

Lecture 9:

Machine Learning Overview



Markus Hohle

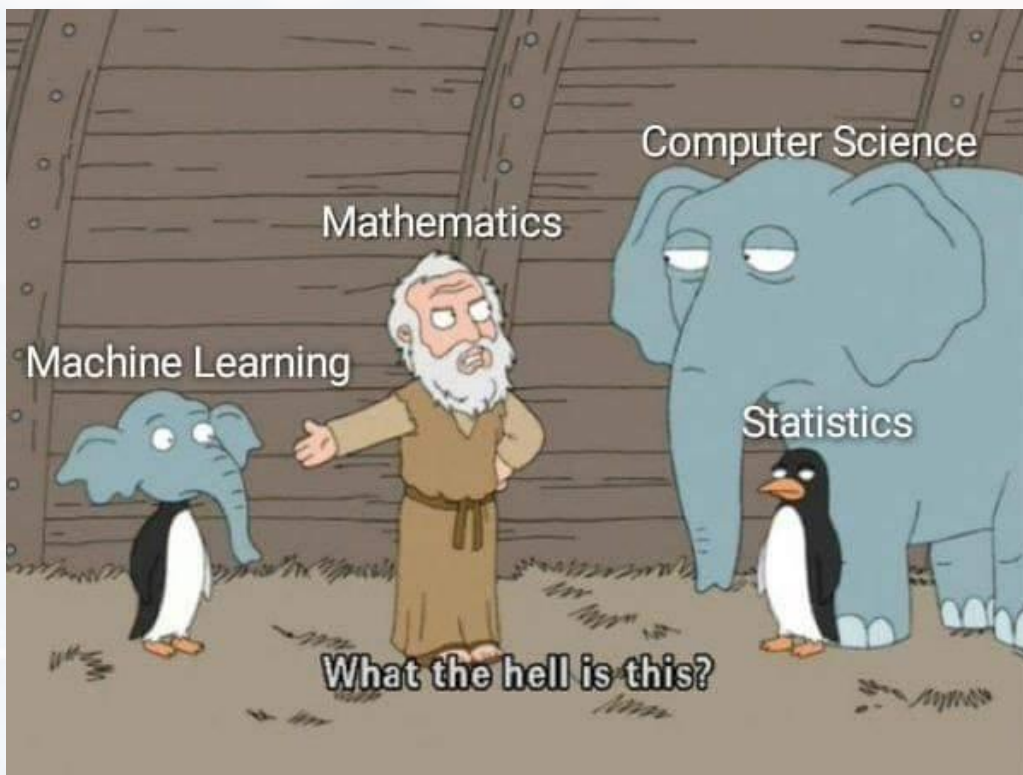
University California, Berkeley

**Bayesian Data Analysis and
Machine Learning for Physical
Sciences**



Course Map

Module 1	Maximum Entropy and Information, Bayes Theorem
Module 2	Naive Bayes, Bayesian Parameter Estimation, MAP
Module 3	MLE, Lin Regression
Module 4	Model selection I: Comparing Distributions
Module 5	Model Selection II: Bayesian Signal Detection
Module 6	Variational Bayes, Expectation Maximization
Module 7	Hidden Markov Models, Stochastic Processes
Module 8	Monte Carlo Methods
Module 9	Machine Learning Overview, Supervised Methods & Unsupervised Methods
Module 10	ANN: Perceptron, Backpropagation, SGD
Module 11	Convolution and Image Classification and Segmentation
Module 12	RNNs and LSTMs
Module 13	RNNs and LSTMs + CNNs
Module 14	Transformer and LLMs
Module 15	Graphs & GNNs

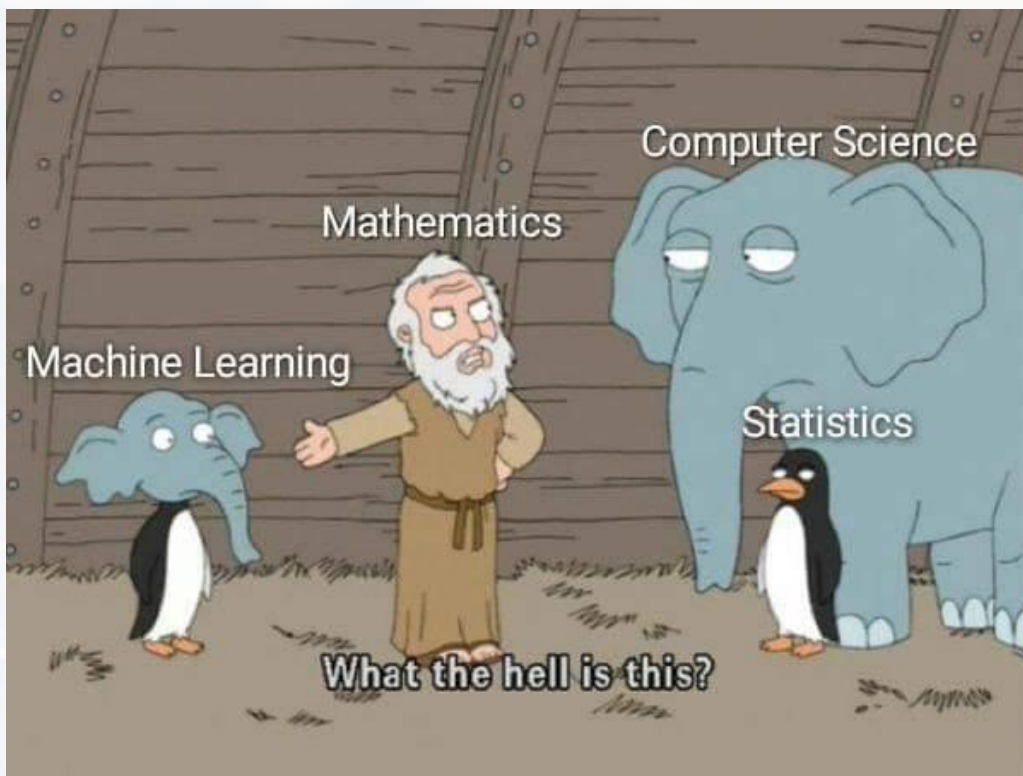


Outline

General Overview

Methods we haven't discussed yet

- Support Vector Machine
- Trees



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General Overview

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	supervised	unsupervised
regression	linear regression ✓ ANNs (soon)	
classification	logistic regression ✓ K-nearest (homework) ✓ SVM (today) ANNs (soon)	GMM ✓ K-means ✓ HMM ✓ Trees (today)



supervised

Workflow

1) creating the model:

```
my_model = library.method(argument1 = 'arg1', ... )
```

2) training the model

```
out = my_model.fit(xtrain, ytrain)
```

3) evaluation

```
ypred = out.predict(xeval)  
accur = (ypred == yeval).sum()/len(yeval)
```

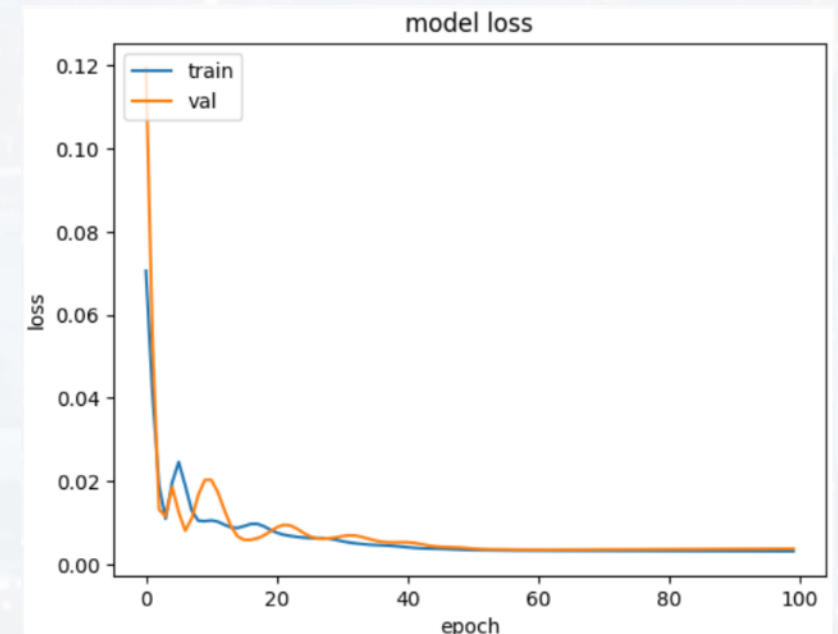
4) prediction (actual application)

```
ypred = out.predict(xnew)
```

How to split the data?

- 80% training (60% actual training 20% evaluation)
- 20% test

evaluation while training!





supervised

Workflow

1) creating the model:

```
my_model = library.method(argument1 = 'arg1', ... )
```

2) training the model

```
out = my_model.fit(xtrain, ytrain)
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3) evaluation

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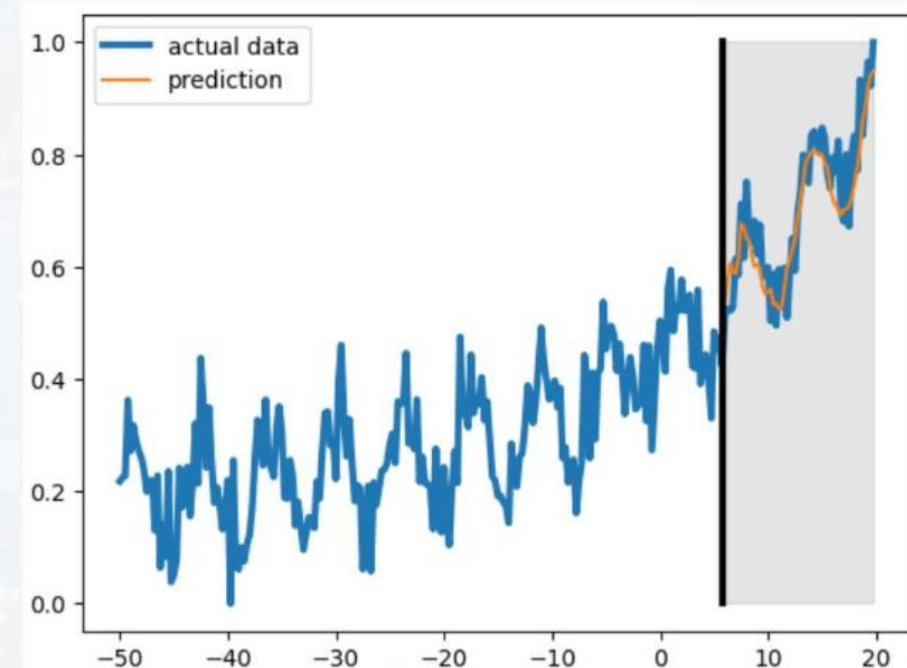
4) prediction (actual application)

```
ypred = out.predict(xnew)
```

How to split the data?

- 80% training (60% actual training 20% evaluation)
- 20% test

prediction after training/evaluation completed





Workflow

- 1) setting up the model
- ~~2) fitting the model: X are the **features** (sepal lengths/widths and petal lengths/widths),
 Y are the **classes** (setosa, versicolor, virginica)~~
- 3) evaluating the model
- 4) applying the model to a new data set

unsupervised learning:

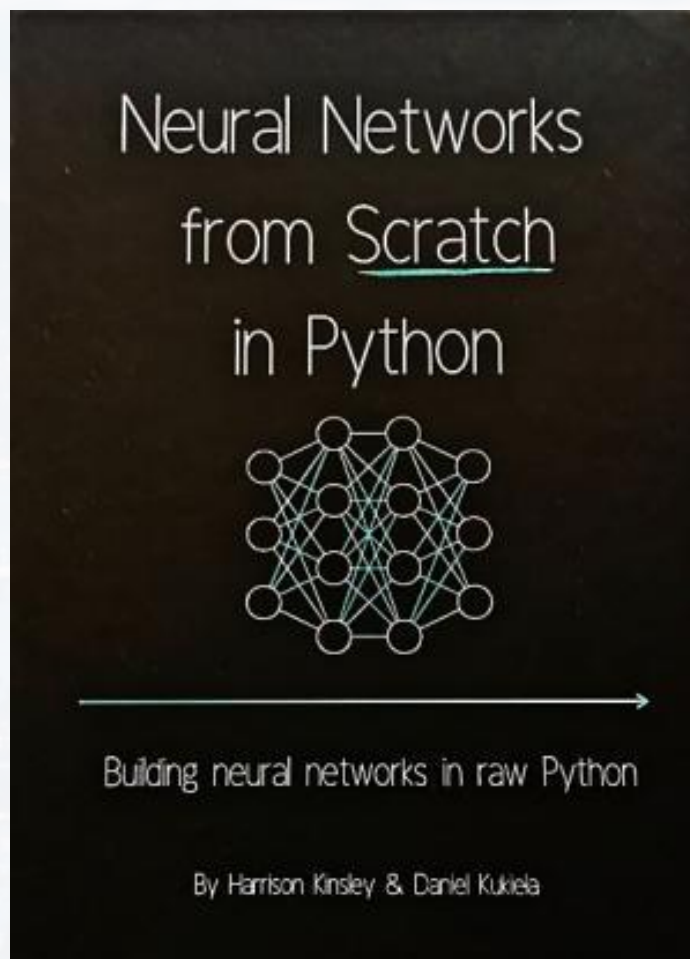
- we don't know the classes
- sometimes we even don't know the **number k of classes**

unsupervised



resources for the next lectures to come:

Tutorials and Books



Dr Fridolin
@DrFridolin · 227 subscribers · 37 videos
Dr Fridolin shows you how to program AI step by step, line by line without using external li...more
github.com/DrBigMau
Customize channel Manage videos

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For You

Recurrent Neural Networks - from scratch
$$h(t) = \tanh[x(t) \cdot W_x + [W_h] \cdot h(t-1) + b]$$

$$y(t) = h(t) \cdot W_y$$

43:37
725 views · 11 months ago

Recurrent Neural Networks - from Scratch
10:48
615 views · 11 months ago

ANN 1 Single Neuron
33:05
272 views · 11 months ago

building ANNs, RNNs, LSTMs, CNNs **from scratch**
(only numpy and matplotlib)



Tutorials and Books

examples and **application** (CNN/RNN/LSTM and more):



Jason Brownlee
Machine Learning Mastery

all about **transformers, LLM/NLP** and way more



Andrej Karpathy

@AndrejKarpathy · 451K subscribers · 14 videos

FAQ ...more

karpathy.ai and 2 more links

Subscribe



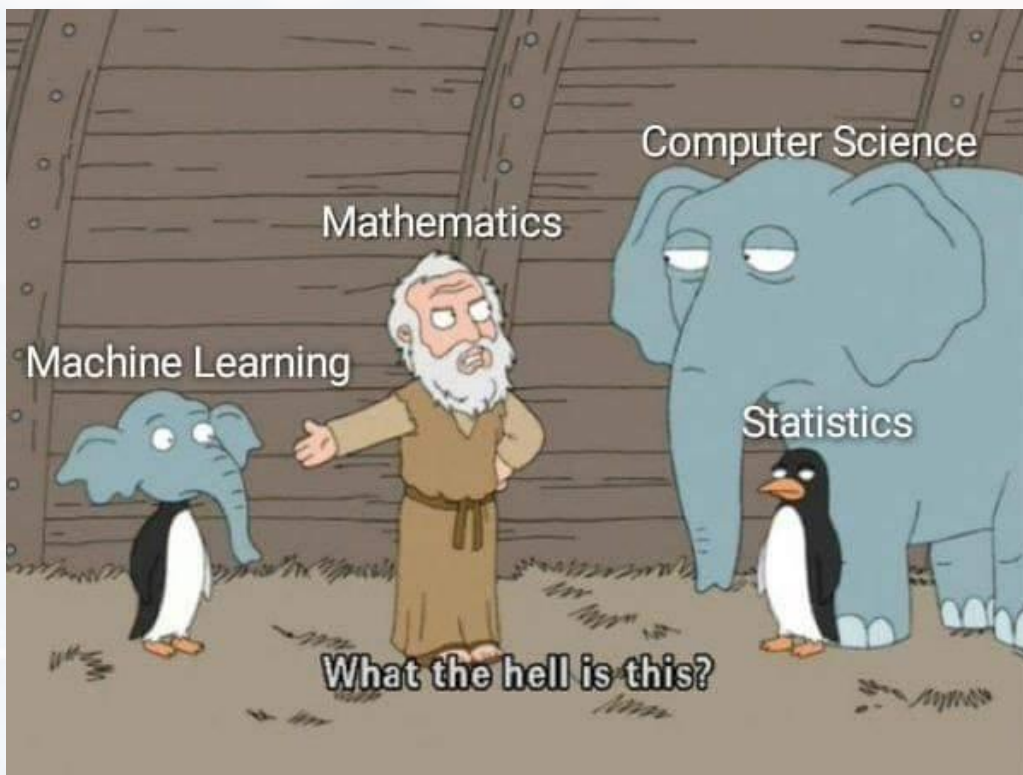
Misra Turp

@misraturp · 38.2K subscribers · 163 videos

Here is where we learn! This is a space to take it slow

misraturp.com/roadmap and 3 more links

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Outline

General Overview

Methods we haven't discussed yet

- Support Vector Machine
- Trees

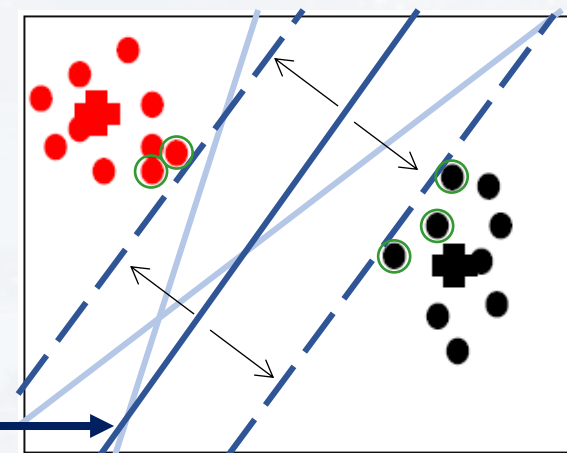


SVM = **S**upport **V**ector **M**achine

- idea:
- 1) finds best **linear** classifier for separating **two** classes by **maximizing margin** using **support vectors**
 - 2) assign new data points to these categories
 - 3) **supervised** learning
 - 4) uses the “kernel trick”

○ support vectors (data points at the edge)

best separator



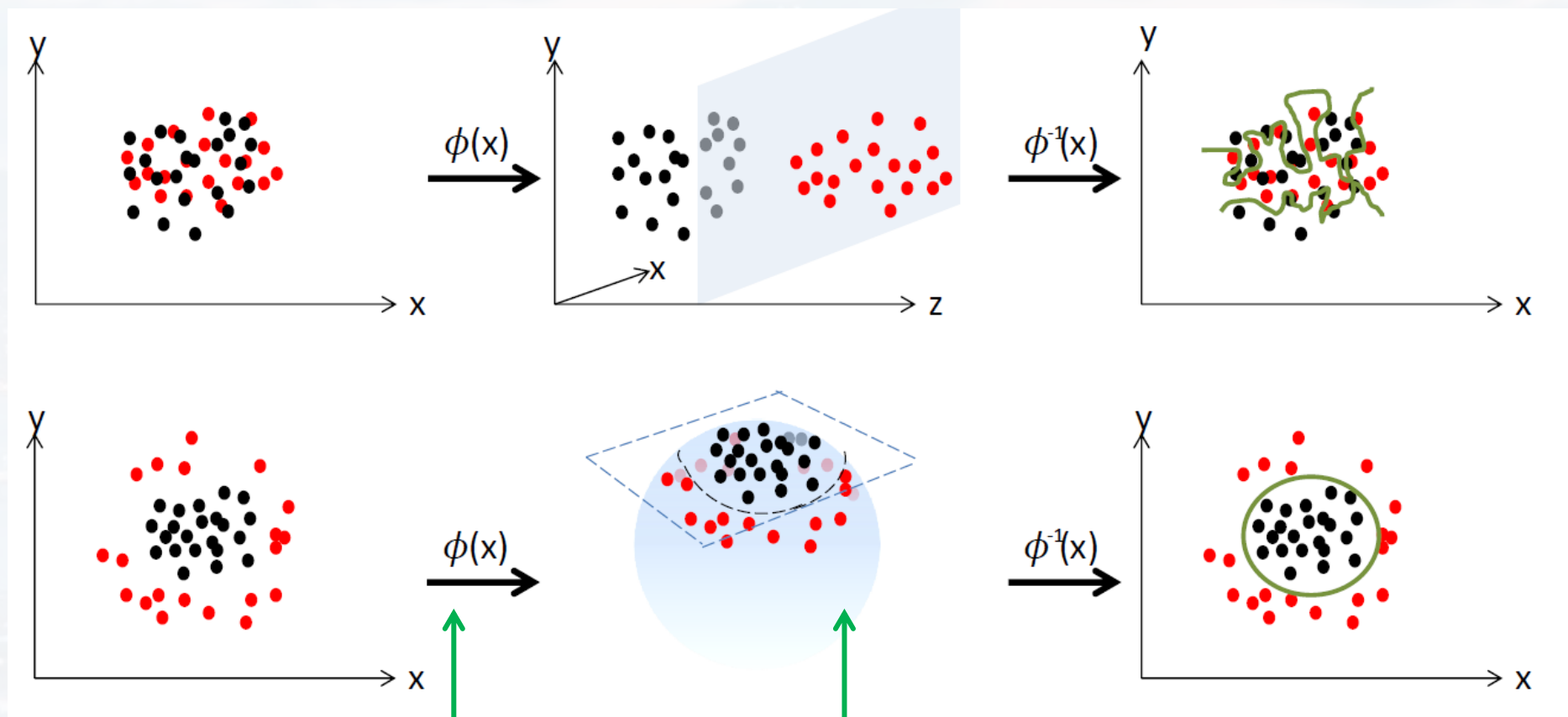
- 1) What if linear separation is not possible?
- 2) Is there a multiclass SVM?



1) What if linear separation is not possible?

2) Is there a multiclass SVM?

idea: mapping data to higher dimensional feature space



a) data space in N-D

b) a function ϕ maps the data into a M-D ($M > N$) feature space

c) find hyperplane separator in feature space

d) map back into data space (separator not linear)



1) What if linear separation is not possible?

2) Is there a multiclass SVM?

problems:

- computationally intensive
- ϕ usually unknown

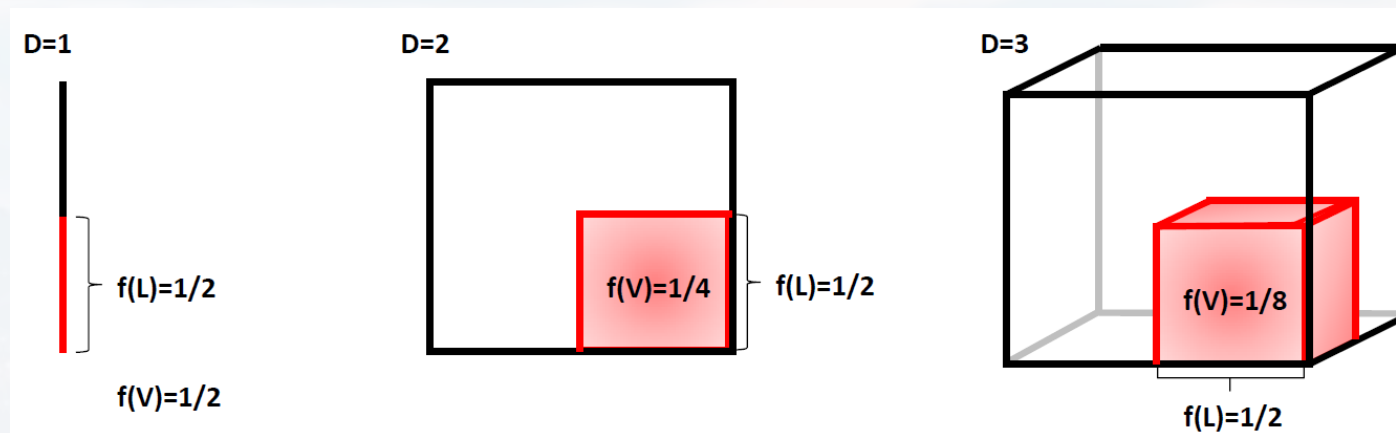
...and dimensionality!!



1) What if linear separation is not possible?

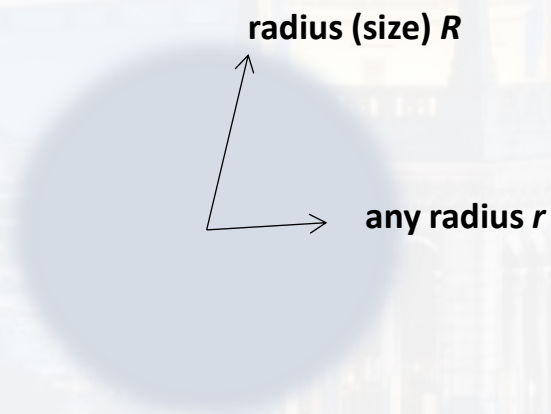
2) Is there a multiclass SVM?

What is the fraction of volume $f(V)$ covered by a certain fraction of length $f(L)$ for different dimensions D ?



answer: $f(V) = f(L)^D$

N - D space



hypersphere:

$$V_D(r) = C(D) r^D$$

$C(D)$: constant that only depends on D

fraction of volume between r and $r - dr$

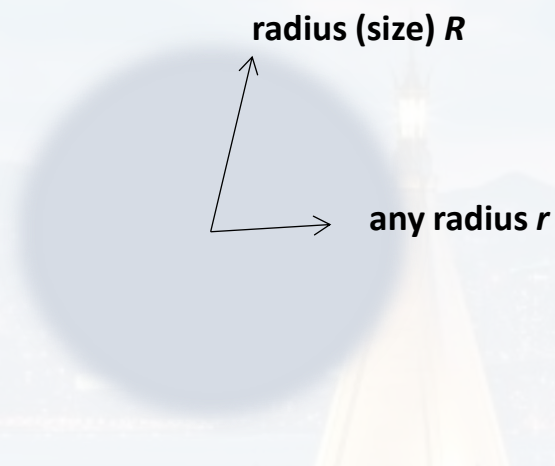
$$\frac{V_D(r) - V_D(r - dr)}{V_D(r)} = 1 - \frac{(r - dr)^D}{r^D}$$



1) What if linear separation is not possible?

2) Is there a multiclass SVM?

N - D space



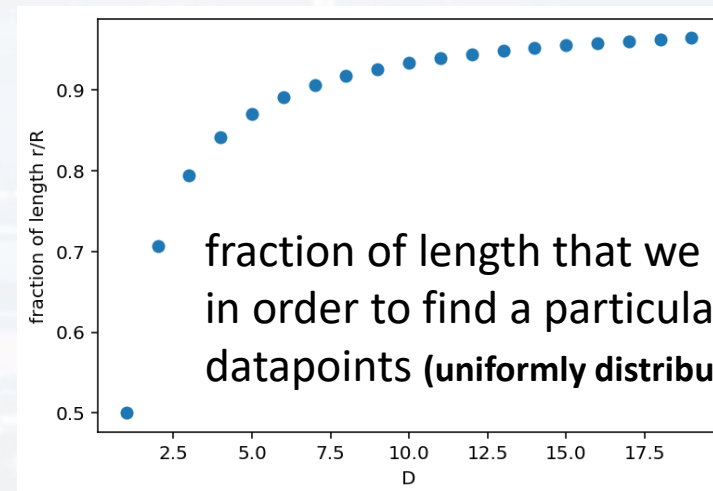
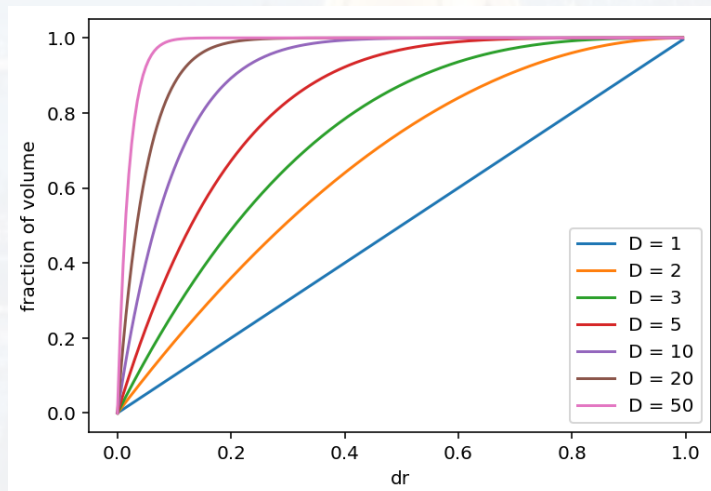
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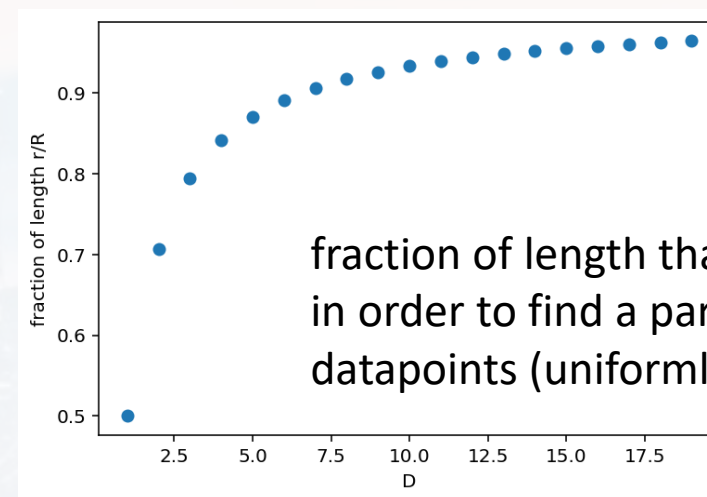
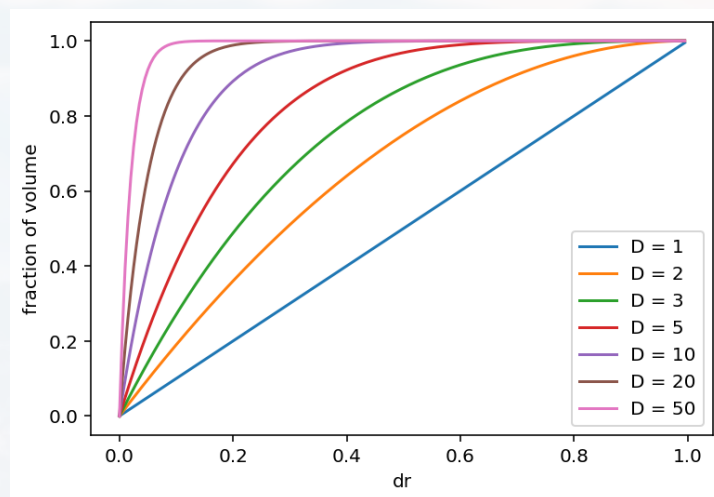


• fraction of length that we need to explore in order to find a particular fraction of datapoints (uniformly distributed in V)



1) What if linear separation is not possible?

2) Is there a multiclass SVM?



fraction of length that we need to explore in order to find a particular fraction of datapoints (uniformly distributed in R)

- for **large D**, one has to explore a **larger fraction $\frac{\rho}{R}$ of the data space** in order to get the **same fraction of data points**
- many algorithms get **less efficient** for large D
- for $D \rightarrow \infty$, the entire volume is located on the surface of the hyperspace



1) What if linear separation is not possible?

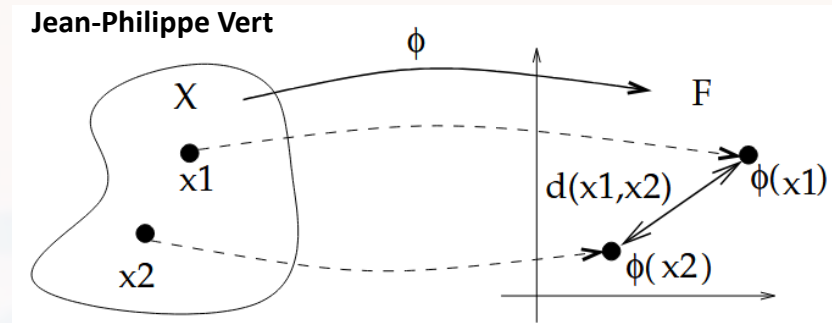
2) Is there a multiclass SVM?

problems:

- computationally intensive
- ϕ usually unknown

idea:

- entire mathematical framework not needed
- for separation: need distances d in data space and feature space



$$d^2(x, y) = \langle x - y, x - y \rangle$$

$$d_{\phi}^2(\phi(x), \phi(y)) = \langle \phi(x) - \phi(y), \phi(x) - \phi(y) \rangle$$

$$= \langle \phi(x), \phi(x) \rangle - 2\langle \phi(x), \phi(y) \rangle + \langle \phi(y), \phi(y) \rangle \quad \text{kernel } K(x, y) := \langle \phi(x), \phi(y) \rangle$$

$$d_{\phi}^2(\phi(x), \phi(y)) = K(x, x) - 2K(x, y) + K(y, y)$$

kernel trick:

- we don't know K either: **we guess it!**



1) What if linear separation is not possible?

2) Is there a multiclass SVM?

$$d^2(\phi(x), \phi(y)) = K(x, x) - 2K(x, y) + K(y, y)$$

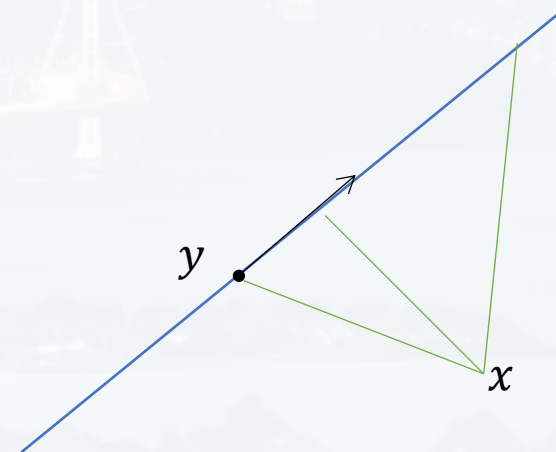
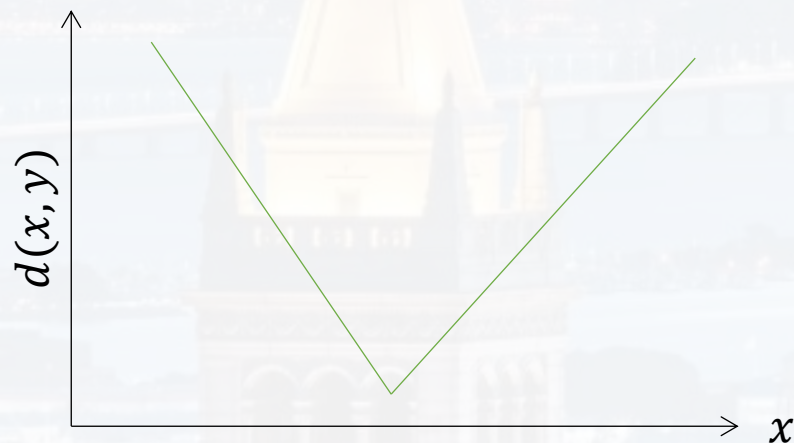
example: linear kernel

$$\phi: x \mapsto x$$

$$\phi(x) = x$$

$$d_{\phi}^2(x, y) = \langle x, x \rangle - 2\langle x, y \rangle + \langle y, y \rangle = x^2 - 2xy + y^2 = (x - y)^2$$

$$d_{\phi}^2(x, y) = |x - y|$$

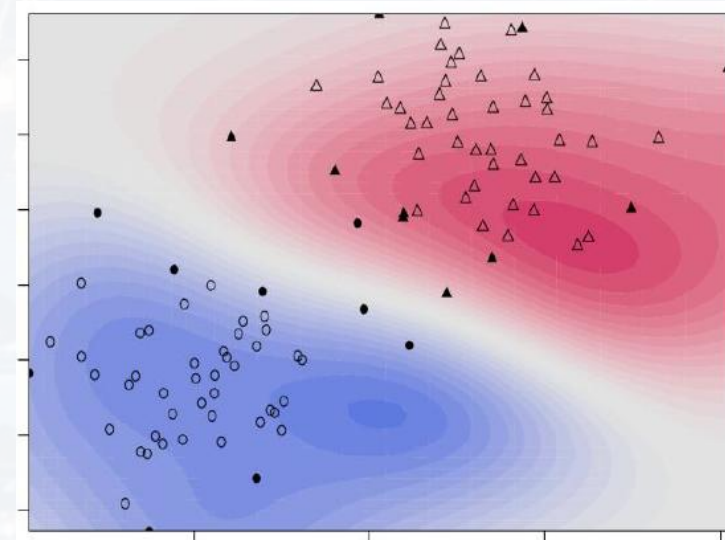
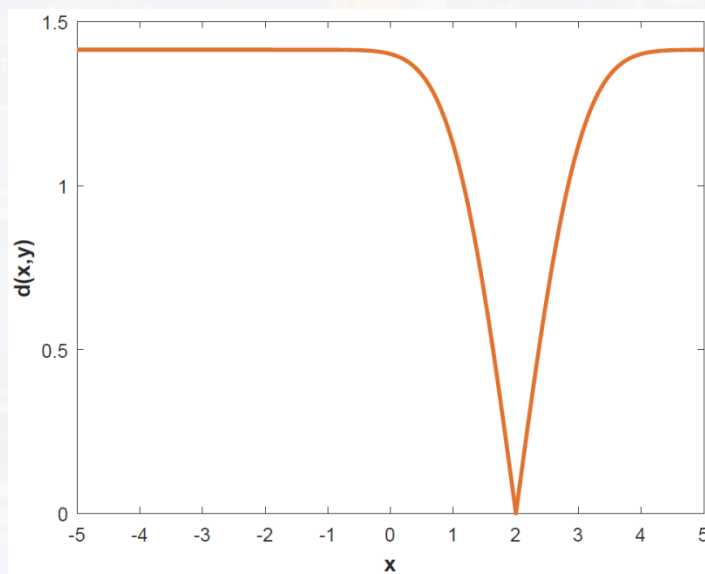


1) What if linear separation is not possible?

2) Is there a multiclass SVM?

example: : RBF (radial basis function) $\phi: x \mapsto \zeta$ $\phi(x) = \exp(-\frac{\|x\|^2}{2\sigma^2})$

$$K(x, y) = \exp\left(-\frac{\|x - y\|^2}{2\sigma^2}\right) \quad d_{\phi}^2(\phi(x), \phi(y)) = 2\left[1 - \exp\left(-\frac{\|x - y\|^2}{2\sigma^2}\right)\right]$$





1) What if linear separation is not possible?

2) Is there a multiclass SVM?

kernels available in sklearn:

- linear:

$$K(x, y) = \|x - y\|$$

- Gaussian aka RBF (radial basis function):

$$K(x, y) = \exp\left(-\frac{\|x - y\|^2}{2\sigma^2}\right)$$

in sklearn we can adjust $\gamma := \frac{1}{2\sigma^2}$

- polynomial:

$$K(x, y) = \sum_{n=1}^N \|x - y\|^n$$

in sklearn we can adjust N

- sigmoidal:

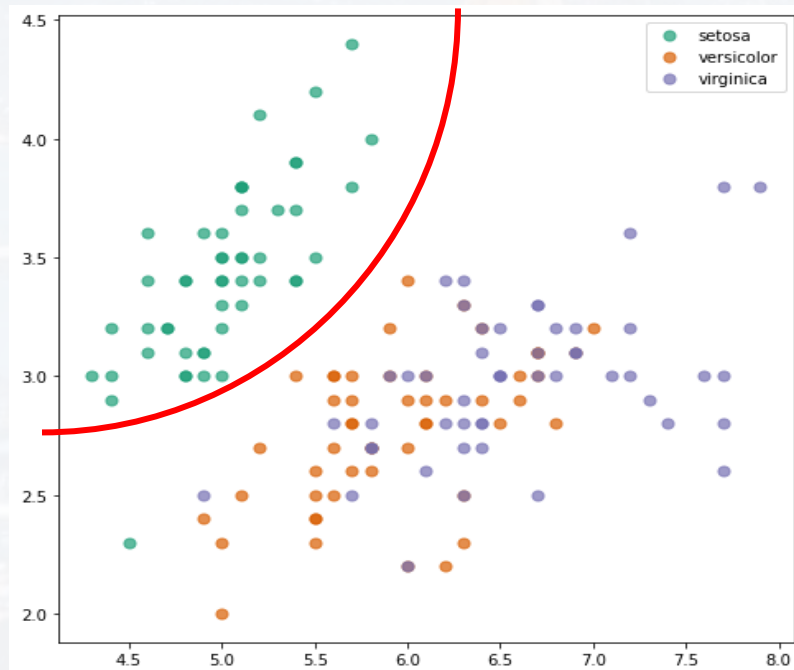
$$K(x, y) = \frac{e^{\|x-y\|}}{1 + e^{\|x-y\|}}$$

1) What if linear separation is not possible?

2) Is there a multiclass SVM?

→ one vs rest / one vs one

green vs the rest
→ storing probabilities

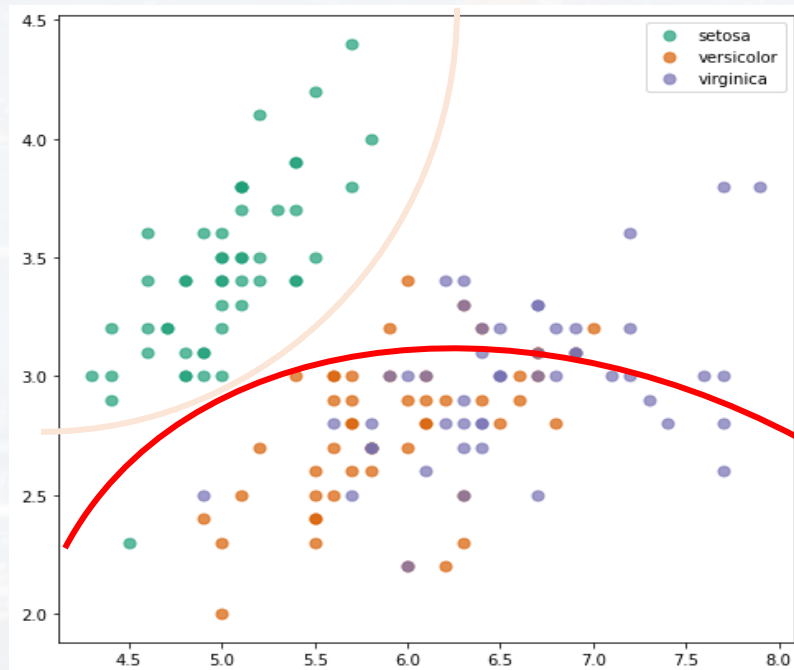


1) What if linear separation is not possible?

2) Is there a multiclass SVM?

→ one vs rest / one vs one

green vs the rest
→ storing probabilities



orange vs the rest
→ storing probabilities



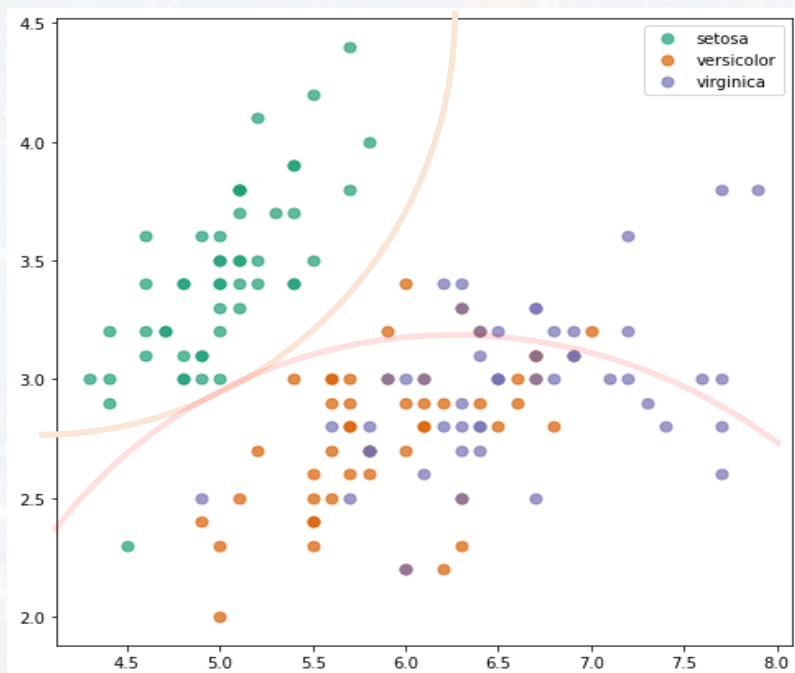


1) What if linear separation is not possible?

2) Is there a multiclass SVM?

→ one vs rest / one vs one

green vs the rest
→ storing probabilities



blue vs the rest
→ storing probabilities

orange vs the rest
→ storing probabilities

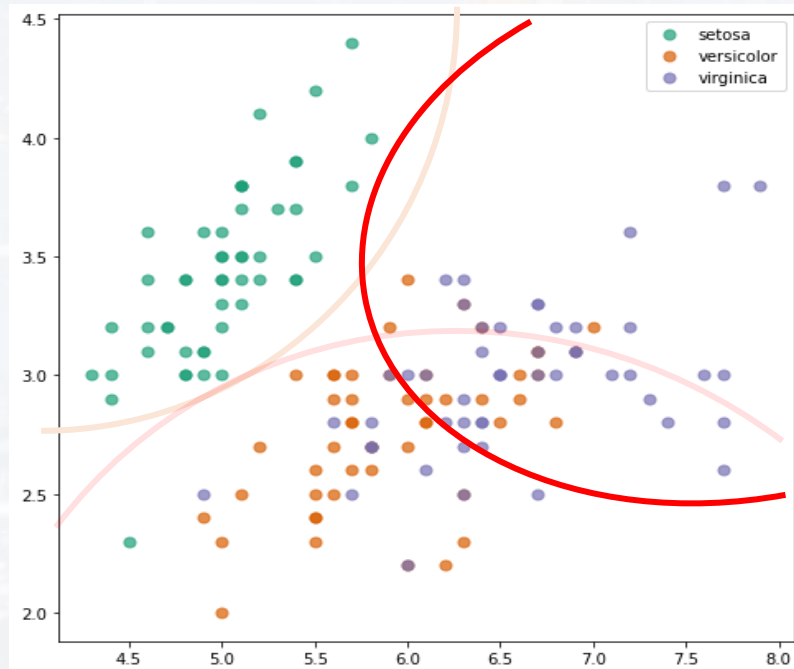


1) What if linear separation is not possible?

2) **Is there a multiclass SVM?**

→ one vs rest / one vs one

green vs the rest
→ storing probabilities



blue vs the rest
→ storing probabilities

orange vs the rest
→ storing probabilities



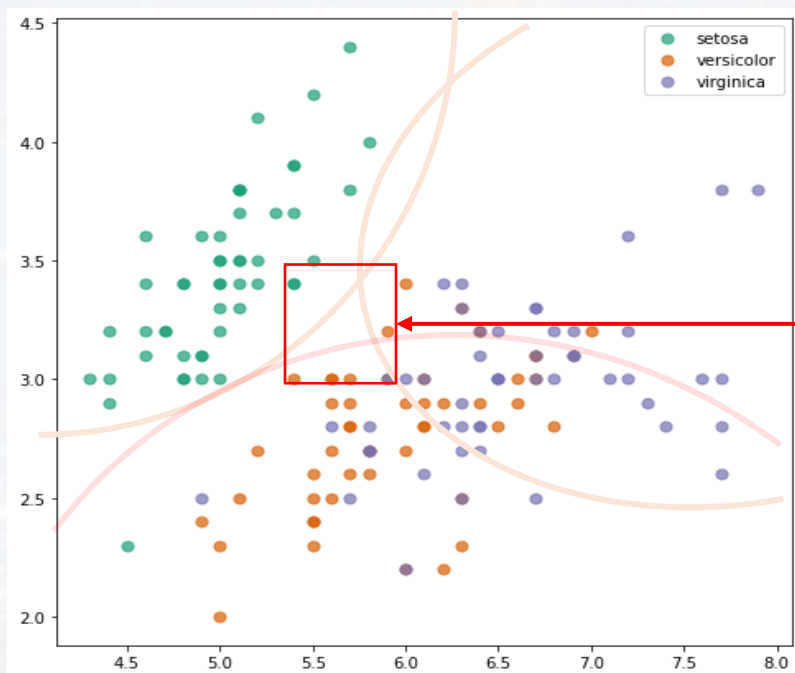


1) What if linear separation is not possible?

2) Is there a multiclass SVM?

→ one vs rest / one vs one

green vs the rest
→ storing probabilities



three probabilities for each data point
→ assign class to most probable value

k class classification with two-class discriminant functions is ambiguous!



```
from sklearn import svm
```

see [Walk_Through_SVM.ipynb](#)

1) setting up the model & 2) fitting the model

running analysis with different kernel

```
outlinear = svm.SVC(kernel = 'linear', C = 1, decision_function_shape = 'ovr')  
linear     = outlinear.fit(X2D, Y)
```

One Versus Rest

L2 regularization parameter for error
tolerance when calculating the classifier

```
outrbf     = svm.SVC(kernel = 'rbf', gamma = 1, C = 1, \  
rbf         = outrbf.fit(X2D, Y)                        decision_function_shape = 'ovr')
```

$$\gamma := \frac{1}{2\sigma^2}$$

```
outpoly    = svm.SVC(kernel = 'poly', degree = 3, C = 1, \  
poly       = outpoly.fit(X2D, Y)                        decision_function_shape = 'ovr')
```

refers to N in
 $\sum_{n=1}^N \|x - y\|^n$

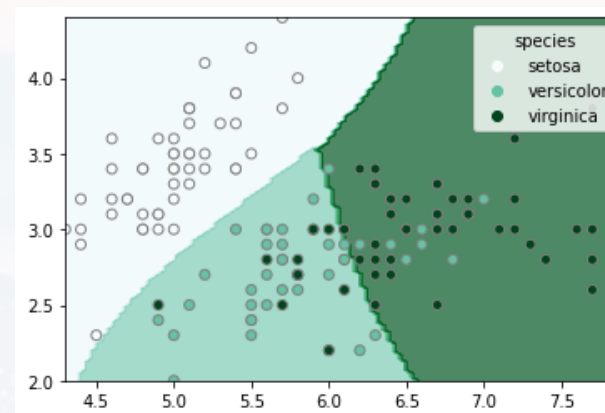
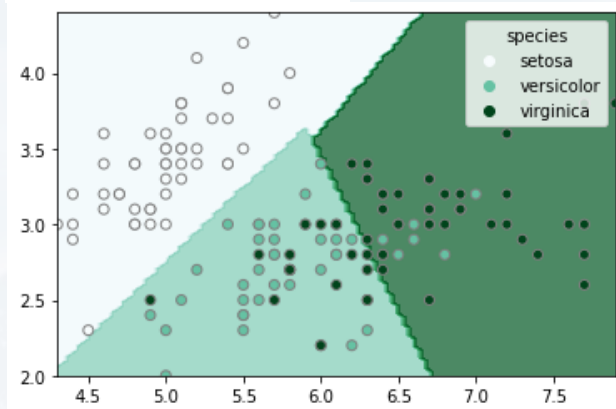
```
outsig     = svm.SVC(kernel = 'sigmoid', C = 1, decision_function_shape = 'ovr')  
sig        = outsig.fit(X2D, Y)
```




```
from sklearn import svm
```

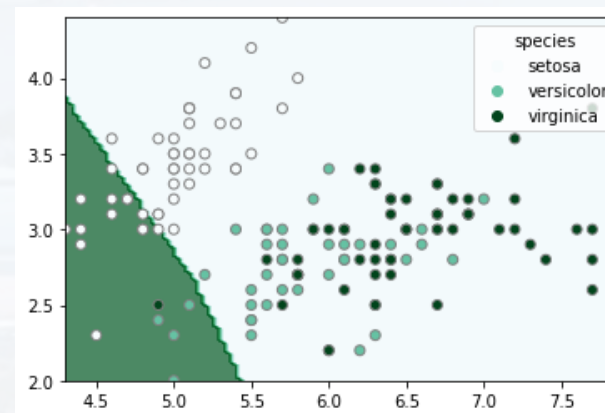
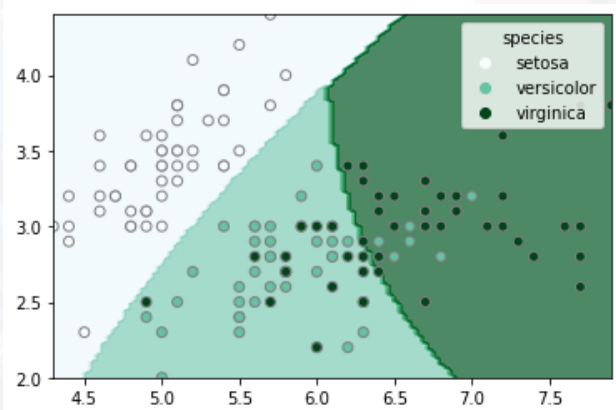
see [Walk_Through_SVM.ipynb](#)

$$K(x, y) = \|x - y\|$$



$$K(x, y) = \exp\left(-\frac{\|x - y\|^2}{2\sigma^2}\right)$$

$$K(x, y) = \sum_{n=1}^N \|x - y\|^n$$



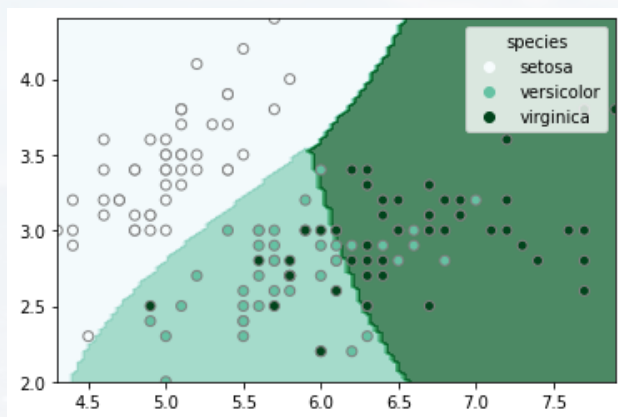
$$K(x, y) = \frac{e^{\|x - y\|}}{1 + e^{\|x - y\|}}$$



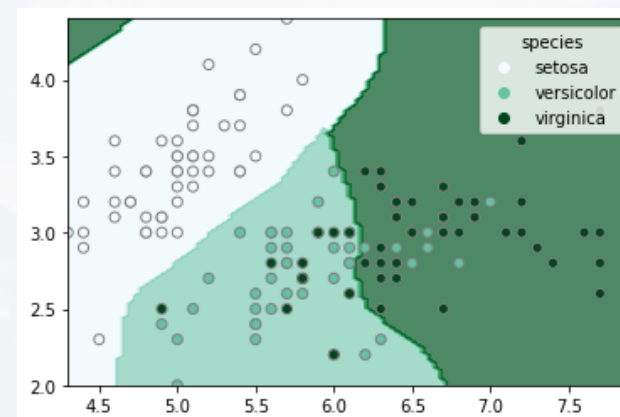
```
from sklearn import svm
```

see [Walk_Through_SVM.ipynb](#)

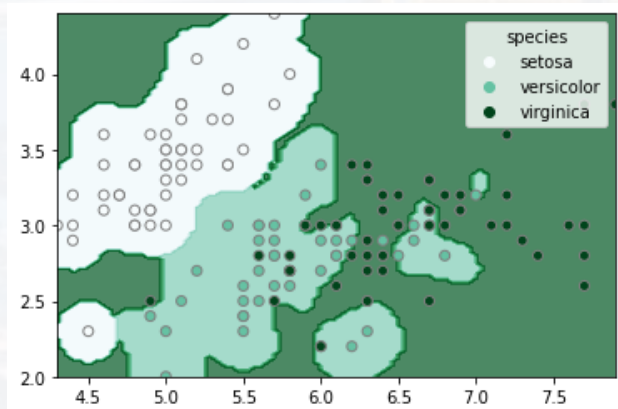
$$K(x, y) = \exp\left(-\frac{1}{2\sigma^2} \|x - y\|^2\right)$$



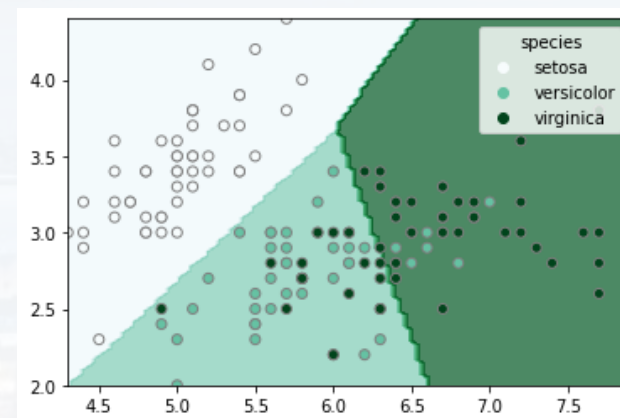
$$\gamma := \frac{1}{2\sigma^2} = 1$$



$$\gamma := \frac{1}{2\sigma^2} = 5$$



$$\gamma := \frac{1}{2\sigma^2} = 50$$



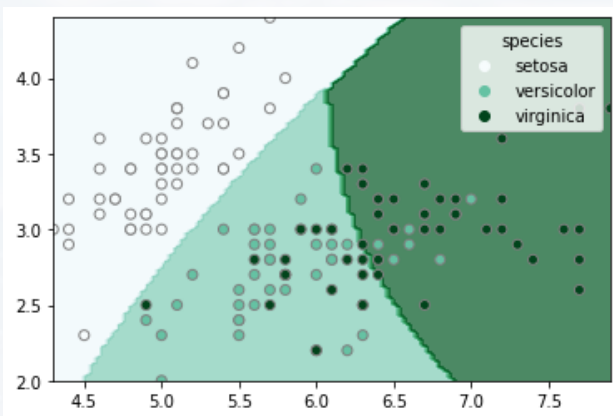
$$\gamma := \frac{1}{2\sigma^2} = 0.1$$



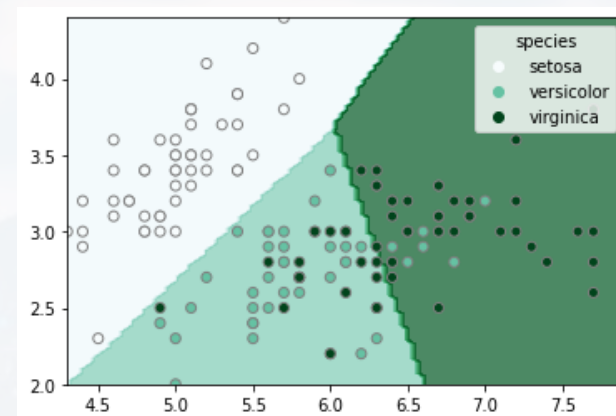
```
from sklearn import svm
```

see [Walk_Through_SVM.ipynb](#)

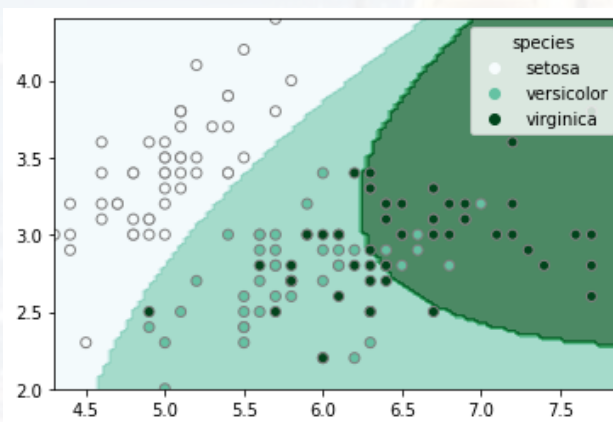
$$K(x, y) = \sum_{n=1}^N \|x - y\|^n$$



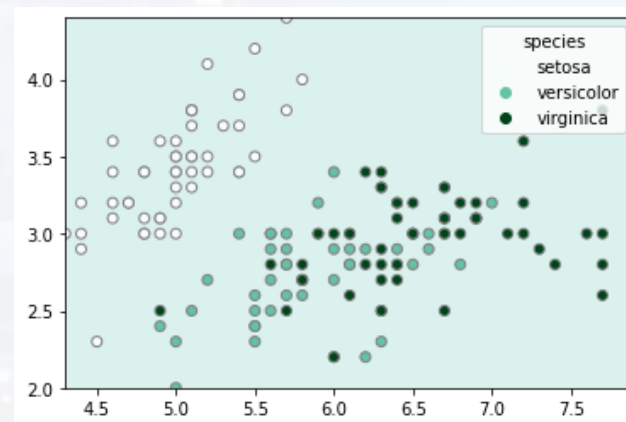
$N = 3$



$N = 1$



$N = 5$



$N = 0$

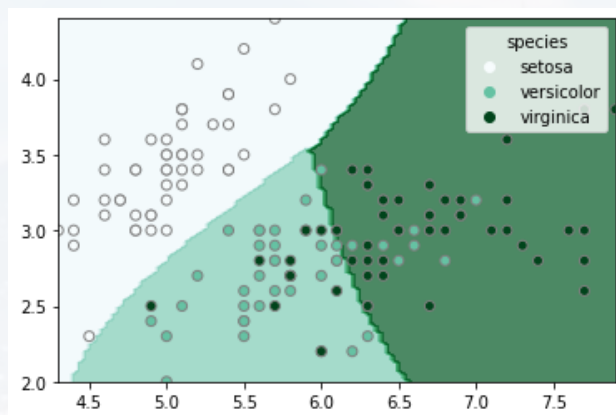


```
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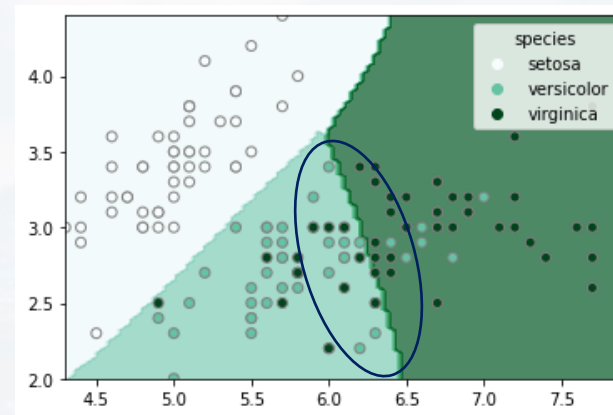
see [Walk_Through_SVM.ipynb](#)

$$K(x, y) = \exp\left(-\frac{1}{2\sigma^2} \|x - y\|^2\right)$$

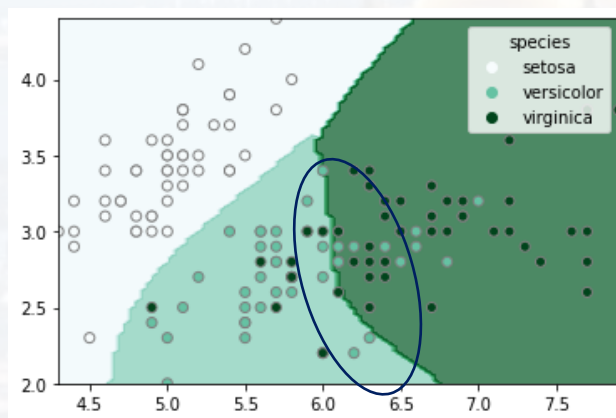
C is a [L2 regularization parameter](#)



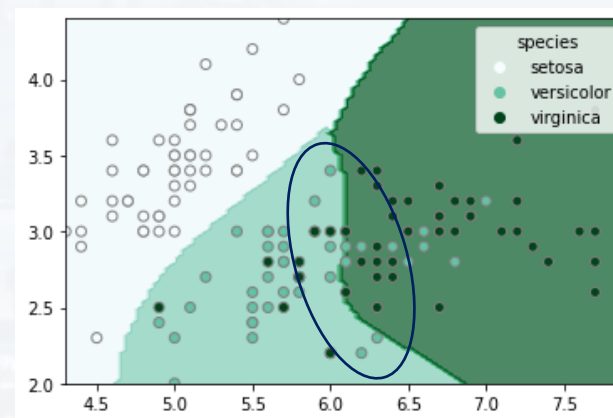
$C = 1$



$C = 0.1$



$C = 10$



$C = 20$

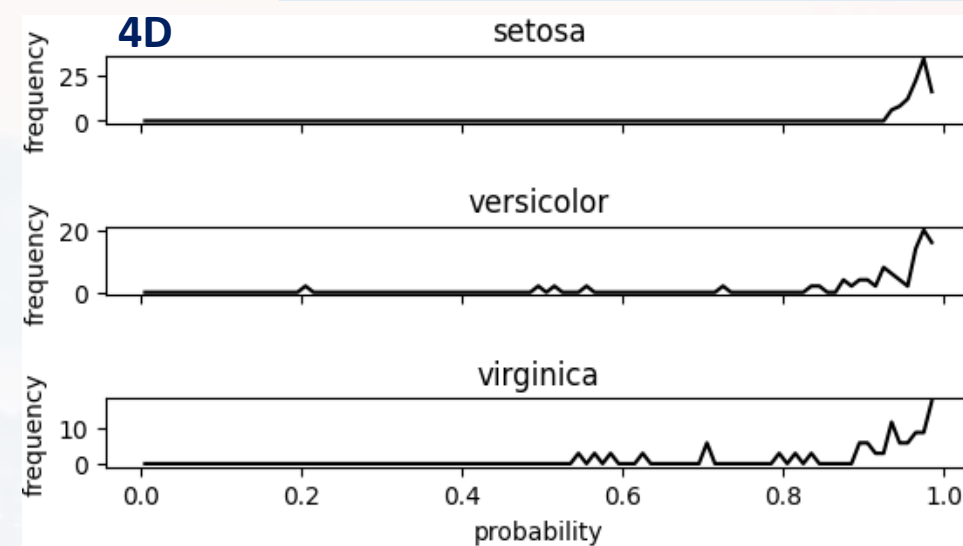
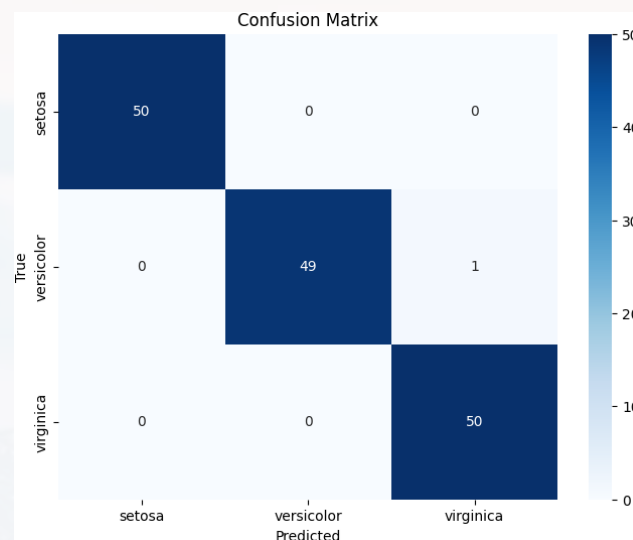


full **4D** data set

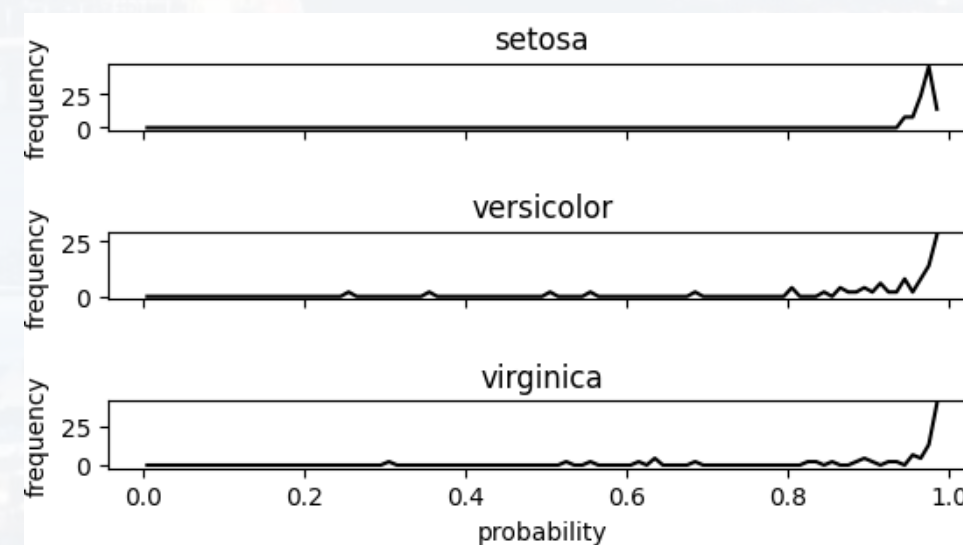
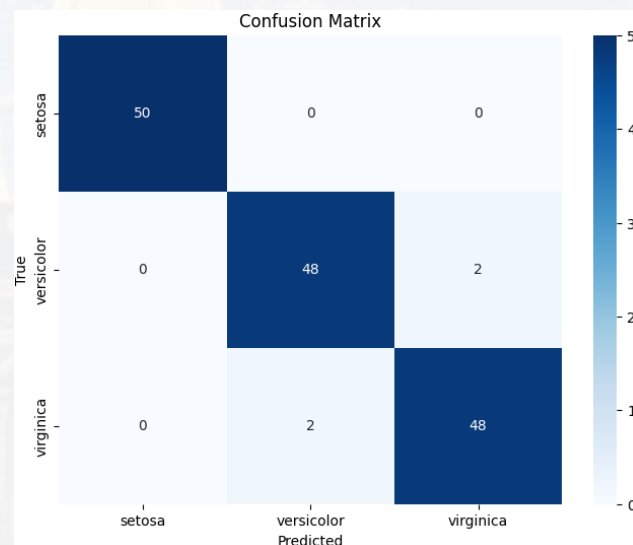
3) evaluating the model

see [Walk_Through_SVM.ipynb](#)

linear
accuracy: 99.3%



Gaussian ($\gamma = 1$)
accuracy: 97.3%



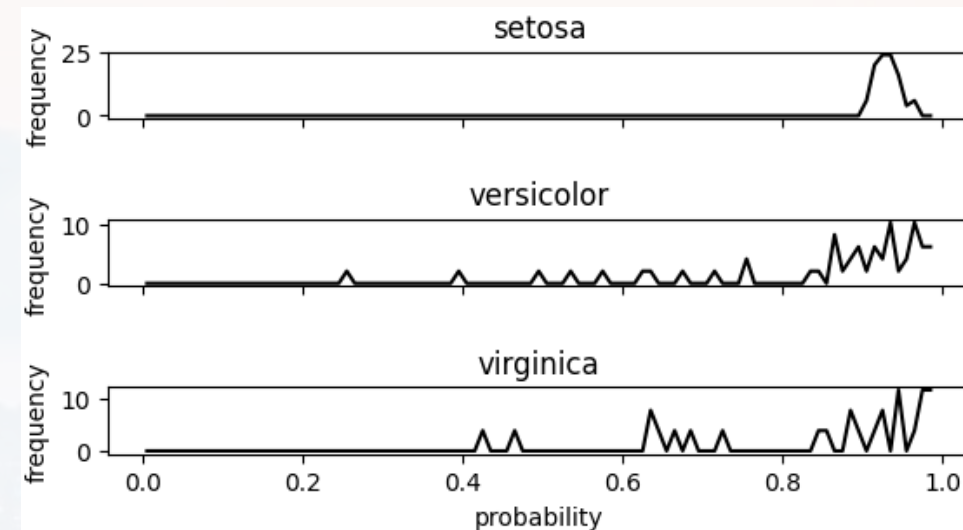
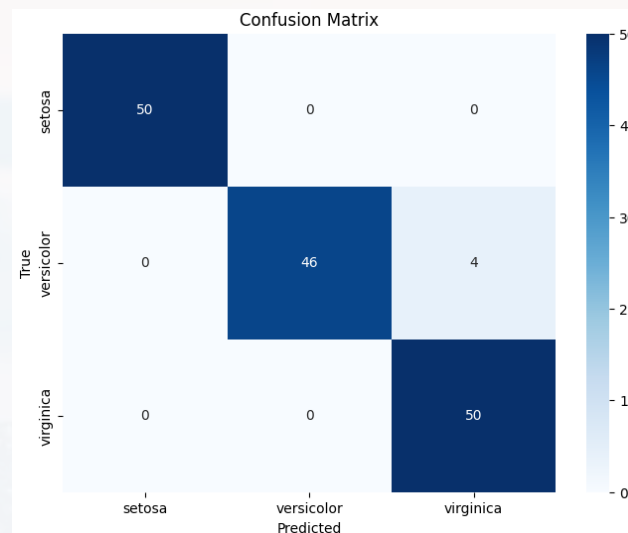


full **4D** data set

3) evaluating the model

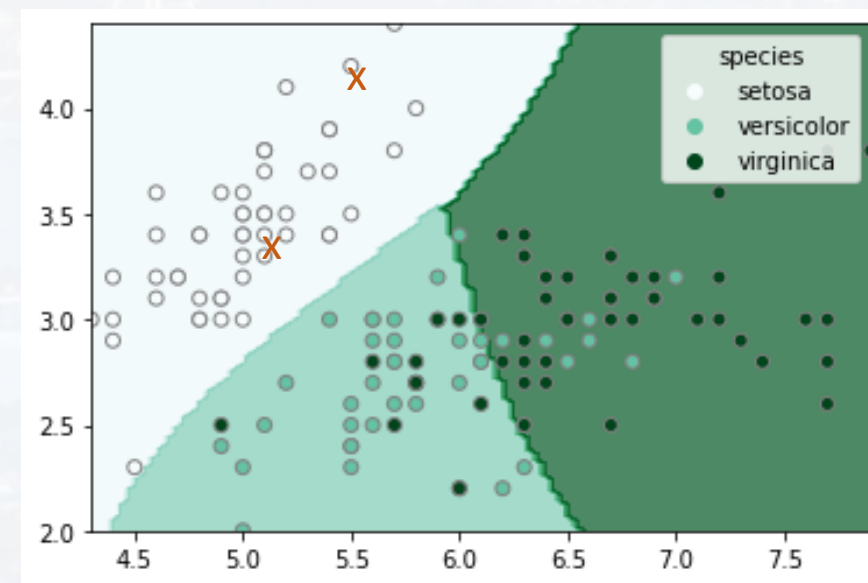
see [Walk_Through_SVM.ipynb](#)

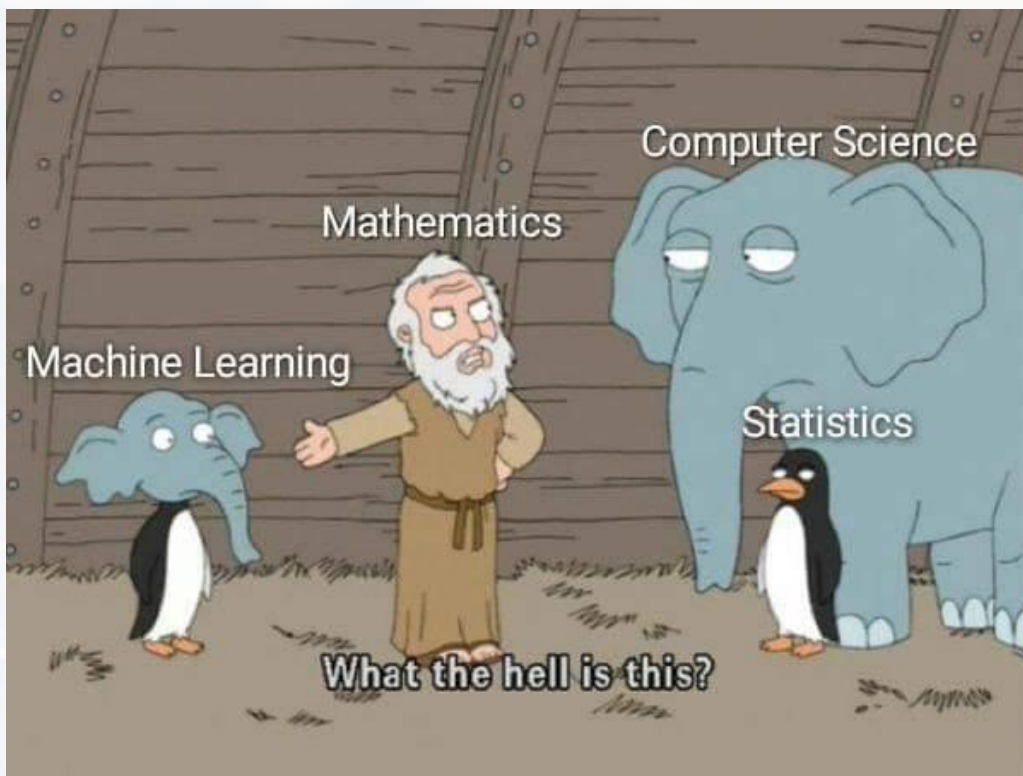
polynomial ($n = 3$)
accuracy: 97.3%



4) applying the model to a new data set

```
ypred = outpoly.predict([[6, 3.5],[6.3, 4.5]])
```



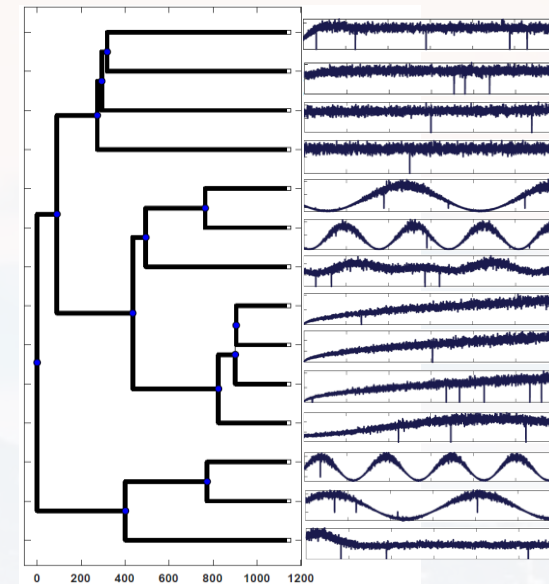
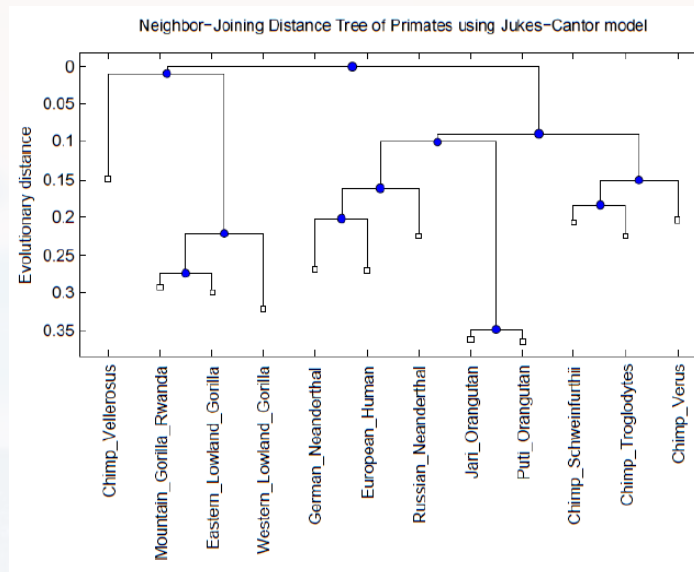


Outline

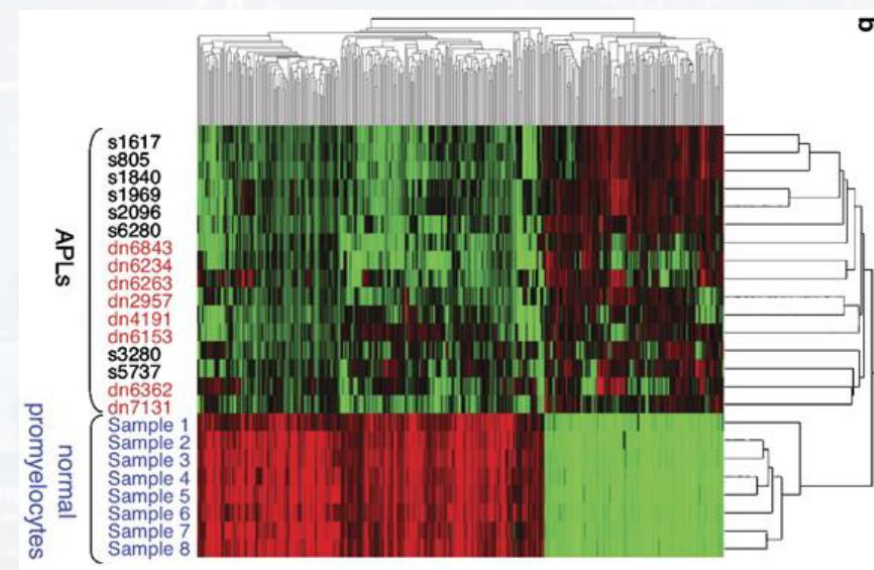
General Overview

Methods we haven't discussed yet

- Support Vector Machine
- Trees

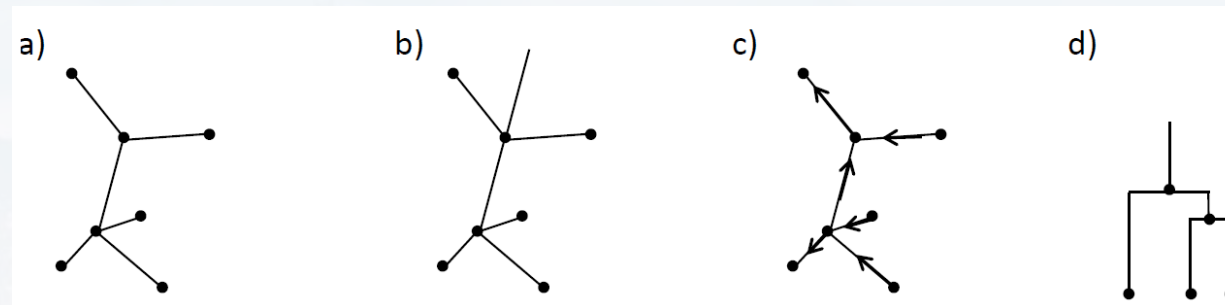
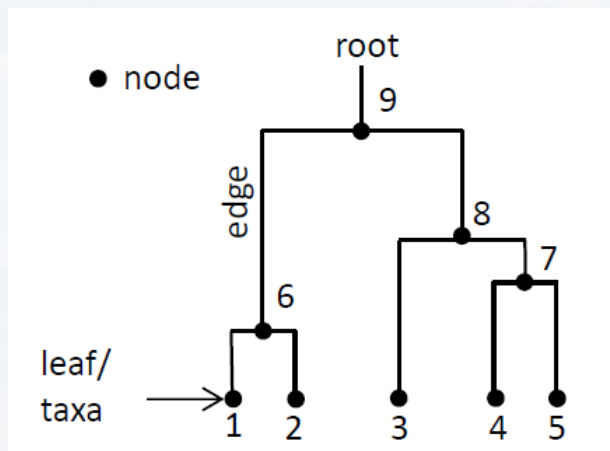


- What is a tree?
- Different kinds of trees...?
- How to build a tree?
- Why do we need trees?
- Examples...

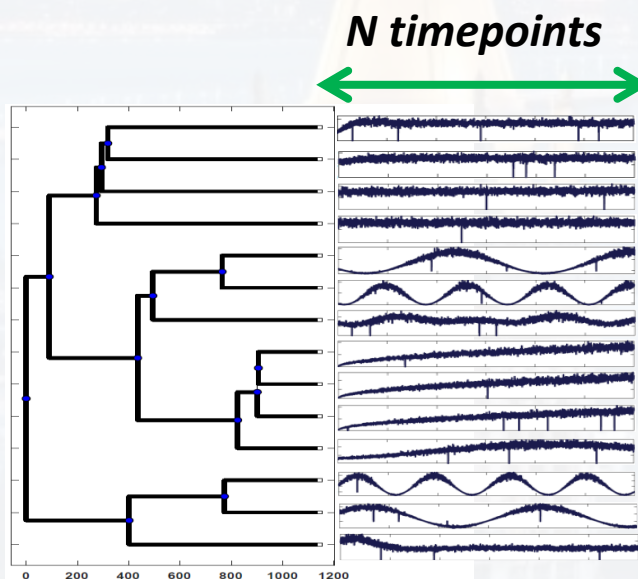




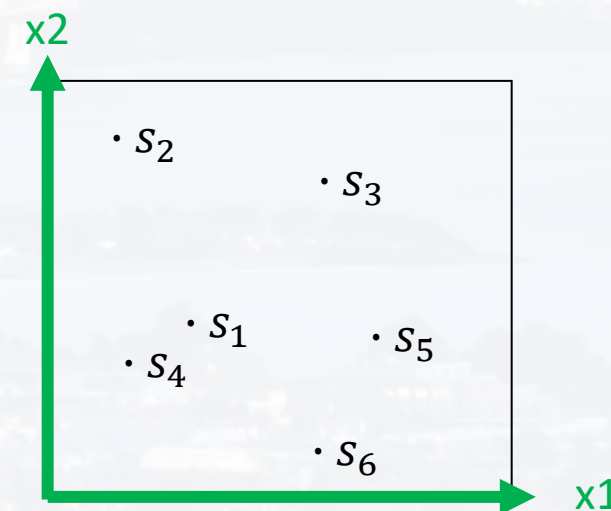
trees are a subclass of graphs (but: not fully connected \rightarrow “hierarchy”, no loops):



- a) unrooted, undirected multinary tree
- b) rooted, undirected multinary tree
- c) unrooted, directed multinary tree
- d) rooted, undirected binary tree

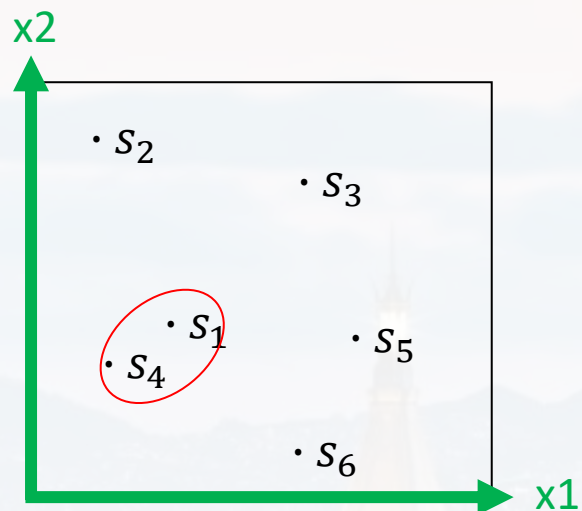


*each sample s is
a vector of N rows,
hence, a data point
in N -D*





constructing trees:



- calculating a distance between each pair of samples

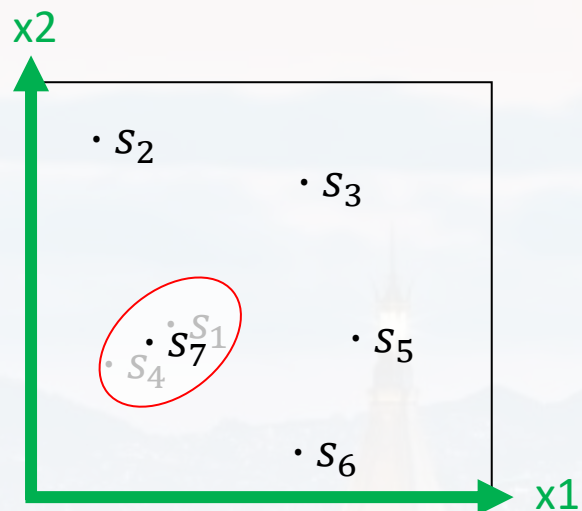
	s_1	s_2	s_3	s_4	s_5	s_6
s_1	0	$d(s_1, s_2)$	$d(s_1, s_3)$	$d(s_1, s_4)$	$d(s_1, s_5)$	$d(s_1, s_6)$
s_2		0	$d(s_2, s_3)$	$d(s_2, s_4)$	$d(s_2, s_5)$	$d(s_2, s_6)$
s_3			0	$d(s_3, s_4)$	$d(s_3, s_5)$	$d(s_3, s_6)$
s_4				0	$d(s_4, s_5)$	$d(s_4, s_6)$
s_5					0	$d(s_5, s_6)$
s_6						0

...once a distance has been defined (see soon)...

→ find the closest pair

t_4 $t_1 = t_4 = \frac{1}{2} d(s_1, s_4)$

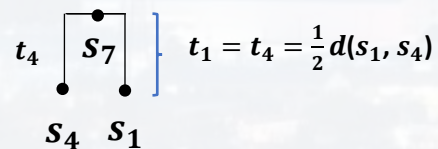
constructing trees:



- calculating a distance between each pair of samples

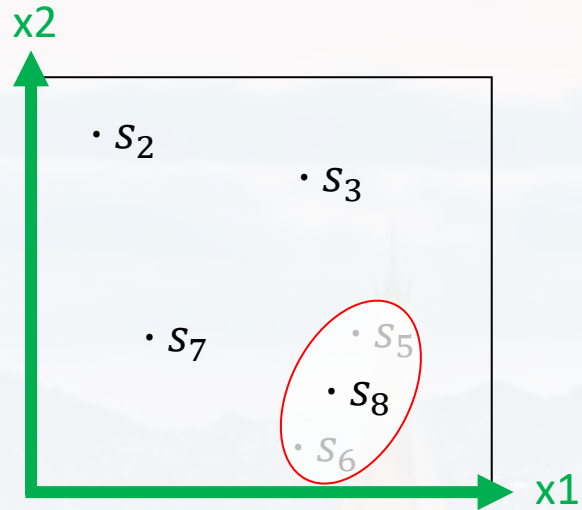
	s_1	s_2	s_3	s_4	s_5	s_6
s_1	0	$d(s_1, s_2)$	$d(s_1, s_3)$	$d(s_1, s_4)$	$d(s_1, s_5)$	$d(s_1, s_6)$
s_2		0	$d(s_2, s_3)$	$d(s_2, s_4)$	$d(s_2, s_5)$	$d(s_2, s_6)$
s_3			0	$d(s_3, s_4)$	$d(s_3, s_5)$	$d(s_3, s_6)$
s_4				0	$d(s_4, s_5)$	$d(s_4, s_6)$
s_5					0	$d(s_5, s_6)$
s_6						0

- treat it as a new cluster $s_{1,4}$
- use average of distance from cluster elements





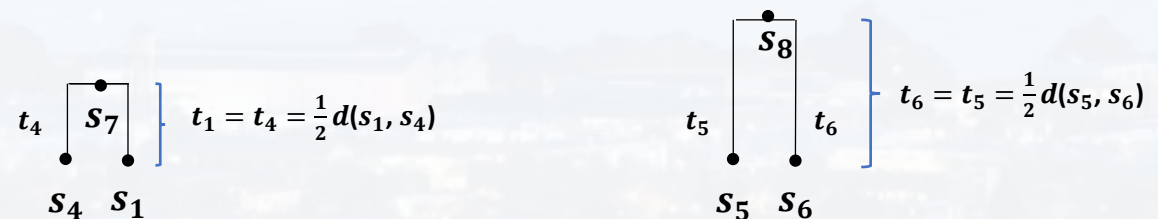
constructing trees:



- calculating a distance between each pair of samples

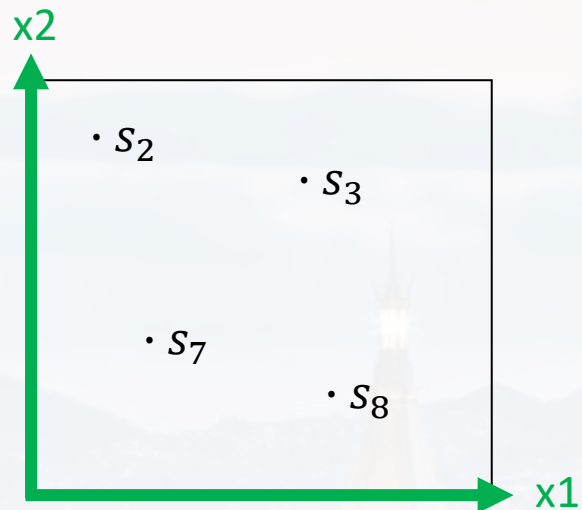
	s_1	s_2	s_3	s_4	s_5	s_6
s_1	0	$d(s_1, s_2)$	$d(s_1, s_3)$	$d(s_1, s_4)$	$d(s_1, s_5)$	$d(s_1, s_6)$
s_2		0	$d(s_2, s_3)$	$d(s_2, s_4)$	$d(s_2, s_5)$	$d(s_2, s_6)$
s_3			0	$d(s_3, s_4)$	$d(s_3, s_5)$	$d(s_3, s_6)$
s_4				0	$d(s_4, s_5)$	$d(s_4, s_6)$
s_5					0	$d(s_5, s_6)$
s_6						0

→ find the closest pair
(now including the cluster)





constructing trees:

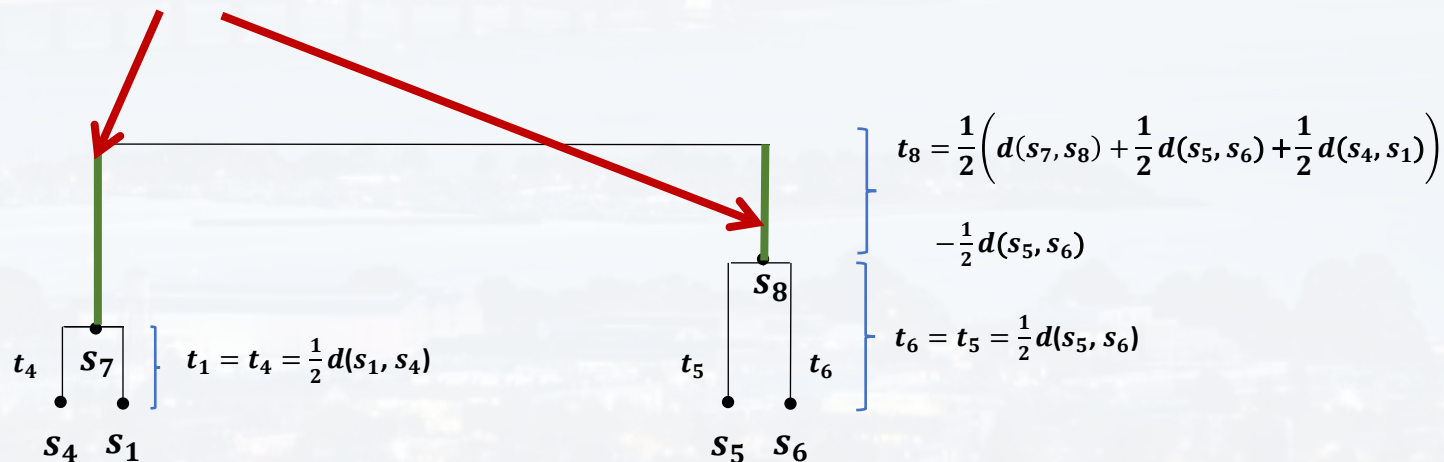


- calculating a distance between each pair of samples

	s_1	s_2	s_3	s_4	s_5	s_6
s_1	0	$d(s_1, s_2)$	$d(s_1, s_3)$	$d(s_1, s_4)$	$d(s_1, s_5)$	$d(s_1, s_6)$
s_2		0	$d(s_2, s_3)$	$d(s_2, s_4)$	$d(s_2, s_5)$	$d(s_2, s_6)$
s_3			0	$d(s_3, s_4)$	$d(s_3, s_5)$	$d(s_3, s_6)$
s_4				0	$d(s_4, s_5)$	$d(s_4, s_6)$
s_5					0	$d(s_5, s_6)$
s_6						0

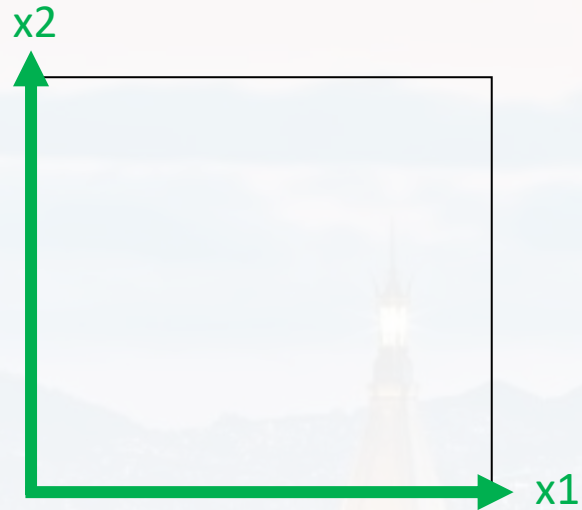
→ and so on....

$$d(s_7, s_8) = \frac{d(s_5, s_7) + d(s_6, s_7)}{2} = \frac{d(s_1, s_5) + d(s_4, s_5) + d(s_1, s_6) + d(s_4, s_6)}{4}$$





constructing trees:

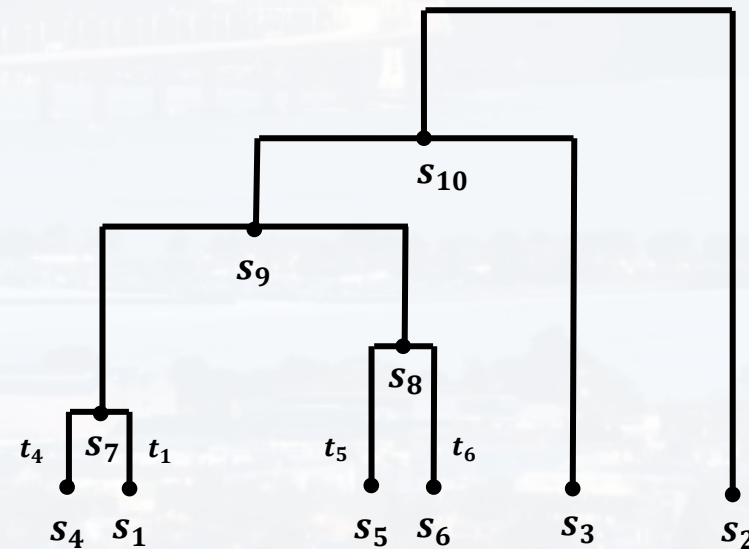


- calculating a distance between each pair of samples

	s_1	s_2	s_3	s_4	s_5	s_6
s_1	0	$d(s_1, s_2)$	$d(s_1, s_3)$	$d(s_1, s_4)$	$d(s_1, s_5)$	$d(s_1, s_6)$
s_2		0	$d(s_2, s_3)$	$d(s_2, s_4)$	$d(s_2, s_5)$	$d(s_2, s_6)$
s_3			0	$d(s_3, s_4)$	$d(s_3, s_5)$	$d(s_3, s_6)$
s_4				0	$d(s_4, s_5)$	$d(s_4, s_6)$
s_5					0	$d(s_5, s_6)$
s_6						0

....finally

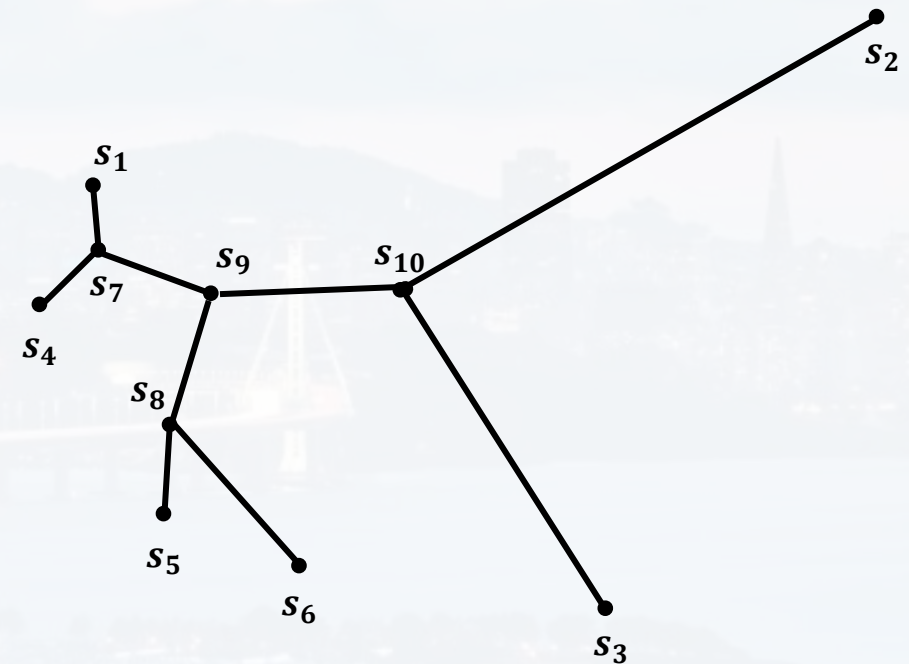
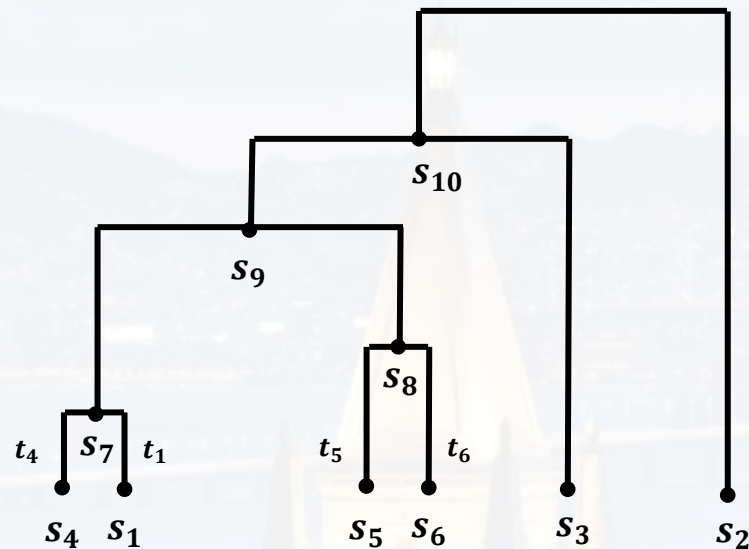
→ **Unweighted Pair Group Method**
Using **Arithmetic Averages (UPGMA)**





constructing trees:

→ **Unweighted Pair Group Method**
Using **Arithmetic Averages (UPGMA)**



note: sometimes these diagrams might be misleading when interpreting the distances between the nodes



distances:

“A distance ***d*** is a function that assigns a **positive real number** to a set and/or to elements of a set.”

properties:

- $d(x, y) \geq 0$
- $d(x, y) = 0 \Leftrightarrow x = y$
- $d(x, y) = d(y, x)$
- $d(x, z) \leq d(x, y) + d(y, z)$

frequently used distances:

- Euclidean
- cityblock
- cosine
- correlation
- hamming
- Jukes Cantor



distances:

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- Euclidean
- cityblock
- cosine
- correlation
- hamming
- Jukes Cantor

```
from pyclustering.utils.metric import *
```

type_metric.

CANBERRA
CHEBYSHEV
CHI_SQUARE
EUCLIDEAN
EUCLIDEAN_SQUARE
GOWER
MANHATTAN



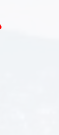
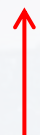
distances:

The Jukes-Cantor distance

question: What could be a measure of distance here?

Seq1 = {AAGTCTTTGAATCGTATGGGCGCGGCTTTCAAAA}

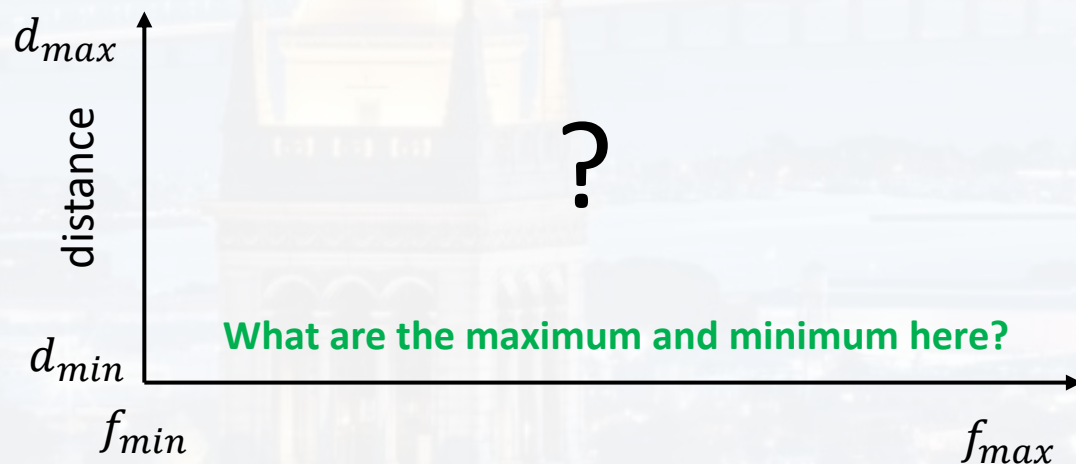
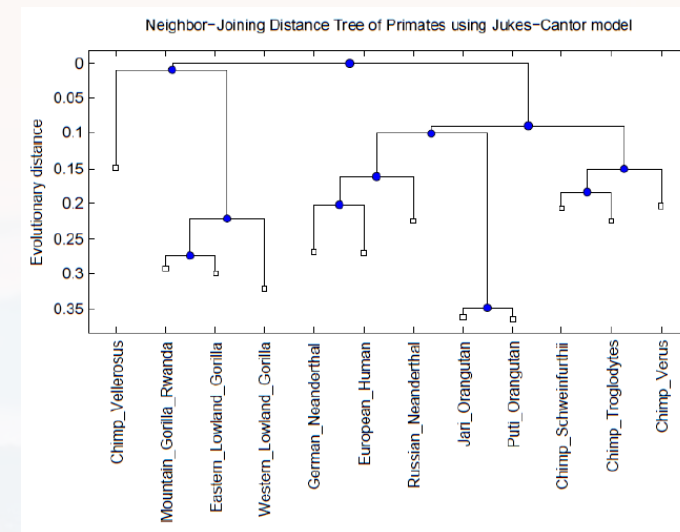
Seq2 = {A^{AG}GTCT^ATGAATCGTATGGG^{TT}CGGCTTTCAAAA}



fraction f of different sites

if f is large $\rightarrow d$ is large

if f is small $\rightarrow d$ is small





distances:

The Jukes-Cantor distance

f : fraction of different sites

Seq1 = {AAGTCTTTGAATCGTATGGGCGCGGCTTTCAAAA}

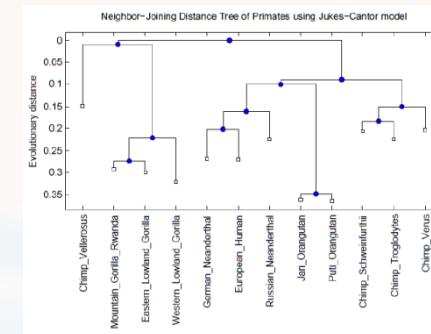
Seq2 = {AAGTCTATGAATCGTATGGGTCGGCTTTCAAAA}

$f_{min} = 0 \rightarrow d_{min} = 0$ (sequences are identical)

for N letters ($N = 4$ nucleotides, $N = 20$ amino acids)

$$f_{max} = 1 - \frac{1}{N} \rightarrow d_{max} = \infty$$

(sequences have no relations, matches are coincidence)



- the probability that a site **has been** mutated, given a mutation rate λ equals:

$$P(any|\lambda) = 1 - e^{-\lambda t}$$

- the probability that this mutation will lead to a **particular letter** is

$$P(part|\lambda) = \frac{1}{N} (1 - e^{-\lambda t})$$

- the probability that this mutation will lead to a **letter other than the previous one** is

$$P(part|\lambda) = \frac{N-1}{N} (1 - e^{-\lambda t})$$



distances:

The Jukes-Cantor distance

f : fraction of different sites

Seq1 = {AAGTCTTTGAATCGTATGGGCGCGGCTTTCAAAA}

Seq2 = {AAGTCTATGAATCGTATGGGTTTCGGCTTTCAAAA}

$f_{min} = 0 \rightarrow d_{min} = 0$ (sequences are identical)

for N letters ($N = 4$ nucleotides, $N = 20$ amino acids)

- the probability that this mutation will lead to a **letter other than the previous one** is

$$P(part|\lambda) = \frac{N-1}{N} (1 - e^{-\lambda t})$$

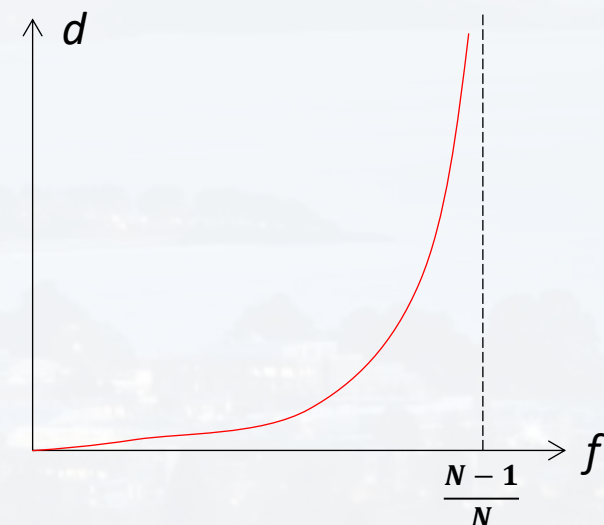
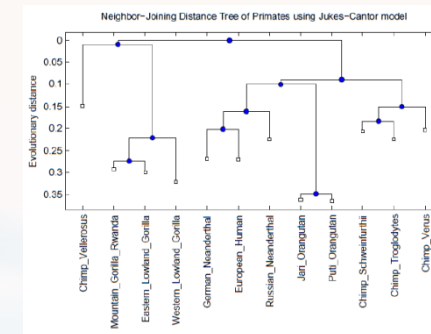
$\lambda t \sim d$ since cumulative mutations is what makes species different!

$$d \sim \lambda t = -\ln \left(1 - \frac{N-1}{N} f \right)$$

often:

$$d = -\frac{N-1}{N} \ln \left(1 - \frac{N-1}{N} f \right)$$

Jukes – Cantor distance





distances:

Jukes – Cantor distance
$$d(x, \bar{x}) = -\frac{N-1}{N} \ln \left(1 - \frac{N}{N-1} f(x, \bar{x}) \right)$$

Euclidean distance
$$d(x, \bar{x})^2 = (x_1 - \bar{x}_1)^2 + (x_2 - \bar{x}_2)^2 \dots (x_N - \bar{x}_N)^2$$

cityblock
$$d(x, \bar{x}) = |x_1 - \bar{x}_1| + |x_2 - \bar{x}_2| \dots |x_N - \bar{x}_N|$$

cosine
$$d(x, \bar{x}) = 1 - \frac{x \cdot \bar{x}}{\sqrt{(x \cdot x)(\bar{x} \cdot \bar{x})}}$$

correlation
$$d(x, \bar{x}) = 1 - \frac{\text{cov}(x, \bar{x})}{\sqrt{\text{var}(x)\text{var}(\bar{x})}}$$

...and many others

note: for sequence alignment and phylogenetic trees, chemical properties of the AA or NT have to be taken into account → **score matrices**



Python libraries:

see [Walk_Through_Tree.ipynb](#)

libraries from the *Bio* package

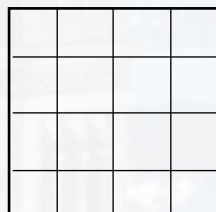
```
from Bio.Phylo.TreeConstruction import DistanceCalculator, DistanceTreeConstructor  
from Bio import Phylo  
from scipy import spatial
```

for plotting a
phylogenetic tree

for rearranging a
distance matrix

general idea:

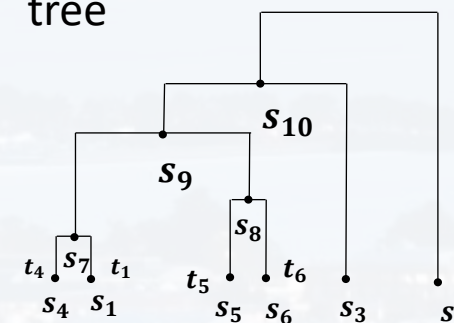
distance matrix



linkage algorithm (e.g. UPGMA)



tree





Python libraries:

see `Walk_Through_Tree.ipynb`

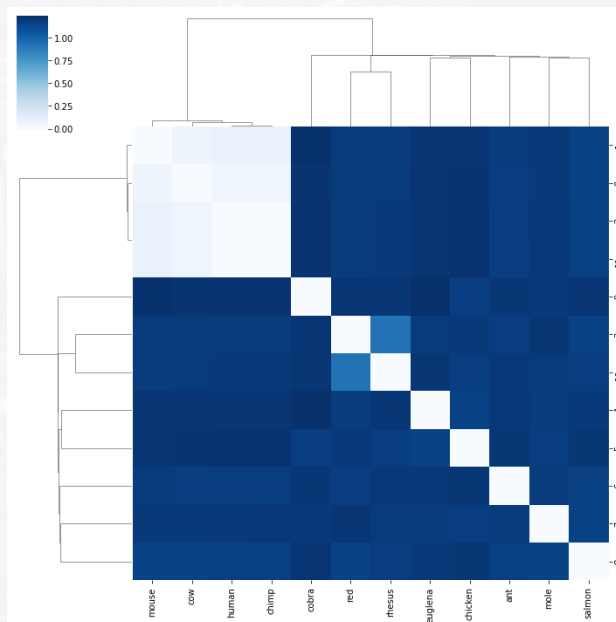
also most heatmap tools have some abilities to construct trees:

`sns.clustermap`

```
sns.clustermap(D_df, cmap = 'Blues', \
               row_cluster = True, col_cluster = True, \
               metric = 'euclidean', method = 'average', \
               yticklabels = True)
```

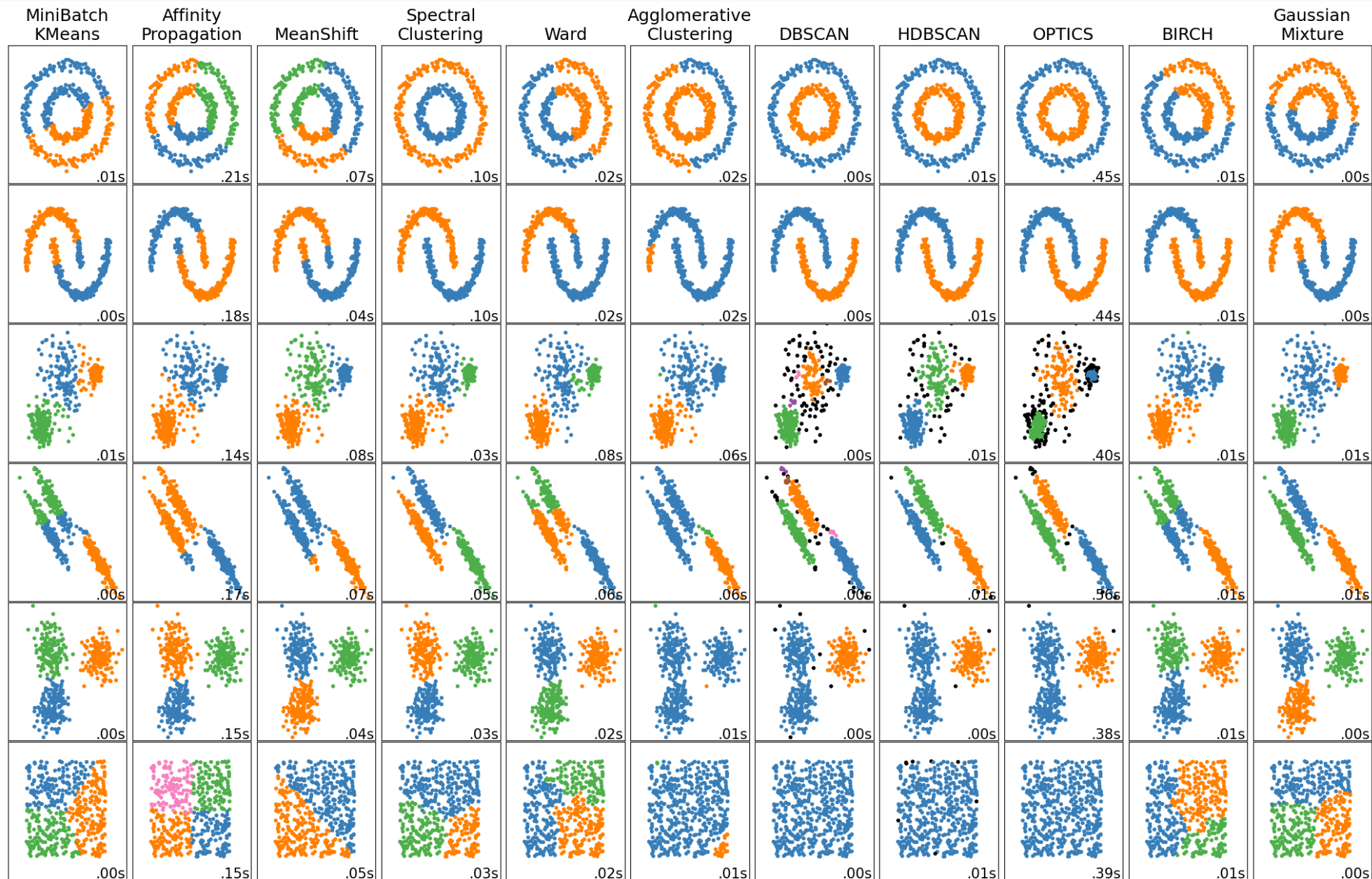
`plt.show()`

similar to UPGMA





there is a lot more...





Thank you very much for your attention!

