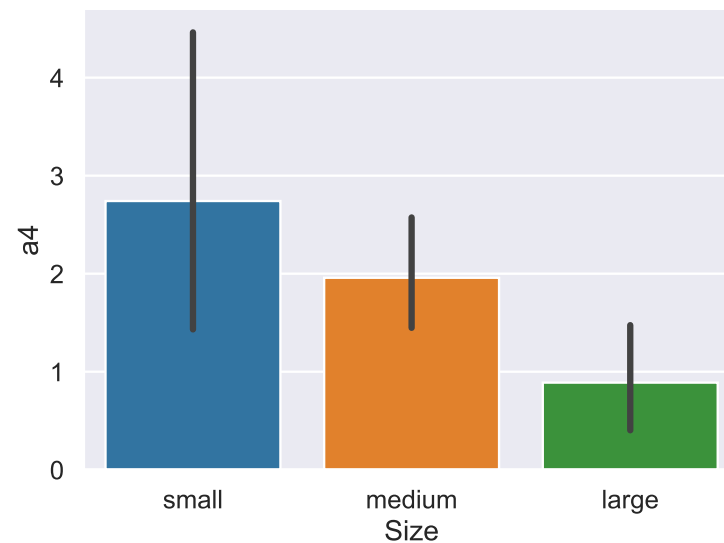
```
sns.countplot(x="Size", data=df);
```



- Shows the counts of observations in each categorical level using bar (height/width).

Is it usable?

```
sns.catplot(x="Size", y="a4", data=df, kind='bar');
```



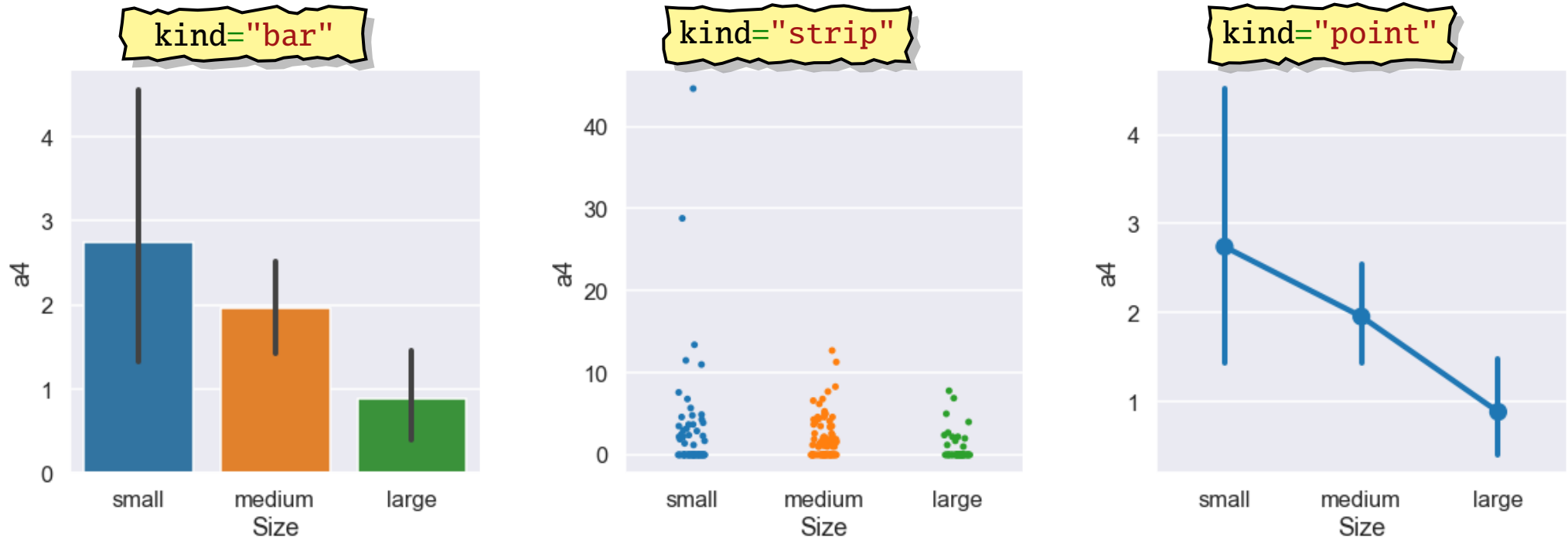
- Shows the average level (mean) and uncertainty (std) of the numerical target (a4) in each categorical level of the categorical variable.
- Vertical bar shows 95% confidence interval.

Is it useful?

Categorical Variables — Relationship with (Numerical) Target

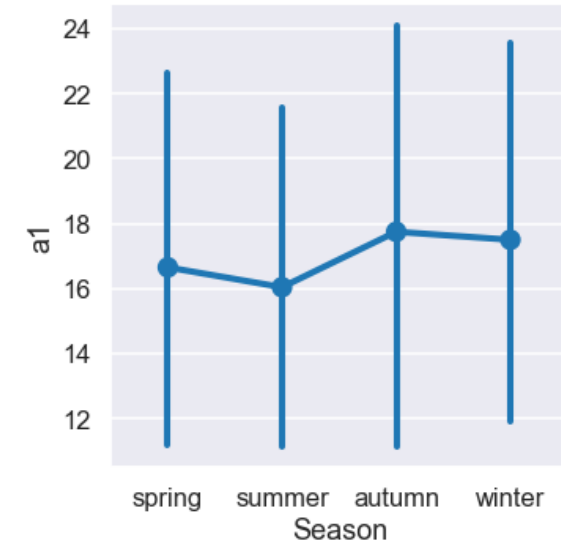
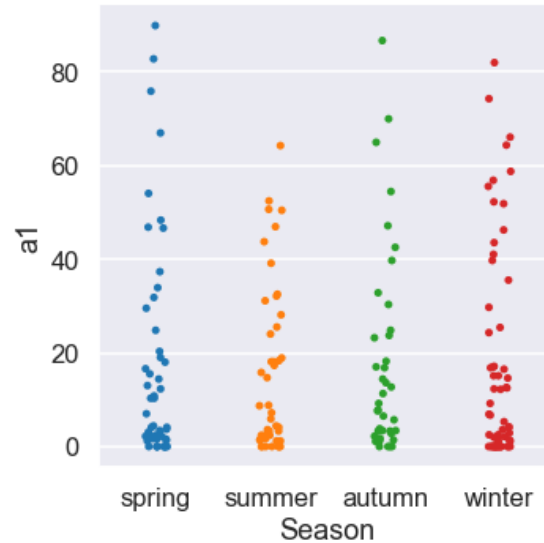
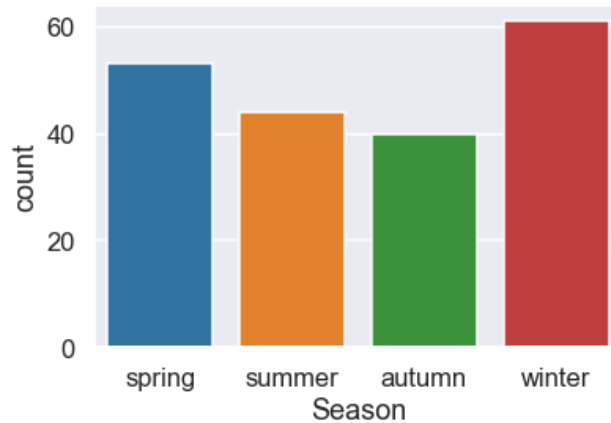
II

The option `kind` in `catplot` can be:



- bar and point show essentially the same information, but point is more compact when comparing multiple categorical features to a continuous target on the same plot.
- strip shows individual observations — useful (as in this case) to show that the larger uncertainty in `Size="small"` observations is mainly due to two outliers.

Example — Dataset: Algae Blooms, Feature: Season, Target: a1

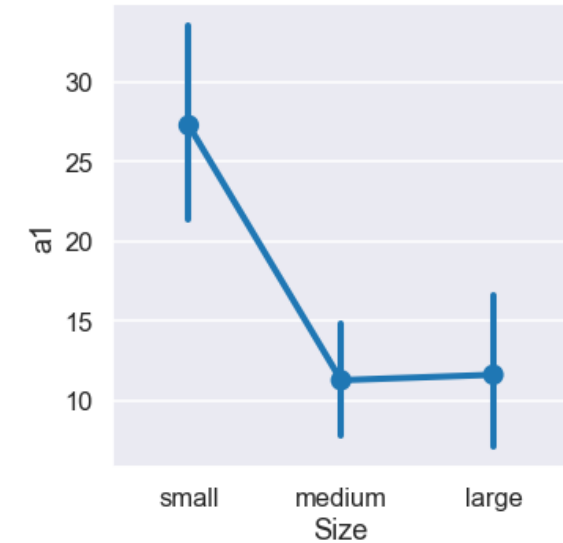
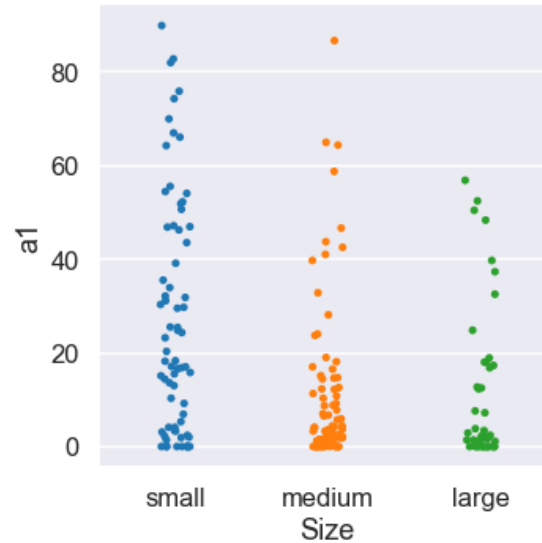
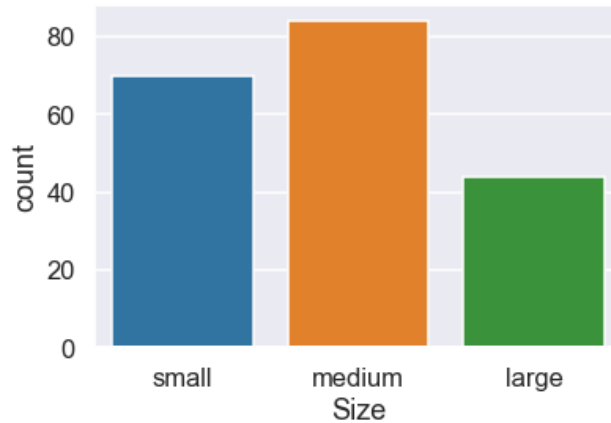


```
df.groupby("Season")["a1"].agg(["mean", "count", "std"])
```

	mean count		std
Season	\bar{x}	n	σ
spring	16.649057	53	23.093786
summer	16.038636	44	17.920798
autumn	17.745000	40	21.611203
winter	17.498361	61	22.568256

- Countplot shows no issues with feature **Season** — all levels approximately equally represented.
 - Catplots show slightly less spread in **a1** for **Season="summer"** observations. (**strip** shows smaller range, **point** shows smaller standard deviation).
- ⇒ Mean levels of **a1** for different levels of **Season** are well within the 95% confidence intervals ($\bar{x} \pm \sigma 1.96/\sqrt{n}$), so no/weak relationship between categorical feature and numerical target.

Example — Dataset: Algae Blooms, Feature: Size, Target: a1



```
df.groupby("Size")["a1"].agg(["min", "max", "mean", "count", "std"])
```

	min	max	mean	count	std
Size			\bar{x}	n	σ
small	0.0	89.8	27.255714	70	24.895426
medium	0.0	86.6	11.267857	84	17.163124
large	0.0	56.8	11.611364	44	16.556123

- Countplot shows no issues with feature Size.
 - Catplot (point) shows that levels of a1 are higher for Size="small" observations.
- ⇒ Confidence interval for Size="small" observations do not overlap with CI for other levels, so significant relationship between categorical feature and numerical target.

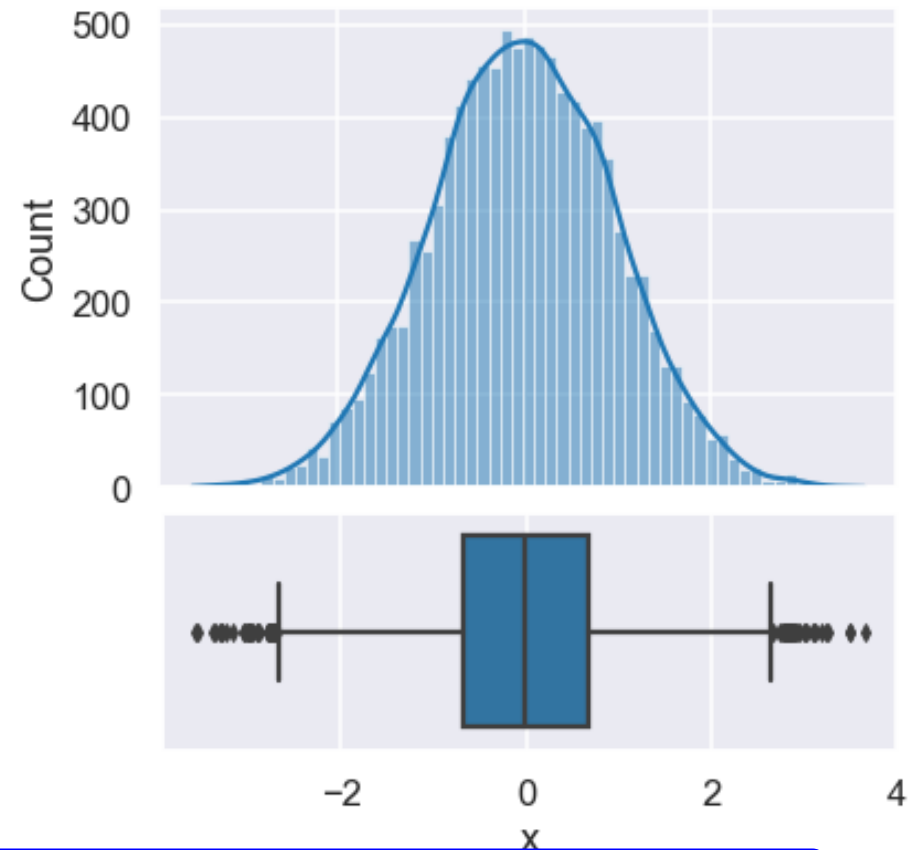
Numerical Variables

Things here are more complicated as a numerical variable could follow many different distributions. Here we look at data following the standard normal distribution. To start we generate 10,000 values and put in to new DataFrame, df2.

```
rv = stats.norm()
data = rv.rvs(size=10_000)
df2 = pd.DataFrame(data, columns=["x"])
df2.head(5)
```

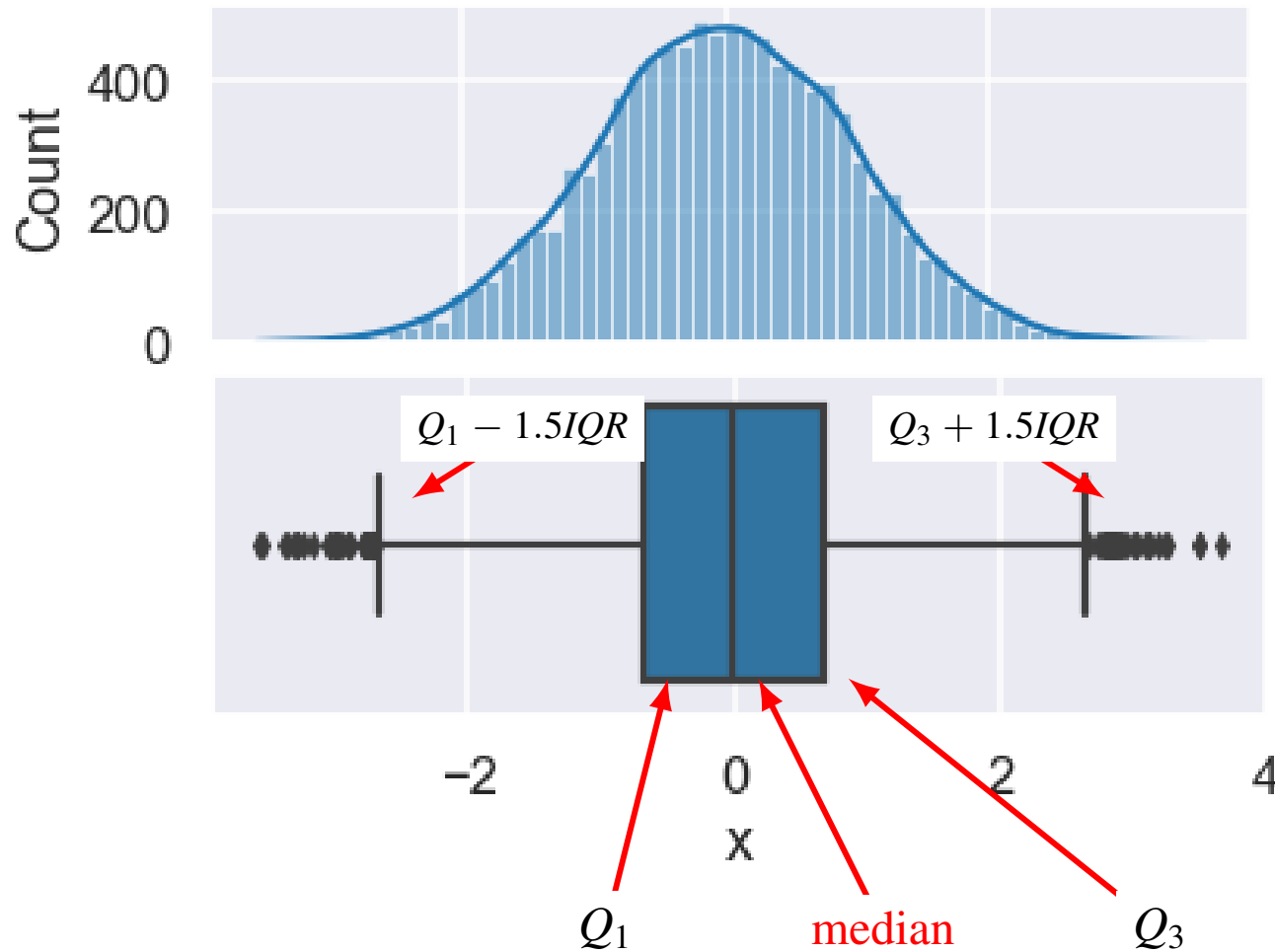
	x
0	-0.440553
1	0.507263
2	2.791102
3	0.157782
4	-2.740130

```
sns.histplot(x="x", data=df2, kde=True);
```



```
sns.boxplot(x="x", data=df2);
```

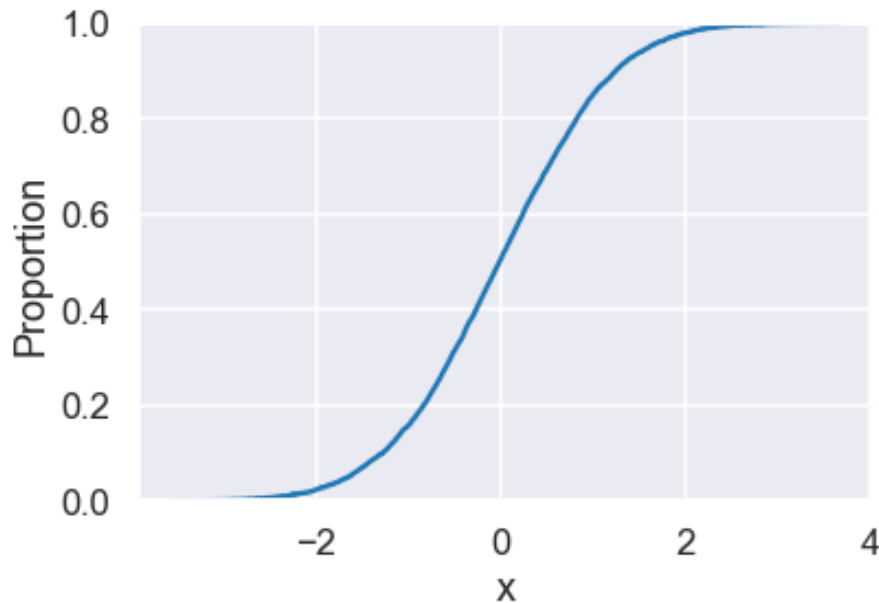
Histplot (Histogram) and Boxplot



- Histogram is useful in depicting location, spread and shape.
- Curve, is estimate of shape given infinite data and infinite number of bins.
- Boxplots also depicts location, spread and shape, but uses median for estimate of centre, and quartiles for spread.
- Half the data is within the box, data points outside the whiskers (lines) are possible outliers, denoted by circles.

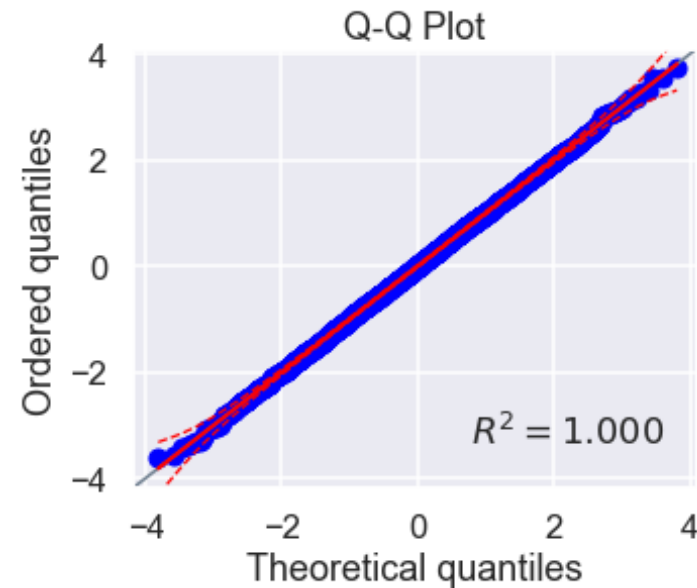
Cumulative Plot and QQ-Plot

```
sns.ecdfplot(data=df2, x="x");
```



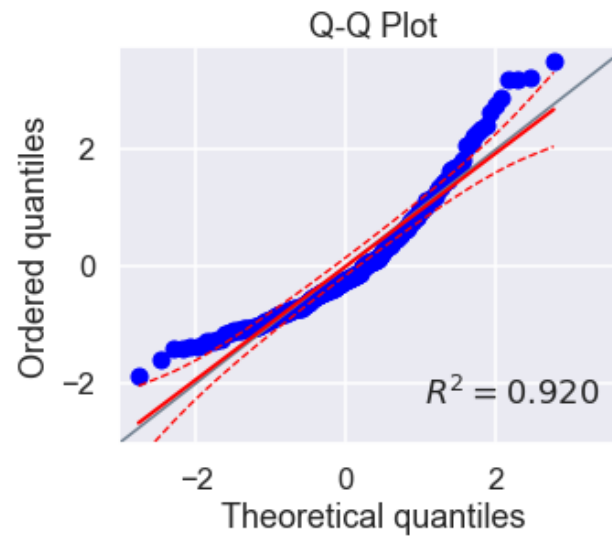
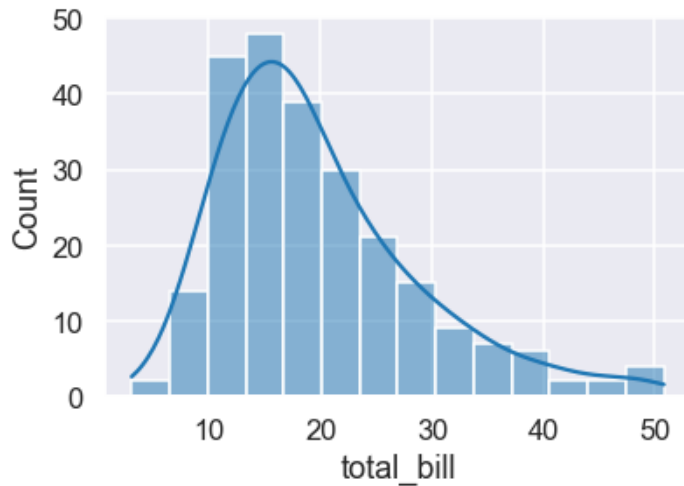
- Represents the proportion of observations less than or equal to given value.

```
import pingouin as pg  
pg.qqplot(df2.x);
```



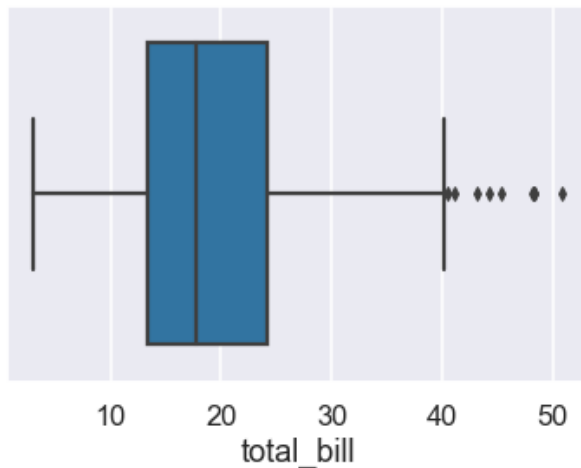
- Plot of observed quantiles against theoretical (assuming normal) quantiles. If both sets of quantiles came from the same distribution, we should see the points forming a line that's roughly straight.

Example — Dataset: Tips, Feature: total_bill



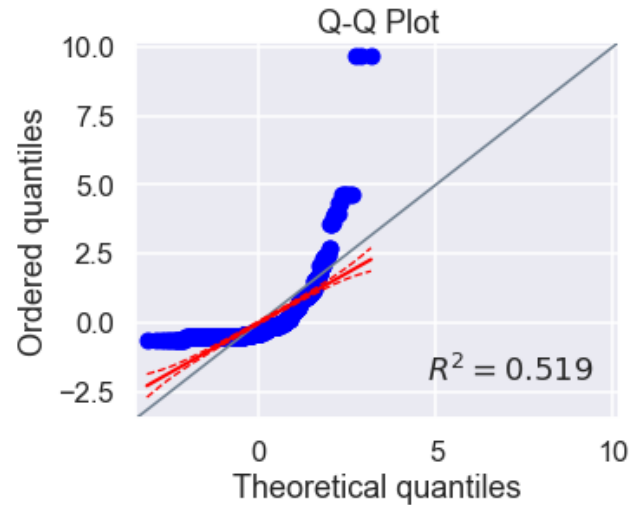
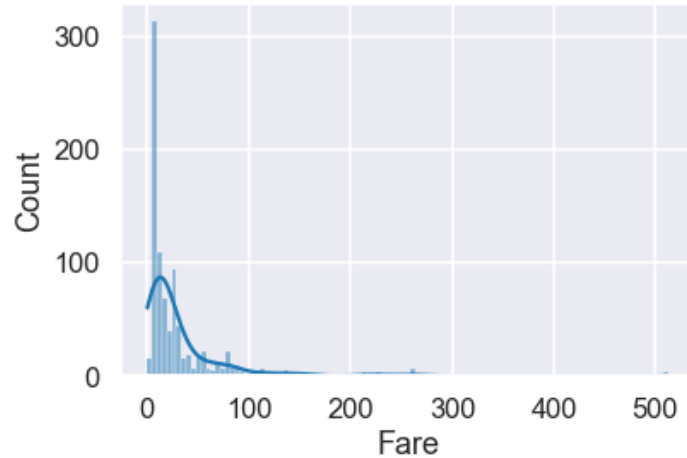
`df.total_bill.describe()`

```
count    244.000000
mean      19.785943
std       8.902412
min       3.070000
25%      13.347500
50%      17.795000
75%      24.127500
max      50.810000
Name: total_bill, dtype: float64
```



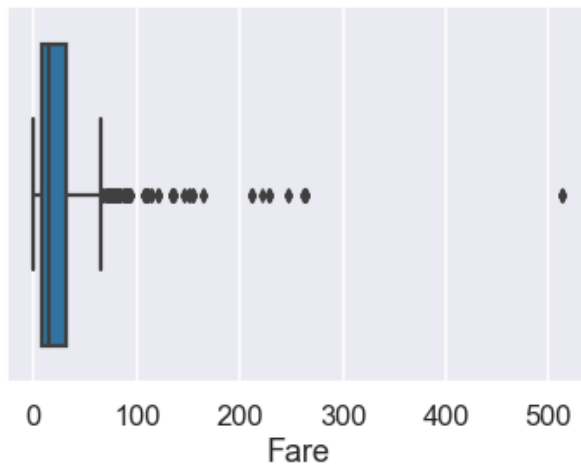
- Data is bell curve shaped, but right skewed (data is more spread out to the right).
- Outliers to the right.
- QQ-Plot indicate that data is not normal, but we could transform it to be more closer to normal.

Example — Dataset: Titanic, Feature: Fare



`df.Fare.describe()`

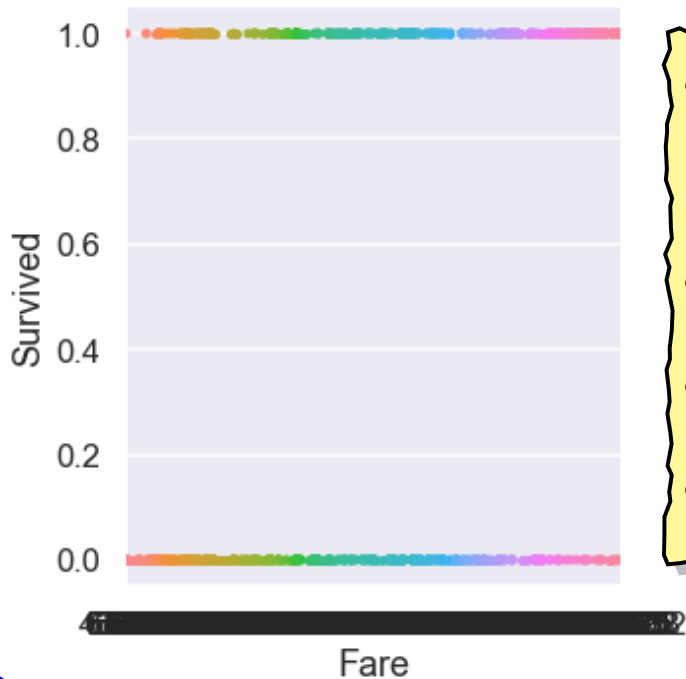
```
count    891.000000
mean      32.204208
std       49.693429
min        0.000000
25%        7.910400
50%       14.454200
75%       31.000000
max      512.329200
Name: Fare, dtype: float64
```



- This variable is more skewed and dominated by its outliers which need to be resolved.

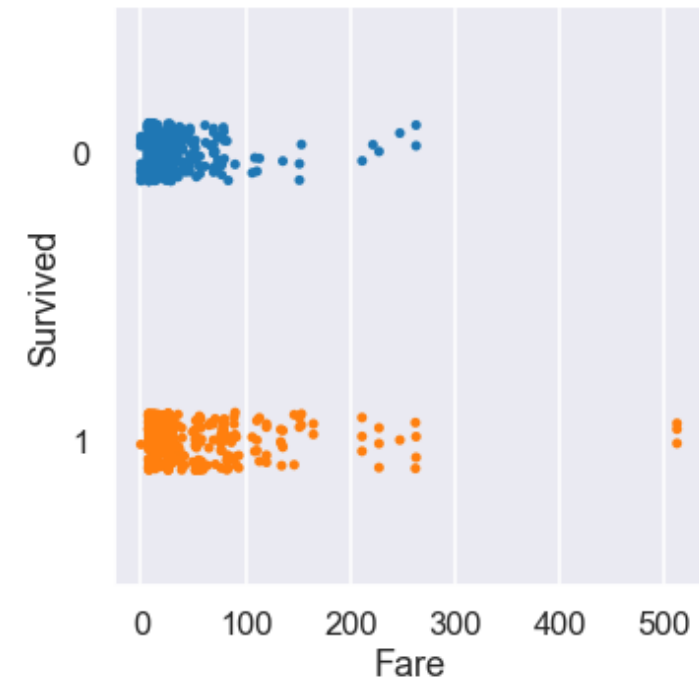
Warning — Plot Output Depends on Data Assumptions

```
df = pd.read_csv("train.csv")
sns.catplot(data=df, x="Fare", y="Survived");
```



- seaborn tries to infer the correct graph based on the data values/type, but it does not always get it correct.
- Survived stores 0 and 1 and has dtype `int`.
- Converting to a Categorical with numeric levels is not enough.
- `astype(str)` converts `0` and `1` to `"0"` and `"1"`.

```
df = pd.read_csv("train.csv")
df.Survived = df.Survived.astype(str)
sns.catplot(data=df, x="Fare", y="Survived");
```



```
df = pd.read_csv("train.csv")
df.Survived = pd.Categorical(df.Survived)
sns.catplot(data=df, x="Fare", y="Survived");
```

Second Pass — Individual Features and Target

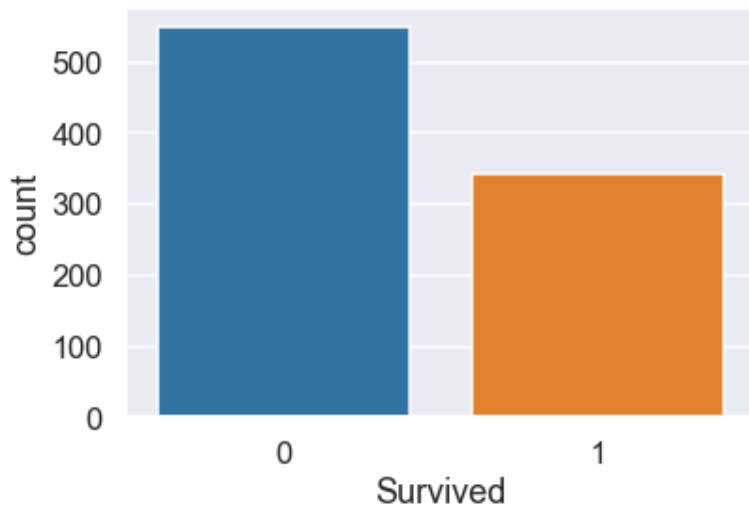
- Categorical vs numerical target
 - Categorical vs numerical features
 - Identify (and possibly address) issues
 - Relationship to target.
- } Is it usable?
- } Is it useful?

Dataset: Titanic, Target: Survived

```
df.Survived.value_counts(normalize=True, dropna=False)
```

```
0    0.616162  
1    0.383838  
Name: Survived, dtype: float64
```

```
sns.countplot(x="Survived", data=df);
```



```
df.Survived.describe()
```

```
[0, 1]  
Categories (2, int64): [0, 1]
```

```
df.Survived.unique()
```

```
count    891  
unique    2  
top       0  
freq     549  
Name: Survived, dtype: int64
```

- Simplest classification problem (two classes) with both classes nearly equal frequency.
- In a **unbalanced** classification problem where the minority class occurs about 20% or lower, models can focus on the majority class.

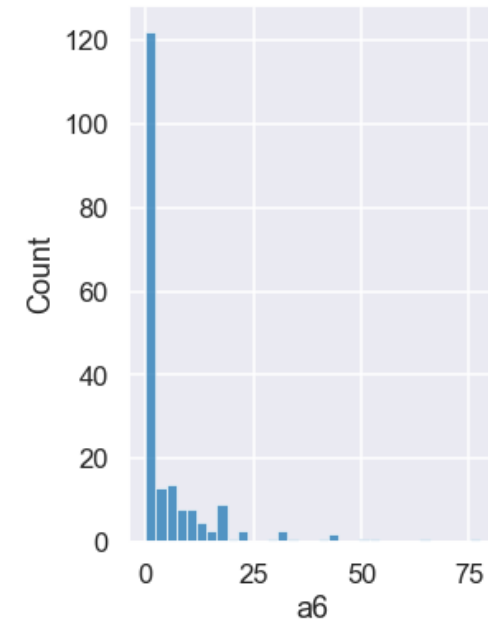
Dataset: Algae Blooms, Target: a1,..., a7

```
targets = [c for c in df.columns if c[0]=="a"]
targets
```

```
df[targets].describe()
```

	a1	a2	a3	a4	a5	a6	a7
count	198.000000	198.000000	198.000000	198.000000	198.000000	198.000000	198.000000
mean	16.996465	7.470707	4.334343	1.997475	5.115657	6.004545	2.487374
std	21.421713	11.065461	6.976788	4.439205	7.511846	11.711053	5.181536
min	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000
25%	1.525000	0.000000	0.000000	0.000000	0.000000	0.000000	0.000000
50%	6.950000	3.000000	1.550000	0.000000	2.000000	0.000000	1.000000
75%	24.800000	11.275000	4.975000	2.400000	7.500000	6.975000	2.400000
max	89.800000	72.600000	42.800000	44.600000	44.400000	77.600000	31.600000

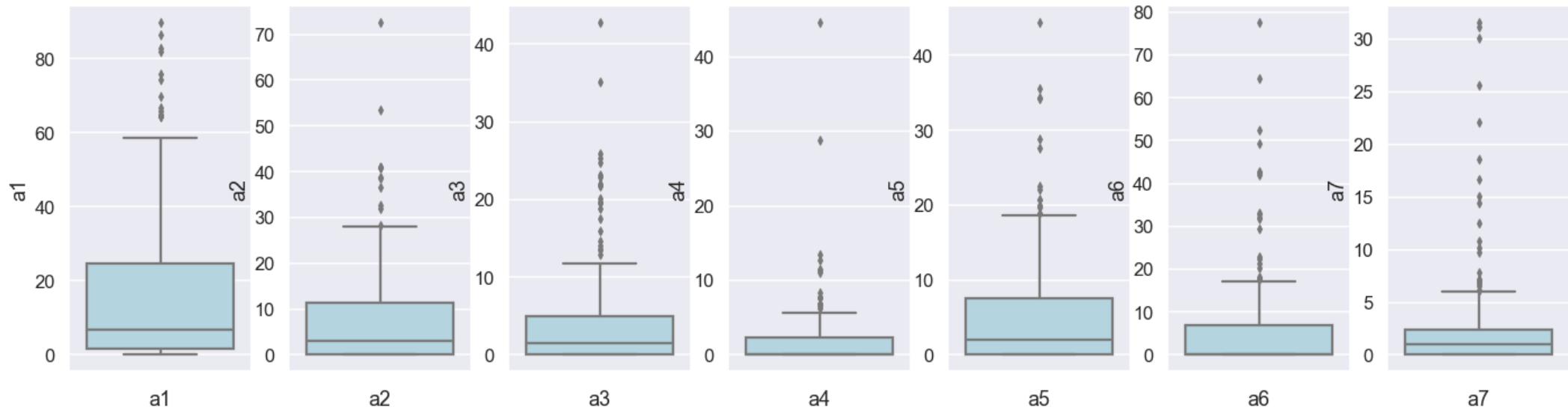
```
plt.figure(figsize=(4,6))
sns.histplot(x="a6", data=df);
```



All distributions are heavily skewed to the right, many with outliers (see next slide). All of the zero measurements are probably due to population levels too low to be measured.

Dataset: Algae Blooms, Target: a_1, \dots, a_7

```
fig, axs = plt.subplots(1, 7, figsize=(24,6))
for k, c in enumerate(targets):
    sns.boxplot(data=df, y=c, color="lightblue", ax=axs[k])
    axs[k].set_xlabel(c)
```



The outliers are likely to be true measurements, but their presence can heavily influence the model training — common strategy is to fit two models (one with the case with target outliers and one without) to assess impact of outliers.

Individual Features

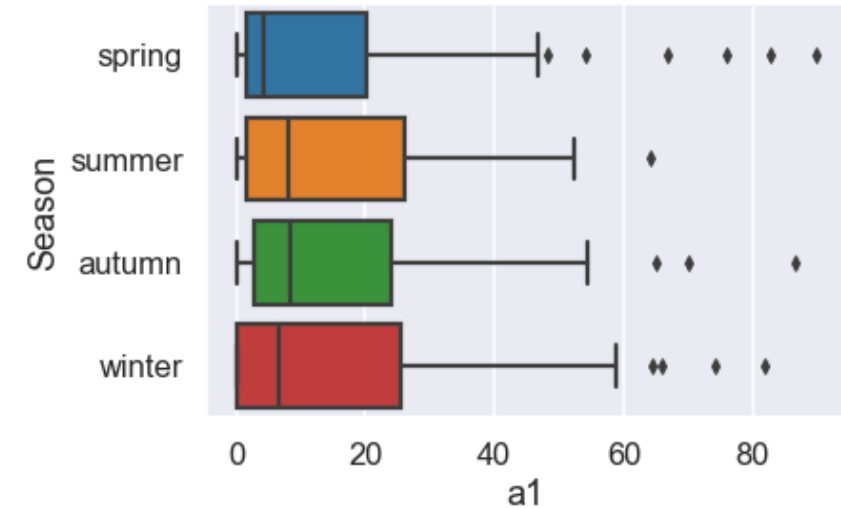
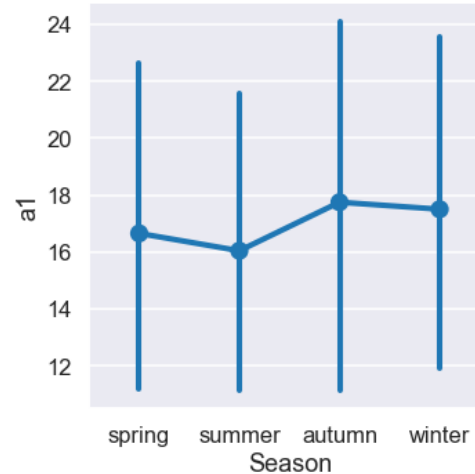
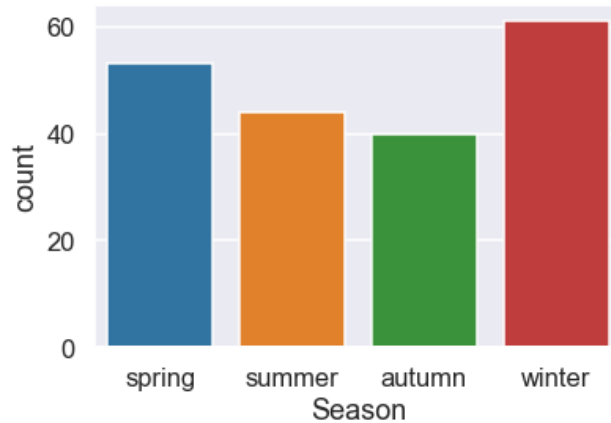
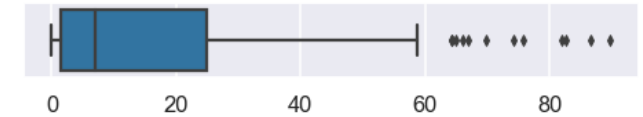
To keep this more manageable we will focus more on the Algae Blooms data set ...

	Season	Size	Speed	max_pH	min_O2	mean_Cl	mean_NO3	mean_NH4	mean_oPO4	mean_PO4	mean_Chlor	a1	a2	a3	a4	a5	a6	a7
0	winter	small	medium	8.00	9.8	60.800	6.238	578.00000	105.00000	170.00000	50.000	0.0	0.0	0.0	0.0	34.2	8.3	0.0
1	spring	small	medium	8.35	8.0	57.750	1.288	370.00000	428.75000	558.75000	1.300	1.4	7.6	4.8	1.9	6.7	0.0	2.1
2	autumn	small	medium	8.10	11.4	40.020	5.330	346.66699	125.66700	187.05701	15.600	3.3	53.6	1.9	0.0	0.0	0.0	9.7
3	spring	small	medium	8.07	4.8	77.364	2.302	98.18200	61.18200	138.70000	1.400	3.1	41.0	18.9	0.0	1.4	0.0	1.4

Sneak preview

- Three categorical variables Season, Size, and Speed.
 - No missing values
 - No high cardinality, and reasonable balanced.
- Eight numerical variables max_pH, ..., mean_Chlor
- Missing values present
- Some variables heavily skewed — might need to transform.
- Possibility of features being interrelated — **multicollinearity** — try **principal component analysis**.

Dataset: Algae Blooms, Feature: Season, Target: a1

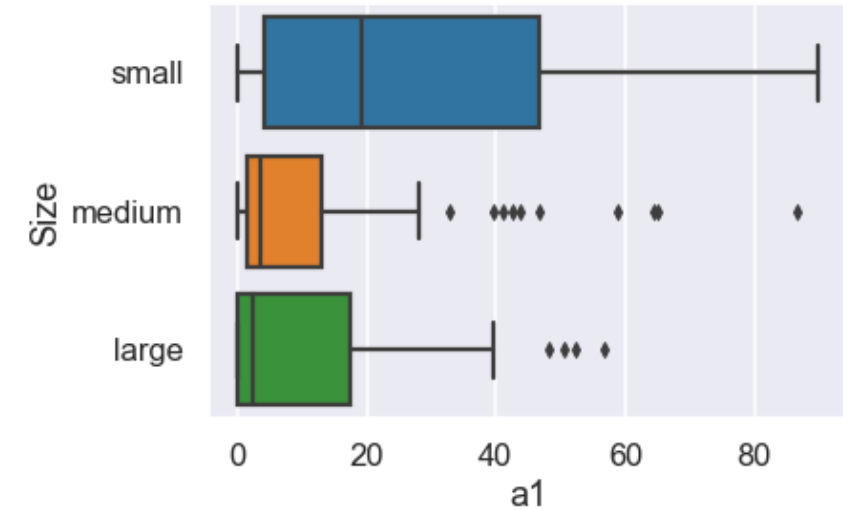
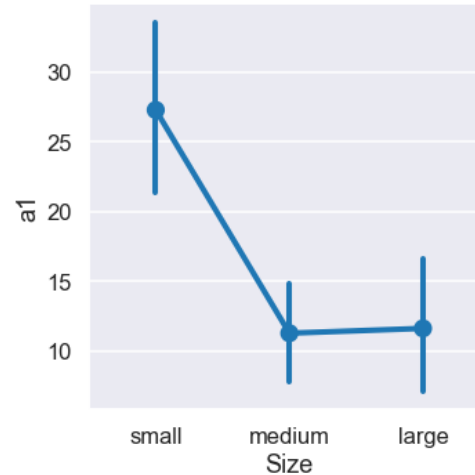
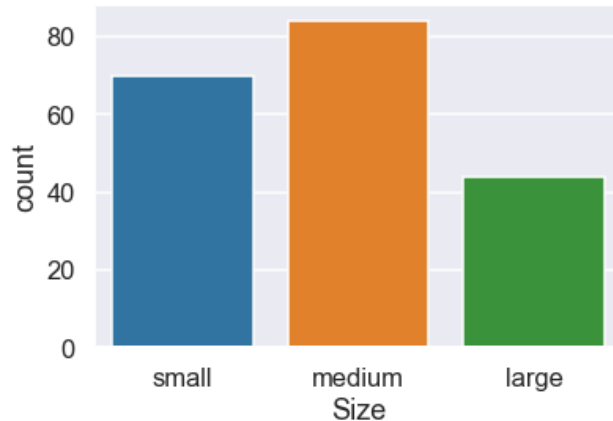
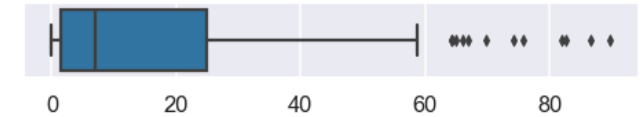


```
df.groupby("Season")["a1"].agg(["min", "max", "mean", "count", "std"])
```

	min	max	mean	count	std
Season	\bar{x}		n	σ	
spring	0.0	89.8	16.649057	53	23.093786
summer	0.0	64.2	16.038636	44	17.920798
autumn	0.0	86.6	17.745000	40	21.611203
winter	0.0	81.9	17.498361	61	22.568256

- Countplot shows no issues with feature Season — all levels approximately equally represented.
- Catplots show slightly less spread in a1 for Season="summer" observations.
- No/weak relationship between Season feature and a1 target.

Dataset: Algae Blooms, Feature: Size, Target: a1

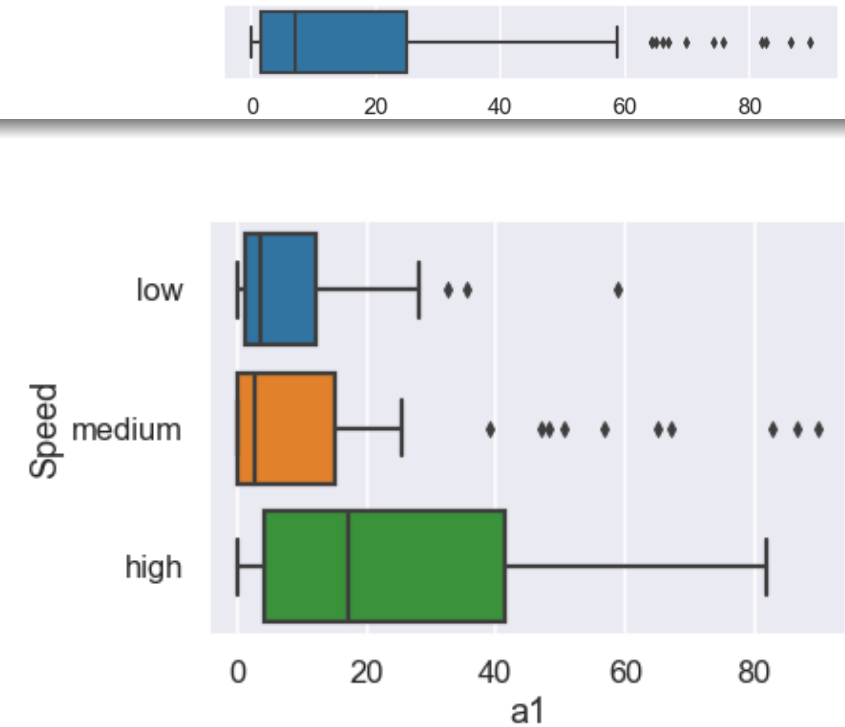
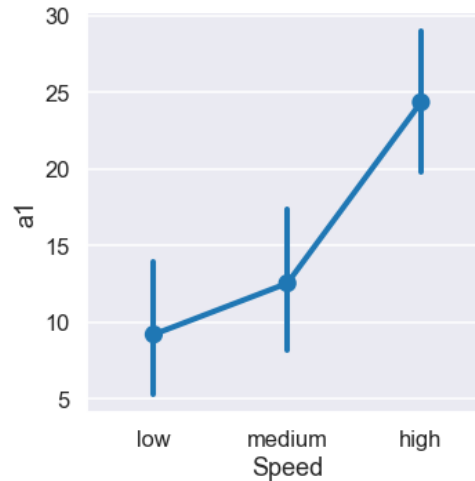
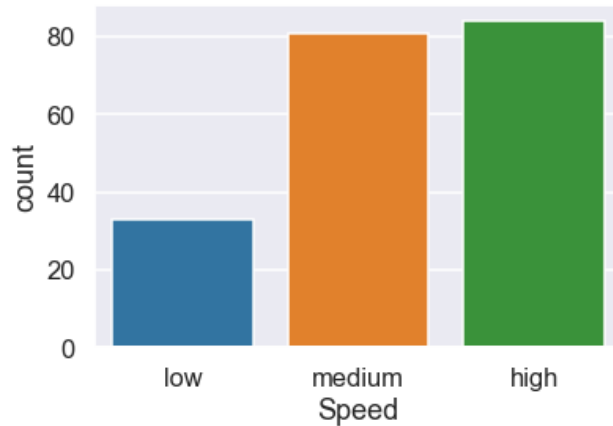


```
df.groupby("Size")["a1"].agg(["min", "max", "mean", "count", "std"])
```

	min	max	mean	count	std
Size					
small	0.0	89.8	27.255714	70	24.895426
medium	0.0	86.6	11.267857	84	17.163124
large	0.0	56.8	11.611364	44	16.556123

- Countplot shows no issues with feature Size.
- Size="small" rivers have higher frequencies of a1 alga ((point catplot), and observed frequencies for small rivers is much more widespread across the domain of frequencies than for other types of rivers (boxplot).

Dataset: Algae Blooms, Feature: Speed, Target: a1

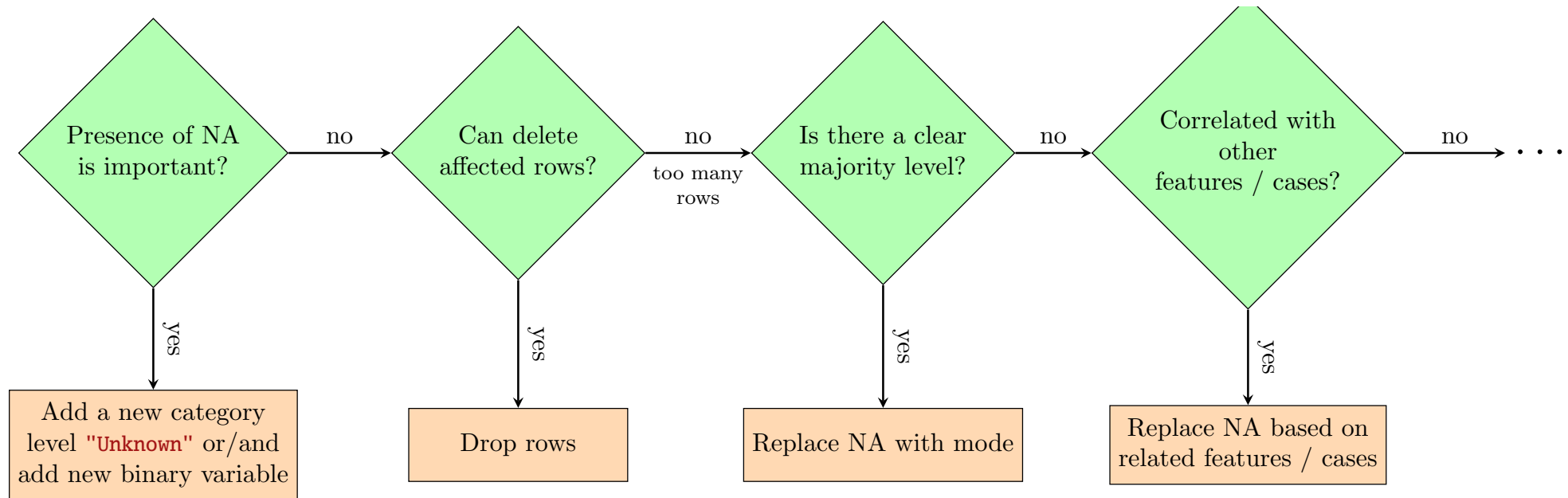


```
df.groupby("Speed")["a1"].agg(["min", "max", "mean", "count", "std"])
```

	min	max	mean	count	std
Speed					
low	0.0	58.7	9.209091	33	13.164758
medium	0.0	89.8	12.548148	81	21.146986
high	0.0	81.9	24.345238	84	22.209123

- Countplot shows no issues with feature Speed.
- Speed="high" rivers have average population of a1 alga ((point) catplot), and observed frequencies is much more widespread across the domain of frequencies than for other types of rivers (boxplot).

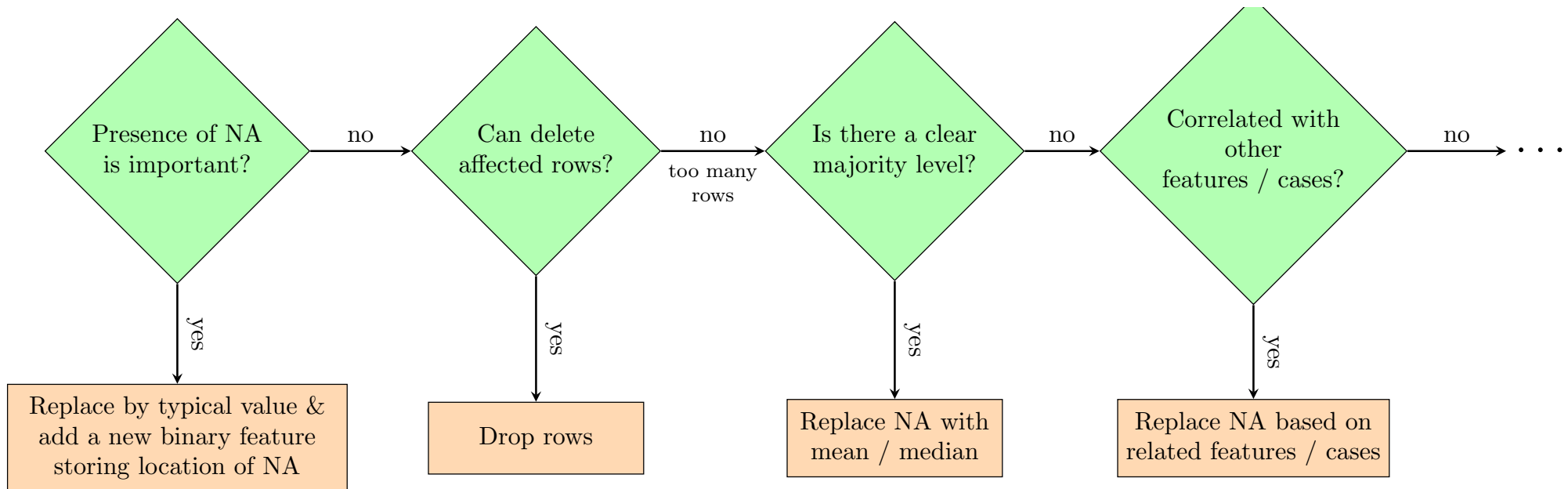
Categorical Variables — Dealing with Missing Values



In terms of our three datasets, only Titanic has missing values in categorical features:

- Location of cabin's missing values are important (1st class passengers were most likely to have a cabin) so add new category level "Unknown".
- Replace Embarked's 2 missing values with mode ("S", 644/891=72%).
Note: Use `df.Embarked.value_counts(dropna=False)` to include missing values in count tables.

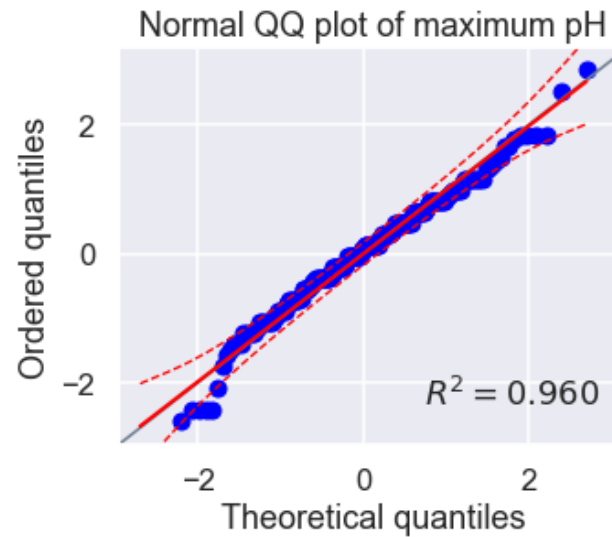
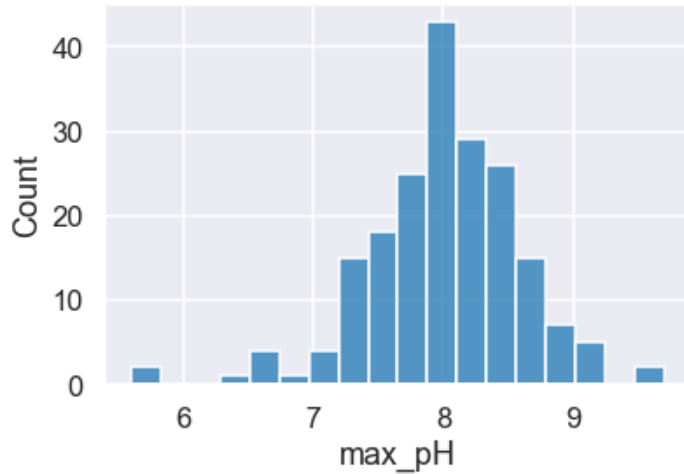
Numerical Variables — Dealing with Missing Values



In terms of our three datasets:

- In Titanic, feature Fare appears to have no missing values, but has 15 zero entries. Are these missing values? or free tickets due to age? ...
- In Algae Blooms, some of the 8 numeric features have NAs ... next few slides.

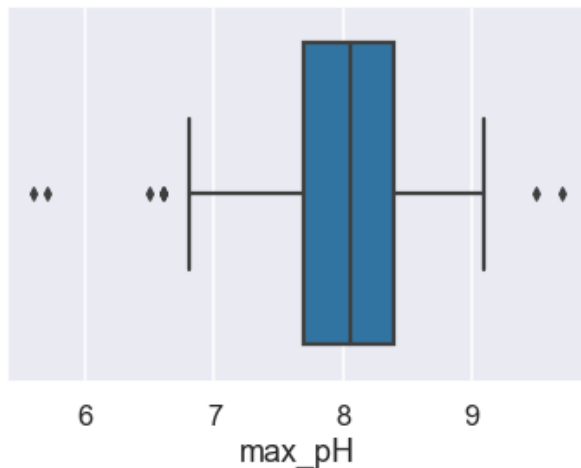
Dataset: Algae Blooms, Feature: max_pH



```
df.max_pH.isna().sum()
```

1

```
count    197.000000
mean      8.019975
std       0.590169
min       5.600000
25%       7.700000
50%       8.060000
75%       8.400000
max       9.700000
Name: max_pH, dtype: float64
```



- Data is relatively normal — minor issue with (left) outliers.
⇒ Will replace (single) NA by mean

```
df.max_pH.fillna(df.max_pH.mean(), inplace=True)
```

Dataset: Algae Blooms, Feature: max_pH, Target: a1

Is there a relationship between feature max_pH and target a1?

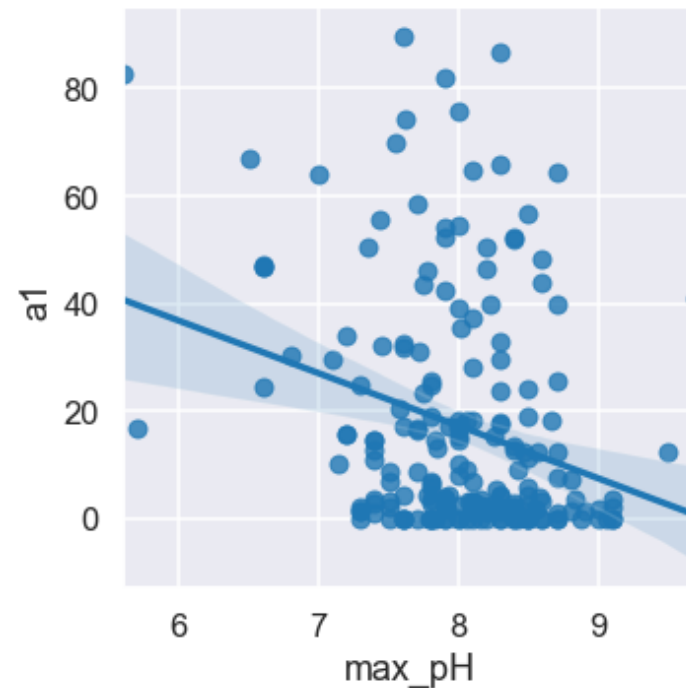
```
df[["max_pH", "a1"]].corr()
```

```
sns.lmplot(x="max_pH", y="a1", data=df);
```

	max_pH	a1
max_pH	1.000000	-0.268539
a1	-0.268539	1.000000

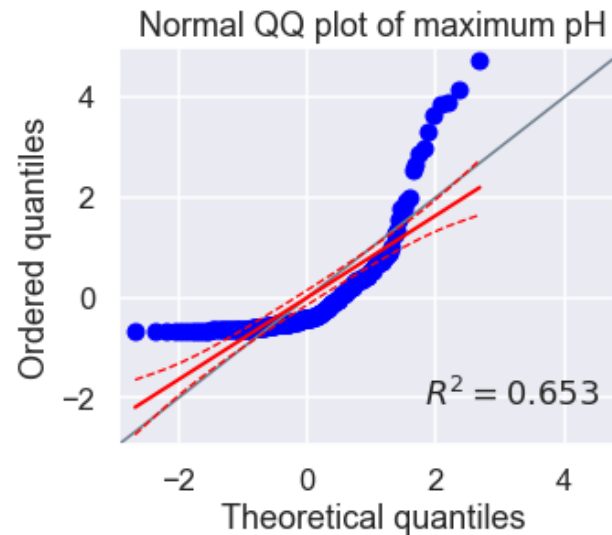
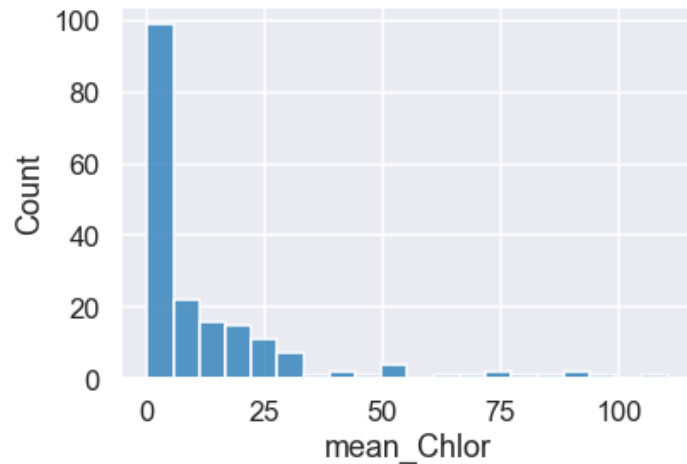
(Pearson's) Correlation coefficient, r , measures the strength of a **linear** relationship between two numerical variables.

- near zero means no/weak linear relationship.
- near ± 1 zero means strong linear relationship.
- sign indicates direction.



- Correlation coefficient, $r = -0.27$, shows (at most) a weak negative linear relationship.
- No obvious relationship visible in scatter plot.

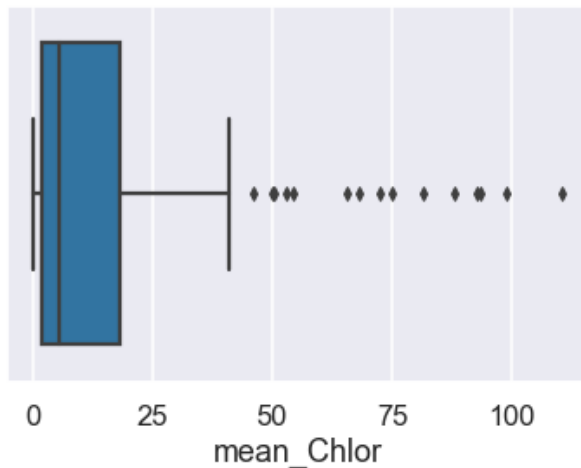
Dataset: Algae Blooms, Feature: mean_Chlor



```
df.mean_Chlor.isna().sum()
```

10

count	188.000000
mean	13.971197
std	20.495920
min	0.200000
25%	2.000000
50%	5.475000
75%	18.307500
max	110.456000
Name: mean_Chlor, dtype: float64	



- Data is not normal, heavily skewed to the right \Rightarrow mean is a poor representative of the central location.
 \Rightarrow Will replace (single) NA by median

```
df.mean_Chlor.fillna(df.mean_Chlor.median(), inplace=True)
```

After Target and Individual Feature Pass — Where are we?

Tips

- Reviewed each feature — location, spread, shape, issues.
- No missing values
- total_bill, and total_tip have possible outliers.

Titanic

- Reviewed each feature — location, spread, shape, issues.
- Generated ToDo list for for cleaning, feature extraction
 - Identified features that appear to be related to the target.
 - Feature age has missing values.
 - Feature Fare
 - has 15 measurements with value 0 — decide missing value or not.
 - distribution has large outliers and is skewed — remove/fix outliers and transform.
 - Feature Name has could be used to obtain new feature Title.
 - ...

Algae Blooms

- Reviewed each feature — location, spread, shape, issues.
- Imputed missing values using feature distributions (mean/median).
- Identified features that appear to be related to the target.

Aside: Steps needed to create new feature `Title` from feature `Name`

```
df = pd.read_csv('assets/train.csv')
df.head()
```

	PassengerId	Survived	Pclass	Name	Sex	Age	SibSp	Parch	Ticket	Fare	Cabin	Embarked
0	1	0	3	Braund, Mr. Owen Harris	male	22.0	1	0	A/5 21171	7.25	NaN	S
1	2	1	1	Cumings, Mrs. John Bradley (Florence Briggs Th...	female	38.0	1	0	PC 17599	71.28	NaN	S
				Heikkinen, Miss. Laina	female	26.0	0	0	STON/O2. 3101282	7.92	NaN	S
				Futrelle, Mrs. Jacques Heath (Lily May Peel)	female	35.0	1	0	113803	53.1000	C123	S
				Allen, Mr. William Henry	male	35.0	0	0	373450	8.0500	NaN	S

1 Have a (text) feature representing the passenger's name.

Title	Count
Capt	1
Col	4
Don	1
Dona	1
Dr	8
Jonkheer	1
Lady	1
Major	2
Master	61
Miss	260
Mlle	2
Mme	1
Mr	757
Mrs	197
Ms	2
Rev	8
Sir	1
the Countess	1

2 Rare categories can be merged under a single label – 'Dona', 'Lady', 'the Countess', 'Capt', 'Col', etc. . Duplicate/redundant categories can be merged – the titles 'Mlle', and 'Ms' and can be merged under 'Miss'. 'Mme' can be merged with 'Mrs'.

Capt
Col
Don
Dona
Dr
Jonkheer
Lady
Major
Rev
Sir
the Countess

rare_title

Mlle
Ms

Miss

Mme

→ Mrs

3 New categorical feature with 5 unique values

Master	Miss	Mr	Mrs	rare_title
61	264	757	198	29

Third Pass — Relationships Between Features (and Target)

- Correlations

Correlations — Relationship Between two Variables

Pearson's correlation coefficient, r

is a measure of linear correlation between two variables. Its value lies between -1 and +1, -1 indicating total negative linear correlation, 0 indicating no linear correlation and 1 indicating total positive linear correlation.

Spearman's rank correlation coefficient, ρ

is a measure of monotonic correlation between two variables, and is therefore better in catching nonlinear monotonic correlations than Pearson's r . Its value also lies between -1 and +1, with values near zero indicating no monotonic relation.

Kendall rank correlation coefficient, τ

measures ordinal association between two variables. Its value lies between -1 and +1 with values near zero indicating no relation.

Phi-k, ϕ_k

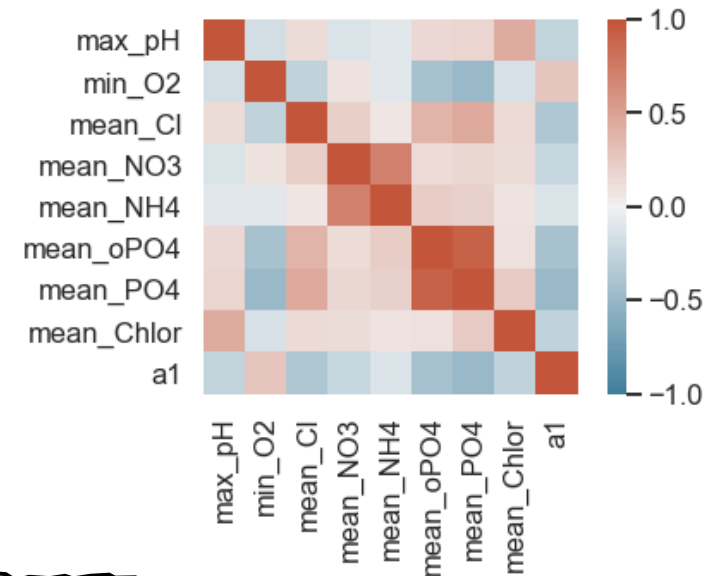
is a new and practical correlation coefficient that works consistently between categorical, ordinal and interval variables, captures non-linear dependency and reverts to the Pearson correlation coefficient in case of a bivariate normal input distribution. Its value also lies between 0 and +1, with values near zero indicating no relation.

Pearson's Correlation Coefficient — Dataset: Algae Blooms

```
columns = df.columns[:12]
corr = df[columns].corr()
corr
```

```
cmap = sns.diverging_palette(230, 20, as_cmap=True)
sns.heatmap(corr, square=True, vmin=-1, vmax=1, cmap=cmap);
```

	max_pH	min_O2	mean_Cl	mean_NO3	mean_NH4	mean_oPO4	mean_PO4	mean_Chlor	a1
max_pH	1.000000	-0.167981	0.136369	-0.130762	-0.093521	0.158769	0.179885	0.445864	-0.268539
min_O2	-0.167981	1.000000	-0.278333	0.099444	-0.087478	-0.416163	-0.487486	-0.153265	0.285564
mean_Cl	0.136369	-0.278333	1.000000	0.225041	0.071913	0.391054	0.457449	0.149856	-0.371171
mean_NO3	-0.130762	0.099444	0.225041	1.000000	0.721444	0.144588	0.168601	0.139679	-0.241211
mean_NH4	-0.093521	-0.087478	0.071913	0.721444	1.000000	0.227237	0.208180	0.088947	-0.132656
mean_oPO4	0.158769	-0.416163	0.391054	0.144588	0.227237	1.000000	0.914365	0.115621	-0.417358
mean_PO4	0.179885	-0.487486	0.457449	0.168601	0.208180	0.914365	1.000000	0.253621	-0.487023
mean_Chlor	0.445864	-0.153265	0.149856	0.139679	0.088947	0.115621	0.253621	1.000000	-0.277987
a1	-0.268539	0.285564	-0.371171	-0.241211	-0.132656	-0.417358	-0.487023	-0.277987	1.000000



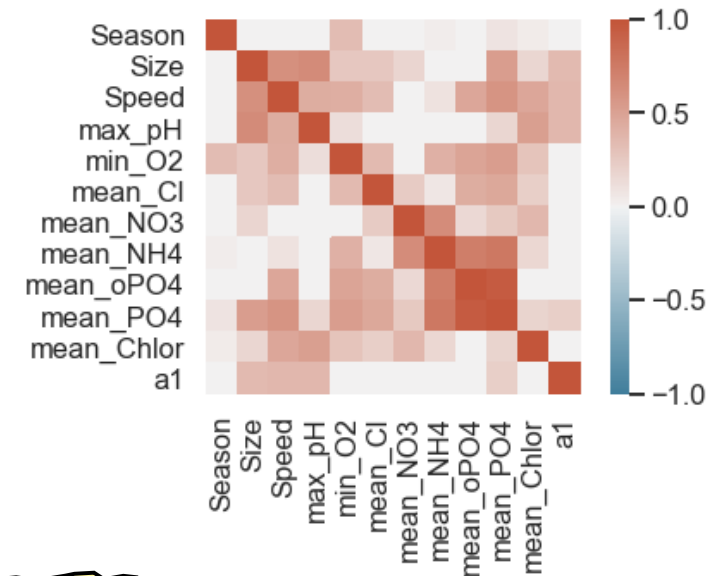
- Categorical variables are not included.
- Suggests best predictors for a1 are mean_PO4, mean_oPO4, and meanCl.
- mean_PO4 and mean_oPO4 are highly correlated (0.91) — could use values of one to estimate missing values of the other.

Spearman's Rank Correlation Coefficient — Dataset: Algae Blooms

```
columns = df.columns[:12]
cor = df[columns].corr(method='spearman')
cor
```

```
cmap = sns.diverging_palette(230, 20, as_cmap=True)
sns.heatmap(corr, square=True, vmin=-1, vmax=1,
```

	max_pH	min_O2	mean_Cl	mean_NO3	mean_NH4	mean_oPO4	mean_PO4	mean_Chlor	a1
max_pH	1.000000	-0.148676	0.159079	-0.145182	0.026160	0.290245	0.214569	0.394813	-0.247787
min_O2	-0.148676	1.000000	-0.405142	0.057610	-0.348226	-0.457805	-0.519786	-0.217714	0.283418
mean_Cl	0.159079	-0.405142	1.000000	0.530374	0.592052	0.670399	0.713479	0.564915	-0.546845
mean_NO3	-0.145182	0.057610	0.530374	1.000000	0.425010	0.432303	0.451272	0.346805	-0.382403
mean_NH4	0.026160	-0.348226	0.592052	0.425010	1.000000	0.603157	0.646690	0.406656	-0.449194
mean_oPO4	0.290245	-0.457805	0.670399	0.432303	0.603157	1.000000	0.914921	0.510930	-0.671019
mean_PO4	0.214569	-0.519786	0.713479	0.451272	0.646690	0.914921	1.000000	0.554167	-0.656670
mean_Chlor	0.394813	-0.217714	0.564915	0.346805	0.406656	0.510930	0.554167	1.000000	-0.537823
a1	-0.247787	0.283418	-0.546845	-0.382403	-0.449194	-0.671019	-0.656670	-0.537823	1.000000



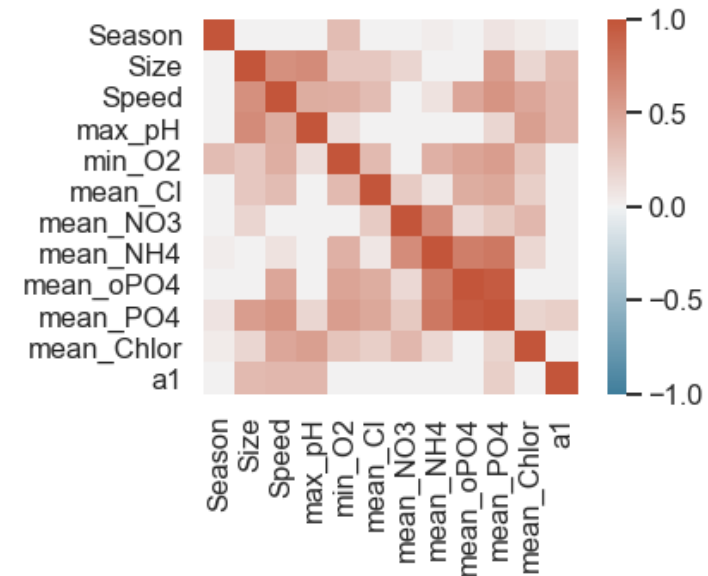
- Now best predictors for a1 also include mean_Chlor and mean_NH4.

Phik Correlation Coefficient — Dataset: Algae Blooms

```
import phik
columns = df.columns[:12]
corr = df[columns].phik_matrix()
corr
```

```
cmap = sns.diverging_palette(230, 20, as_cmap=True)
sns.heatmap(corr, square=True, vmin=-1, vmax=1,
```

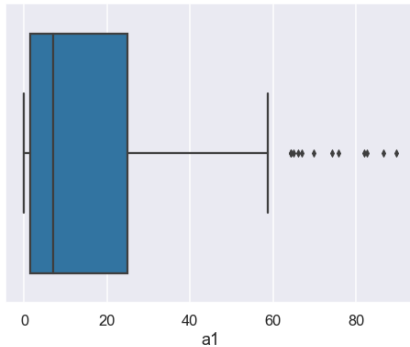
	Season	Size	Speed	max_pH	min_O2	mean_Cl	mean_NO3	mean_NH4	mean_oPO4	mean_PO4	mean_Chlor	a1
Season	1.000000	0.000000	0.000000	0.000000	0.343496	0.000000	0.000000	0.034202	0.000000	0.093199	0.045361	0.000000
Size	0.000000	1.000000	0.620101	0.655207	0.270013	0.268198	0.182410	0.000000	0.000000	0.531635	0.173516	0.353390
Speed	0.000000	0.620101	1.000000	0.445096	0.437356	0.339237	0.000000	0.101348	0.483298	0.594480	0.479735	0.369374
max_pH	0.000000	0.655207	0.445096	1.000000	0.125231	0.000000	0.000000	0.000000	0.000000	0.175105	0.528134	0.372031
min_O2	0.343496	0.270013	0.437356	0.125231	1.000000	0.353196	0.000000	0.416999	0.492457	0.535996	0.296376	0.000000
mean_Cl	0.000000	0.268198	0.339237	0.000000	0.353196	1.000000	0.243887	0.073692	0.443047	0.472824	0.225583	0.000000
mean_NO3	0.000000	0.182410	0.000000	0.000000	0.000000	0.243887	1.000000	0.642789	0.158463	0.259915	0.368142	0.000000
mean_NH4	0.034202	0.000000	0.101348	0.000000	0.416999	0.073692	0.642789	1.000000	0.734681	0.776197	0.167533	0.000000
mean_oPO4	0.000000	0.000000	0.483298	0.000000	0.492457	0.443047	0.158463	0.734681	1.000000	0.954601	0.000000	0.000000
mean_PO4	0.093199	0.531635	0.594480	0.175105	0.535996	0.472824	0.259915	0.776197	0.954601	1.000000	0.192920	0.221308
mean_Chlor	0.045361	0.173516	0.479735	0.528134	0.296376	0.225583	0.368142	0.167533	0.000000	0.192920	1.000000	0.000000
a1	0.000000	0.353390	0.369374	0.372031	0.000000	0.000000	0.000000	0.000000	0.000000	0.221308	0.000000	1.000000



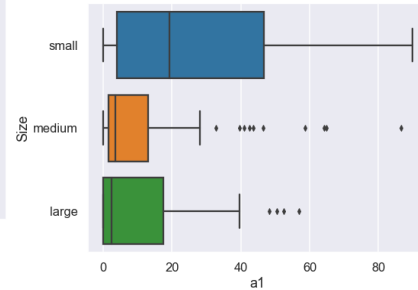
- Now include categorical variables — Season is not related, but Size and Speed are.

Multi-Relation Plots

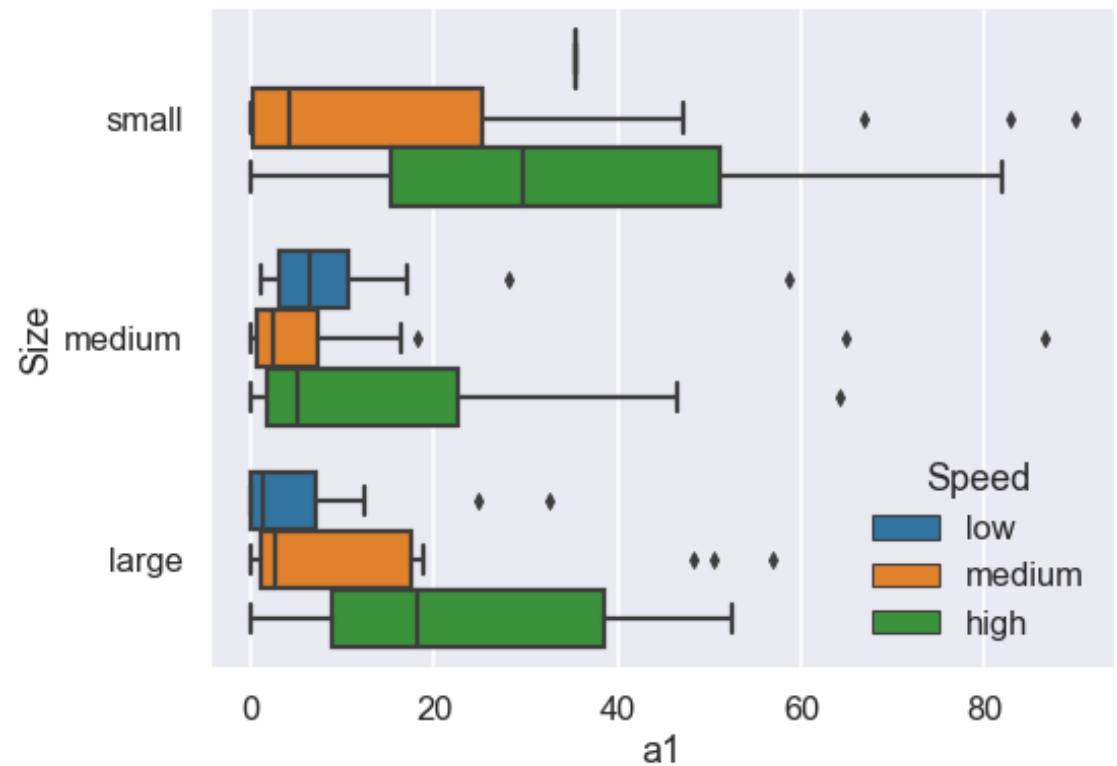
```
sns.boxplot(x="a1", data=df);
```



```
sns.boxplot(x="a1", y="Size", data=df);
```



```
sns.boxplot(x="a1", y="Size", hue="Speed", data=df);
```



- If have n features, then have $n(n - 1)$ possible visualisations — gets a bit crazy.

After Third Pass — Where are we?

- Reviewed each feature — location, spread, shape, issues.
- Identified any correlation among features and with target.
- Located and resolved missing values.
- Generated list of possible feature engineering tasks.

Resources

Resources

Guides

- 1 hour, Youtube on generating seaborn plots — excellent (but wrong on interpretation of box plot)

www.youtube.com/watch?v=6GUZXDef2U0&t=1363s

Articles on Exploratory Data Analysis

- Exploratory Data Analysis (EDA) and Data Visualization with Python

www.kite.com/blog/python/data-analysis-visualization-python/

- Titanic Survival Dataset Part 1/2: Exploratory Data Analysis (9 min read)

www.kaggle.com/mcromao/titanic-exploratory-data-analysis

- Titanic - Exploratory Data Analysis

becominghuman.ai/

titanic-survival-dataset-part-1-2-exploratory-data-analysis-5b98f7917913

- When Should You Delete Outliers from a Data Set?

humansofdata.atlan.com/2018/03/when-delete-outliers-dataset