

In[2]:= ? BesselJ

Symbol i

Out[2]:= BesselJ [n, z] gives the Bessel function of the first kind J_n(z).

▼

In[10]:= Limit[D[D[BesselJ[0, k Sqrt[(x1 - x2)^2 + (y1 - y2)^2 + (z1 - z2)^2], x1], x2],
{x1 -> 0, x2 -> 0, y1 -> 0, y2 -> 0, z1 -> d, z2 -> d}]

Out[10]= $\frac{k^2}{2}$

In[11]:= D[D[BesselJ[0, k Sqrt[(x1 - x2)^2 + (y1 - y2)^2 + (z1 - z2)^2], x1], x2]

Out[11]=
$$-\frac{k (x1 - x2)^2 \text{BesselJ}\left[1, k \sqrt{(x1 - x2)^2 + (y1 - y2)^2 + (z1 - z2)^2}\right]}{\left((x1 - x2)^2 + (y1 - y2)^2 + (z1 - z2)^2\right)^{3/2}} +$$

$$\frac{k \text{BesselJ}\left[1, k \sqrt{(x1 - x2)^2 + (y1 - y2)^2 + (z1 - z2)^2}\right]}{\sqrt{(x1 - x2)^2 + (y1 - y2)^2 + (z1 - z2)^2}} +$$

$$\left(k^2 (x1 - x2)^2 \left(\text{BesselJ}\left[0, k \sqrt{(x1 - x2)^2 + (y1 - y2)^2 + (z1 - z2)^2}\right] - \text{BesselJ}\left[2, k \sqrt{(x1 - x2)^2 + (y1 - y2)^2 + (z1 - z2)^2}\right]\right)\right) / \left(2 \left((x1 - x2)^2 + (y1 - y2)^2 + (z1 - z2)^2\right)\right)$$

In[12]:= Limit[BesselJ[0, k Sqrt[(x1 - x2)^2 + (y1 - y2)^2 + (z1 - z2)^2],
{x1 -> 0, x2 -> 0, y1 -> 0, y2 -> 0, z1 -> d, z2 -> d}]

Out[12]= 1