LAB2 REPORT

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Part 3: Summary & Experience.

Part 1: Introduction.

- In this lab, we mainly discuss the Discrete-Time Systems. And a definition to a discrete-time system is that anything that takes a discrete-time signal as input and generates a discrete-time signal as output.
- In order to understand discrete-time systems, it is important to first understand their classification into categories of linear/nonlinear, time-invariant/ time-varying, causal/noncausal, memoryless/with-memory, and stable/unstable.
- The main content contains in this lab:
 - Background Exercises
 - o Example Discrete-Time Systems
 - o Difference Equations
 - Audio Filtering
 - o Inverse Systems
 - System Tests
 - Stock Market Example

Part 2: Result & Analysis.

2.2 Background Exercises

2.2.1 Example Discrete-time Systems

• For the DT approximation of differentiator:

$$y(t) = \frac{d}{dt}x(t)$$

We have difference equation:

$$y[n] = x[n] - x[n-1]$$

• For the DT approximation of integrator:

$$y(t) = \int_{-\infty}^{t} x(\tau) d\tau$$

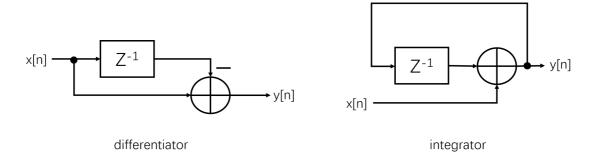
We have difference equation:

$$y[n] - y[n-1] = x[n]$$

which could be also wirtten as

$$y[n] = x[n] + y[n-1]$$

• Block diagram for these two discrete-time system (Figure 2.1):



2.2.2 Stock Market Example

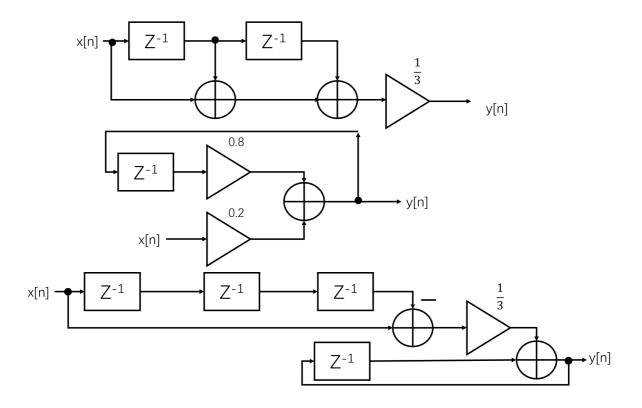
• Let n be the nth day, y[n] be avgvalue, and x[n] be value.

Then we have below three difference equations:

$$System1: y[n] = rac{1}{3}(x[n] + x[n-1] + x[n-2])$$

 $System2: y[n] = 0.8y[n-1] + 0.2x[n]$
 $System3: y[n] = y[n-1] + rac{1}{3}(x[n] - x[n-3])$

• System diagrams for these three equations (Figure 2.2):



• Impulse response for these four systems:

$$System1: h[n] = rac{1}{3}(\delta[n] + \delta[n-1] + \delta[n-2])$$

 $System2: h[n] = 0.8h[n-1] + 0.2\delta[n]$
 $System3: h[n] = h[n-1] + rac{1}{3}(\delta[n] - \delta[n-3])$

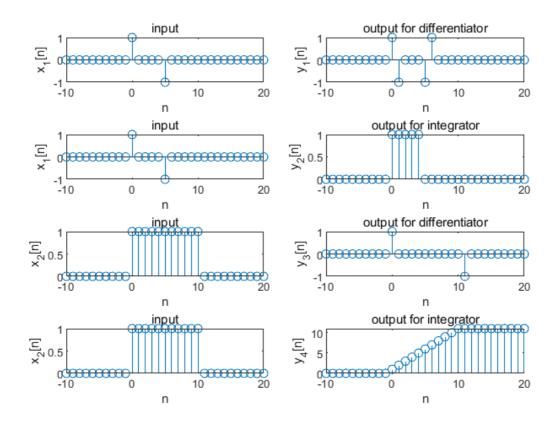
• Methods (2.3) and methods (2.5) are known as moving average becasue the absolute value of weights applied on the time sequence is equal, which will make the average value line become smoother and much more flat.

2.3 Example Discrete-Time Systems

• Codes for two functions:

```
function y=differentiator(x)
% y[n]=x[n]-x[n-1]
x=[0 x];
y=zeros(1,length(x)-1);
for n=1:length(x)-1
     y(n)=x(n+1)-x(n);
end
end
```

```
function y=integrator(x)
% y[n]=x[n]+y[n-1]
y=zeros(1,length(x)+1);
for n=1:length(x)
y(n+1)=x(n)+y(n);
end
y=y(2:length(x)+1);
end
```



Analysis:
 For these four cases, they all satisfy the BIBO stability.

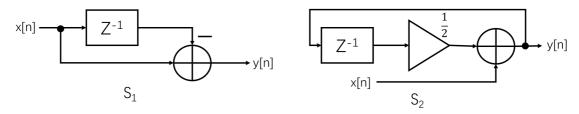
2.4 Differential Systems

• Codes for two functions:

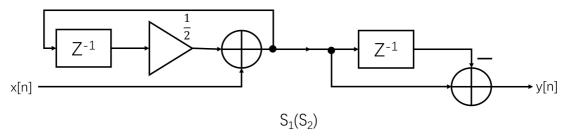
```
function y=S1(x)
% y[n]=x[n]-x[n-1]
N=length(x);
x=[0 x];
y=zeros(1,N);
for n=1:N
     y(n)=x(n+1)-x(n);
end
end
```

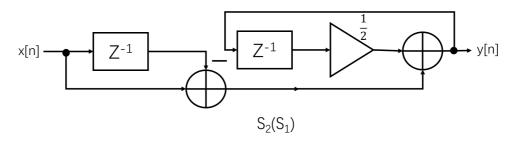
```
function y=S2(x)
% y[n]=(1/2)y[n-1]+x[n]
N=length(x);
y=zeros(1,N+1);
for n=1:length(x)
y(n+1)=x(n)+(1/2)*y(n);
end
y=y(2:N+1);
end
```

Block diagram for each case
 Block diagrams for S1 and S2:

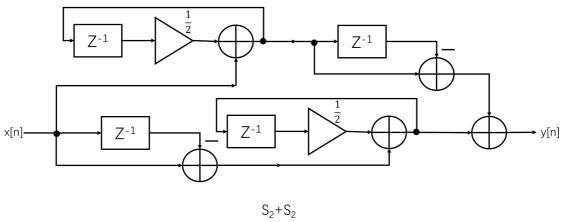


Block diagrams for S1(S2) and S2(S1):





Block diagram for S1+S2:



• Impulse responses for these five cases:

Impulse responses for five cases

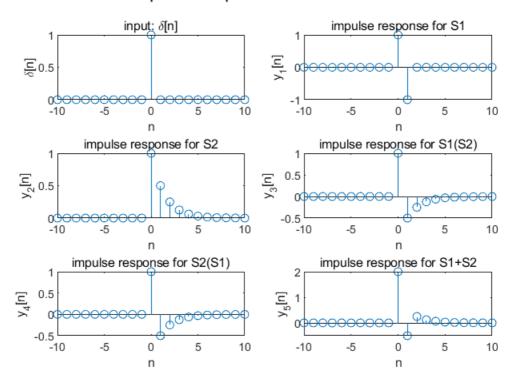


Figure 2.7 Impulse responses of five systems

- Oberservations:
 - Impulse response of S1+S2 equals the sum of impulse responses of S1 and S2; (Parrallel connection results in addition.)
 - Impulse response of S1(S2) is same with impulse response of S2(S1), and the impulse response of this two system is S1⊗S2 ;(Series connection results in convolution.)

2.5 Aduio Filtering

• Code for this section:

```
clear;
[s,fs]=audioread('music.au');
s=s';
s1=S1(s);
s2=S2(s);
sound(s1,fs);
next=input('press any key to the next song');
sound(s2,fs);
```

- Analysis:
 - Compared with the original song, the song filtered by System S1 is much more smoother.
 - Compared with the original song, the song filtered by System S2 is louder and much more tighter.

2.6 Inverse Systems

• For system S2, we have $y_2[n] = \frac{1}{2}y_2[n-1] + x_2[n]$;

For system S3, we have $y_3[n]=ax_3[n]+bx_3[n-1]$, where a and b are constant;

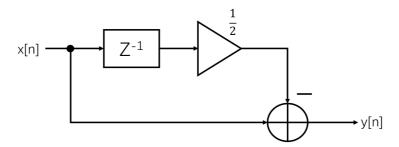
To calculate the output of $S_3(S_2)$, let x3[n]=y2[n]. After the variable substitution, we have:

$$y_3[n] = a(\frac{1}{2}y_2[n-1] + x_2[n]) + by_2[n-1]$$

= $(\frac{a}{2} + b)y_2[n-1] + ax_2[n]$

Since we need y3[n]=x2[n], then we have: $\left\{ egin{array}{l} rac{a}{2}+b=0 \\ a=1 \end{array}
ight.$ Therefore, a=1 and b=-12;

- The difference equation for S3: $y[n] = x[n] \frac{1}{2}x[n-1]$
- Block diagram for S3:

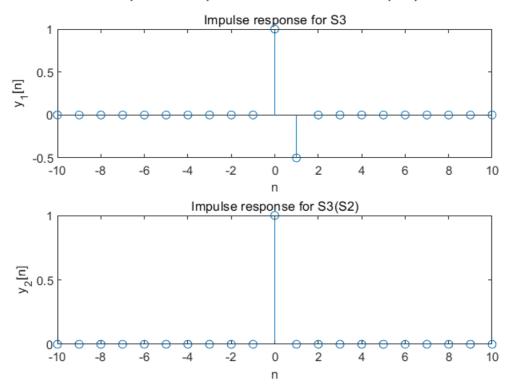


• Code for function S3:

```
function y=S3(x)
%y[n]=x[n]-1/2x[n-1]
N=length(x);
x=[0 x];
y=zeros(1,N);
for n=1:N
     y(n)=x(n+1)-(1/2)*x(n);
end
end
```

• Impulse response:

Impulse responses for S3 and S3(S2)



2.7 System Tests

• Code for linearity test:

```
clear;
% linearity test
% check T{Ax1[n]+Bx2[n]}=A*T{x1[n]}+ B*T{x2[n]}
x1=10*rand(1,10); x2=10*rand(1,10);
figure(1)%input
subplot(1,3,1),stem(x1),xlabel('n'),title('x1[n]');
subplot(1,3,2),stem(x2),xlabel('n'),title('x2[n]');
subplot(1,3,3),stem(2*x1+3*x2),xlabel('n'),title('2*x1[n]+3*x2[n]');
figure(2)%linearity test
orient('tall')
sgtitle('linearity test')
% bbox1
subplot(3,2,1), stem(2*bbox1(x1)+3*bbox1(x2)), xlabel('n'), title('2*bbox1(x1)+3*bbox1(x2))
3*bbox1(x2)');
subplot(3,2,2),stem(bbox1(2*x1+3*x2)),xlabel('n'),title('bbox1(2*x1+3*x2)');
% bbox2
subplot(3,2,3), stem(2*bbox2(x1)+3*bbox2(x2)), xlabel('n'), title('2*bbox2(x1)+3*bbox2(x2))
3*bbox2(x2)');
subplot(3,2,4),stem(bbox2(2*x1+3*x2)),xlabel('n'),title('bbox2(2*x1+3*x2)');
% bbox3
subplot(3,2,5), stem(2*bbox3(x1)+3*bbox3(x2)), xlabel('n'), title('2*bbox3(x1)+3*bbox3(x2))
3*bbox3(x2)');
subplot(3,2,6),stem(bbox3(2*x1+3*x2)),xlabel('n'),title('bbox3(2*x1+3*x2)');
```

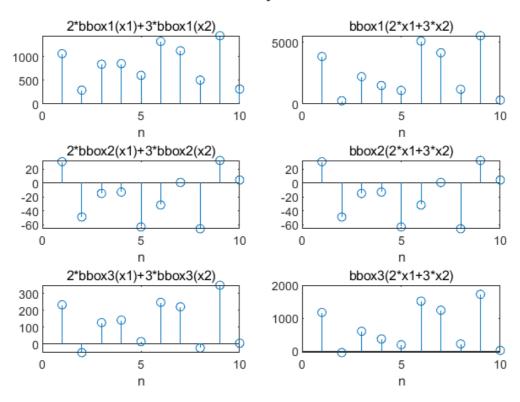
• Code for time invariance test:

```
clear;
% time invariance test
```

```
n=-5:5;
% let x denote x[n], x1 denote x1[n]=x[n-n0]
% let y[n], y1[n] denote the outputs of x[n] and x1[n]
% check y[n-n0]=y1[n]
x=[zeros(1,3) ones(1,5) zeros(1,3)];%input
x1=[zeros(1,5) ones(1,5) 0];% set n0=2
nhead=-7:5;%find the new element after the right shifting
xhead=[zeros(1,2) x];
yahead=bbox1(xhead);yahead=yahead(1:2);
ybhead=bbox2(xhead);ybhead=ybhead(1:2);
ychead=bbox3(xhead);ychead=ychead(1:2);
ya=bbox1(x); ya\_delay=[yahead ya(1:length(ya)-2)]; ya1=bbox1(x1);
yb=bbox2(x); yb\_delay=[ybhead yb(1:length(yb)-2)]; yb1=bbox2(x1);
yc=bbox3(x); yc_delay=[ychead yc(1:length(yc)-2)]; yc1=bbox3(x1);
sgtitle('time invariance test')
orient('tall')
% bbox1
subplot(321),stem(n,ya_delay),title('y[n-2] for bbox1'),xlabel('n');
subplot(322),stem(n,ya1),title('y1[n] for bbox1'),xlabel('n');
% bbox2
subplot(323),stem(n,yb_delay),title('y[n-2] for bbox2'),xlabel('n');
subplot(324),stem(n,yb1),title('y1[n] for bbox2'),xlabel('n');
% bbox3
subplot(325),stem(yc_delay),title('y[n-2] for bbox3'),xlabel('n');
subplot(326),stem(yc1),title('y1[n] for bbox3'),xlabel('n');
```

• Result for linearity test

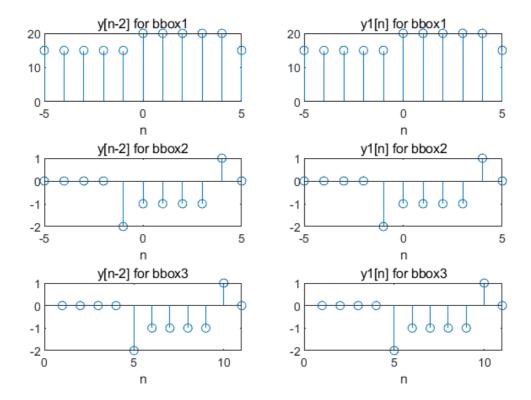
linearity test



According to the figure above, system bbox1 is not linear.

• Result for time invariance test

time invariance test



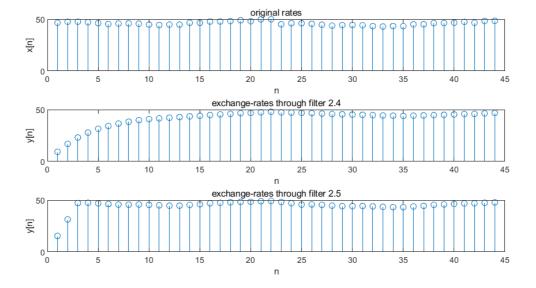
According to the figure above, system bbox3 is time varying.

2.8 Stock Market Example

• Codes for two functions:

```
function y=filter2_4(x)
% y[n]=0.8y[n-1]+0.2x[n]
N=length(x);
y=zeros(1,N+1);
for n=1:N
y(n+1)=0.2*x(n)+0.8*y(n);
end
y=y(2:N+1);
end
```

Result



• Analysis:

- o For filter 2.4:
 - Adavantages: As time passing, the filtered average value would gradually converge to a constant, and the average level line would be smoother.
 - Disadvantages: This filter need 10 ~ 15 days to reach a stable constant, which means that the waiting time is too long.
- o For filter 2.5:
 - Adavantages: The average value line is almost flat all the time, which means that there is nearly no waiting time.
 - Disadvantages: Compared with filter 2.4, the resulted average value line fluctuates a lot, and the filtered result is not stable.
- Better methods for initializing the filter outputs:
 - Collect 3 more passed original rates as a "head" to initialize x[n-3], x[n-2], and x[n-1].
 - Use x[n-1] to approximate y[n-1].

Part 3: Summary & Experience.

- Matlab is a very useful and powerful tool in digital signal processing.
- We could use many Matlab functions in signal processing toolbox to solve the problems.
- Use for loop to create function of difference equation.
- To design an inverse system, we could use the method of underterminated coefficients.