

kokchun giang

when your model is too  
complex, you can **regularize** it  
to make it simpler



many features leads to many parameters, which makes the model too complex

$$\begin{pmatrix} | & | & & | \\ x_1 & x_2 & \dots & x_n \\ | & | & & | \end{pmatrix}$$

each column is a feature

want to  $\uparrow$  bias  
 $\downarrow$  variance

many features  $\rightarrow$  model has

many parameters

$$y = w_0 + w_1 x_1 + w_2 x_2 + \dots + w_n x_n$$

$\rightarrow$  risk for multicollinearity

$\rightarrow$  redundancy in features

$\rightarrow$  inaccurate estimate of  $w_i$

$\rightarrow$  overfitting

add a **penalty** to decrease the role of parameters other than the bias

ridge regression  
( $l_2$ -regularization)

$\uparrow \lambda \Rightarrow \downarrow \text{variance}$   
 $\uparrow \text{bias}$



penalty parameter

$$0 \leq \lambda \leq 1$$

$\uparrow \lambda \Rightarrow w_i \text{ close to } 0$   
 $i \geq 1$

lasso regression  
( $l_1$ -regularization)

$\uparrow \lambda \Rightarrow \downarrow \text{variance}$   
 $\uparrow \text{bias}$

$$0 \leq \lambda \leq 1$$

$\uparrow \lambda \Rightarrow \text{least important}$   
features set to zero

elastic net  
combines  $l_1$  &  $l_2$

Hyperparameters

$\lambda$  - penalty

$\alpha$  -  $l_1$ -ratio



$$0 \leq \alpha \leq 1$$

regularisation models require **feature scaling**

the models are trained  
using numerical approach  
such as gradient descent

=> require feature scaling

e.g. . feature standardization  
· normalization

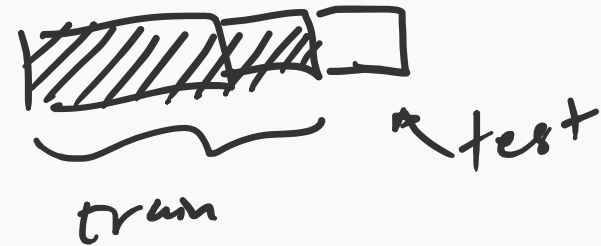
# k-fold cross validation for hyperparameter tuning



1. train w. different hyperparameters
2. predict & evaluate on validation data
3. choose new values on the hyperparameters & repeat 1. & 2.

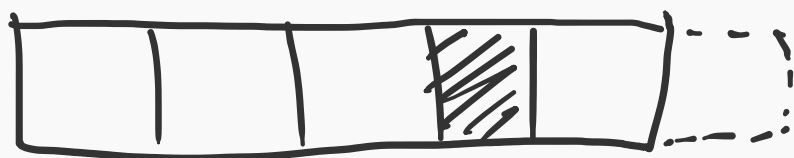
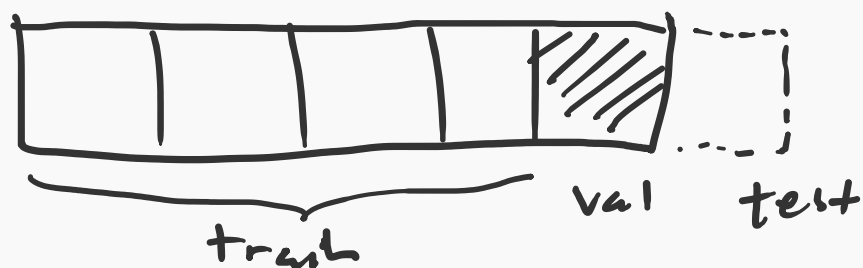
4. choose the value on hyper-param that gave least validation error

5. train on train & val datasets

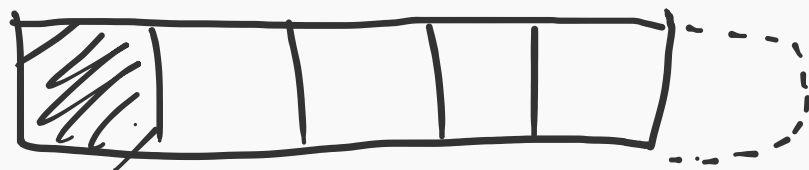


6. evaluate on test set

# k-fold cross validation for hyperparameter tuning



⋮



5-fold CV

compute mean  
error

for small datasets, we  
utilizes the data well

for larger it costs as

we repeat training  $k$  times