Transforming protatility distribution (density) function Let p(x) be POF - dW = p(x) dx $\begin{array}{c} probability & for hid x, x to dx \\ probability & for hid x, x to dx \\ p(x) & for hid x, x to dx \\ p$ Let x = x/y) be a monotonous function. Ansatz: $p(x)dx = p(x|x)) \frac{dx}{dy} dy = f(y)dy$ Let us start with eq. distr. p(x) = 1 = 1 $\beta(y) = \left| \frac{dx}{dy} \right|$; without loss of generality $\frac{dx}{dy} > 0 : \quad f(y) = \frac{dx}{dy} = x - x_0$ $F(y) - F(x_0) = \int \frac{dx}{dy} dy' = x - x_0$ $= \int f(y')dy'$

 $F(y) = F(y_0) + x - x_0$ - Deposites $F(y) = \times =) y(x) = F^{-1}(x)$ F is indefinite integral (Staum Runkhon)
F-1 is inverse function of F (Unkelvbrunkhon) Example: We want exponentially distributed PWs $p(x) dx = f(y) dy = e^{-y} dy = \frac{dx}{dy} dy$ $F(y) = F(y_0) + \int e^{-y} dy$ $= F(\gamma_0) - \left(e^{-\gamma}\right)^{\gamma} \quad \gamma_0$ $= F(\gamma_0) - e^{-\gamma} + e^{-\gamma_0}$ Let xo=%=0 $= F(\gamma_0) + X - X_0$ $\Rightarrow e^{-y} = 1 - x$ $y(x) = -\ln(1-x)$ Note: $x = 1 - e^{-x}$ $dx = e^{-x}$ $dx = e^{-x}$

general: monot. = JA/y)dy= Ymax

Rijection Method 8.24. What if F-1(x) cannot be computed? majorant $\widetilde{f}(y) \ge f(y)$ (p(x)dx = f(y)dy) - then $\widetilde{F}(y) = \widetilde{F}/y_0 + \int \widetilde{f}(y')dy' =$ $x_0 = y_0 = 0 - p(x) dx =$ $=y(x)=\widetilde{F}^{-1}(x)$ $X_i \in (0,1)$ $\chi_i = \widetilde{F}^{-1}(\chi_i)$ is distr. acc. to

Next: choose eq. distr. RN $x \in [0, \hat{f}(y)]$ If $x' \leq f(y)$ accept. (prol. $\frac{f(y)}{f(y')}$)

If x' > f(y) reject Seq. Xo, Xo, Xi, Xita, ---Seg. Xo, Rej. Xi, - Xi -- Xi+2, - $\gamma_i' = \widetilde{F}^{-1}(x_i')$ is dish. acc. to F(y)!Good majorant: $\tilde{f}(y) = \frac{C_0}{1 + (y - y_{in})^2/a_0^2}$ Maximum istat y= xm; F(xm) = Co FWHM = Zao

$$\begin{aligned}
& \text{Rox-Muller Algorithms: Gaussian PDF } & \text{G} \\
& \text{ip } | \text{lx}_1 \text{ p } | \text{lx}_1 \text{ dx}_1 \text{ dx}_2 = \text{fly}_1 \text{ fly}_2 \text{ dy}_1 \text{ dy}_2 \\
& = | \text{det} f | \text{dy}_1 \text{ dy}_2 \text{ dy}_2 \\
& = | \frac{\partial f | \text{lx}_1 \text{ x}_1}{\partial x_1 x_2} | \text{dy}_1 \text{ dy}_2 \\
& = | \frac{\partial f | \text{lx}_1 \text{ x}_2}{\partial x_1 x_2} | \text{dy}_1 \text{ dy}_2 \\
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& \text{det} f = | \frac{\partial f | \text{lx}_2 \text{ x}_2}{\partial x_1 x_2} |$$

Let
$$x_0 = 0$$
, $x_0 = 0$

$$x = \widehat{F}(y) = a_0 c_0 \text{ avely } \left(\frac{y - y_m}{q}\right) + \widehat{c}$$

$$= \int_0^\infty \widehat{f}(y') dy'$$

$$x_0 = \widehat{F}(y_0) = 0 = a_0 c_0 \text{ avely } \left(\frac{-y_m}{q_0}\right) + \widehat{c}$$

$$= \int_0^\infty \widehat{c} = + a_0 c_0 \text{ avely } \frac{y_m}{q_0}$$

$$\Rightarrow y(x) = y_m + a_0 + a_0 \left(\frac{x}{q_0 c_0}\right) + a_0 + a_0 \left(\frac{x}{q_0 c_0}\right)$$

yi = y(xi) distr.aa. F(x)