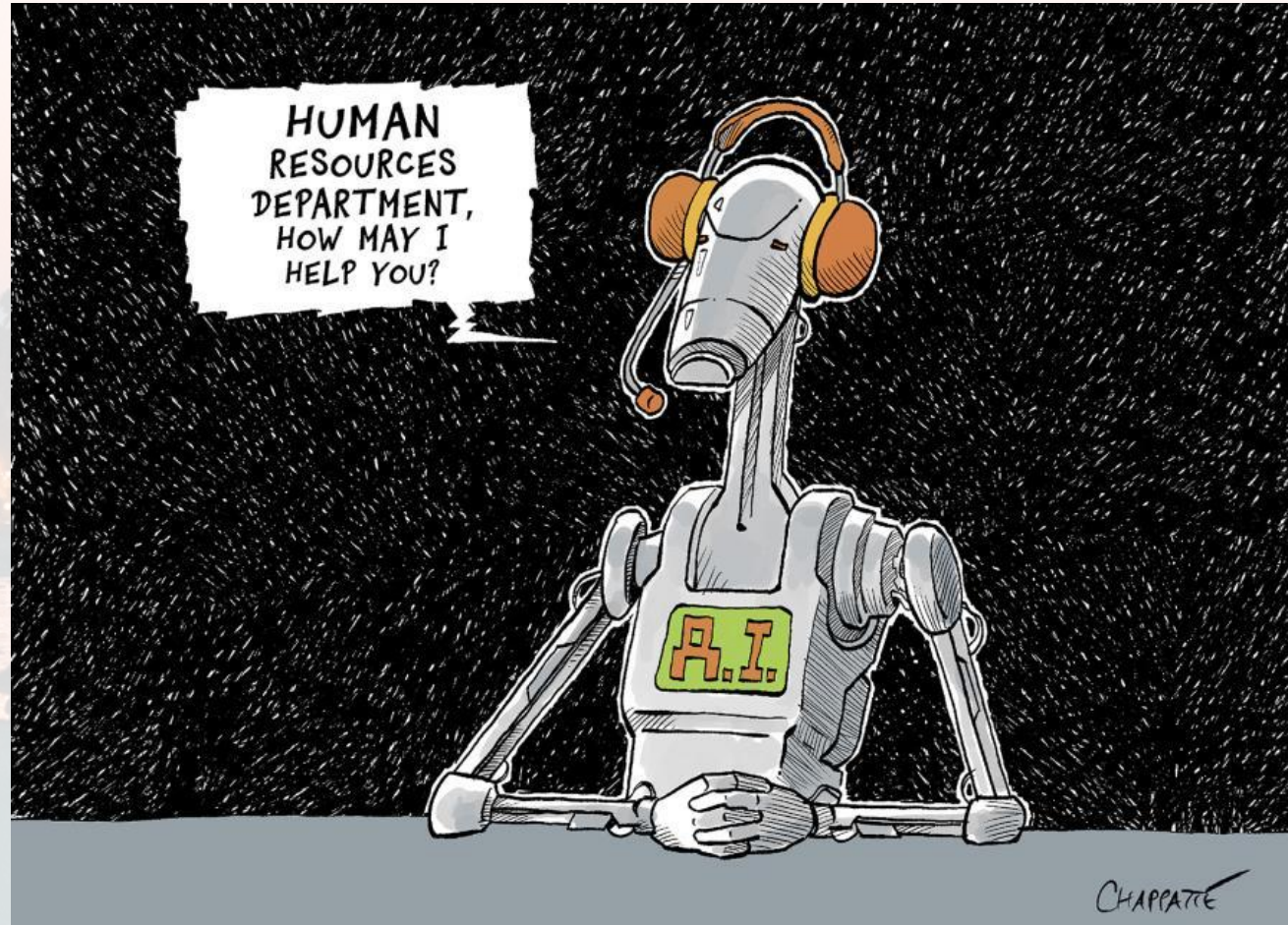


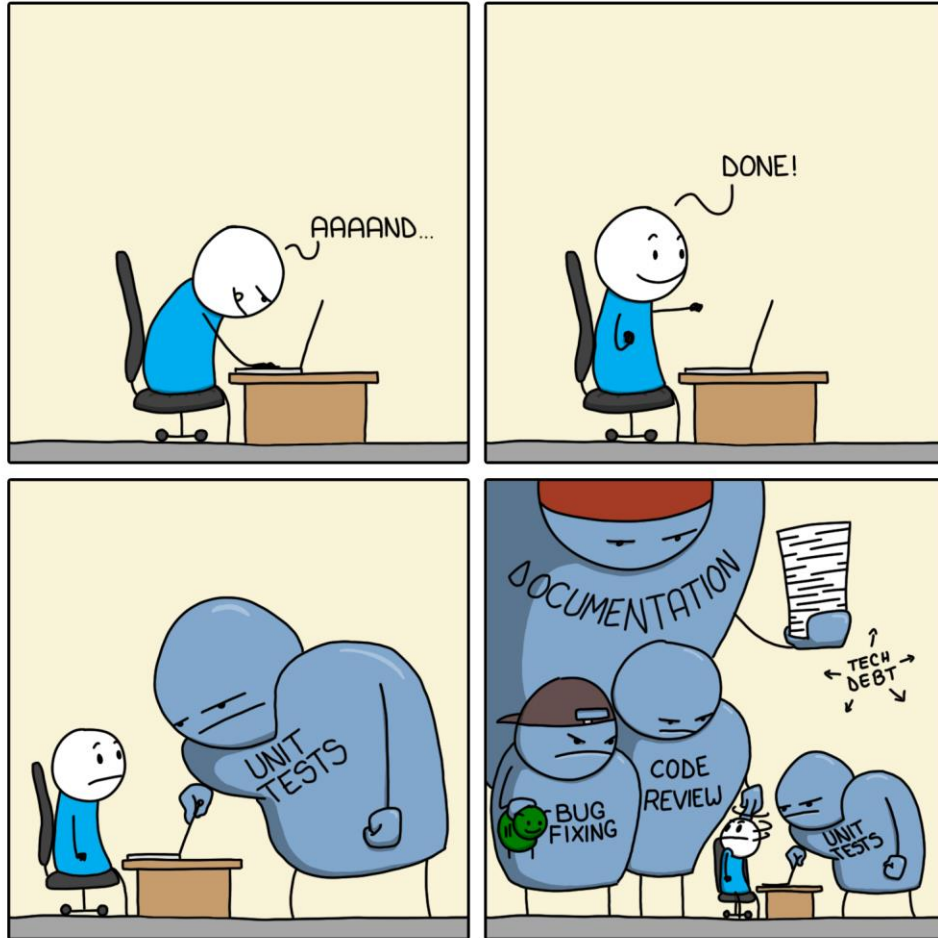
Recurrent Neural Networks – from Scratch





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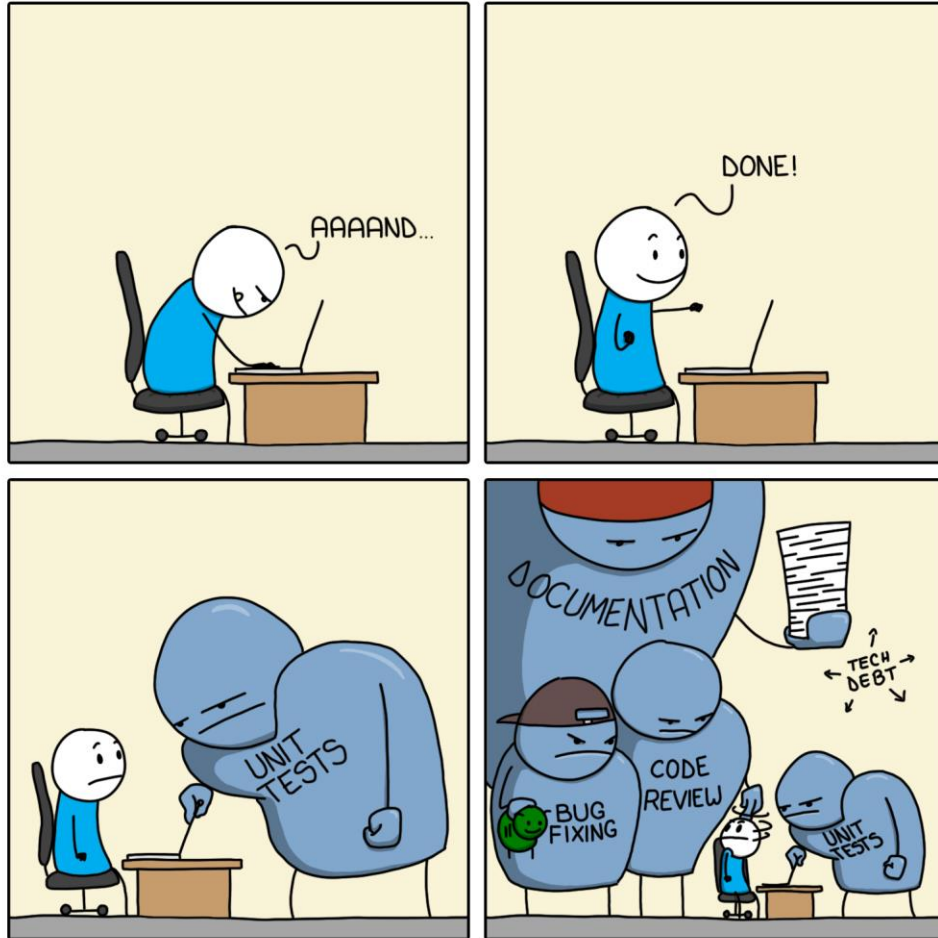
you should be fluent with:

- *basic OOP* (methods, classes, inheritance)
- *Linear algebra* (dot product, inner product, outer product)
- *derivatives* (gradient)
- +
- *Optimizer_SGD* from “ANN from Scratch”



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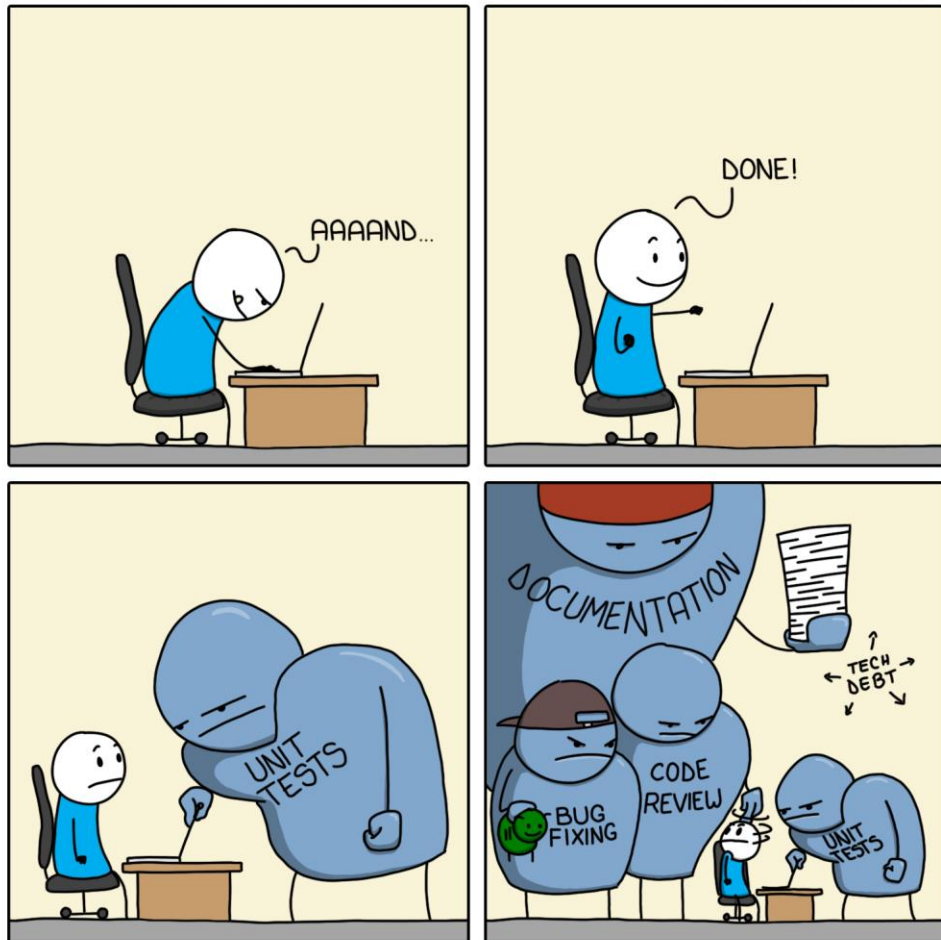
outline:

- the idea
- the RNN cell
- **BackPropagation Through Time**
- full backpropagation
- creating an SGD optimizer
- creating a full package



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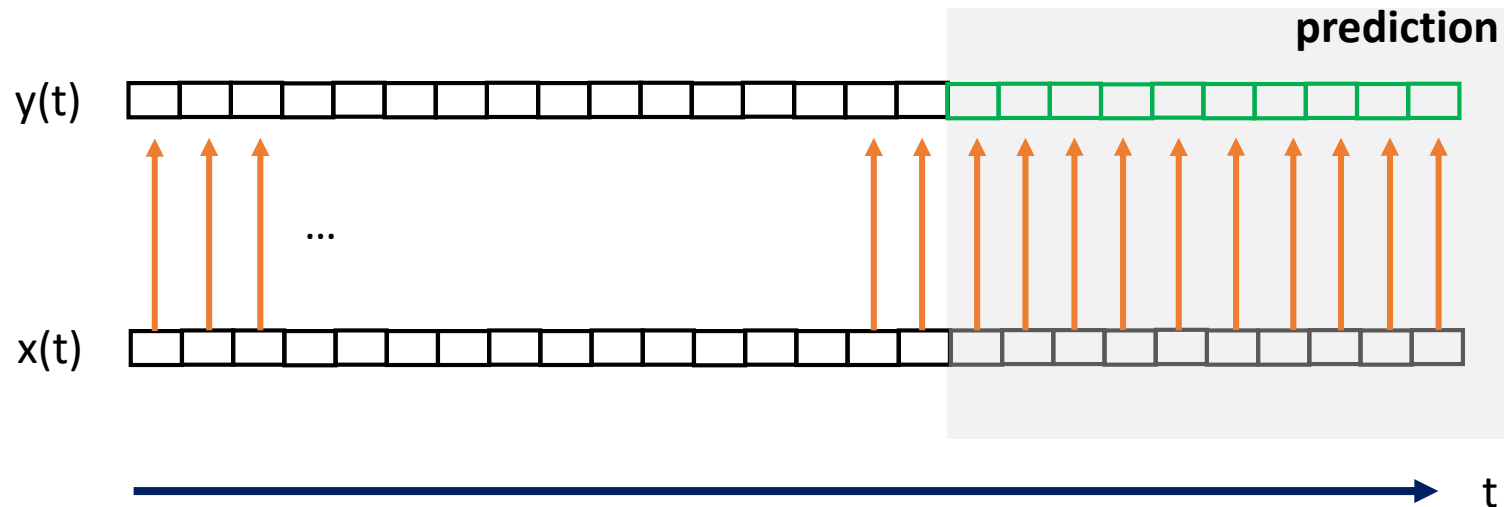


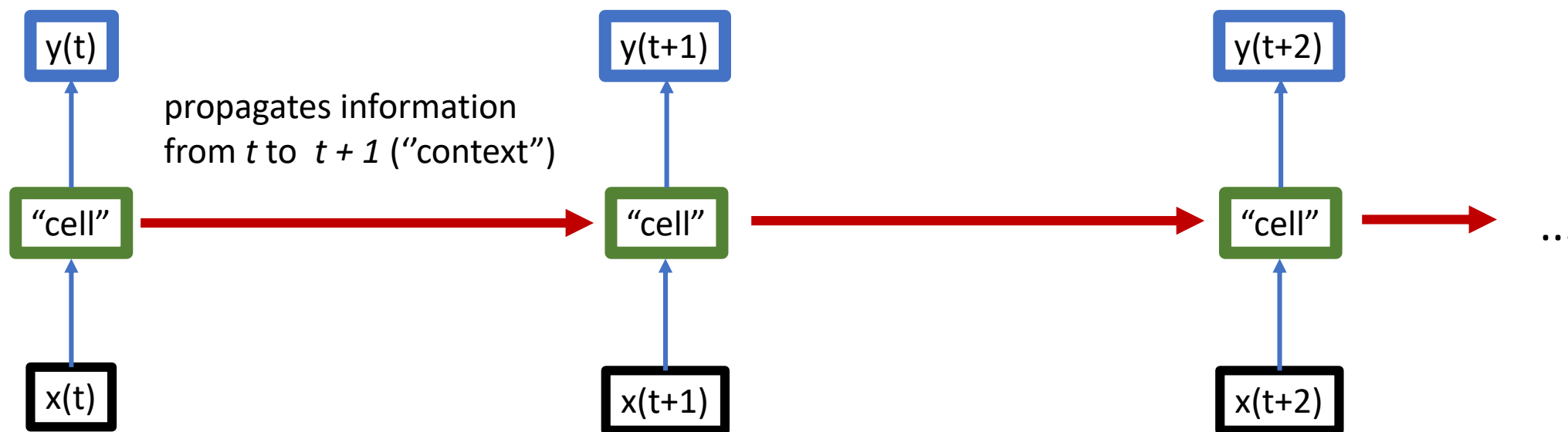
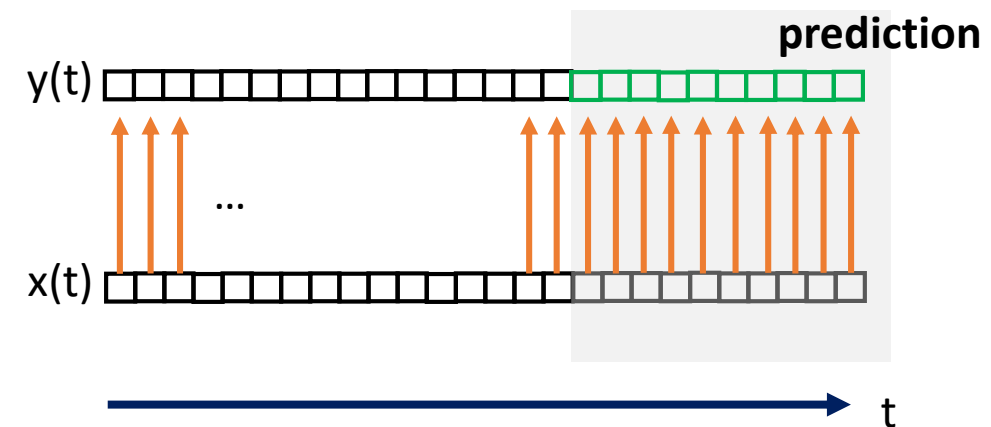
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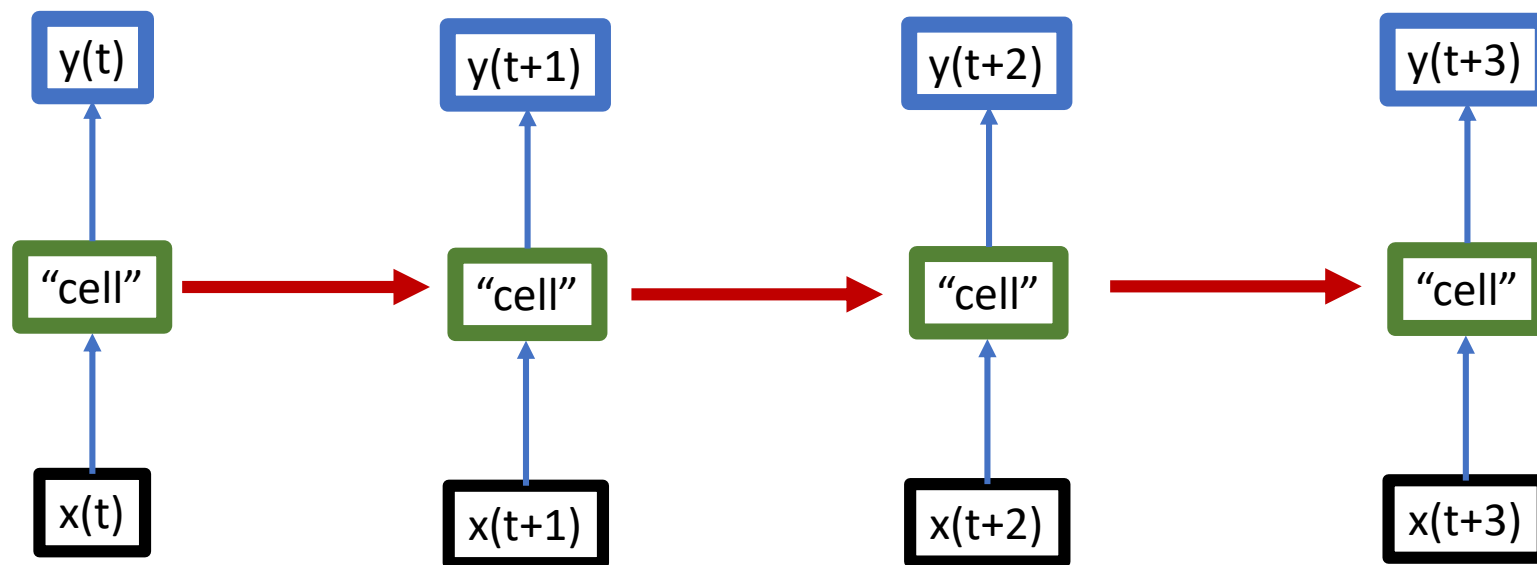
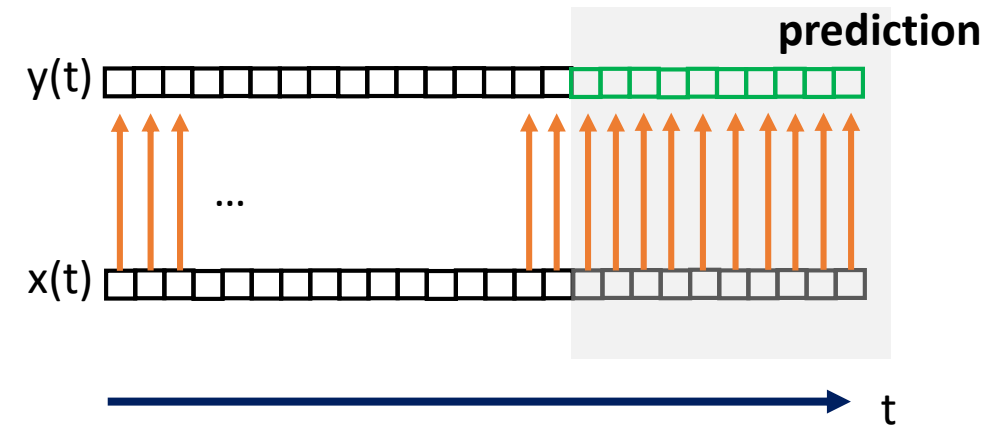
- time series analysis (prediction and forecasting)
- early speech recognition
- handwriting
- “precursor” of LSTMs
- invented by **Shun'ichi Amari** in 1972





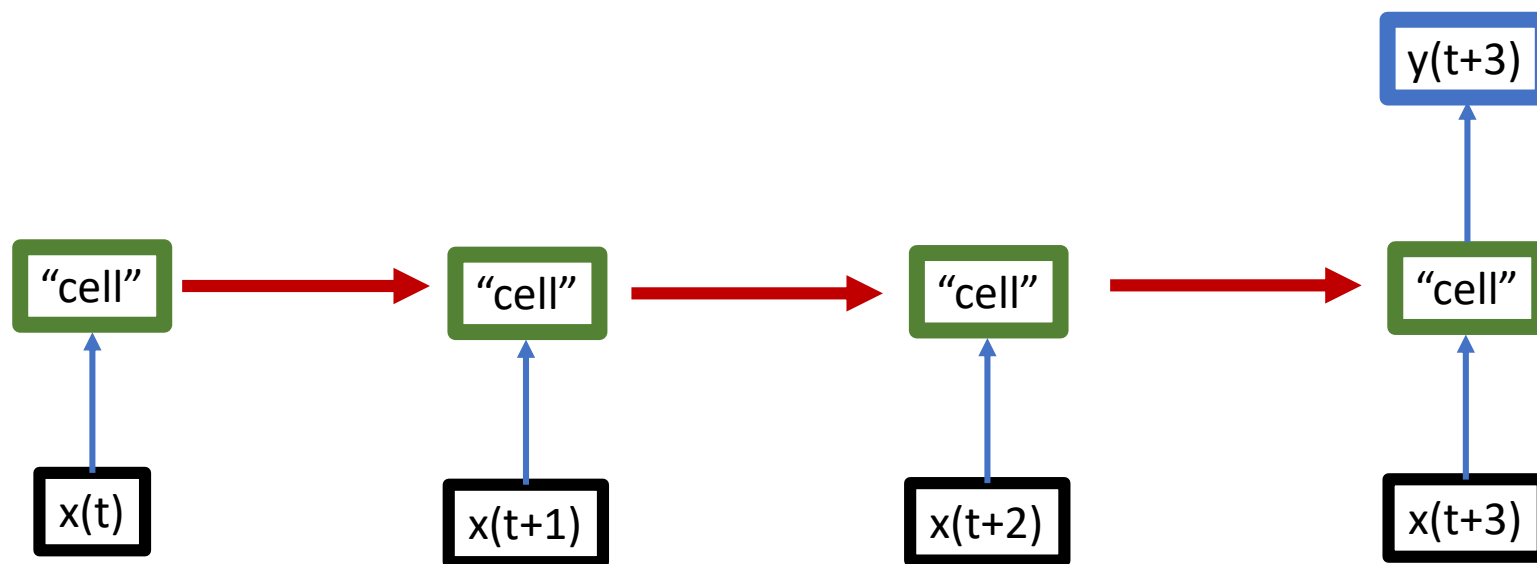
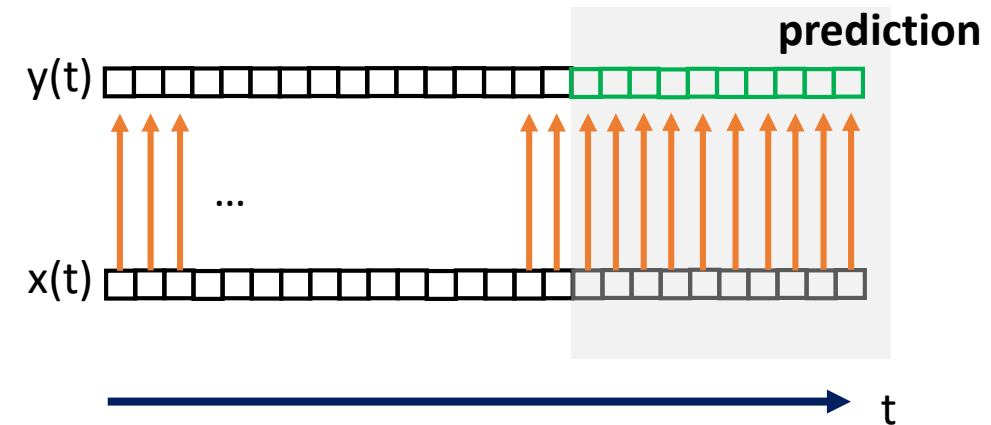


“many to many”



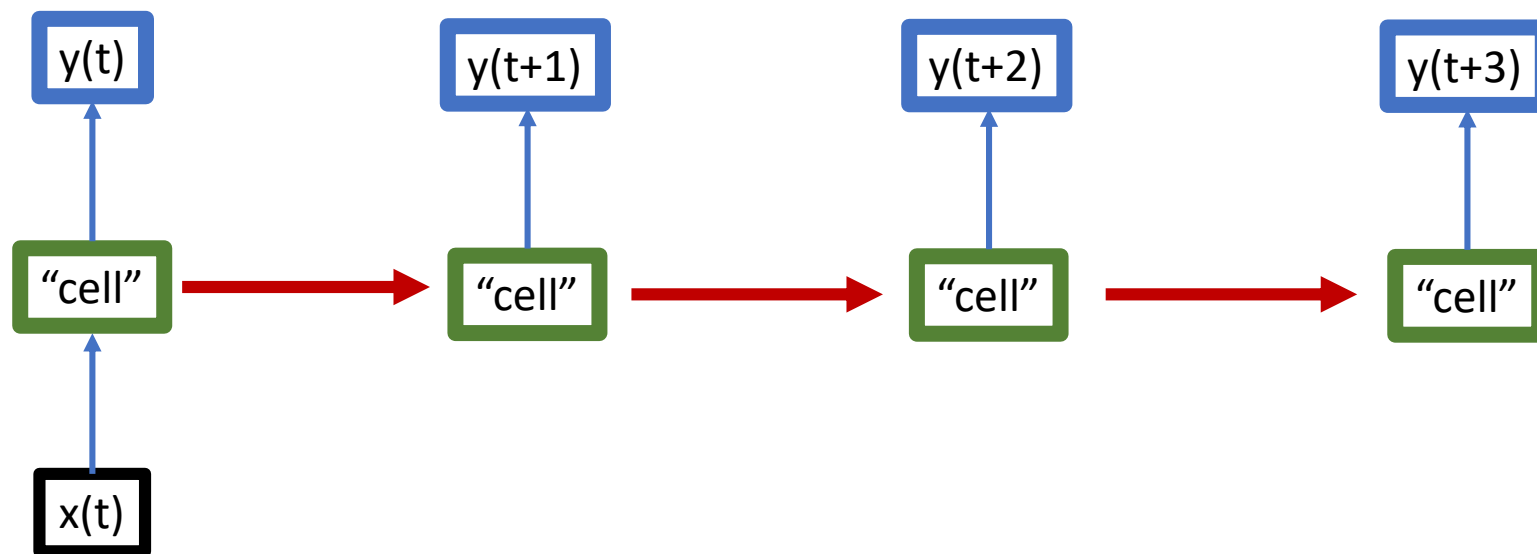
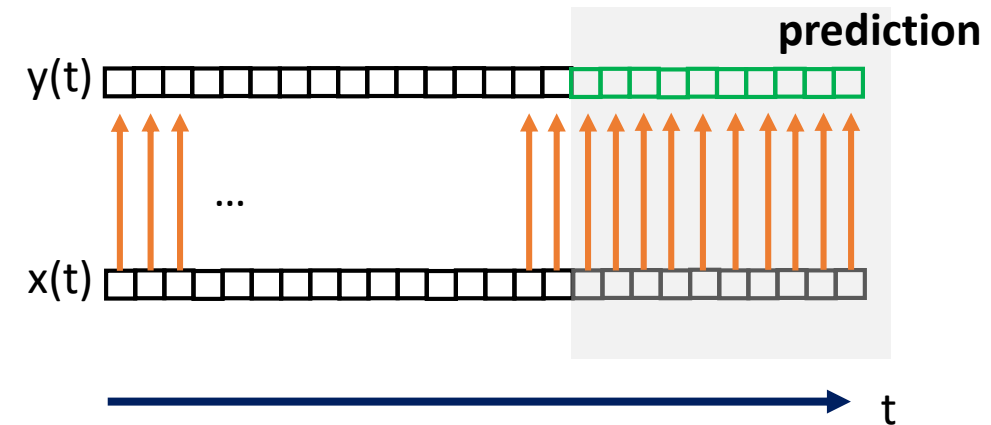


“many to one”





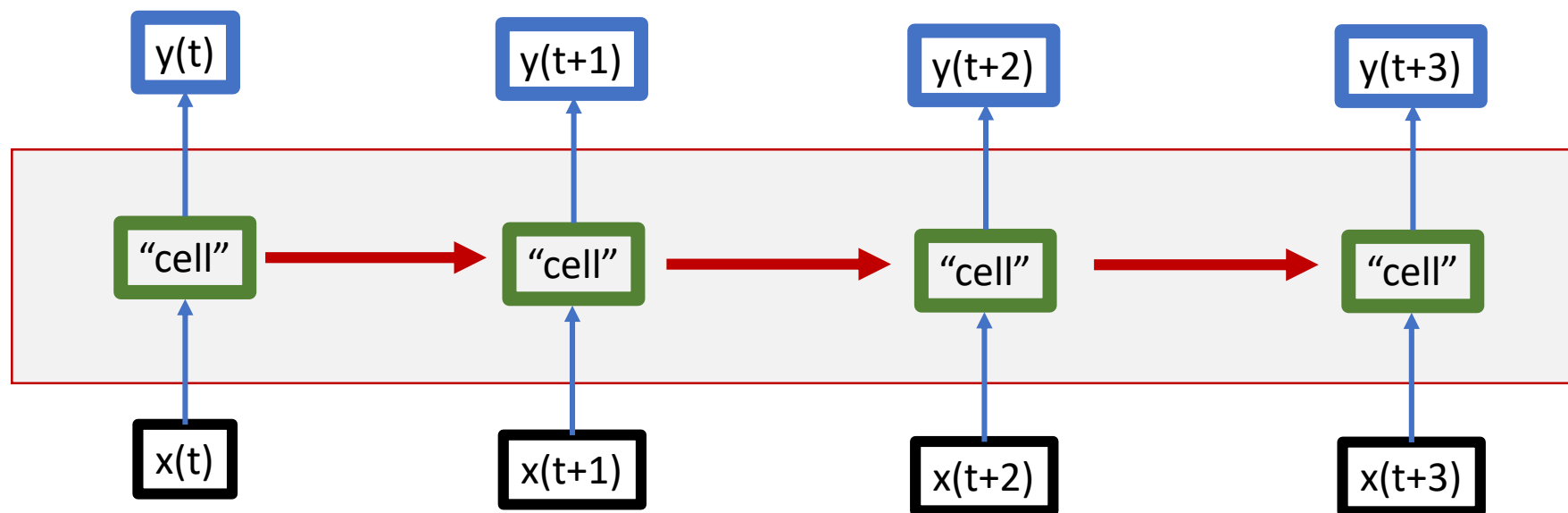
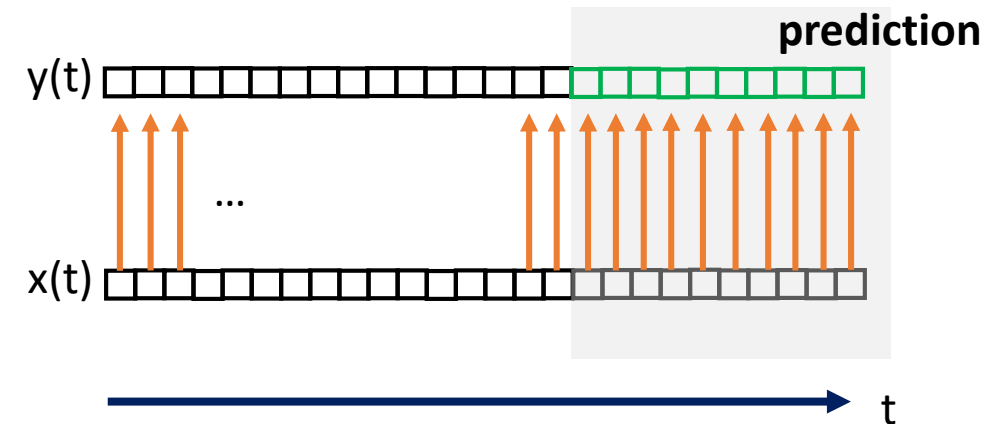
“one to many”





Applying the **identical** cell **recursively**!

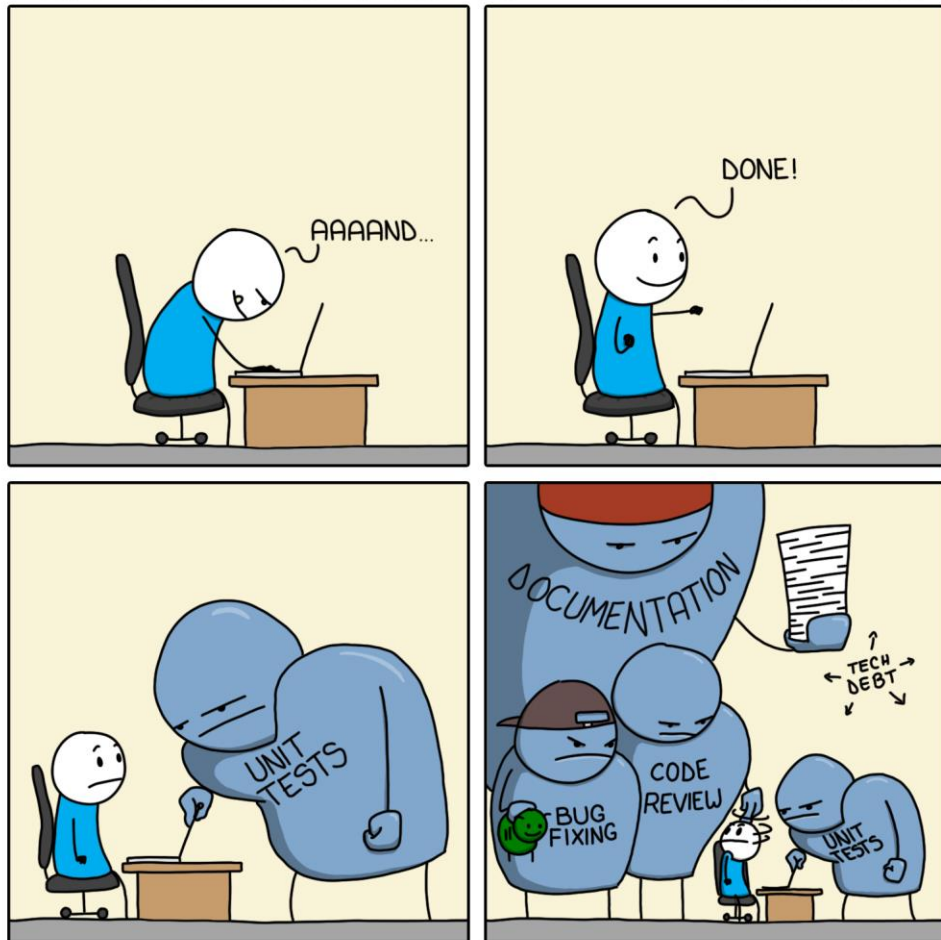
- easy to implement
- direction (arrow of time, see later)
- exploding/vanishing gradients
- has a “short memory”





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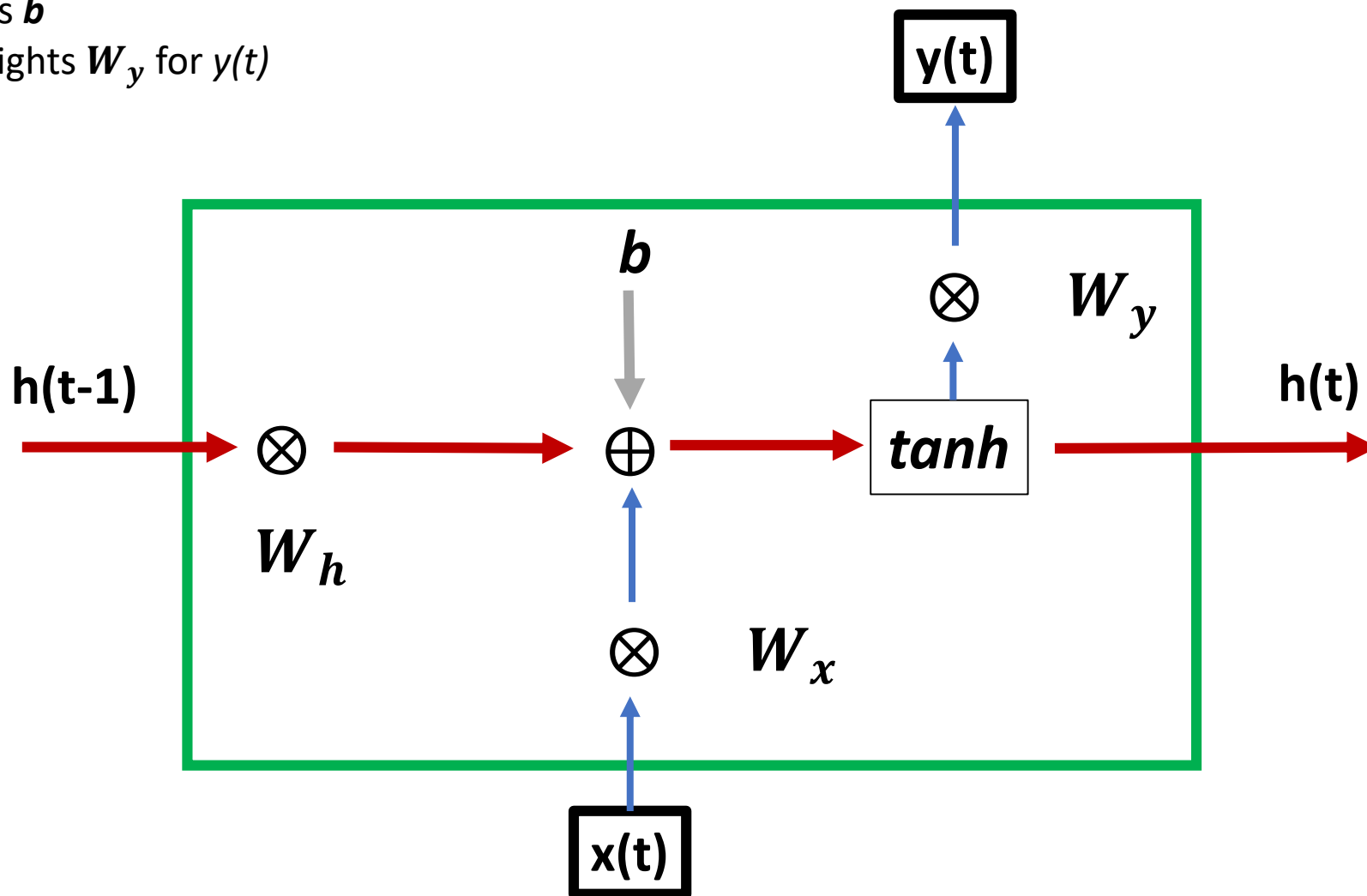
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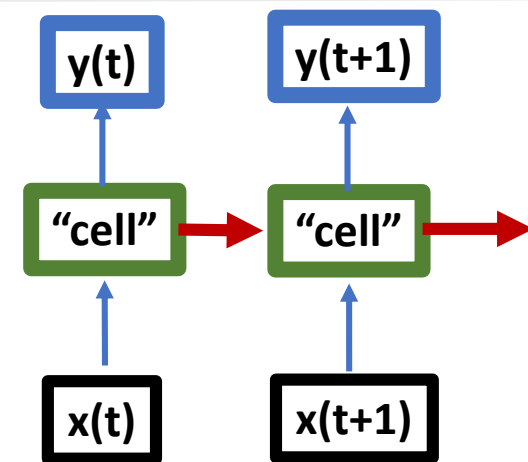


Recurrent Neural Networks - from Scratch

- **state vector** $h(t)$, i. e. the “memory” the system has along time
- weights W_x for $x(t)$
- weights W_h for $h(t)$
- bias b
- weights W_y for $y(t)$



the RNN cell



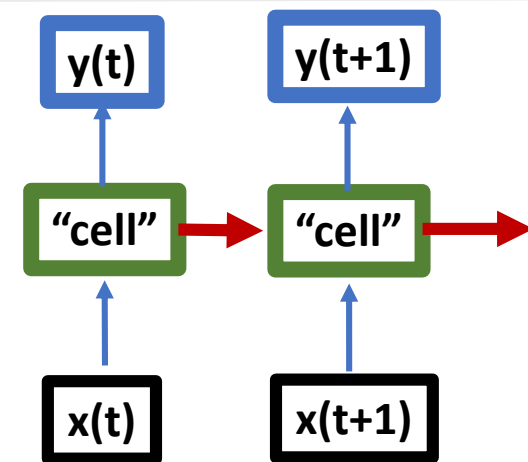
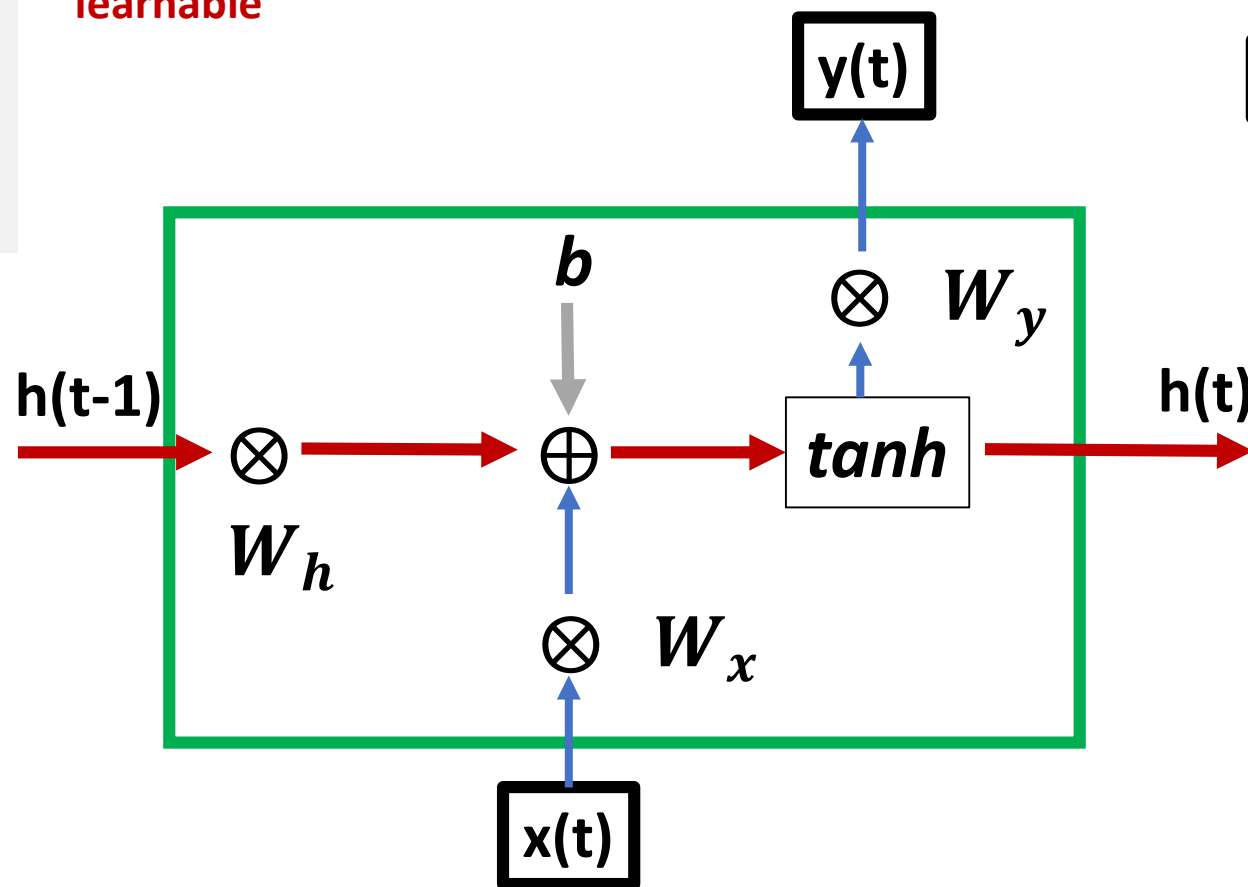


Recurrent Neural Networks – from Scratch

the RNN cell

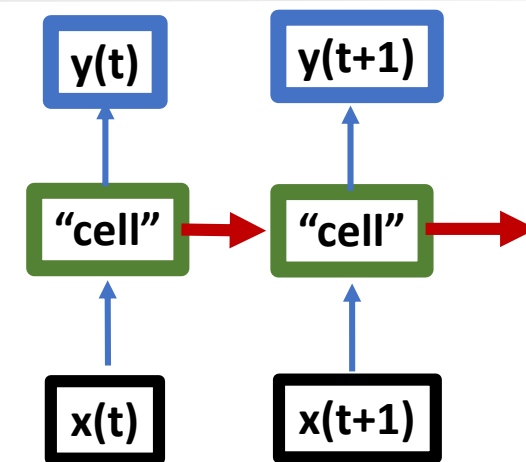
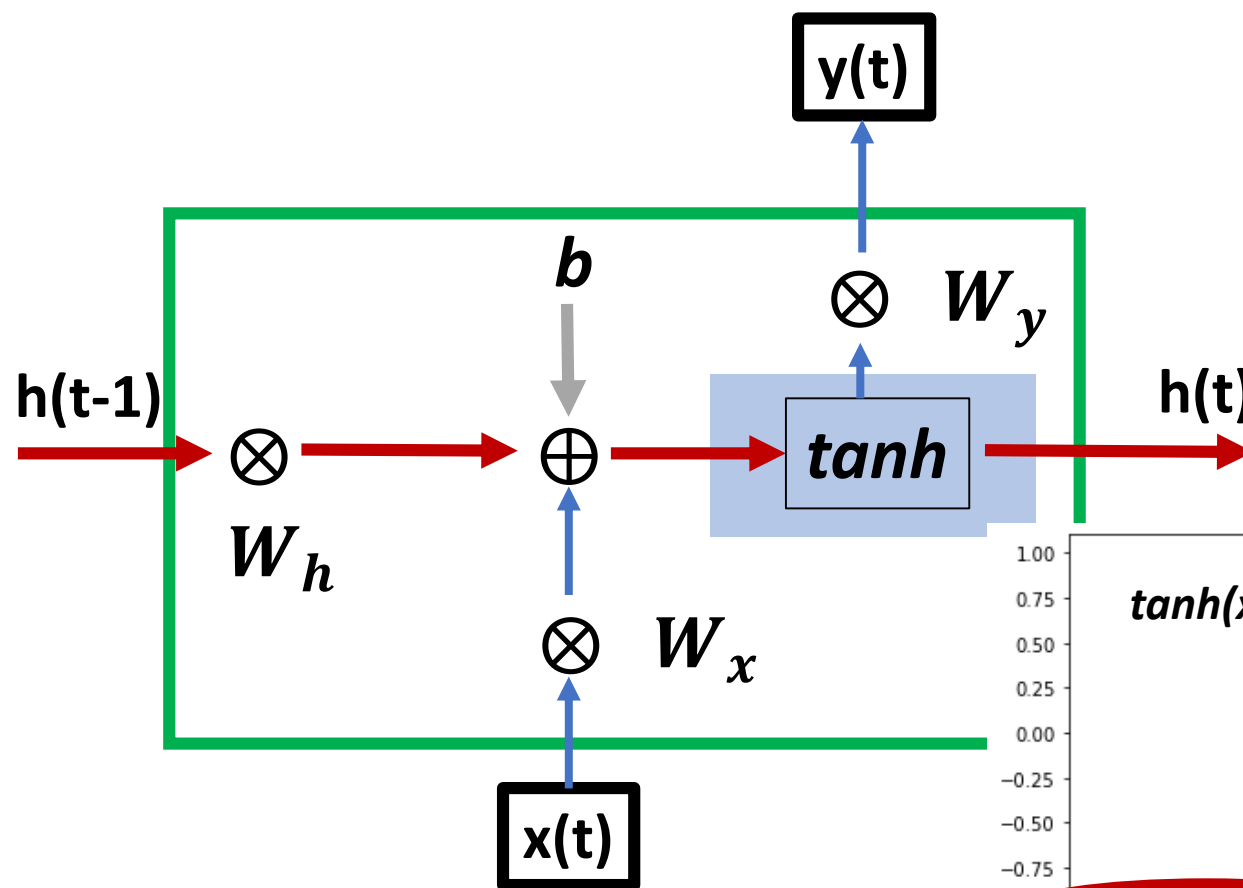
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learnable





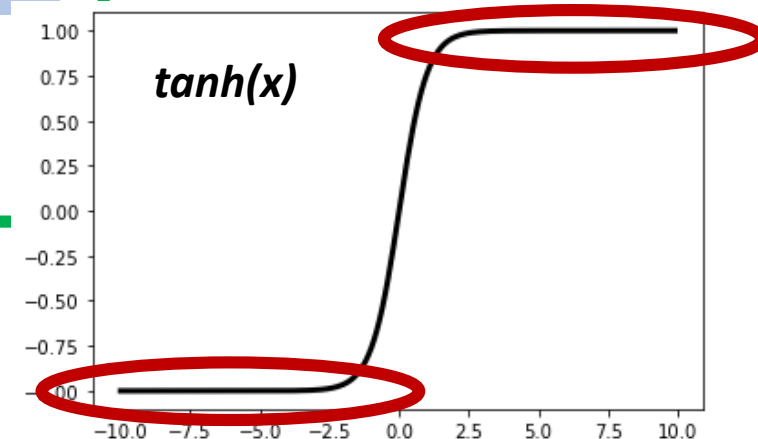
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- weights W_x for $x(t)$
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- bias b
- weights W_y for $y(t)$



for large absolute values:

$$\frac{d \tanh(x)}{dx} \approx 0$$

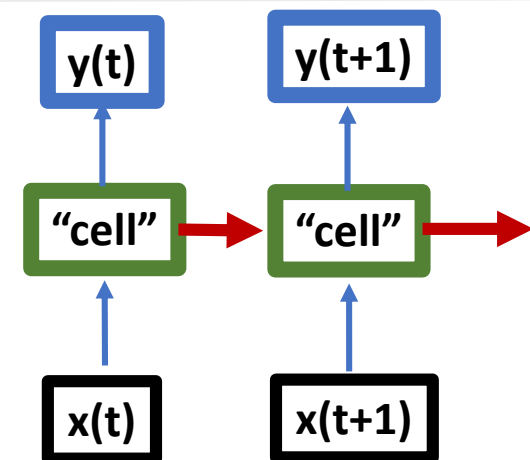
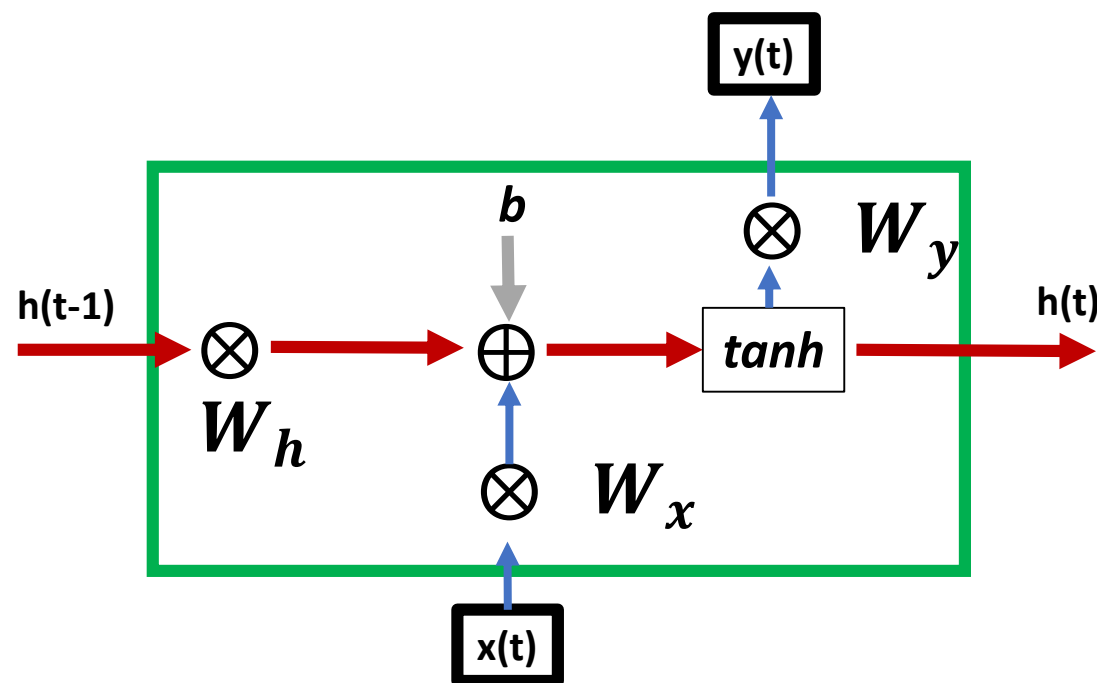
(see later backpropagation)





Recurrent Neural Networks - from Scratch

- **state vector** $h(t)$, i. e. the “memory” the system has along time
- weights W_x for $x(t)$
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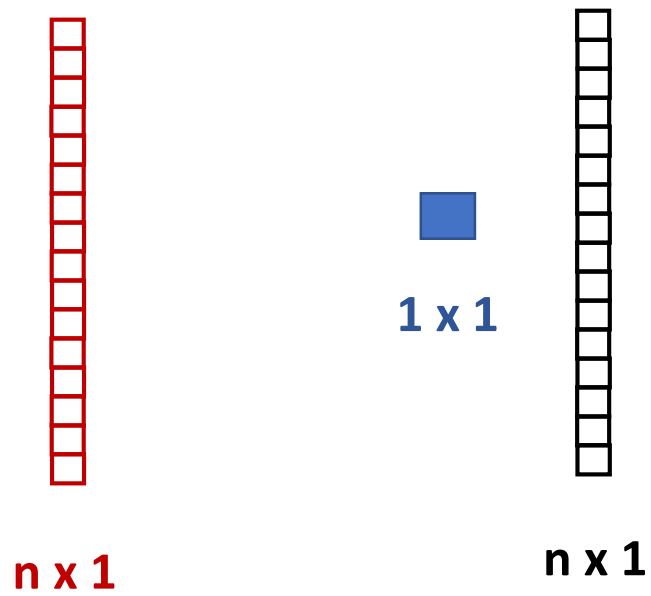


$$h(t) = \tanh[x(t) * W_x + W_h * h(t - 1) + b]$$

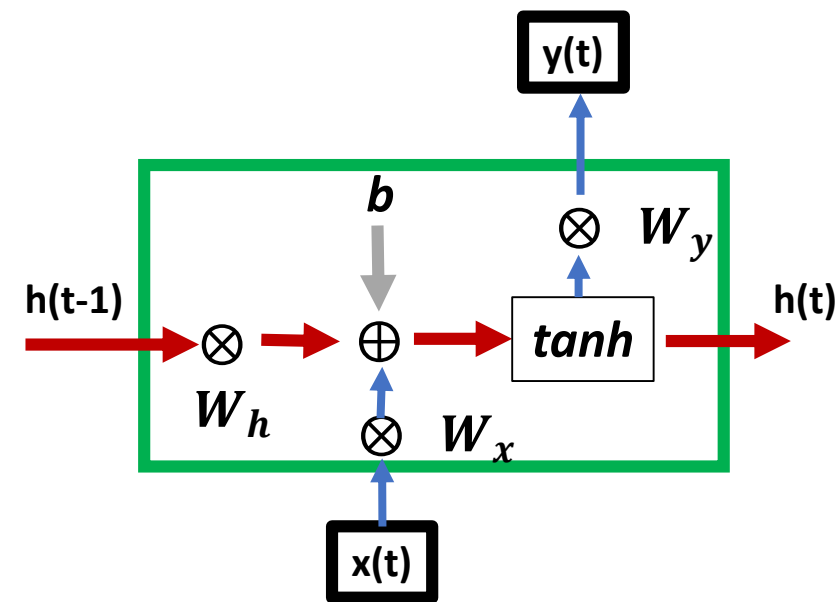
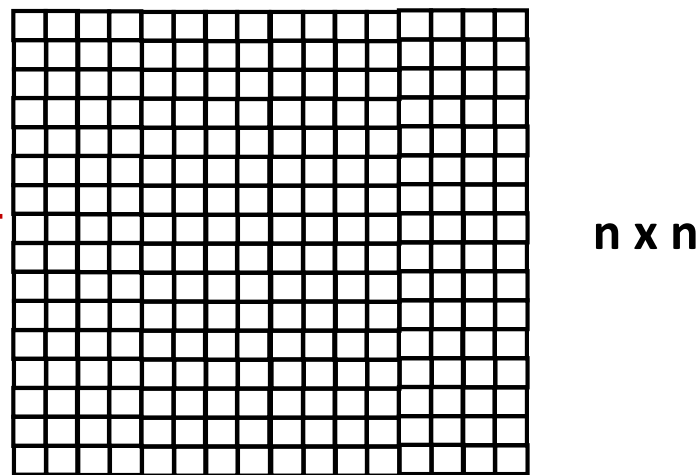
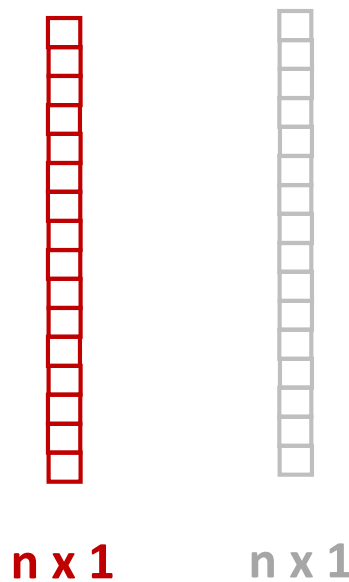
$$y(t) = h(t) * W_y$$



$$h(t) = \tanh[x(t) * W_x + W_h * h(t-1) + b]$$



$$y(t) = h(t) * W_y$$

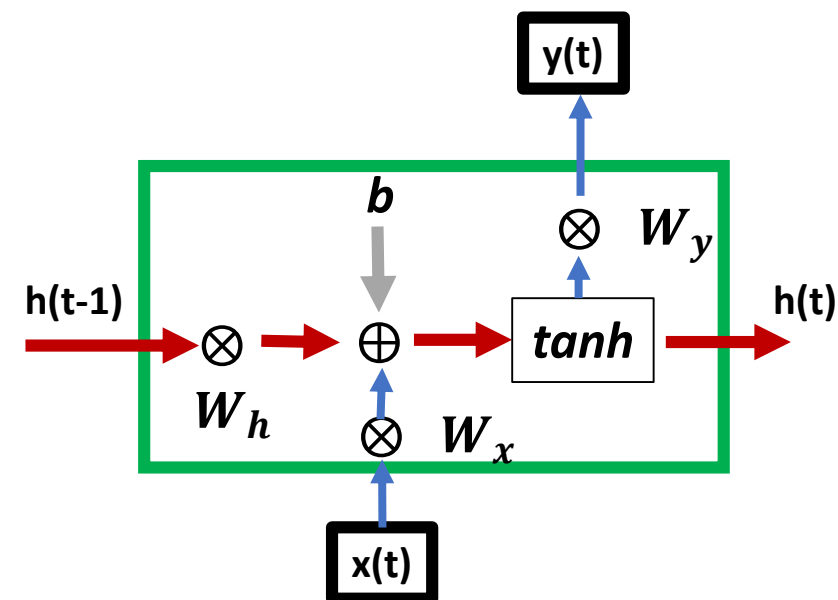
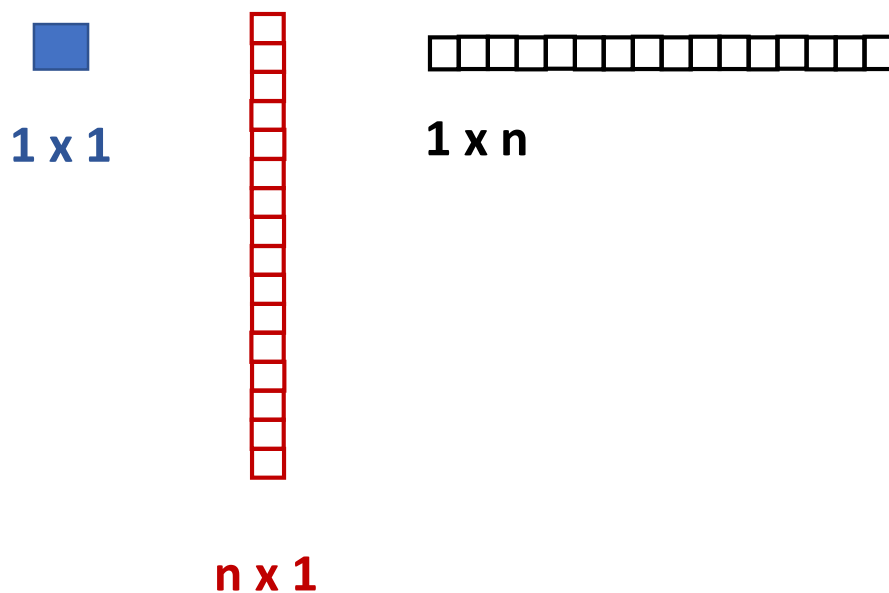


n : number of states/ neurons



$$h(t) = \tanh[x(t) * W_x + W_h * h(t-1) + b]$$

$$y(t) = h(t) * W_y$$



n: number of states/ neurons



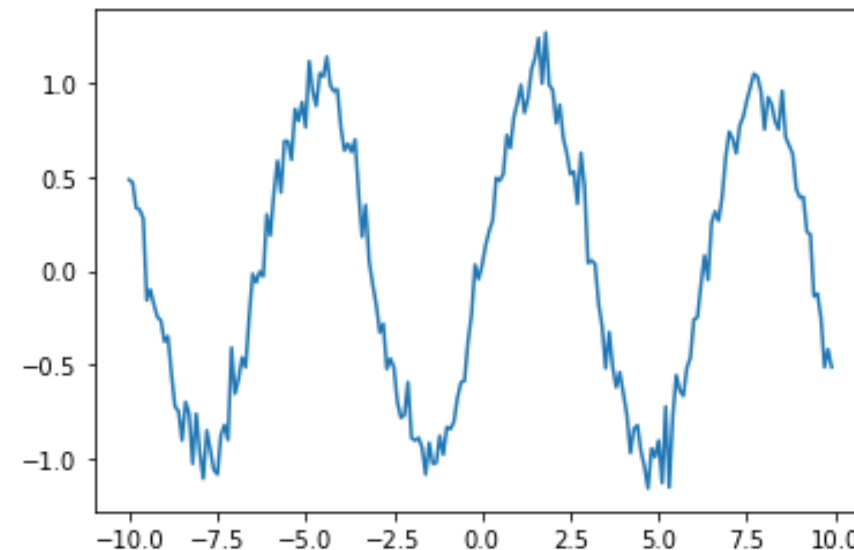
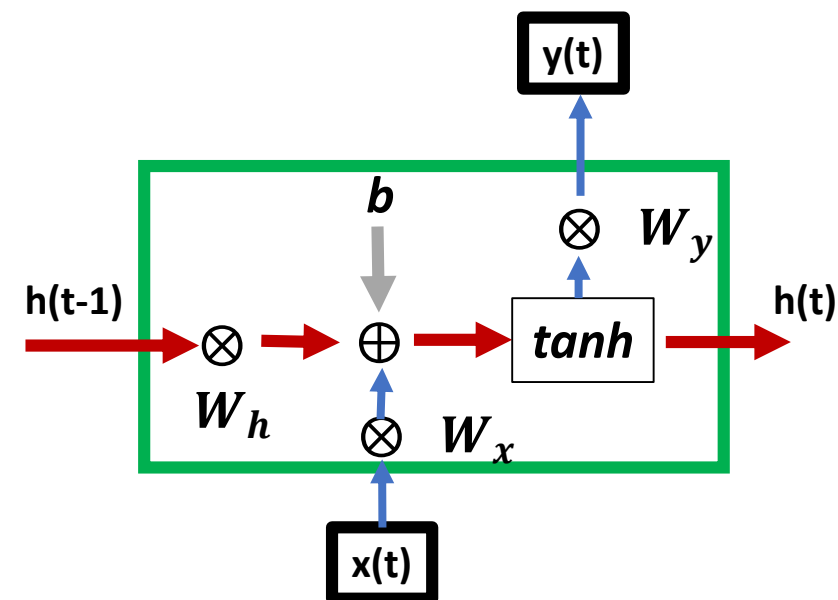
We are ready to build the first cell now!

Aim: training an RNN on noisy periodic data

```
import numpy as np
import matplotlib.pyplot as plt
```

```
X_t = np.arange(-10, 10, 0.1)
X_t = X_t.reshape(len(X_t), 1)
Y_t = np.sin(X_t) + 0.1*np.random.randn(len(X_t), 1)
```

```
plt.plot(X_t, Y_t)
plt.show()
```





We are ready to build the first cell now!

Aim: training an RNN on noisy periodic data

```
import numpy as np
```

```
class RNN():
```

```
    def __init__(self, X_t, n_neurons):
```

```
        self.T      = max(X_t.shape)
```

```
        self.X_t    = X_t
```

```
        self.Y_hat  = np.zeros((self.T, 1))
```

initializing a vector for
the prediction of y , \hat{y}

```
        self.n_neurons = n_neurons
```

we also want to keep
track of the state
vector

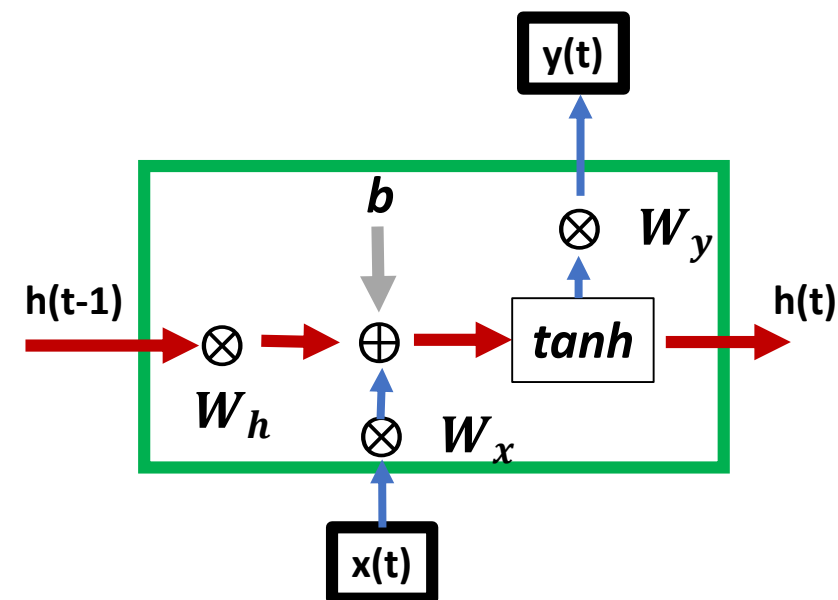
```
        self.Wx      = 0.1*np.random.randn(n_neurons, 1)
```

```
        self.Wh      = 0.1*np.random.randn(n_neurons, n_neurons)
```

```
        self.Wy      = 0.1*np.random.randn(1, n_neurons)
```

```
        self.biases  = 0.1*np.random.randn(n_neurons, 1)
```

```
        self.H       = [np.zeros((n_neurons, 1)) for t in range(self.T + 1)]
```

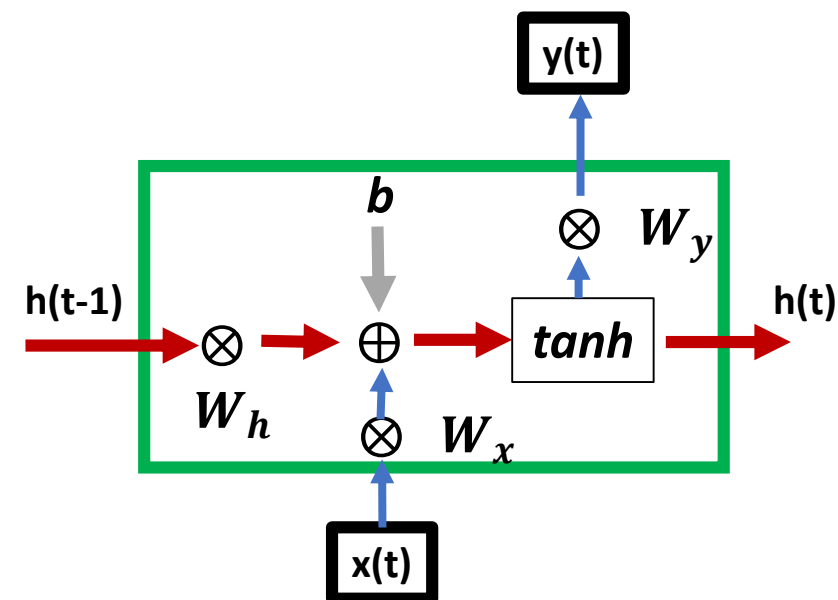




We are ready to build the first cell now!

Aim: training an RNN on noisy periodic data

```
class RNN():  
    def __init__(self, X_t, n_neurons):  
        ...  
        self.H = [np.zeros((n_neurons, 1)) for t in range(self.T + 1)]  
  
    def forward(self, xt, ht_1):  
  
        out      = np.dot(self.Wx, xt) + np.dot(self.Wh, ht_1) + self.biases  
        ht       = np.tanh(out)  
        y_hat_t  = np.dot(self.Wy, ht)  
  
        return ht, y_hat_t, out
```



$$h(t) = \tanh[x(t) * W_x + W_h * h(t-1) + b]$$



let us run a test:

```
n_neurons = 500
```

```
from RNN import *
```

```
rnn = RNN(X_t, n_neurons)
```

```
Y_hat = rnn.Y_hat
```

```
H = rnn.H
```

```
T = rnn.T
```

```
ht = H[0]
```

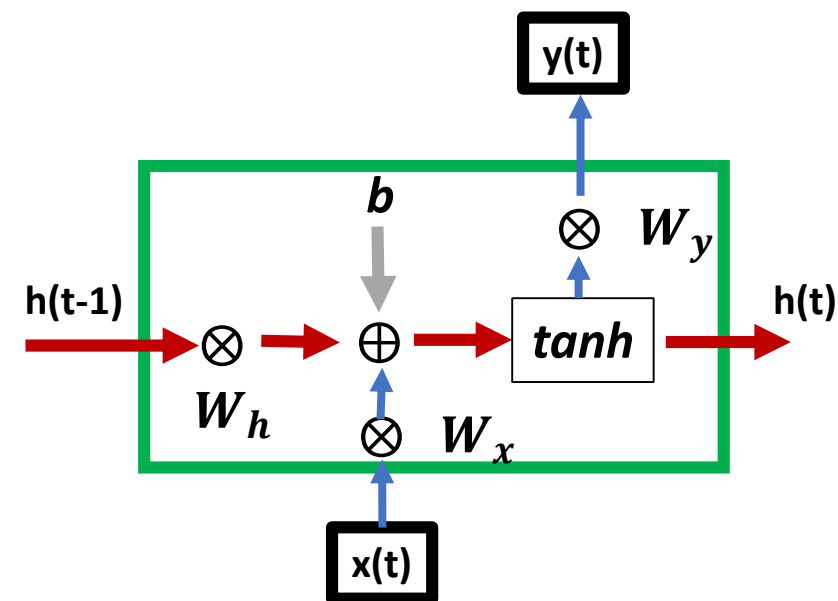
```
for t, xt in enumerate(X_t):
```

```
    xt = xt.reshape(1, 1)
```

```
    [ht, y_hat_t, out] = rnn.forward(xt, ht)
```

```
    H[t+1] = ht
```

```
    Y_hat[t] = y_hat_t
```



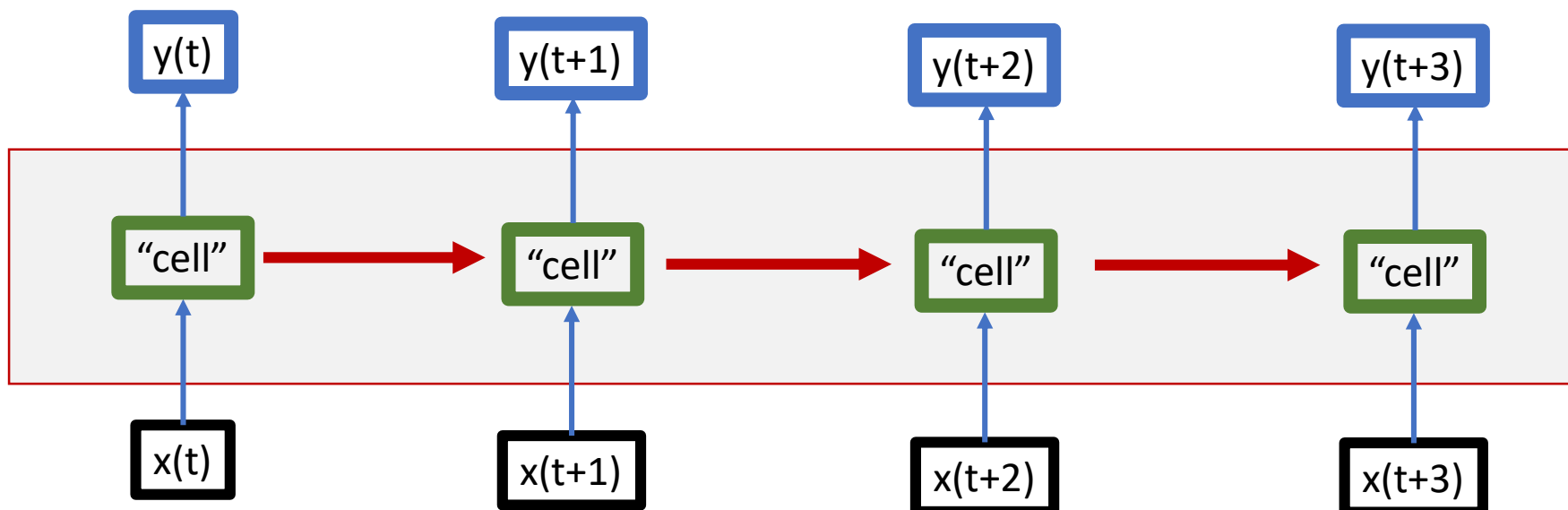
initial state vector

we apply the cell recursively over all t



we apply the cell **recursively** over all t

```
for t, xt in enumerate(X_t):  
    xt = xt.reshape(1, 1)  
    [ht, y_hat_t, out] = rnn.forward(xt, ht)  
    H[t+1] = ht  
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```

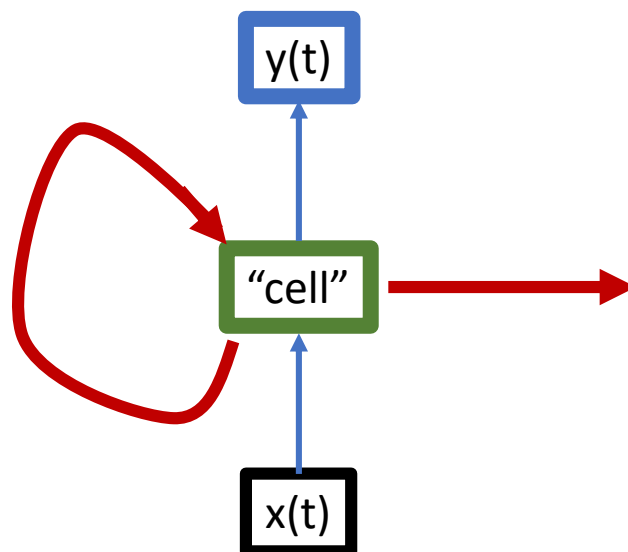




we apply the cell **recursively** over all t

```
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    [ht, y_hat_t, out] = rnn.forward(xt, ht)  
    H[t+1] = ht  
    Y_hat[t] = y_hat_t
```

loop over X_t





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```
rnn = RNN(X_t, n_neurons)
```

```
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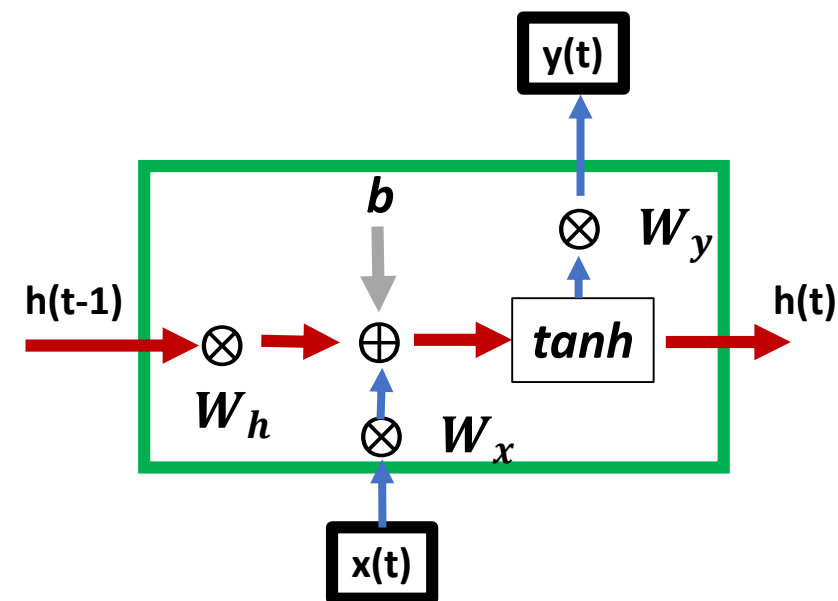
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```

```
    [ht, y_hat_t, out] = rnn.forward(xt, ht)
```

```
    H[t+1] = ht
```

```
    Y_hat[t] = y_hat_t
```





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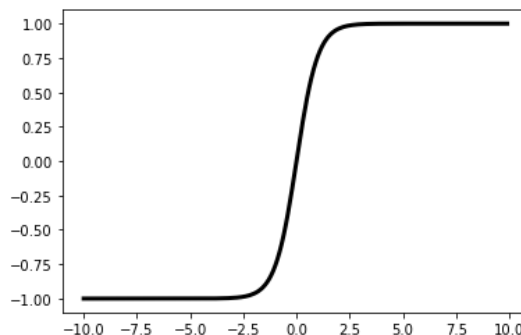
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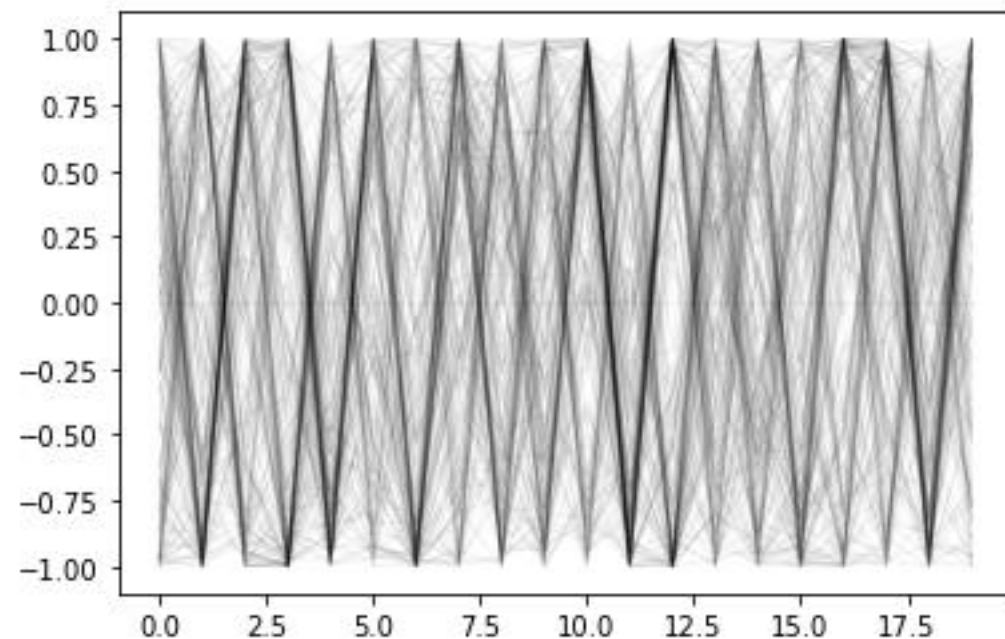
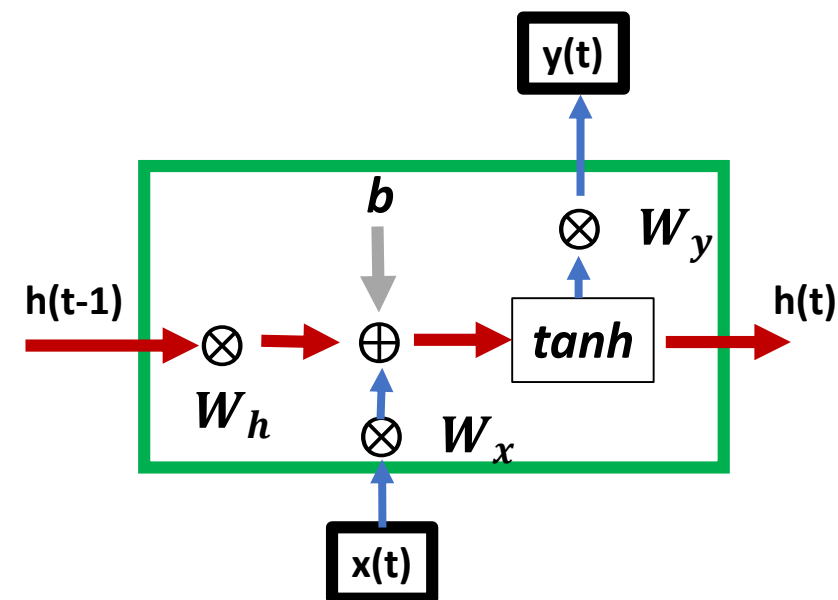
...

```
for h in H:
```

```
    plt.plot(np.arange(20), h[0:20], \
             'k-', linewidth = 1, alpha = 0.05)
```



defined states -1 or +1





let us run a test:

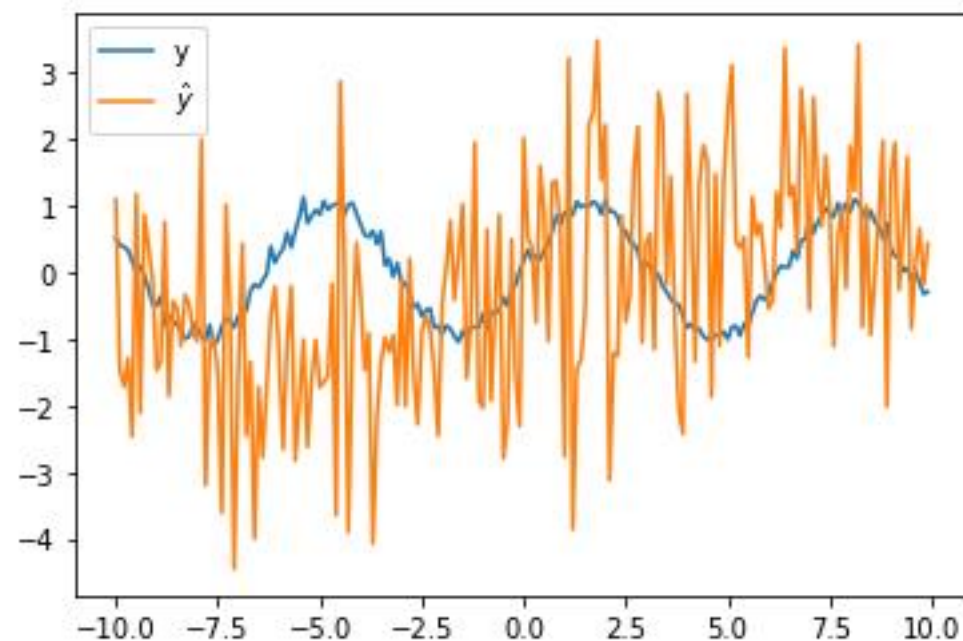
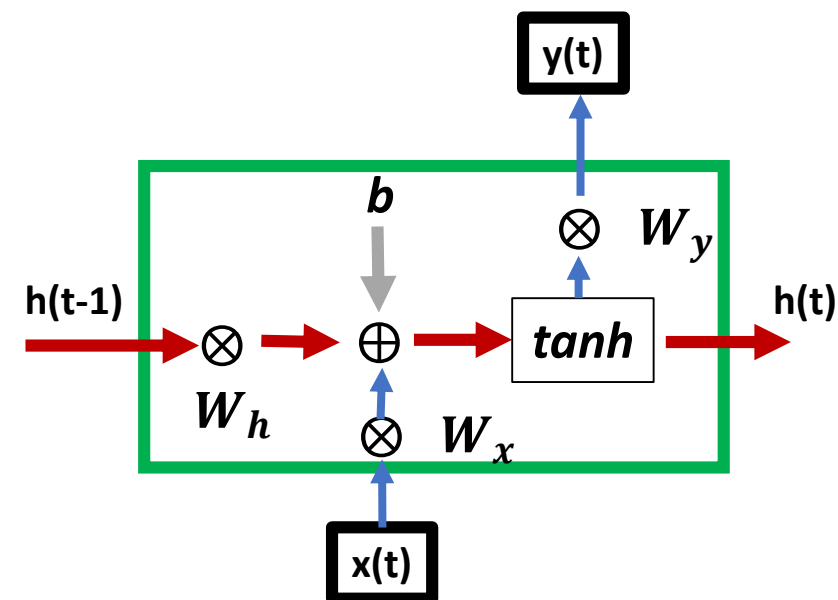
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n_neurons = 500
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```
rnn = RNN(X_t, n_neurons)
```

...

```
plt.plot(X_t, Y_t)  
plt.plot(X_t, Y_hat)  
plt.legend(['y', '$\hat{y}$'])  
plt.show()
```





let us run a test:

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n_neurons = 500
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```
from RNN import *
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rnn = RNN(X_t, n_neurons)
```

```
...
```

```
plt.plot(X_t, Y_t)
```

```
plt.plot(X_t, Y_hat)
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plt.legend(['y', '$\hat{y}$'])
```

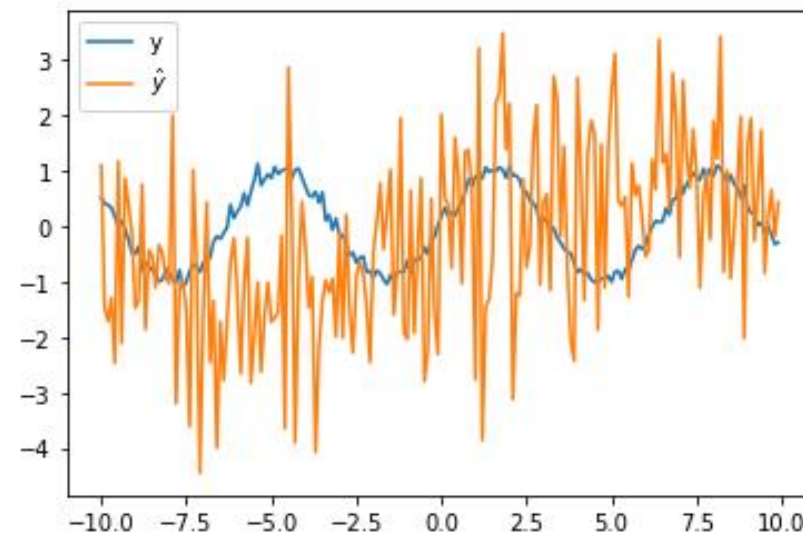
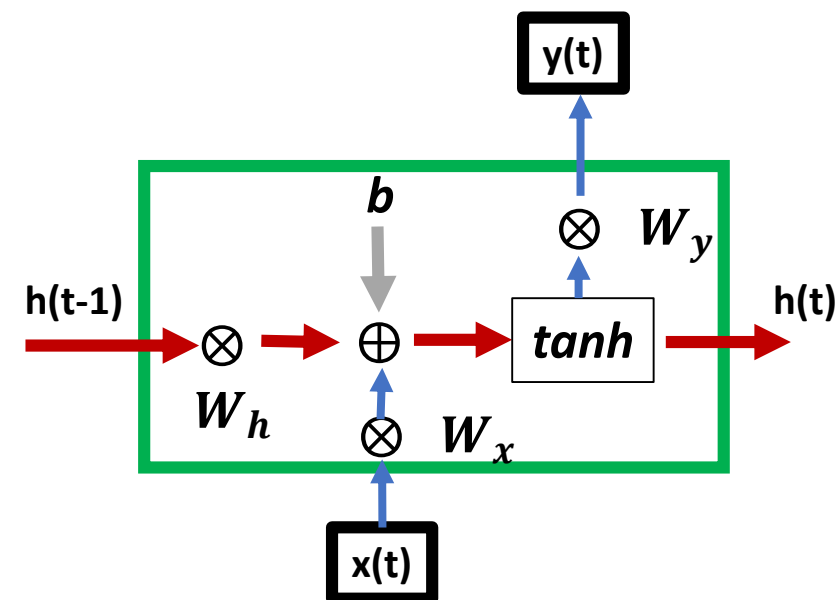
```
plt.show()
```

We can therefore define the **loss** L as MSSE:

dY $= Y_{\text{hat}} - Y_t$

L $= 0.5 * \text{np.dot}(dY.T, dY) / T$

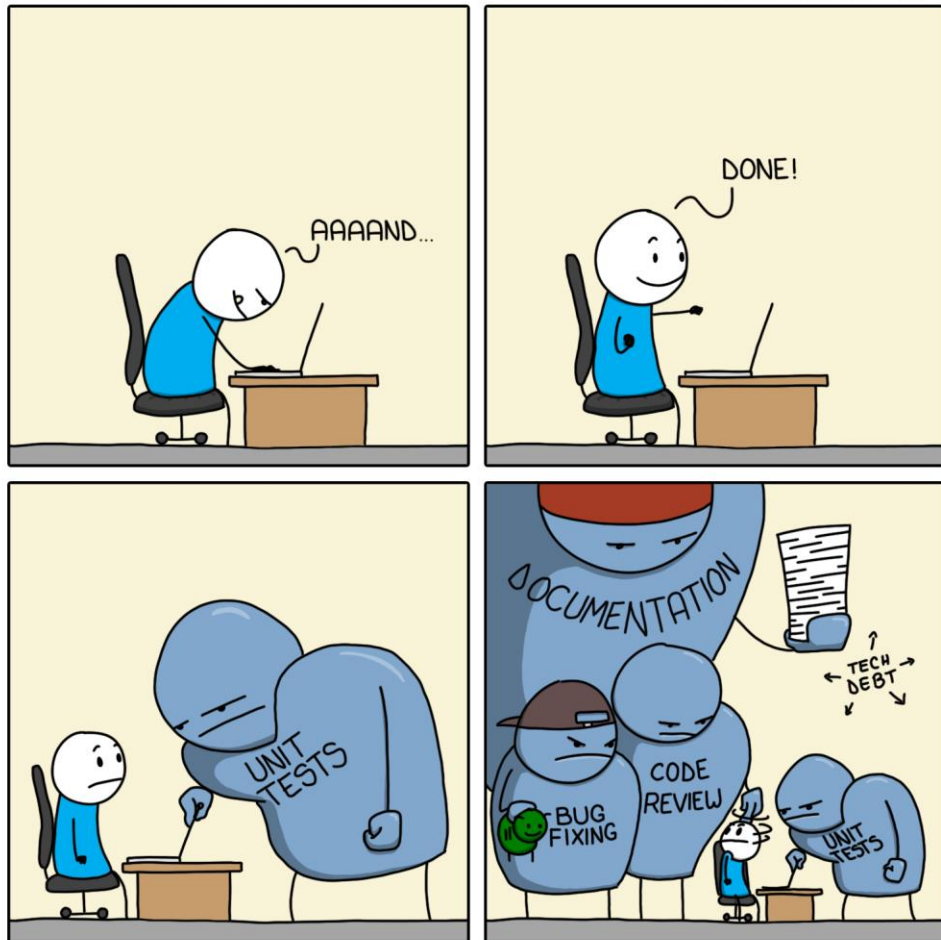
$$L = \frac{1}{2} \sum_{t=1}^T [\hat{y}(t) - y(t)]^2$$





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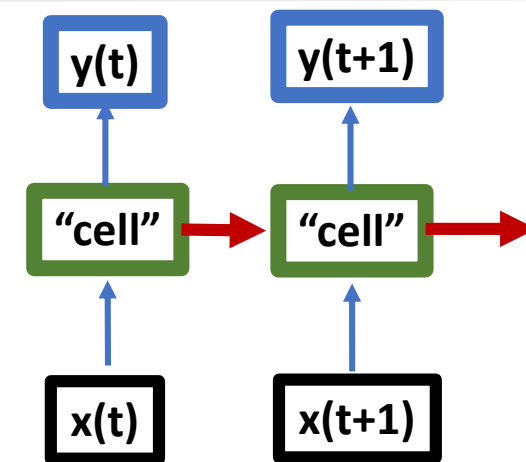
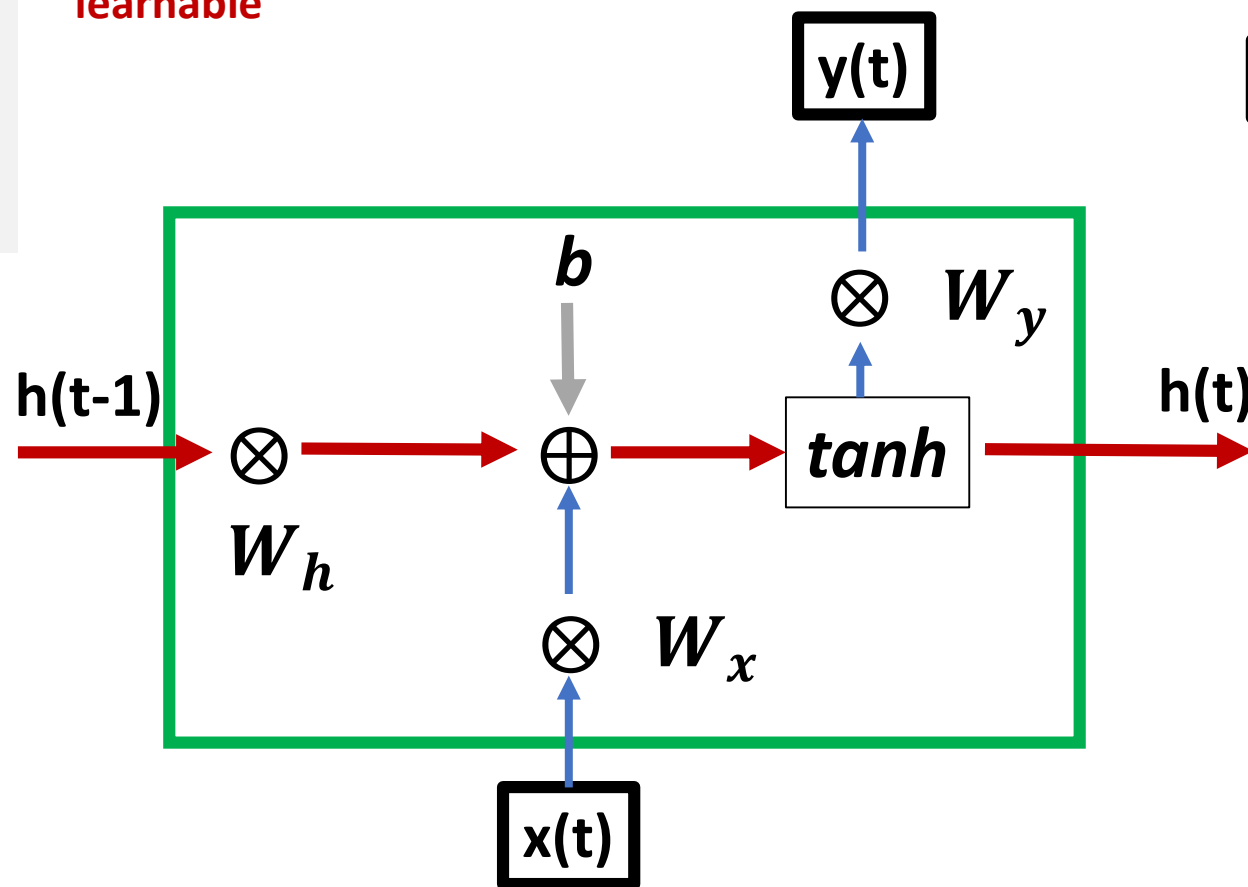
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- weights W_x for $x(t)$
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- bias b
- weights W_y for $y(t)$

learnable



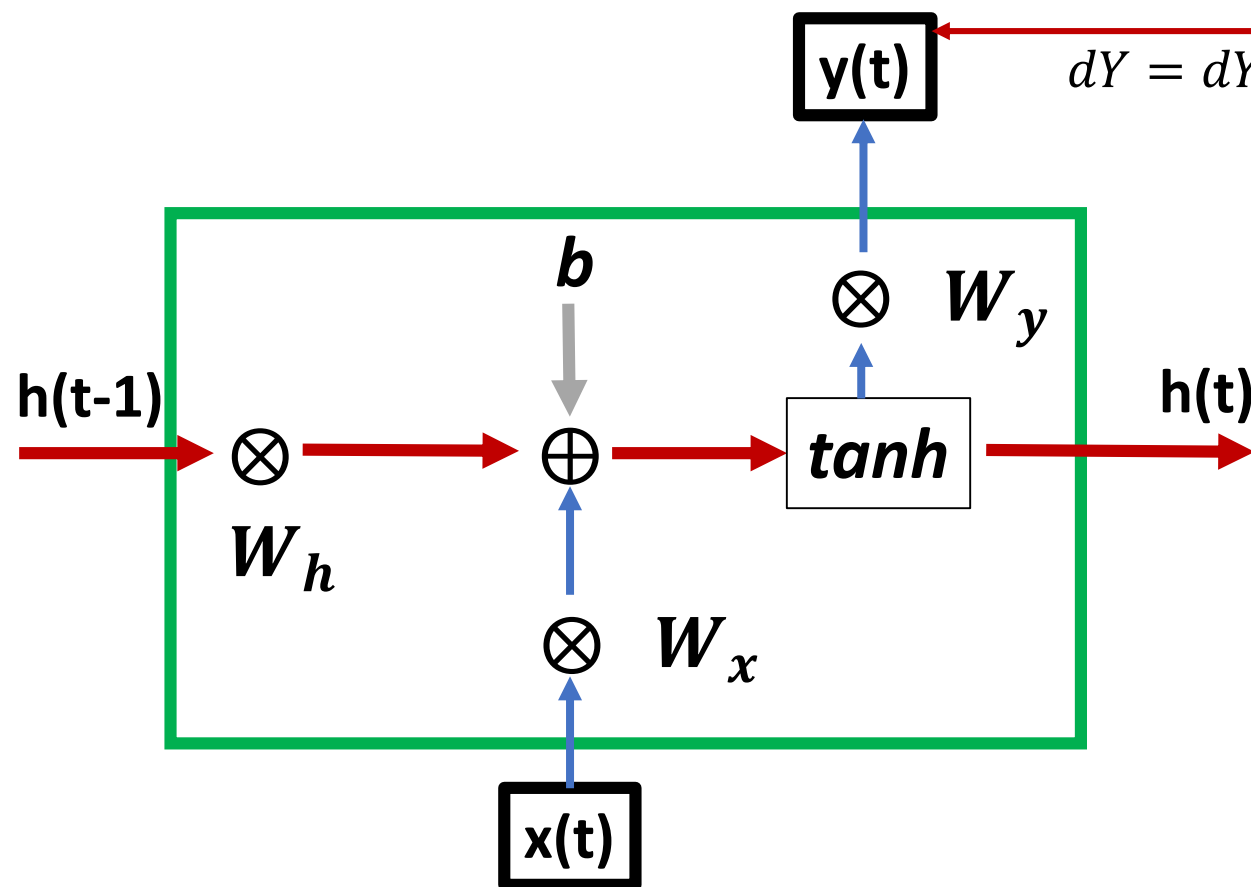


- weights W_x for $x(t)$
- weights W_h for $h(t)$
- bias b
- weights W_y for $y(t)$

$$h(t) = \tanh[x(t) * W_x + W_h * h(t-1) + b]$$

$$y(t) = h(t) * W_y$$

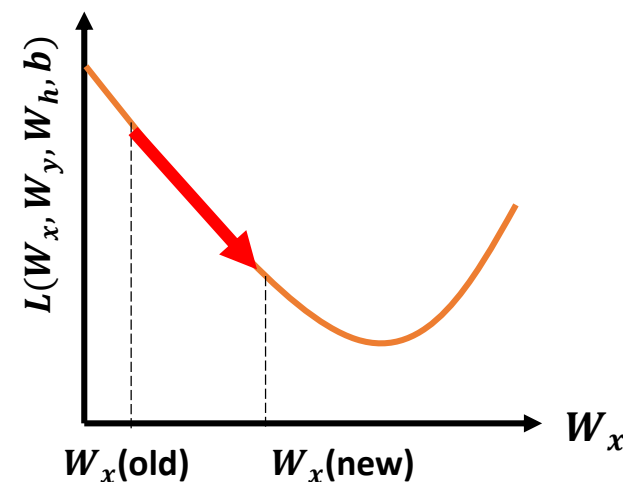
$$L = \frac{1}{2} \sum_{t=1}^T [\hat{y}(t) - y(t)]^2$$



$$dY = dY(W_x, W_y, W_h, b)$$

ϵ : learning rate

$$W_x(\text{new}) = W_x(\text{old}) - \epsilon \frac{dL(W_x, W_y, W_h, b)}{dW_x}$$



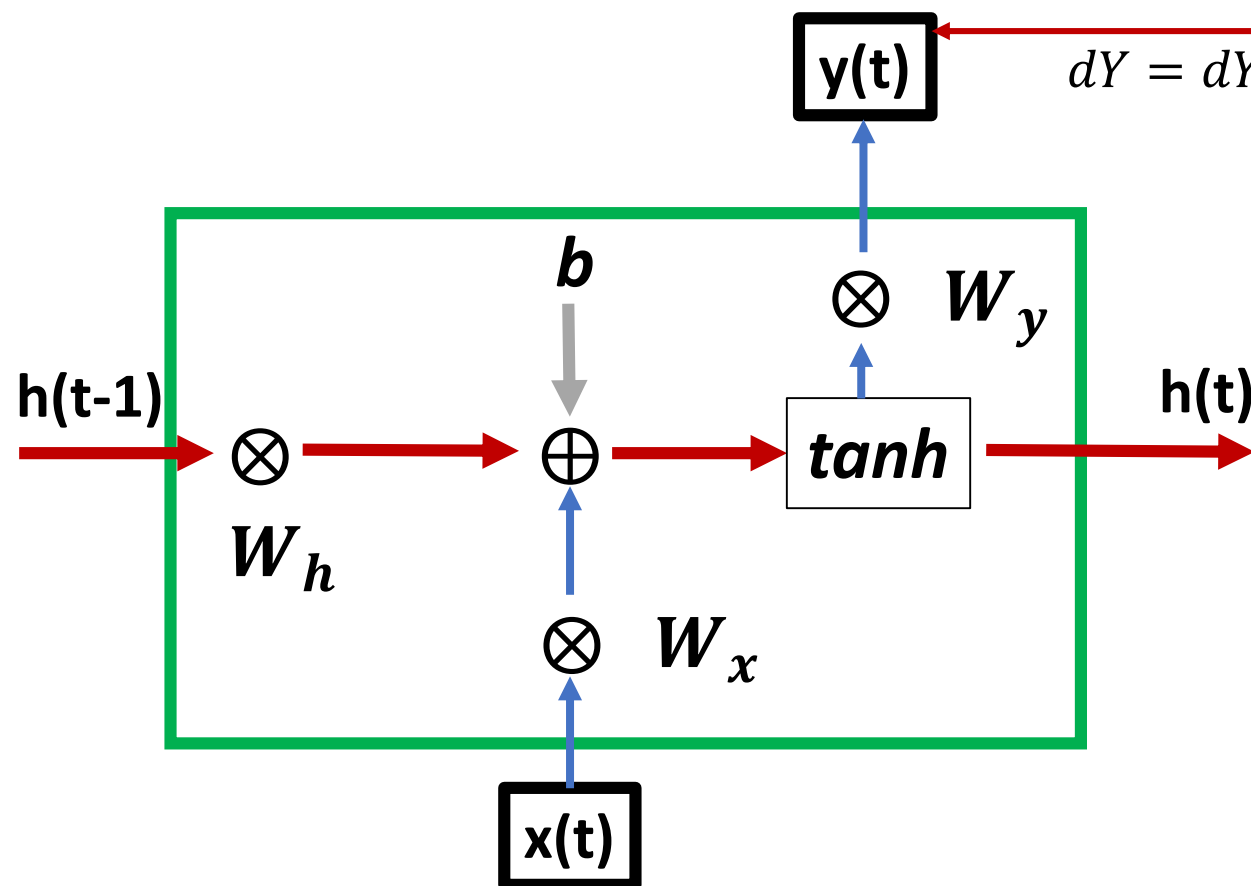


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- bias b
- weights W_y for $y(t)$

$$h(t) = \tanh[x(t) * W_x + W_h * h(t-1) + b]$$

$$y(t) = h(t) * W_y$$

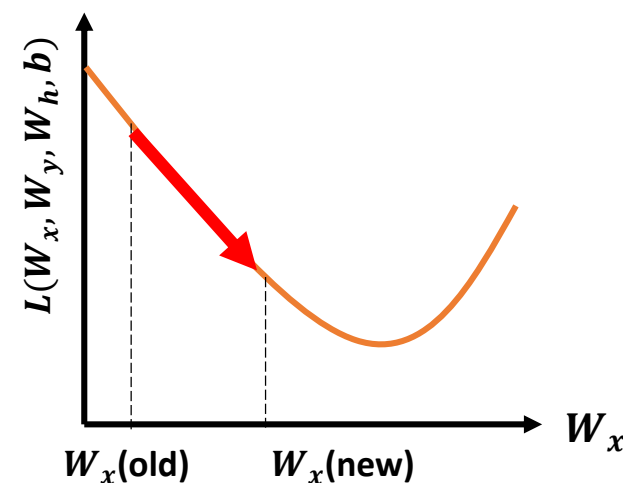
$$L = \frac{1}{2} \sum_{t=1}^T [\hat{y}(t) - y(t)]^2$$



$$dY = dY(W_x, W_y, W_h, b)$$

ϵ : learning rate

$$dW_x = -\epsilon \frac{dL(W_x, W_y, W_h, b)}{dW_x}$$





- weights W_x for $x(t)$
- weights W_h for $h(t)$
- bias b
- weights W_y for $y(t)$

$$h(t) = \tanh[x(t) * W_x + W_h * h(t-1) + b]$$

$$y(t) = h(t) * W_y$$

$$L = \frac{1}{2} \sum_{t=1}^T [\hat{y}(t) - y(t)]^2$$

ϵ : learning rate

$$dW_x = -\epsilon \frac{dL(W_x, W_y, W_h, b)}{dW_x} = -\epsilon \boxed{\frac{dL}{dy}} \frac{dy}{dh(t)} \frac{dh(t)}{d \tanh} \frac{d \tanh}{dW_x}$$

$dY \leftarrow$

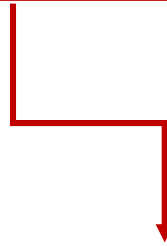


- weights W_x for $x(t)$
- weights W_h for $h(t)$
- bias b
- weights W_y for $y(t)$

ϵ : learning rate

$$h(t) = \tanh[x(t) * W_x + W_h * h(t-1) + b]$$

$$y(t) = h(t) * W_y$$



$$dW_x = -\epsilon \frac{dL(W_x, W_y, W_h, b)}{dW_x} = -\epsilon \frac{dL}{dy} \frac{dy}{dh(t)} \frac{dh(t)}{d \tanh} \frac{d \tanh}{dW_x}$$



- weights W_x for $x(t)$
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$$dW_x = -\epsilon \frac{dL(W_x, W_y, W_h, b)}{dW_x} = -\epsilon \frac{dL}{dy} \frac{dy}{dh(t)} \frac{dh(t)}{d \tanh} \frac{d \tanh}{dW_x}$$

$\frac{dh(t)}{d \tanh}$ is highlighted with a red box in the original image.



- weights W_x for $x(t)$
- weights W_h for $h(t)$
- bias b
- weights W_y for $y(t)$

$$h(t) = \tanh[x(t) * W_x + W_h * h(t-1) + b]$$

$$y(t) = h(t) * W_y$$

ϵ : learning rate

$$dW_x = -\epsilon \frac{dL(W_x, W_y, W_h, b)}{dW_x} = -\epsilon \frac{dL}{dy} \frac{dy}{dh(t)} \frac{dh(t)}{d \tanh} \frac{d \tanh}{dW_x}$$

Diagrammatic annotations: A red box highlights $x(t) * W_x$ in the forward pass equation. A red arrow points from this box to the $\frac{d \tanh}{dW_x}$ term in the backward pass equation. Above the backward pass equation, the terms $\frac{dL}{dy}$, W_y , $1 - \tanh^2$, and $x(t)$ are written in red.



- weights W_x for $x(t)$
- weights W_h for $h(t)$
- bias b
- weights W_y for $y(t)$

$$h(t) = \tanh[x(t) * W_x + W_h * h(t-1) + b]$$

$$y(t) = h(t) * W_y$$

ϵ : learning rate

$$dW_x = -\epsilon \frac{dL(W_x, W_y, W_h, b)}{dW_x} = -\epsilon \frac{dL}{dy} \frac{dy}{dh(t)} \frac{dh(t)}{d \tanh} \frac{d \tanh}{dW_x} = -\epsilon * dY * W_y * (1 - \tanh^2) * x(t)$$

$$dW_y = -\epsilon \frac{dL(W_x, W_y, W_h, b)}{dW_y} = -\epsilon \frac{dL}{dy} \frac{dy}{dW_y} = -\epsilon * dY * h(t)$$



- weights W_x for $x(t)$
- weights W_h for $h(t)$
- bias b
- weights W_y for $y(t)$

$$h(t) = \tanh[x(t) * W_x + W_h * h(t-1)] + b$$

$$y(t) = h(t) * W_y$$

ϵ : learning rate

$$dW_x = -\epsilon \frac{dL(W_x, W_y, W_h, b)}{dW_x} = -\epsilon \frac{dL}{dy} \frac{dy}{dh(t)} \frac{dh(t)}{d \tanh} \frac{d \tanh}{dW_x} = -\epsilon * dY * W_y * (1 - \tanh^2) * x(t)$$

$$dW_y = -\epsilon \frac{dL(W_x, W_y, W_h, b)}{dW_y} = -\epsilon \frac{dL}{dy} \frac{dy}{dW_y} = -\epsilon * dY * h(t)$$

$$dW_h = -\epsilon \frac{dL(W_x, W_y, W_h, b)}{dW_h} = -\epsilon \frac{dL}{dy} \frac{dy}{dh(t)} \frac{dh(t)}{d \tanh} \frac{d \tanh}{dW_h} = -\epsilon * dY * W_y * (1 - \tanh^2) * h(t-1)$$



- weights W_x for $x(t)$
- weights W_h for $h(t)$
- bias b
- weights W_y for $y(t)$

$$h(t) = \tanh[x(t) * W_x + W_h * h(t-1) + b]$$

$$y(t) = h(t) * W_y$$

ϵ : learning rate

$$dW_x = -\epsilon * dY * W_y * (1 - \tanh^2) * x(t)$$

$$dW_y = -\epsilon * dY * h(t)$$

$$dW_h = -\epsilon * dY * W_y * (1 - \tanh^2) * h(t-1)$$

$$db = -\epsilon * dY * W_y * (1 - \tanh^2)$$



- weights W_x for $x(t)$
- weights W_h for $h(t)$
- bias b
- weights W_y for $y(t)$

$$h(t) = \tanh[x(t) * W_x + W_h * h(t-1) + b]$$

$$y(t) = h(t) * W_y$$

ϵ : learning rate

$$dW_x = -\epsilon * dY * W_y * (1 - \tanh^2) * x(t)$$

$$dW_y = -\epsilon * dY * h(t)$$

$$dW_h = -\epsilon * dY * W_y * (1 - \tanh^2) * h(t-1)$$

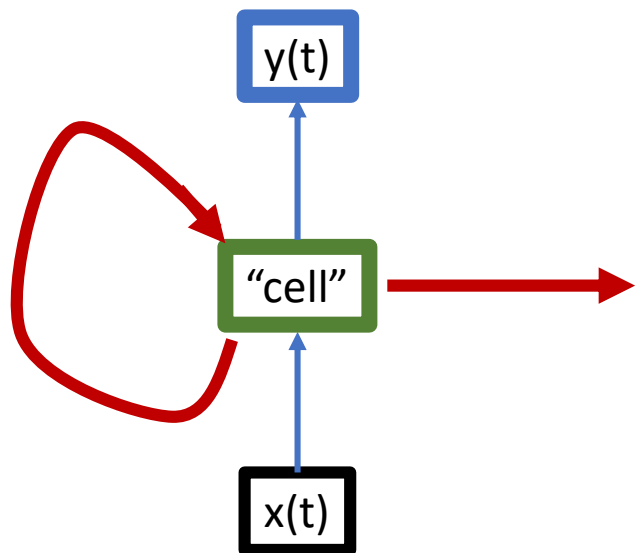
$$db = -\epsilon * dY * W_y * (1 - \tanh^2)$$



$$\begin{aligned}dW_x &= -\epsilon * dY * W_y * (1 - \tanh^2) * x(t) \\dW_y &= -\epsilon * dY * h(t) \\dW_h &= -\epsilon * dY * W_y * (1 - \tanh^2) * h(t-1) \\db &= -\epsilon * dY * W_y * (1 - \tanh^2)\end{aligned}$$

```
for t, xt in enumerate(X_t):  
    xt = xt.reshape(1, 1)  
    [ht, y_hat_t, out] = rnn.forward(xt, ht)  
    H[t+1] = ht  
    Y_hat[t] = y_hat_t
```

loop over X_t



this has to be done **reversely over time**

- different $dy(t)$ for **each t**
- derivative for **each \tanh at time t**
- they **all** contribute to dW_x , dW_y , dW_h and db
- we need to write a **reversed loop** for the backpropagation part
- **BackPropagation Through Time (BPTT)**



We need to restructure the code slightly:

- 1) creating a class for the activation function (tanh)
 - we can call **different instances during the loop** and **keep track of the derivatives**
- 2) defining the forward part of the cell as own method
 - makes the code more readable



We need to restructure the code slightly:

1) creating a class for the activation function (tanh)

→ we can call **different instances during the loop** and **keep track of the derivatives**

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→ makes the code more readable

$$h(t) = \tanh[x(t) * W_x + W_h * h(t-1) + b]$$

class Tanh:

```
def forward(self, inputs):  
    self.output = np.tanh(inputs)  
    self.inputs = inputs
```

```
def backward(self, dvalues):  
    deriv = 1 - self.output**2  
    self.dinputs = np.multiply(deriv, dvalues)
```

$dh(t)$

$(1 - \tanh^2)$

$(1 - \tanh^2) * dh(t)$



We need to restructure the code slightly:

- 1) creating a class for the activation function (tanh)
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- 2) defining the forward part of the cell as own method
→ makes the code more readable

```
class RNN():
```

```
    def __init__(self, X_t, n_neurons, Activation):
```

```
        ...
```

```
        self.H = [np.zeros((n_neurons, 1)) for t in range(self.T + 1)]
```

```
        self.Activation = Activation
```

```
    def forward(self, xt, ht_1):
```

we want to be more flexible
concerning the activation
(see also later)



- 2) defining the forward part of the cell as own method
→ makes the code more readable

```
def forward(self):
```

```
    #initializing dweights
```

```
    self.dwx = np.zeros((self.n_neurons, 1))
```

```
    self.dwh = np.zeros((self.n_neurons, self.n_neurons))
```

```
    self.dwy = np.zeros((1, self.n_neurons))
```

```
    self.dbiases = np.zeros((self.n_neurons, 1))
```

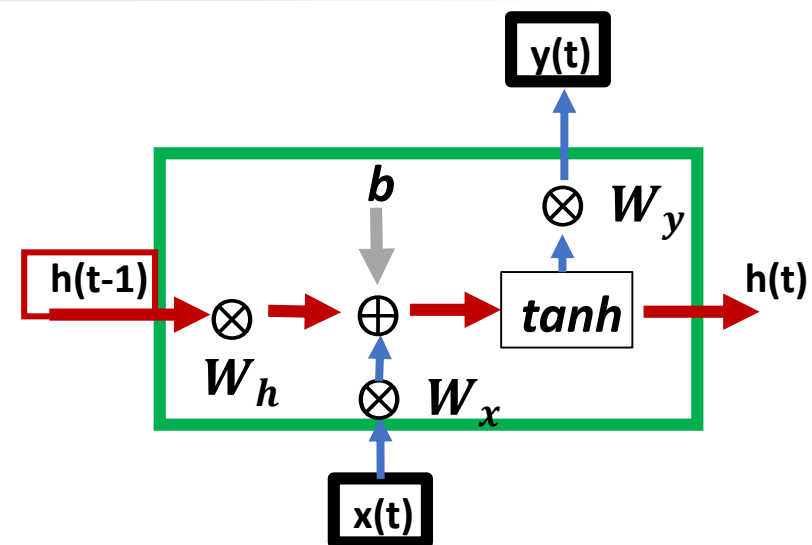
```
    #extracting variables we are going to need
```

```
    X_t = self.X_t
```

```
    H = self.H
```

```
    Y_hat = self.Y_hat
```

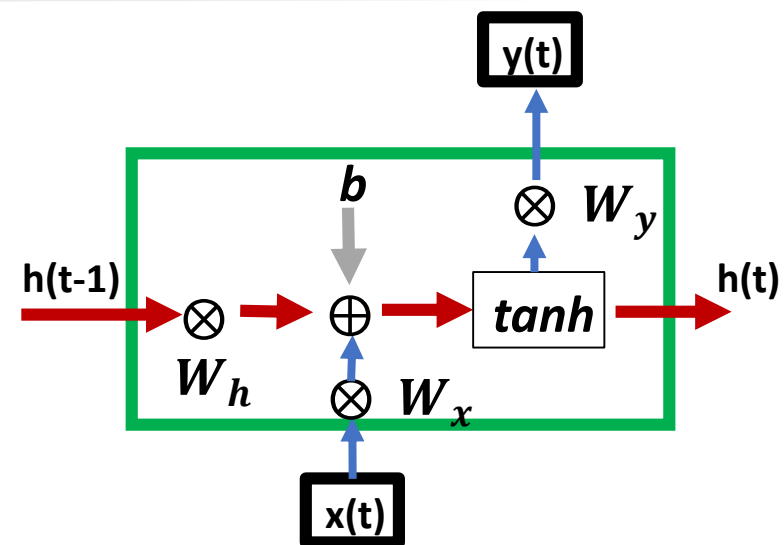
```
    ht = H[0] # initial state vector
```





We need to store the outer derivative ($1 - \tanh^2$)
for every time point t :

```
self.output = np.tanh(inputs)
...
deriv        = 1 - self.output**2
```



```
def forward(self):
```

```
...
```

```
    ht          = H[0]# initial state vector
```

```
    Activation   = self.Activation
```

```
    ACT         = [Activation for i in range(self.T)]
```

storing instances of an activation
function in a list:
makes the code even more flexible



- 1) creating a class for the activation function (tanh)
→ we can call **different instances during the loop** and **keep track of the derivatives**
- 2) defining the forward part of the cell as **own method in the RNN class**
→ makes the code more readable

```
def RNNCell(self, X_t, ht, ACT, H, Y_hat):
```

```
    for t, xt in enumerate(X_t):
```

```
        xt      = xt.reshape(1, 1)
```

```
        out     = np.dot(self.Wx, xt) + np.dot(self.Wh, ht) + self.biases
```

```
        ACT[t].forward(out)
```

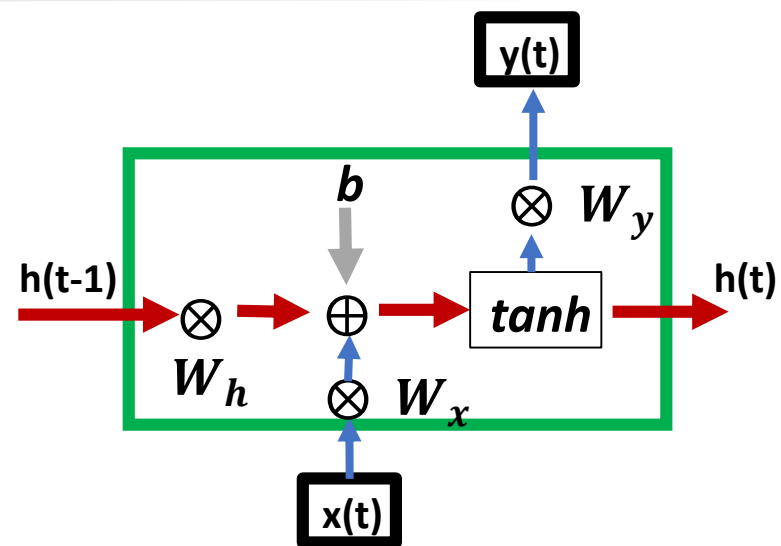
```
        ht     = ACT[t].output
```

```
        y_hat_t = np.dot(self.Wy, ht)
```

```
        H[t+1]  = ht
```

```
        Y_hat[t] = y_hat_t
```

```
    return(ACT,H,Y_hat)
```





- 1) creating a class for the activation function (tanh)
→ we can call **different instances during the loop** and **keep track of the derivatives**
- 2) defining the forward part of the cell as **own method in the RNN class**
→ makes the code more readable

```
def forward(self):
```

```
...
```

```
    ht = H[0]# initial state vector
```

```
    Activation = self.Activation
```

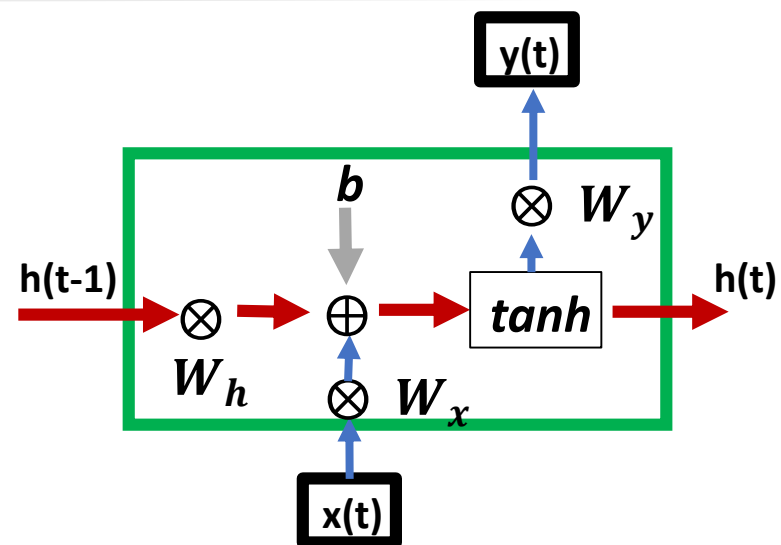
```
    ACT = [Activation for i in range(self.T)]
```

```
    [ACT,H,Y_hat] = self.RNNCell(X_t, ht, ACT, H, Y_hat)
```

```
    self.Y_hat = Y_hat
```

```
    self.H = H
```

```
    self.ACT = ACT
```





The code so far:

```
class Tanh:
```

```
    def forward(self, inputs):  
        self.output = np.tanh(inputs)  
        self.inputs = inputs  
  
    def backward(self, dvalues):  
        deriv = 1 - self.output**2  
        self.dinputs = np.multiply(deriv, dvalues)
```



The code so far:

```
import numpy as np
```

```
class RNN():
```

```
    def __init__(self, X_t, n_neurons, Activation):
```

```
        self.T = max(X_t.shape)
```

```
        self.X_t = X_t
```

```
        self.Y_hat = np.zeros((self.T, 1))
```

```
        self.n_neurons = n_neurons
```

```
        self.Wx = 0.1*np.random.randn(n_neurons, 1)
```

```
        self.Wh = 0.1*np.random.randn(n_neurons, n_neurons)
```

```
        self.Wy = 0.1*np.random.randn(1, n_neurons)
```

```
        self.biases = 0.1*np.random.randn(n_neurons, 1)
```

```
        self.H = [np.zeros((self.n_neurons,1)) for t in range(self.T + 1)]
```

```
        self.Activation = Activation
```



The code so far:

```
class RNN():
```

```
...
```

```
    self.Activation = Activation
```

```
    def forward(self):
```

```
        self.dWx = np.zeros((self.n_neurons, 1))
```

```
        self.dWh = np.zeros((self.n_neurons, self.n_neurons))
```

```
        self.dWy = np.zeros((1, self.n_neurons))
```

```
        self.dbiases = np.zeros((self.n_neurons, 1))
```

```
        X_t = self.X_t
```

```
        H = self.H
```

```
        Y_hat = self.Y_hat
```

```
        ht = H[0]# initial state vector
```

```
        Activation = self.Activation
```

```
        ACT = [Activation for i in range(self.T)]
```

```
        [ACT,H,Y_hat] = self.RNNCell(X_t, ht, ACT, H, Y_hat)
```



The code so far:

```
class RNN():
```

```
...
```

```
    self.Activation = Activation
```

```
    def forward(self):
```

```
...
```

```
        ACT = [Activation for i in range(self.T)]
```

```
        [ACT,H,Y_hat] = self.RNNCell(X_t, ht, ACT, H, Y_hat)
```

```
        self.Y_hat = Y_hat
```

```
        self.H = H
```

```
        self.ACT = ACT
```



The code so far:

```
class RNN():
    ...

    def forward(self):
        ...

        self.ACT          = ACT

    def RNNCell(self, X_t, ht, ACT, H, Y_hat):

        for t, xt in enumerate(X_t):

            xt          = xt.reshape(1, 1)
            out         = np.dot(self.Wx, xt) + np.dot(self.Wh, ht) + self.biases

            ACT[t].forward(out)
            ht  = ACT[t].output

            y_hat_t     = np.dot(self.Wy, ht)
            H[t+1]      = ht
            Y_hat[t]    = y_hat_t

        return(ACT,H,Y_hat)
```



Let us test run the code:

```
from RNN import *
```

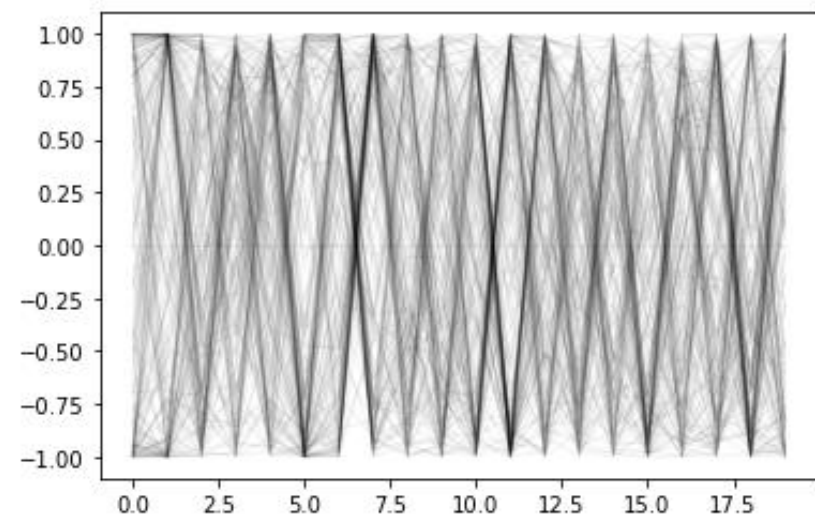
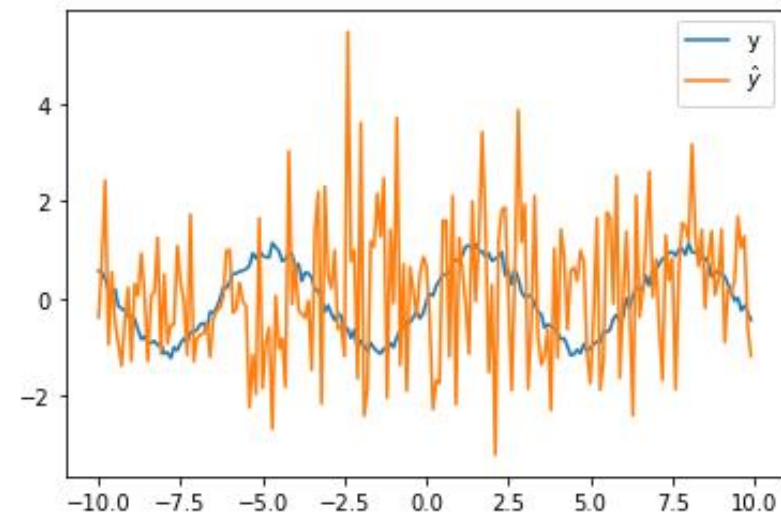
```
rnn = RNN(X_t, n_neurons, Tanh())  
rnn.forward()
```

```
Y_hat = rnn.Y_hat  
H      = rnn.H  
T      = rnn.T
```

```
dY      = Y_hat - Y_t  
L        = 0.5*np.dot(dY.T,dY)/T
```

```
plt.plot(X_t, Y_t)  
plt.plot(X_t, Y_hat)  
plt.legend(['y', '$\hat{y}$'])  
plt.show()
```

```
for h in H:  
    plt.plot(np.arange(20), h[0:20], 'k-', linewidth = 1, alpha = 0.05)
```





Let us test run the code:

```
from RNN import *
```

```
rnn = RNN(X_t, n_neurons, Tanh())  
rnn.forward()
```

```
Y_hat = rnn.Y_hat  
H      = rnn.H  
T      = rnn.T
```

```
dY      = Y_hat - Y_t  
L        = 0.5*np.dot(dY.T,dY)/T
```

```
plt.plot(X_t, Y_t)  
plt.plot(X_t, Y_hat)  
plt.legend(['y', '$\hat{y}$'])  
plt.show()
```

```
for h in H:  
    plt.plot(np.arange(20), h[0:20], 'k-', linewidth = 1, alpha = 0.05)
```

```
rnn.ACT[0].
```

backward
forward
inputs
output

We have T instances, each contains the $(1 - \tanh^2) * dh(t)$ part for each t already!



```
class RNN():
```

```
...
```

```
def backward(self, dvalues):
```

```
    T = self.T
```

```
    H = self.H
```

```
    X_t = self.X_t
```

```
    ACT = self.ACT
```

```
    dwx = self.dwx
```

```
    dwy = self.dwy
```

```
    dwh = self.dwh
```

```
    dbiases = self.dbiases
```

```
    wy = self.wy
```

```
    wh = self.wh
```

$$dW_x = -\epsilon * dY * W_y * (1 - \tanh^2) * x(t)$$

$$dW_y = -\epsilon * dY * h(t)$$

$$dW_h = -\epsilon * dY * W_y * (1 - \tanh^2) * h(t-1)$$

$$db = -\epsilon * dY * W_y * (1 - \tanh^2)$$

will be dY



```
def backward(self, dvalues): dy
```

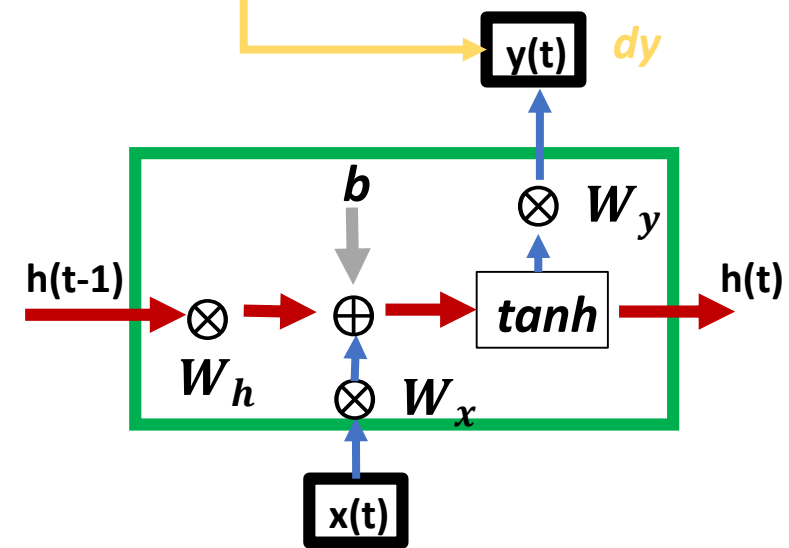
```
...
```

```
    Wh = self.Wh
```

```
    dvalues[-1].reshape(1,1)
```

$$\begin{aligned}dW_x &= -\epsilon * dY * W_y * (1 - \tanh^2) * x(t) \\dW_y &= -\epsilon * dY * h(t) \\dW_h &= -\epsilon * dY * W_y * (1 - \tanh^2) * h(t-1) \\db &= -\epsilon * dY * W_y * (1 - \tanh^2)\end{aligned}$$

$$\frac{dL}{dW_i} = -\epsilon \frac{dL}{dy} \frac{dy}{dh(t)} \frac{dh(t)}{d \tanh} \frac{d \tanh}{dW_i}$$





```
def backward(self, dvalues):
```

```
...
```

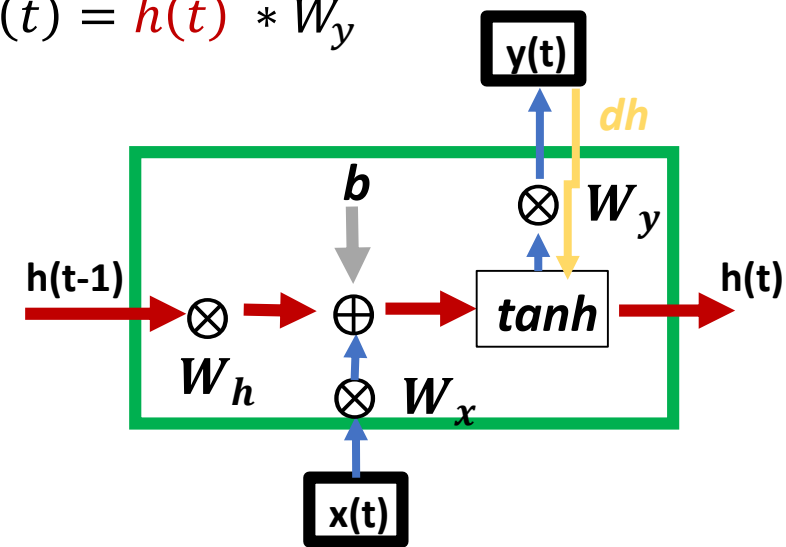
```
    Wh      = self.Wh
```

```
    dht     = np.dot(Wy.T, dvalues[-1].reshape(1,1))
```

$$\begin{aligned}dW_x &= -\epsilon * dY * W_y * (1 - \tanh^2) * x(t) \\dW_y &= -\epsilon * dY * h(t) \\dW_h &= -\epsilon * dY * W_y * (1 - \tanh^2) * h(t-1) \\db &= -\epsilon * dY * W_y * (1 - \tanh^2)\end{aligned}$$

$$\frac{dL}{dW_i} = -\epsilon \frac{dL}{dy} \boxed{\frac{dy}{dh(t)}} \frac{dh(t)}{d \tanh} \frac{d \tanh}{dW_i}$$

$$y(t) = h(t) * W_y$$





```
def backward(self, dvalues):
```

```
...
```

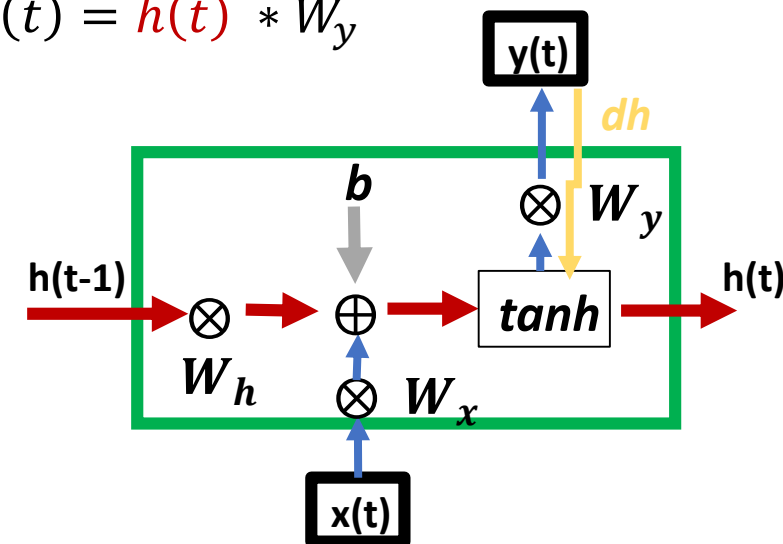
```
    Wh      = self.Wh
```

```
    dht     = np.dot(Wy.T, dvalues[-1].reshape(1,1))
```

$$\begin{aligned} dW_x &= -\epsilon * dY * W_y * (1 - \tanh^2) * x(t) \\ dW_y &= -\epsilon * dY * h(t) \\ dW_h &= -\epsilon * dY * W_y * (1 - \tanh^2) * h(t-1) \\ db &= -\epsilon * dY * W_y * (1 - \tanh^2) \end{aligned}$$

$$\frac{dL}{dW_i} = -\epsilon \frac{dL}{dy} \frac{dy}{dh(t)} \frac{dh(t)}{d \tanh} \frac{d \tanh}{dW_i}$$

$$y(t) = h(t) * W_y$$





```
def backward(self, dvalues):
```

```
...
```

```
    Wh      = self.Wh
```

```
    dht      = np.dot(Wy.T, dvalues[-1].reshape(1,1))
```

```
    for t in reversed(range(T)):
```

```
        dy = dvalues[t].reshape(1,1)
```

```
        xt = X_t[t].reshape(1,1)
```

```
        ACT[t].backward(dht)
```

```
        dtanh = ACT[t].dinputs
```

$$dW_x = -\epsilon * dY * W_y * (1 - \tanh^2) * x(t)$$

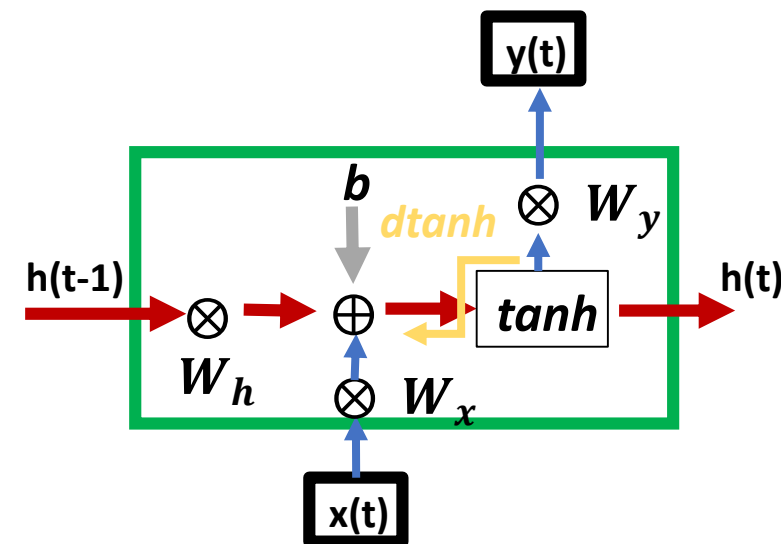
$$dW_y = -\epsilon * dY * h(t)$$

$$dW_h = -\epsilon * dY * W_y * (1 - \tanh^2) * h(t-1)$$

$$db = -\epsilon * dY * W_y * (1 - \tanh^2)$$

$$\frac{dL}{dW_i} = -\epsilon \frac{dL}{dy} \frac{dy}{dh(t)} \frac{dh(t)}{d \tanh} \frac{d \tanh}{dW_i}$$

$$h(t) = \tanh[x(t) * W_x + W_h * h(t-1) + b]$$





```
def backward(self, dvalues):
```

```
...
```

```
    Wh      = self.Wh
```

```
    dht      = np.dot(Wy.T, dvalues[-1].reshape(1,1))
```

```
    for t in reversed(range(T)):
```

```
        dy = dvalues[t].reshape(1,1)
```

```
        xt = X_t[t].reshape(1,1)
```

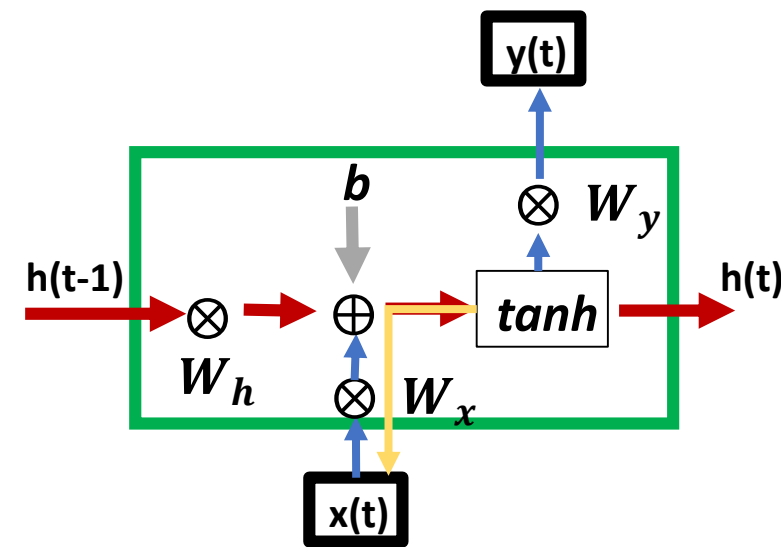
```
        ACT[t].backward(dht)
```

```
        dtanh = ACT[t].dinputs
```

```
        dwx      += np.dot(dtanh, xt)
```

$$\begin{aligned}dW_x &= -\epsilon * dY * W_y * (1 - \tanh^2) * x(t) \\dW_y &= -\epsilon * dY * h(t) \\dW_h &= -\epsilon * dY * W_y * (1 - \tanh^2) * h(t-1) \\db &= -\epsilon * dY * W_y * (1 - \tanh^2)\end{aligned}$$

$$\frac{dL}{dW_i} = -\epsilon \frac{dL}{dy} \frac{dy}{dh(t)} \frac{dh(t)}{d \tanh} \frac{d \tanh}{dW_i}$$





```
def backward(self, dvalues):
```

```
...
```

```
    Wh      = self.Wh
```

```
    dht      = np.dot(Wy.T, dvalues[-1].reshape(1,1))
```

```
    for t in reversed(range(T)):
```

```
        dy = dvalues[t].reshape(1,1)
```

```
        xt = X_t[t].reshape(1,1)
```

```
        ACT[t].backward(dht)
```

```
        dtanh = ACT[t].dinputs
```

```
        dwx   += np.dot(dtanh, xt)
```

```
        dwy   += np.dot(H[t+1], dy).T
```

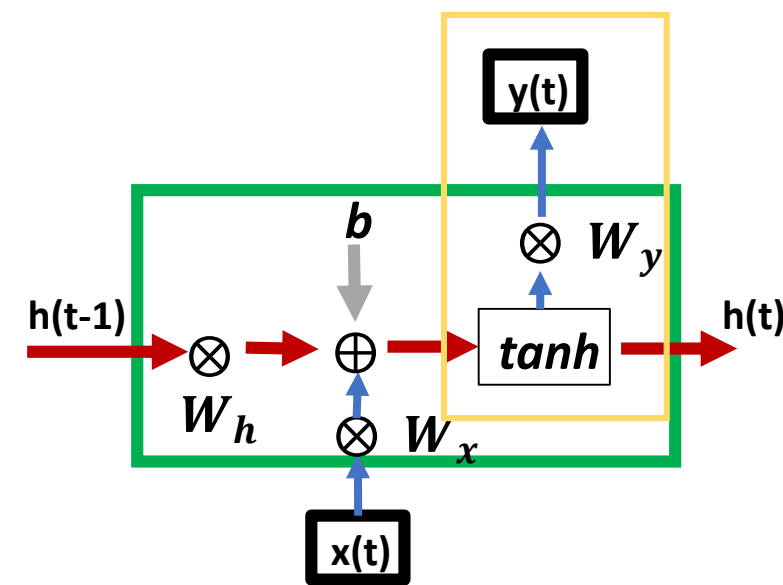
$$dW_x = -\epsilon * dY * W_y * (1 - \tanh^2) * x(t)$$

$$dW_y = -\epsilon * dY * h(t)$$

$$dW_h = -\epsilon * dY * W_y * (1 - \tanh^2) * h(t-1)$$

$$db = -\epsilon * dY * W_y * (1 - \tanh^2)$$

$$\frac{dL}{dW_i} = -\epsilon \frac{dL}{dy} \frac{dy}{dh(t)} \frac{dh(t)}{d \tanh} \frac{d \tanh}{dW_i}$$





```
def backward(self, dvalues):
```

```
...
```

```
    Wh      = self.Wh
```

```
    dht      = np.dot(Wy.T, dvalues[-1].reshape(1,1))
```

```
    for t in reversed(range(T)):
```

```
        dy = dvalues[t].reshape(1,1)
```

```
        xt = X_t[t].reshape(1,1)
```

```
        ACT[t].backward(dht)
```

```
        dtanh = ACT[t].dinputs
```

```
        dwx   += np.dot(dtanh, xt)
```

```
        dwy   += np.dot(H[t+1], dy).T
```

```
        dwh   += np.dot(H[t], dtanh.T)
```

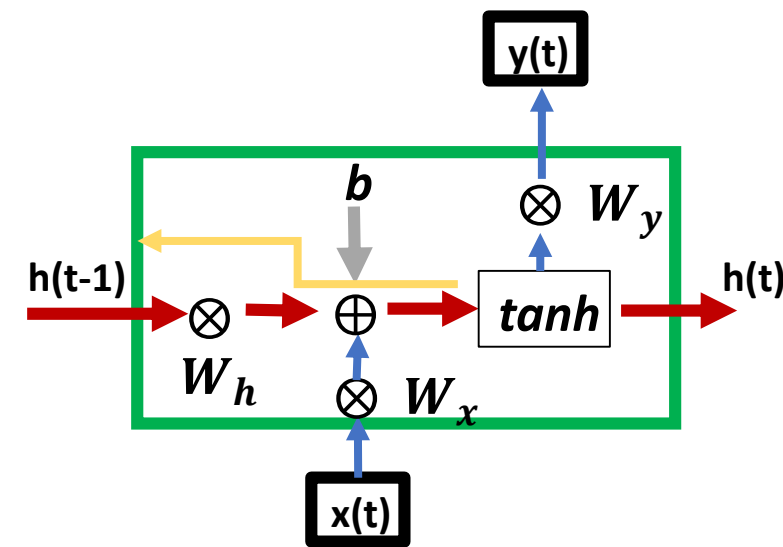
$$dW_x = -\epsilon * dY * W_y * (1 - \tanh^2) * x(t)$$

$$dW_y = -\epsilon * dY * h(t)$$

$$dW_h = -\epsilon * dY * W_y * (1 - \tanh^2) * h(t-1)$$

$$db = -\epsilon * dY * W_y * (1 - \tanh^2)$$

$$\frac{dL}{dW_i} = -\epsilon \frac{dL}{dy} \frac{dy}{dh(t)} \frac{dh(t)}{d \tanh} \frac{d \tanh}{dW_i}$$





```
def backward(self, dvalues):
```

```
...
```

```
    Wh      = self.Wh
```

```
    dht      = np.dot(Wy.T, dvalues[-1].reshape(1,1))
```

```
    for t in reversed(range(T)):
```

```
        dy = dvalues[t].reshape(1,1)
```

```
        xt = X_t[t].reshape(1,1)
```

```
        ACT[t].backward(dht)
```

```
        dtanh = ACT[t].dinputs
```

```
        dwx      += np.dot(dtanh, xt)
```

```
        dwy      += np.dot(H[t+1], dy).T
```

```
        dWh      += np.dot(H[t], dtanh.T)
```

```
        dbiases += dtanh
```

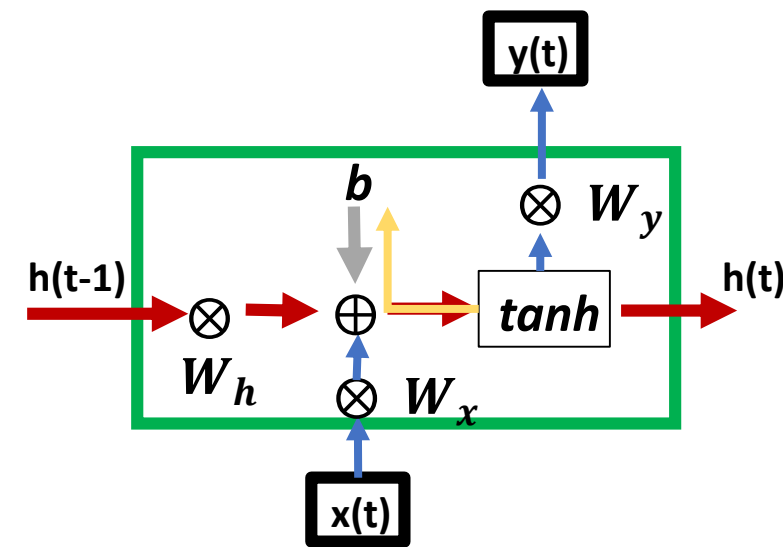
$$dW_x = -\epsilon * dY * W_y * (1 - \tanh^2) * x(t)$$

$$dW_y = -\epsilon * dY * h(t)$$

$$dW_h = -\epsilon * dY * W_y * (1 - \tanh^2) * h(t-1)$$

$$db = -\epsilon * dY * W_y * (1 - \tanh^2)$$

$$\frac{dL}{dW_i} = -\epsilon \frac{dL}{dy} \frac{dy}{dh(t)} \frac{dh(t)}{d \tanh} \frac{d \tanh}{dW_i}$$





```
def backward(self, dvalues):
```

```
...
```

```
    Wh      = self.Wh
```

```
    dht      = np.dot(Wy.T, dvalues[-1].reshape(1,1))
```

```
    for t in reversed(range(T)):
```

```
        dy = dvalues[t].reshape(1,1)
```

```
        xt = X_t[t].reshape(1,1)
```

```
        ACT[t].backward(dht)
```

```
        dtanh = ACT[t].dinputs
```

```
        dWx      += np.dot(dtanh, xt)
```

```
        dWy      += np.dot(H[t+1], dy).T
```

```
        dWh      += np.dot(H[t], dtanh.T)
```

```
        dbiases += dtanh
```

```
        dht = np.dot(Wh, dtanh) + \
              np.dot(Wy.T, dy)
```

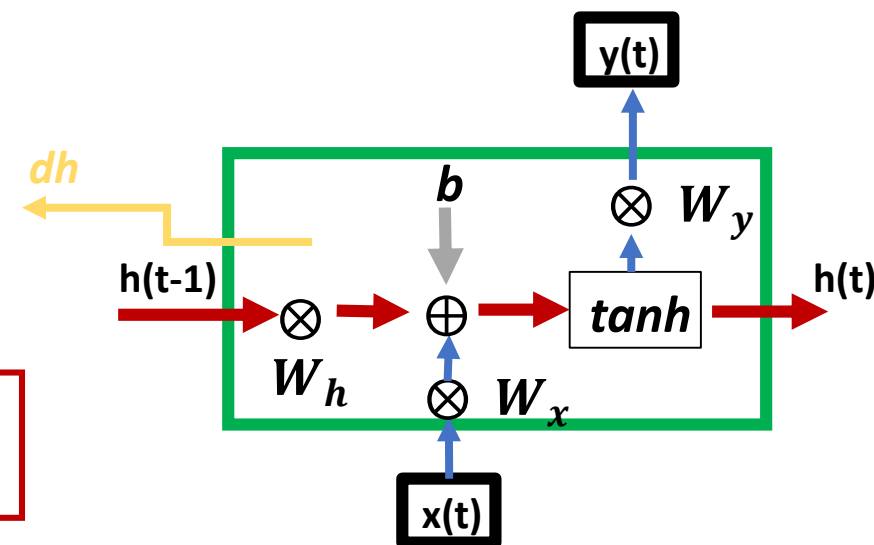
$$dW_x = -\epsilon * dY * W_y * (1 - \tanh^2) * x(t)$$

$$dW_y = -\epsilon * dY * h(t)$$

$$dW_h = -\epsilon * dY * W_y * (1 - \tanh^2) * h(t-1)$$

$$db = -\epsilon * dY * W_y * (1 - \tanh^2)$$

$$h(t) = \tanh[x(t) * W_x + W_h * h(t-1) + b]$$





```
def backward(self, dvalues):  
  
    ...  
    Wh      = self.Wh  
  
    dht      = np.dot(Wy.T, dvalues[-1].reshape(1,1))  
  
    for t in reversed(range(T)):  
  
    ...  
        dht = np.dot(Wh, dtanh) +\  
                np.dot(Wy.T, dy)  
  
        self.dWx      = dWx  
        self.dWy      = dWy  
        self.dWh      = dWh  
        self.dbiases = dbiases  
  
        self.H        = H
```

$$\begin{aligned}dW_x &= -\epsilon * dY * W_y * (1 - \tanh^2) * x(t) \\dW_y &= -\epsilon * dY * h(t) \\dW_h &= -\epsilon * dY * W_y * (1 - \tanh^2) * h(t-1) \\db &= -\epsilon * dY * W_y * (1 - \tanh^2)\end{aligned}$$



```
def backward(self, dvalues):
```

```
    T      = self.T
    H      = self.H
    X_t    = self.X_t
```

```
    ACT    = self.ACT
```

```
    dWx    = self.dWx
    dWy    = self.dWy
    dWh    = self.dWh
    Wy      = self.Wy
    Wh      = self.Wh
```

```
    dht     = np.dot(Wy.T, dvalues[-1].reshape(1,1))
```

```
    dbiases = self.dbiases
```

```
    for t in reversed(range(T)):
```

```
        dy = dvalues[t].reshape(1,1)
        xt = X_t[t].reshape(1,1)
```

```
        ACT[t].backward(dht)
        dtanh = ACT[t].dinputs
```

```
        dWx    += np.dot(dtanh, xt)
        dWy    += np.dot(H[t+1], dy).T
        dWh    += np.dot(H[t], dtanh.T)
        dbiases += dtanh
```

```
        dht = np.dot(Wh, dtanh) + np.dot(Wy.T, dy)
```

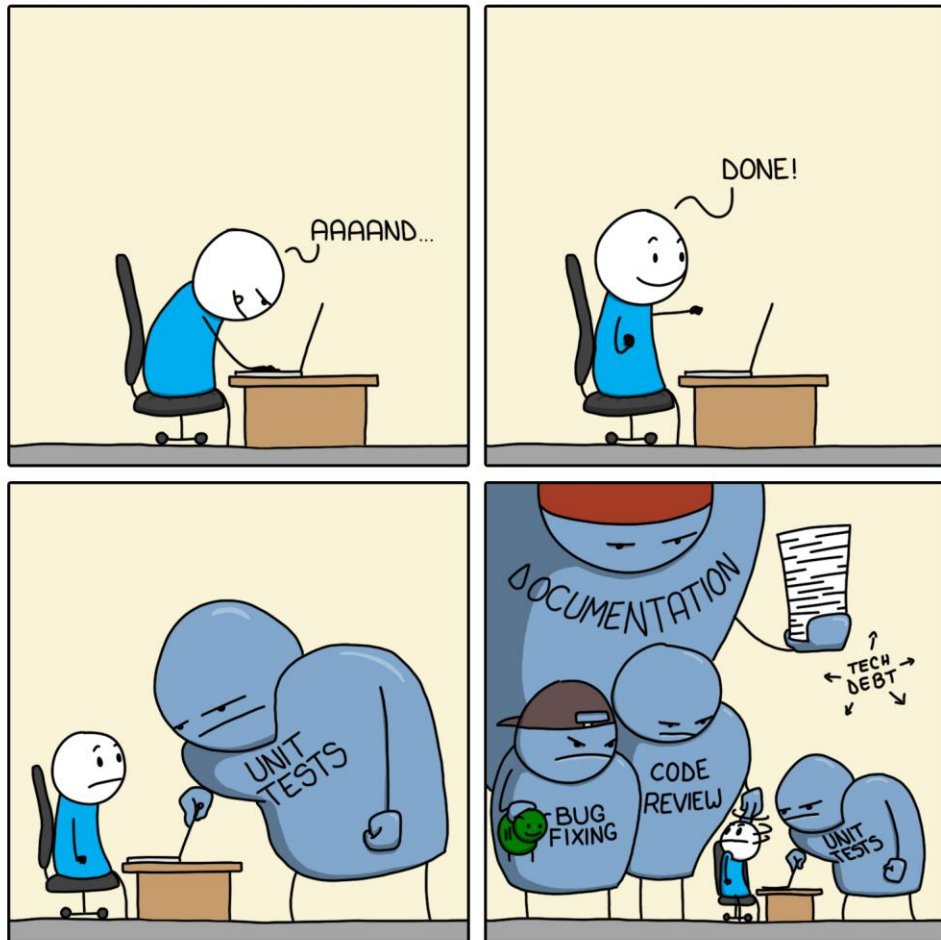
```
    self.dWx    = dWx
    self.dWy    = dWy
    self.dWh    = dWh
    self.dbiases = dbiases
```

```
    self.H      = H
```



FEATURE COMPLETE

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outline:

- *the idea*
- *the RNN cell*
- *BackPropagation Through Time*
- *full backpropagation*
- *creating an SGD optimizer*
- *creating a full package*



The RNN is now ready and it should be able to learn!

```
from RNN import *
```

```
n_neurons = 500
```

```
rnn = RNN(X_t, n_neurons, Tanh())
```

```
T = rnn.T
```

```
n_epoch = 20
```

```
e = 1e-5
```

learning rate



```
for n in range(n_epoch):
```

```
    rnn.forward()
```

```
    Y_hat = rnn.Y_hat
```

```
    dY = Y_hat - Y_t
```

```
    L = 0.5*np.dot(dY.T,dY)/T
```

```
    print(float(L))
```

```
    rnn.backward(dY)
```

```
    rnn.Wx -= e* rnn.dWx
```

```
    rnn.Wy -= e* rnn.dWy
```

```
    rnn.Wh -= e* rnn.dWh
```

```
    rnn.biases -= e* rnn.dbiases
```

```
    plt.plot(X_t, Y_t)
```

```
    plt.plot(X_t, Y_hat)
```

```
    plt.legend(['y', '$\hat{y}$'])
```

```
    plt.title('epoch ' + str(n))
```

```
    plt.show()
```

$$dW_x = -\epsilon * dY * W_y * (1 - \tanh^2) * x(t)$$

$$dW_y = -\epsilon * dY * h(t)$$

$$dW_h = -\epsilon * dY * W_y * (1 - \tanh^2) * h(t) - 1)$$

$$db = -\epsilon * dY * W_y * (1 - \tanh^2)$$



Recurrent Neural Networks - from Scratch

full backpropagation

```
from RNN import *
```

```
...
```

```
for n in range(n_epoch):
```

```
    rnn.forward()
```

```
    Y_hat= rnn.Y_hat
```

```
    dY      = Y_hat - Y_t
```

```
    L      = 0.5*np.dot(dY.T,dY)/T
```

```
    print(float(L))
```

```
    rnn.backward(dY)
```

```
    rnn.Wx      -= e* rnn.dWx
```

```
    rnn.Wy      -= e* rnn.dWy
```

```
    rnn.Wh      -= e* rnn.dWh
```

```
    rnn.biases  -= e* rnn.dbiases
```

```
    plt.plot(X_t, Y_t)
```

```
    plt.plot(X_t, Y_hat)
```

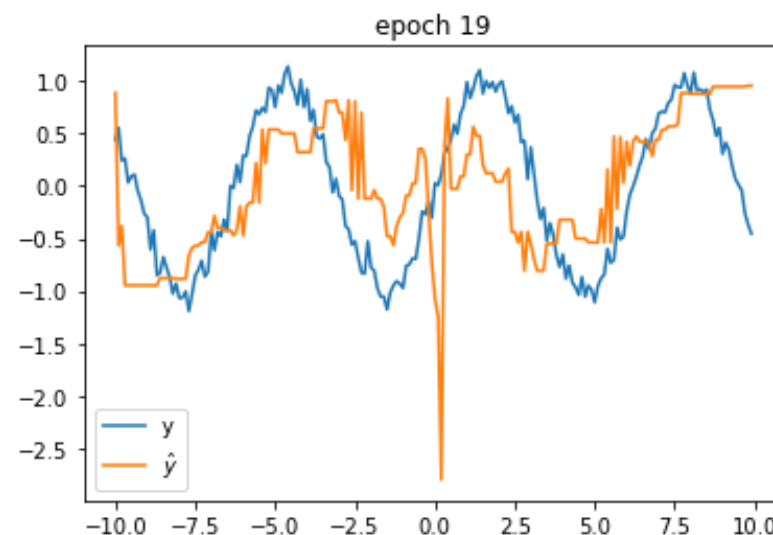
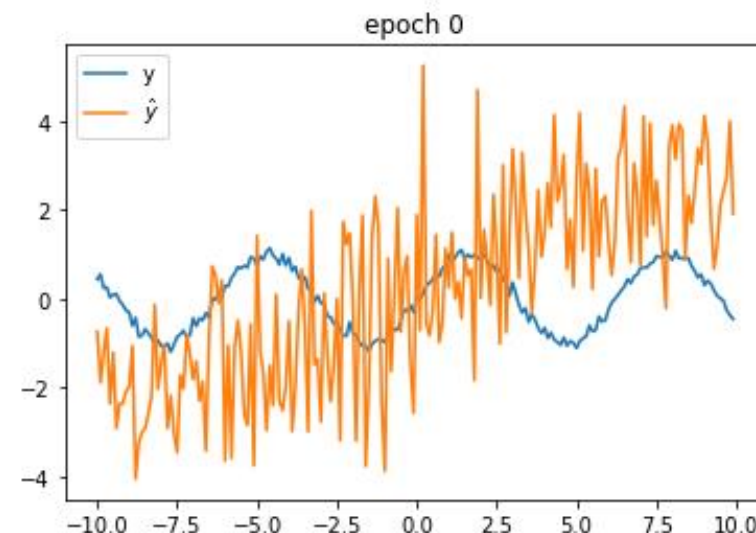
```
    plt.legend(['y', '$\hat{y}$'])
```

```
    plt.title('epoch ' + str(n))
```

```
    plt.show()
```

L

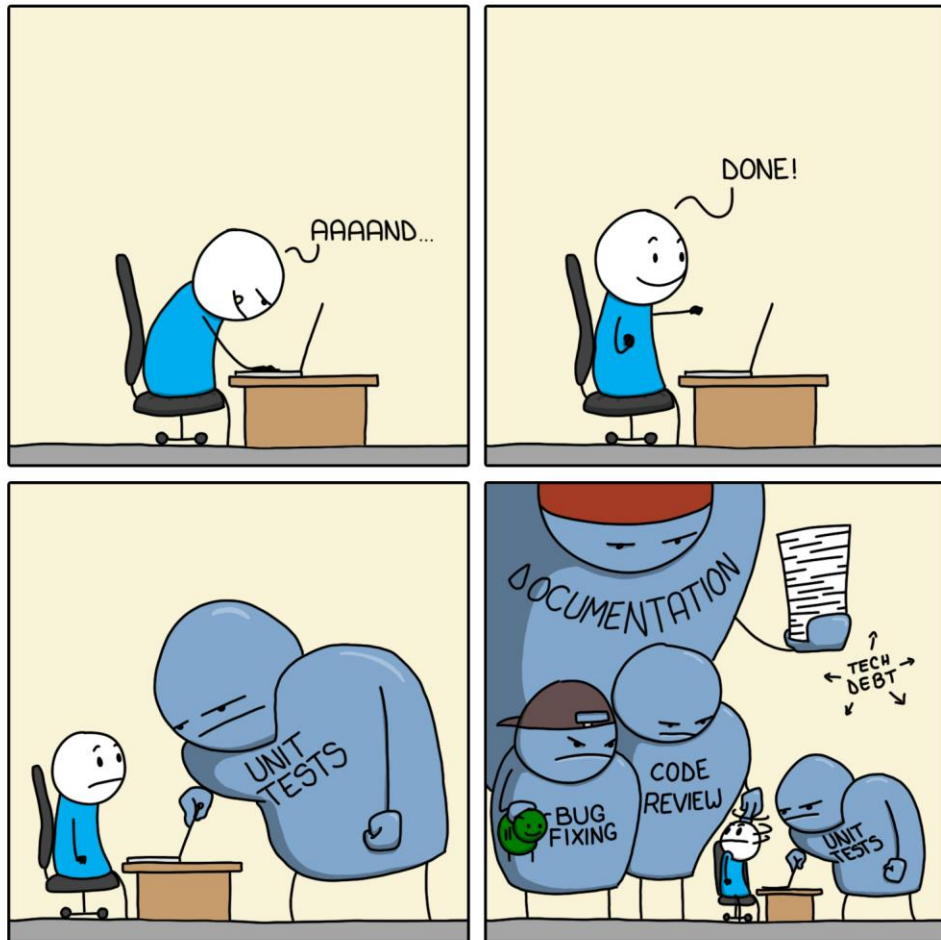
```
2.4421365086946225
3.643908836529324
0.40210259336023235
0.36488299768980115
0.3484465922481833
0.3334452208724845
0.31965178295937685
0.3069639694033091
0.29528875247232894
0.284540967482768
0.27464264441702246
0.2655223998379806
0.25711488022167345
0.2493602523394233
0.24220373671271936
0.23559518050029948
0.22948866648462166
0.2238421551065919
0.21861715675530824
0.21377843175565578
```





FEATURE COMPLETE

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outline:

- *the idea*
- *the RNN cell*
- *BackPropagation Through Time*
- *full backpropagation*
- *creating an SGD optimizer*
- *creating a full package*



- the optimizer will be pretty similar to the one from “ANN from Scratch”
- with momentum and learning rate decay

```
class Optimizer_SGD:
```

```
    def __init__(self, learning_rate = 0.001, decay = 0, momentum = 0):
```

```
        self.learning_rate      = learning_rate
        self.current_learning_rate = learning_rate
        self.decay               = decay
        self.iterations          = 0
        self.momentum            = momentum
```



```
class Optimizer_SGD:
```

```
    def __init__(self, learning_rate = 0.001, decay = 0, momentum = 0):
```

```
        ...
```

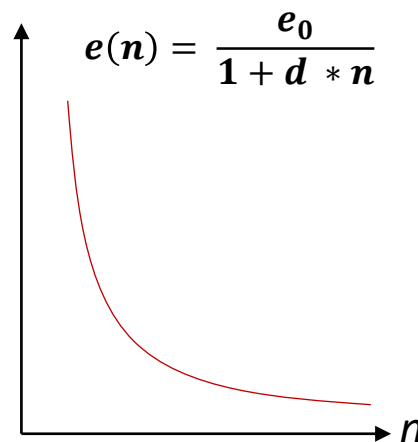
```
            self.momentum = momentum
```

```
    def pre_update_params(self):
```

```
        if self.decay:
```

```
            self.current_learning_rate = self.learning_rate * \
                (1 / (1 + self.decay * self.iterations))
```

for more details see
my “ANN from Scratch”
lecture 😊



e: learning rate
d: decay
n: epochs/iterations



for more details see
my “ANN from Scratch”
lecture

```
class Optimizer_SGD:
```

```
    def __init__(self, learning_rate = 0.001, decay = 0, momentum = 0):
```

```
        ...
```

```
            self.momentum = momentum
```

```
    def pre_update_params(self):
```

```
        if self.decay:
```

```
            self.current_learning_rate = self.learning_rate * \
                (1 / (1 + self.decay * self.iterations))
```

```
    def post_update_params(self):
```

```
        self.iterations += 1
```

Just counting the iterations/epochs
for current learning rate



```
class Optimizer_SGD:
```

```
    ...
```

```
    def update_params(self, layer):
```

```
        if self.momentum:
```

```
            if not hasattr(layer, 'Wx_momentums'):
```

```
                layer.Wx_momentums = np.zeros_like(layer.Wx)
```

```
                layer.Wy_momentums = np.zeros_like(layer.Wy)
```

```
                layer.Wh_momentums = np.zeros_like(layer.Wh)
```

```
                layer.bias_momentums = np.zeros_like(layer.biases)
```

for more details see
my “ANN from Scratch”
lecture



```
class Optimizer_SGD:
```

```
    ...
```

```
    def update_params(self, layer):
```

```
        if self.momentum:
```

```
            if not hasattr(layer, 'Wx_momentums'):
```

```
                layer.Wx_momentums = np.zeros_like(layer.Wx)
```

```
                layer.Wy_momentums = np.zeros_like(layer.Wy)
```

```
                layer.Wh_momentums = np.zeros_like(layer.Wh)
```

```
                layer.bias_momentums = np.zeros_like(layer.biases)
```

```
Wx_updates = self.momentum * layer.Wx_momentums - \
              self.current_learning_rate * layer.dWx
layer.Wx_momentums = Wx_updates
```

```
Wy_updates = self.momentum * layer.Wy_momentums - \
              self.current_learning_rate * layer.dWy
layer.Wy_momentums = Wy_updates
```

```
Wh_updates = self.momentum * layer.Wh_momentums - \
              self.current_learning_rate * layer.dWh
layer.Wh_momentums = Wh_updates
```

```
bias_updates = self.momentum * layer.bias_momentums - \
                self.current_learning_rate * layer.dbiases
layer.bias_momentums = bias_updates
```

for more details see
my *“ANN from Scratch”*
lecture



```
class Optimizer_SGD:
```

```
    ...
```

```
    def update_params(self, layer):
```

```
        if self.momentum:
```

```
            if not hasattr(layer, 'Wx_momentums'):
```

```
                layer.Wx_momentums = np.zeros_like(layer.Wx)
```

```
            ...
```

```
            bias_updates = self.momentum * layer.bias_momentums - \
                self.current_learning_rate * layer.dbiases
            layer.bias_momentums = bias_updates
```

```
        else:
```

```
            Wx_updates = -self.current_learning_rate * layer.dWx
            Wy_updates = -self.current_learning_rate * layer.dWy
            Wh_updates = -self.current_learning_rate * layer.dWh
            bias_updates = -self.current_learning_rate * layer.dbiases
```

```
            layer.Wx += Wx_updates
            layer.Wy += Wy_updates
            layer.Wh += Wh_updates
            layer.biases += bias_updates
```

for more details see
my *“ANN from Scratch”*
lecture

```
rnn.Wx -= e* rnn.dWx
rnn.Wy -= e* rnn.dWy
rnn.Wh -= e* rnn.dWh
```



```
from RNN import *
```

```
n_neurons = 500
```

```
rnn = RNN(X_t, n_neurons, Tanh())
```

```
optimizer = Optimizer_SGD(learning_rate = 1e-5, momentum = 0.95)
```

```
T = rnn.T
```

```
n_epoch = 200
```

```
Monitor = np.zeros((n_epoch, 1))
```

```
for n in range(n_epoch):
```

```
    rnn.forward()
```

```
    Y_hat = rnn.Y_hat
```

```
    dY = Y_hat - Y_t
```

```
    L = 0.5*np.dot(dY.T, dY)/T
```

we want to keep track of
the loss function



```
from RNN import *
```

```
n_neurons = 500
rnn        = RNN(X_t, n_neurons, Tanh())
optimizer  = Optimizer_SGD(learning_rate = 1e-5, momentum = 0.95)
T          = rnn.T
n_epoch    = 200
Monitor    = np.zeros((n_epoch, 1))
```

```
for n in range(n_epoch):
```

```
    rnn.forward()
```

```
    Y_hat      = rnn.Y_hat
```

```
    dY         = Y_hat - Y_t
```

```
    L          = 0.5*np.dot(dY.T, dY)/T
```

```
    Monitor[n] = L
```

```
    rnn.backward(dY)
```

```
    optimizer.pre_update_params()
    optimizer.update_params(rnn)
    optimizer.post_update_params()
```

we want to keep track of
the loss function

updating W_x , W_y , W_h ,
biases and learning rate



```
from RNN import *

n_neurons = 500
rnn = RNN(X_t, n_neurons, Tanh())
optimizer = Optimizer_SGD(learning_rate = 1e-5, momentum = 0.95)
T = rnn.T
n_epoch = 200
Monitor = np.zeros((n_epoch, 1))

for n in range(n_epoch):

    ...
    optimizer.post_update_params()

    r = n/50
    if r - np.ceil(r) == 0:
        plt.plot(X_t, Y_t)
        plt.plot(X_t, Y_hat)
        plt.legend(['y', '$\hat{y}$'])
        plt.title('epoch ' + str(n))
        plt.show()
```



```
for n in range(n_epoch):
```

```
...
```

```
    optimizer.post_update_params()
```

```
    r = n/50
```

```
    if r - np.ceil(r) == 0:
```

```
        plt.plot(X_t, Y_t)
```

```
        plt.plot(X_t, Y_hat)
```

```
        plt.legend(['y', '$\hat{y}$'])
```

```
        plt.title('epoch ' + str(n))
```

```
        plt.show()
```

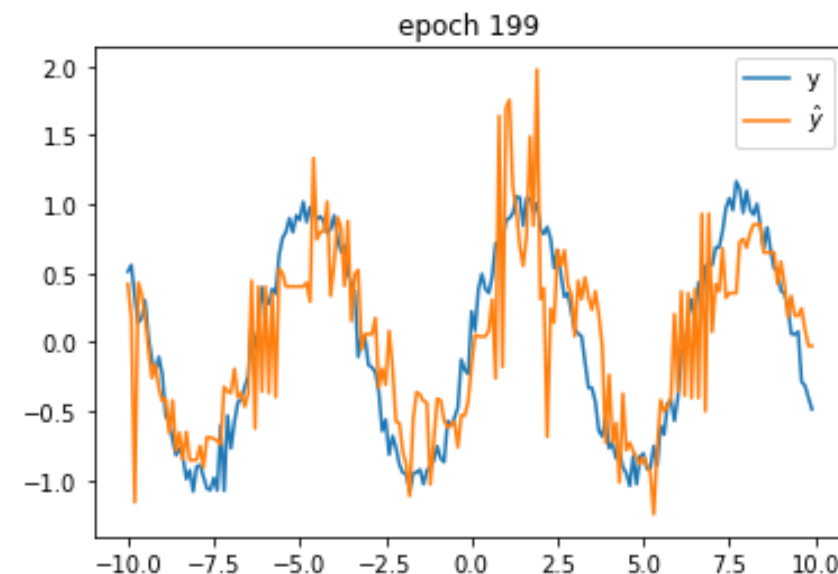
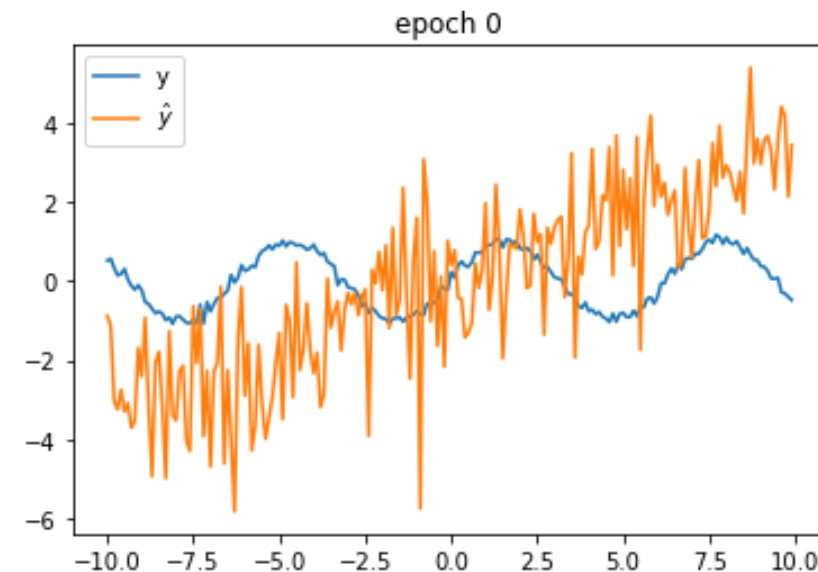
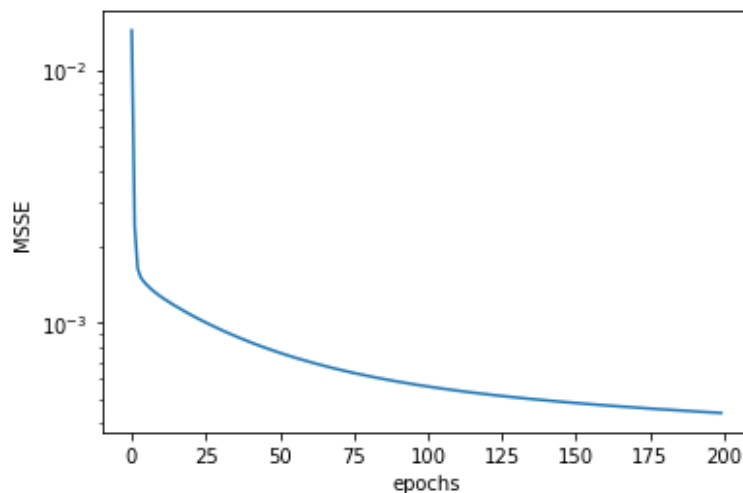
```
plt.plot(range(n_epoch), Monitor)
```

```
plt.xlabel('epochs')
```

```
plt.ylabel('MSSE')
```

```
plt.yscale('Log')
```

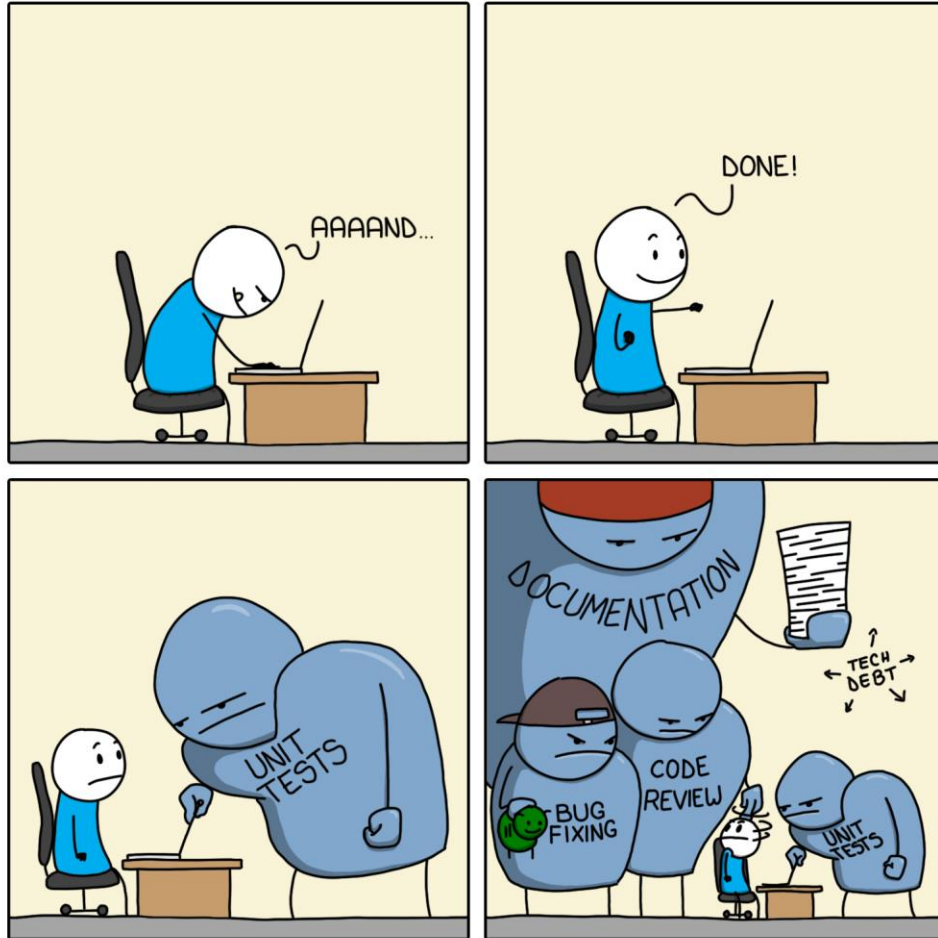
```
plt.show()
```





FEATURE COMPLETE

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outline:

- *the idea*
- *the RNN cell*
- *BackPropagation Through Time*
- *full backpropagation*
- *creating an SGD optimizer*
- *creating a full package*



The RNN works now: → creating a function for training and applying the RNN

```
import matplotlib.pyplot as plt
```

```
def RunMyRNN(X_t, Y_t, Activation, n_epoch = 1000, n_neurons = 800,  
             learning_rate = 1e-5, decay = 0, momentum = 0.95):
```

```
    rnn      = RNN(X_t, n_neurons, Activation)  
    optimizer = Optimizer_SGD(learning_rate, decay, momentum)  
    T        = rnn.T  
    Monitor  = np.zeros((n_epoch, 1))
```

```
    print("RNN is running...")
```

it is nice for the user to see
that the code is running



The RNN works now: → creating a function for **training** and applying the RNN

```
def RunMyRNN(X_t, Y_t, Activation, n_epoch = 1000, n_neurons = 800,  
             learning_rate = 1e-5, decay = 0, momentum = 0.95):
```

```
...
```

```
    print("RNN is running...")
```

```
    for n in range(n_epoch):  
  
        rnn.forward()  
  
        dY = rnn.Y_hat - Y_t  
        L = 0.5*np.dot(dY.T,dY)/T  
  
        rnn.backward(dY)  
  
        optimizer.pre_update_params()  
        optimizer.update_params(rnn)  
        optimizer.post_update_params()  
  
        Monitor[n] = L
```

we just copy/paste
the lines from the
test runs



The RNN works now: → creating a function for **training** and applying the RNN

...

```
Monitor[n] = L
```

```
r = n/100
```

```
if r - np.ceil(r) == 0:  
    plt.plot(X_t, Y_t)  
    plt.plot(X_t, Y_hat)  
    plt.legend(['y', '$\hat{y}$'])  
    plt.title('epoch ' + str(n))  
    plt.show()
```

```
plt.plot(range(n_epoch), Monitor/T)  
plt.xlabel('epochs')  
plt.ylabel('MSSE')  
plt.yscale('log')  
plt.show()
```



The RNN works now: → creating a function for **training** and applying the RNN

...

```
plt.show()
```

```
L = float(L)
```

```
print(f'Done! MSSE = {L:.3f}')
```

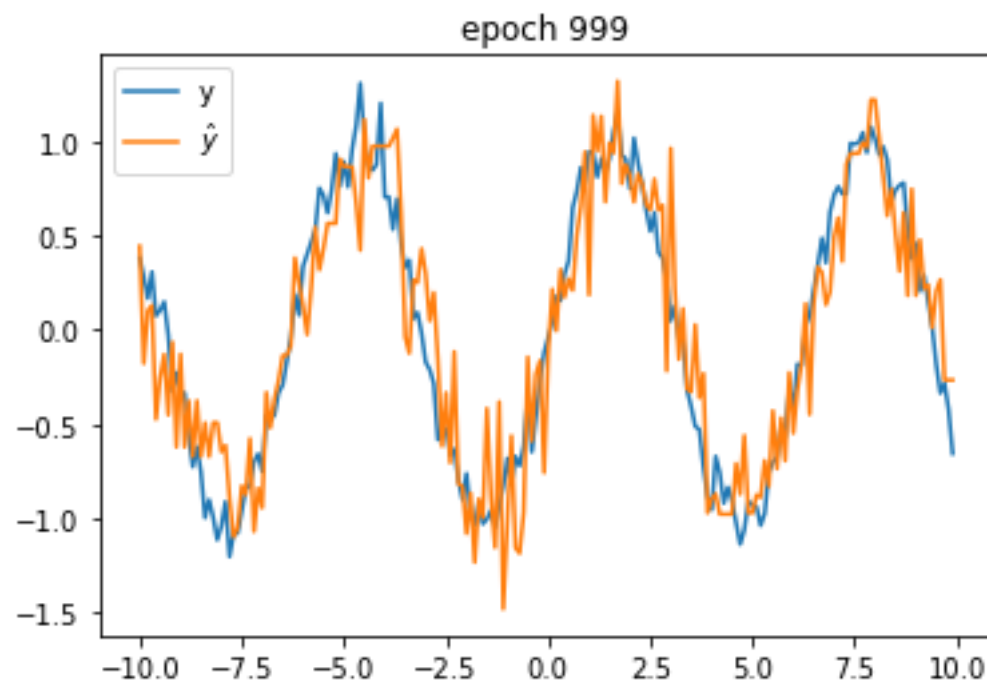
```
return(rnn)
```

we will need the weights for the application of the trained RNN to new data

```
In [57]: from RNN import *
```

```
In [58]: RunMyRNN(X_t, Y_t, Tanh())  
RNN is running...
```

```
Done! MSSE = 0.040
```





The RNN works now: → creating a function for training and **applying** the RNN

```
def ApplyMyRNN(X_t, rnn):  
    T = max(X_t.shape)  
    Y_hat = np.zeros((T, 1))  
  
    H = rnn.H  
    ht = H[0]  
    H = [np.zeros((rnn.n_neurons, 1)) for t in range(T+1)]  
  
    [_,_,Y_hat] = rnn.RNNCell(X_t, ht, rnn.ACT, H, Y_hat)  
  
    plt.plot(X_t, Y_hat)  
    plt.legend('$\hat{y}$')  
    plt.show()  
  
    return(Y_hat)
```

X_t is now the **new** data set and rnn the trained network

We only need the forward part



The RNN works now: → creating a function for training and **applying** the RNN

```
from RNN import *
```

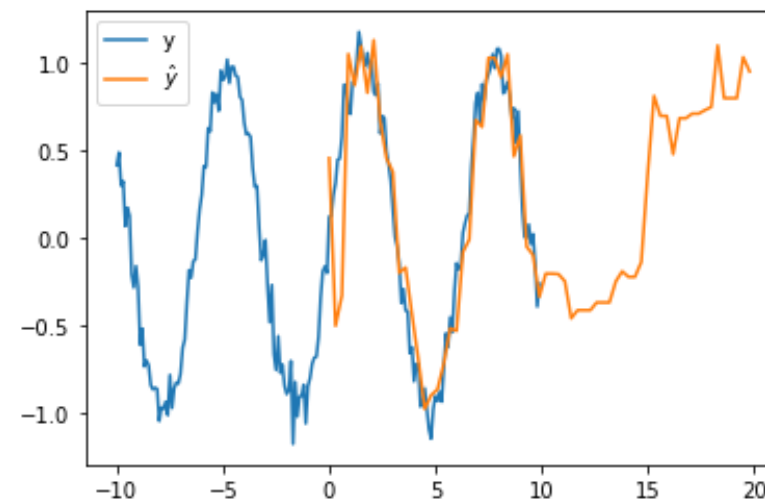
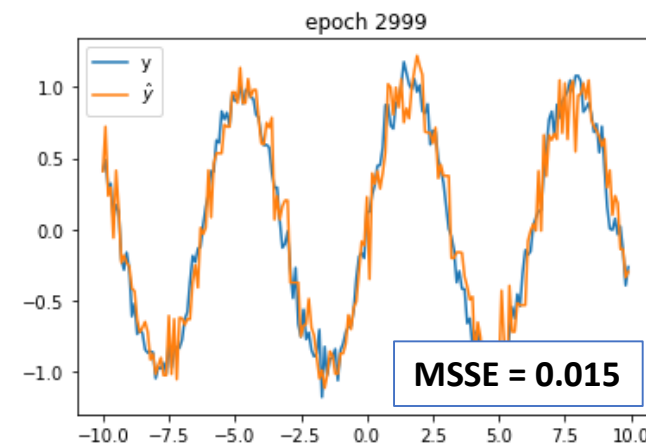
```
rnn = RunMyRNN(X_t, Y_t, Tanh(), n_epoch = 3000)
```

```
X_new = np.arange(0, 20, 0.3)  
X_new = X_new.reshape(len(X_new), 1)
```

```
Y_hat = ApplyMyRNN(X_new, rnn)
```

```
plt.plot(X_t, Y_t)  
plt.plot(X_new, Y_hat)  
plt.legend(['y', '$\hat{y}$'])  
plt.title('epoch ' + str(n))  
plt.show()
```

let us try a X_{new} with different spacing and different length than X_t

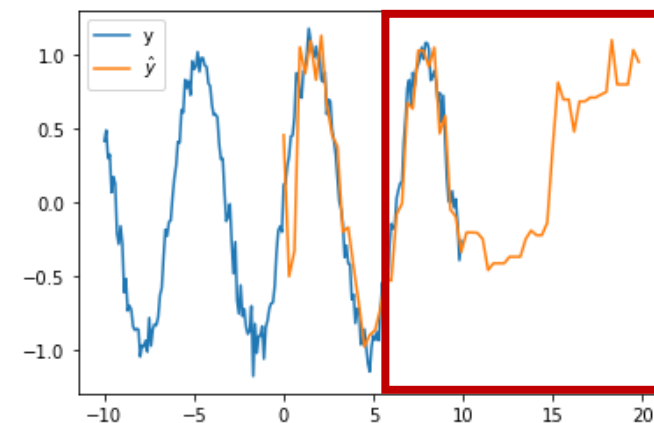


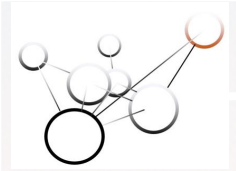


summary and final words:

- + simple, can be implemented easily
- + help to understand more complex architectures

- due to BPTT: RNNs suffer from exploding/vanishing gradient
→ `np.clip`
- training often fails in particular for long sequences
- slow, can't be parallelized
- other prediction methods outperformed RNNs at the time
- short memory (need “context”)
→ solved by LSTMs, self – attention





Thank you very much for your attention!

