# **Efficient Coalition Formation for Web Services**

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Abstract—Web services are loosely-coupled business applications willing to cooperate in distributed settings within different groups called communities. Communities aim to provide better visibility, efficiency, market share and total payoff. There are a number of proposed mechanisms and models on aggregating web services and making them cooperate within their communities. However, forming optimal and stable communities as coalitions to maximize individual and group efficiency and income has not been addressed vet. In this paper, we propose an efficient coalition formation mechanism using cooperative game-theoretic techniques. We propose a mechanism for community membership requests and selections of web services in the scenarios where established communities already exist. Moreover, we analyze the scenarios where communities are not established yet. The ultimate objective is to develop a mechanism for web services to form stable groups allowing them to maximize their efficiency and generate near-optimal (welfare-maximizing) communities. The theoretical and simulation results show that our algorithms provide web services and community owners with applicable and near-optimal decision making mechanisms.

 ${\it Keywords} ext{-Web}$  services; Cooperative game thoery; Community of services;

## I. INTRODUCTION AND RELATED WORK

Over the past years, online services have become part of many scalable business applications. The increasing reliance on web-based applications has significantly influenced the way web services are engineered. Web services provide a set of stateless software functions accessible at a network address over the web. The recent developments are shifting web services from passive and individual components to autonomous and group-based components where interaction, composition, and cooperation are the key challenges [1], [2]. The main objective is to achieve a seamless integration of business processes, applications and web services. Delivering high quality services considering the dynamic and unpredictable nature of the Internet is still a very critical and challenging issue.

The need for highly available and responsive services has called for grouping and collaborative mechanisms of loosely-coupled web services, particularly in business settings. The idea of grouping web services within communities and the way those communities are engineered so that web services can better collaborate have been proposed and

investigated in [3], [4], [5]. Communities are virtual groups of web services having similar functionalities, but probably different non-functional quality attributes, which form the QoS parameters. When communities are used, users send their requests to the masters of those communities, which are responsible of managing the communities, forwarding the requests to the suitable member web services and checking the credentials of those members. Communities aim to provide higher service availability and performance than what individual web services can provide. The high availability of services and the community resilience to failure are guaranteed since web services can cooperate and replace each other within the same community and since there is no single point of failure in the communities architecture.

Most of the recent work on communities of services are either user-centric and focus on user satisfaction [6] or system-centric and focus on the whole system throughput, performance and utilization. There are many contributions in distributed, grid, cluster and cloud services which are system-centric. However, in real world environments and applications, both users and service providers are self-interested agents, aiming to maximize their own profit. In those environments, both parties (users and services) will collaborate as long as they are getting more benefits and payoff.

In this direction, recently [7], [8] proposed mechanisms to help users and services maximize their gain. A two-player non-cooperative game between web services and community master was introduced in [8]. In this game-theoretic model, the strategies available to a web service when facing a new community are requesting to join the community, accepting the master's invitation to join the community, or refusing the invitation to join. The set of strategies for communities are inviting the web service or refusing the web service's join request. Based on their capacity, market share and reputation, the two players have different set of utilities over the strategy profiles of the game. The main limits of this game model are: 1) its consideration of only three quality parameters, while the other factors are simply ignored; and 2) the non-consideration of the web services already residing within the community. The game is only between the community master and the new web service, and the inputs from all the other members are simply ignored. The consideration of those inputs is a significant issue as existing web services can lose utility or payoff because of the new member, which can results in an unhealthy and unstable group. The problem comes from the fact that the existing members should collaborate with the new web services, so probably their performance as a group can suffer. Existing members may even deviate and try to join other communities if they are unsatisfied. Those considerations of forming stable and efficient coalitions are the main contributions of our paper.

In [7] a 3-way satisfaction approach for selecting web services has been proposed. In this approach, the authors proposed a web service selection process that the community masters can use. The approach considerers the efficiency of all the three involved parties, namely users, web services and communities. In this work, it is shown how the gains of these parties are coupled together using a linear optimization process. However, the optimization problem in this solution tends to optimize some parameters considering all web services regardless of their efficiency and contribution to the community's welfare. Moreover, there are no clear thresholds for accepting or rejecting new web services. The solution of the optimization problem could, for instance, suggest web services already residing within the community to increase or decrease their capacity to cover up the weakness of other parties in the system. However, a high performing web service could deviate anytime it finds itself unsatisfied within the community instead of adjusting its service parameters.

Contributions. In this paper, we use game theory to propose a cooperative game model for the aggregation of web services within communities. The solution concepts of our cooperative game seeks to find efficient ways of forming coalitions (teams) of web services so that they can maximize their gain and payoff, and distribute the gain in a fair way among all the web services. Achieving Fairness when the gain is distributed among the community members is the main factor to keep the coalition stable as no web service will expect to gain better by deviating for the community. In other words, the coalition is made efficient if all the members are satisfied. We first propose a representation function for communities of web services based on their QoS attributes. By using this function, we can evaluate the worth of each community of web services. When facing new membership requests, a typical community master checks whether the new coalition having the old and new set of web services will keep the community stable or not. The community master will reject the membership requests if it finds out that the new coalition would be unstable, preventing any subset of web services from gaining significantly more by deviating from the community and joining other communities or forming new ones. The computation of solutions for cooperative game theory problems is combinatorial in nature and proven to be NP-complete [9], making this computation impractical in real world applications. However, using the concepts of coalition stability, we propose approximation algorithms running in polynomial time providing web services and community masters with applicable and near-optimal decision making mechanisms.

The rest of paper is organized as follows. Section II describes the architecture, considered parameters and some basic cooperative game theory concepts. Section III presents our solution model in three different scenarios. Section IV describes our experiments and results. Finally, Section V, concludes the paper and identifies future work.

### II. PRELIMINARIES

In this section, we discuss the parameters and preliminary concepts that we use in the rest of the paper.

### A. The Architecture

Our system consists of three main types of entities working together:

- 1) Web services are rational entities<sup>1</sup> providing services to end users. They aim to maximize their individual income by receiving enough requests from end users. In order to increase their revenue, web services seek for more tasks if they have the capacity and throughput to do so. Web services can join communities to have better efficiency by collaborating with others, to have access to higher market share, and to have opportunity of receiving a bigger task pool from end users. The way the web services reside inside communities and how communities of web services are engineered is described in [3]. Throughout this paper, in our equations, we refer to web services as ws and to the set of web services hosted by a given community as C. To simply the notation, sometimes we simply write ws instead of  $ws \in C$  to go through the elements ws of the set C.
- 2) Master Web Services are representatives of the communities of web services and responsible for their management. Communities receive requests from users and aim to host a healthy set of web services to perform the required tasks. They seek to maximize user satisfaction by having tasks accomplished according to the desired QoS. In fact, higher user satisfaction will bring more user requests and increase the market share and revenue of the community.
- 3) Users generate requests and try to find the best available services. User satisfaction is abstracted as function of quantity and quality of tasks accomplished by a given service.

#### B. Web Service Parameters

Web services come with different quality of service parameters. These parameters with a short description are listed in Table I.

<sup>1</sup>The term rational is used here in the sense that web services are utility maximizers

 $\label{eq:Table I} \mbox{Table I} \\ \mbox{List of web service QoS parameters}.$ 

Parameter	Definition
Availability	Probability of being available during a time frame
Reliability	Probability of successfully handling requests
	during a timeframe
Successability	Rate of successfully handled requests
Throughput	Average rate of handling requests
Latency	The average latency of services
Capacity	Amount of resources available
Cost	Mean service fee
Regulatory	Compliance with standards, law and rules
Security	Quality of confidentiality and non-repudiation

We adopted a real world dataset [10] which has aggregated and normalized each of these parameters to a real value between 0 and 1. Since requests are not shared among web services and are distributed among all of them inside a community, each one of them comes with a given QoS denoted by  $(QoS_{ws})$ . We assume that  $(QoS_{ws})$  is obtained by a certain aggregation function of the parameters considered in Table I. We use this quality output later in evaluating the community worth or payoff function.

## C. Cooperative Game Concepts

Cooperative game is a branch of game theory that studies strategies of self-interested entities or agents in a setting where those agents can increase their payoff by binding agreements and cooperating in groups. We let N be a set of players. Any subset S of N can form a group called coalition. A coalitional game is a pair G = (N, v) where v is called a characteristic function, which given a coalition, is a function  $v: 2^N \to \mathbb{R}$  mapping the set of players of the coalition to a real number v(S), the worth of S. This number usually represents the output or payoff or again the performance of these players working together as coalition. If a coalition S is formed, then it can divide its worth, v(S)in any possible way among its members. The payoff vector  $x \in \mathbb{R}^S$  is the amount of payoff being distributed among the members of the coalition S. The payoff vector satisfies two conditions:

- $x_i \ge 0$  for all  $i \in N$ , and
- $\sum_{i \in S} x_i \le v(S)$

The second criteria is called the *feasibility* condition, according to which, the payoff for each agent cannot be more than the coalition total gain. A payoff vector is also *efficient* if the payoff obtained by a coalition is distributed amongst the coalition members:  $\sum_{i \in S} x_i = v(S)$ . This definition of the characteristic function works in *transferable utility* (TU) settings, where utility (i.e., payoff) is transferable from one player to another, or in other words, players have common currency and a unit of income is worth same for all players [11].

When dealing with cooperative games, two issues need to be addressed:

- 1. What coalition to form (Canonical games)?
- 2. How to reward each member when a task is completed (Coalition-formation games)?

The following definitions help address these two issues.

**Definition 1 (Shapley value)** Given a cooperative game (N, v), the *Shapley value* of player i is given by [12]:

$$\phi_i(N, v) = \sum_{S \subseteq N \setminus \{i\}} \frac{|S|!(|N| - |S| - 1)!}{|N|!} (v(S \cup \{i\}) - v(S))$$
(1)

Shapley value is a unique and fair solution concept for payoff distribution among the members of the coalition. It basically rewards members with the amount of marginal contribution they have to the coalition.

**Definition 2 (Core)** A payoff vector x is in the *core* of a coalitional game (N, v) if and only if:

$$\forall S \subseteq N, \sum_{x_i \in S} x_i \ge v(S) \tag{2}$$

The core is basically a set of payoff vectors where no subset of players S' could gain more than their current payoff by deviating and making their own coalition  $\sum_{i \in S'} x_i \geq v(S')$ . The sum of payoffs of the players in any sub-coalition S is at least as large as the amount that these players could earn by forming a coalition by their own. In a sense, it is analogue to Nash equilibrium, except that core is about deviations from groups of entities. The core is the strongest and most popular solution concept in cooperative game theory. However, its computation is a combinatorial problem and becomes intractable as the number of players increases. The core of some real-world problem games may be empty, which means having the characteristic function of the game (N,v), there might be no possible distribution of payoff assuring stability of subgroups.

**Definition 3 (Convex cooperative games)** A game (N, v) with characteristic function v(S) is convex if:

$$v(S) + v(T) \le v(S \cup T) + v(S \cap T), \forall S, T \subseteq N.$$
 (3)

According to a classic result by Shapley [13], convex games always have a non-empty core. We will use a variation of convexity condition in our algorithm to check whether our coalitions are stable.

 $\epsilon$ -core: When the *core* set of a game is empty, it means no coalition of players can gain anything by deviating. An outcome would be unstable if a coalition can benefit even by a small amount from deviating, which is a strong requirement. In fact, in some situations, deviations can be costly, or players may have loyalty to their coalitions, or even it can be computationally intractable to find those small benefits. It would only make sense for a coalition to deviate if the gain from a deviation exceeds the cost of performing the deviation.  $\epsilon$ -core relaxes the notion of the core, and only requires that no coalition would benefit significantly,

or within a constant amount( $\epsilon$ ) by deviating (see Equation 4).

$$\forall S \subseteq N, \sum_{x_i \in S} x_i \ge v(S) - \epsilon \tag{4}$$

Coalition Structure Formation: Coalition structure formation is the problem of finding the best partition of web services into teams. In these settings, the performance of an individual service is less important than the social welfare of the whole system, which is the sum of the values of all teams. Having the game (N,v), a coalition structure (CS) is socially optimal if CS belongs to set  $\arg\max_{CS}v(CS)$  where v(CS) is the sum of the values of all coalitions inside CS.  $v(CS) = \sum_{C \in CS}v(C)$ .

### III. PROBLEM FORMULATION AND MODELING

In this section, we present different web service community models and focus on the problem of how both web services and community masters as rational entities would adopt strategies to maximize their payoff.

#### A. Web Services and One Community

In this scenario, we assume the existence of a typical community managed by its master web service and web services need to join it to be able to get requests from the master. The community master is characterized by a requests rate  $(R_M)$  from users. Each web service comes with a given QoS  $(QoS_{ws})$  from which the throughput  $T_{ws}$  is excluded. This exclusion allows us to build our analysis on the particular value of  $T_{ws}$ . Throughput is the average rate of tasks a web service can perform per time unit. Therefore, the master web service is providing tasks with the rate of  $R_{ws}$  and web services perform tasks with average output quality of  $QoS_{ws}$  and a throughput rate of  $T_{ws}$ . In this setting, we define the value of the coalition of the web services within a community as a function increasing in both  $T_{ws}$  and  $QoS_{ws}$  as follows:

$$output(C) = \sum_{ws \in C} (T_{ws} \times QoS_{ws})$$

$$v(C) = \begin{cases} output(C) & \text{if } \sum_{ws} T_{ws} \le R_M \\ output(C) \times \frac{R_M}{\sum_{ws} T_{ws}} & \text{if } \sum_{ws} T_{ws} > R_M \end{cases}$$
(5)

The output of a coalition of web services is a function of the throughput and provided QoS. If the throughput rate is more than the master's input request rate, it means the web services inside the community are capable of serving more requests than the demand. Considering this factor, the valuation function is designed to balance the output performance so that it matches the exact throughput rate and QoS the web service can provide within the particular community.

In this first scenario, we only consider one grand coalition and analyze the system from the point of view of one single

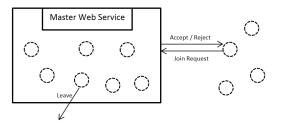


Figure 1. Web Services and A Grand Community

master web service and a collection of web services. The master web service decides which members can join the community and distributes the requests and income among its community members (see Figure 1).

The membership decision is made based on throughput and QoS of the considered web service. The goal is to have quality web services in the community so it stays stable and no other web services would have incentives to deviate and leave the coalition C. Therefore, a basic method would be to check the core of the coalition C considering all the current community members (all web services already residing within the community) and the new web service. This algorithm uses the *Shapley value* distribution method as described in Equation 1 to distribute the gain of v(C) among all the members and then checks if the Shapley value payoff vector for this community having the characteristic function v(C) is in the core. In the Shapley value payoff vector, the payoff for each web service  $ws_i$  is calculated based on its marginal contribution  $v(C \cup i) - v(C)$  over all the possible different permutations in which the coalition can be formed, which makes the payoff distribution fair. Because of going through all the possible permutations of subsets of N, the nature of the Shapley value is combinatorial. This makes it impractical to use as the size of our coalitions grows. However, it is proven that in convex games, the Shapley value lies in the core [14], [11]. Thus, if the Core is nonempty, the payoff vector is a member of the Core. The following proposition is important to make our algorithm tractable.

**Proposition 1.** A game with a characteristic function v is convex if and only if for all S, T, and i where  $S \subseteq T \subseteq N \setminus \{i\}, \forall i \in N$ ,

$$v(S \cup \{i\}) - v(S) \le v(T \cup \{i\}) - v(T) \tag{6}$$

Proof.

1. "only if" direction:

Assume:

$$v(S \cup \{i\}) - v(S) \le v(T \cup \{i\}) - v(T)$$
  
  $\to v(S \cup \{i\}) + v(T) \le v(T \cup \{i\}) + v(S)$ 

Considering  $S \subseteq T$ :

$$S \cup \{i\} = (S \cup \{i\}) \cup T$$
$$T = (S \cup \{i\}) \cap T$$

By setting  $A = S \cup \{i\}$  and B = T we have:

$$v(S \cup \{i\}) + v(T) \le v(T \cup \{i\}) + v(S)$$

$$\to v(S \cup \{i\}) + v(T) \le v((S \cup \{i\}) \cup T) + v((S \cup \{i\}) \cap T)$$

$$\to v(A) + V(B) \le v(A \cup B) + v(A \cap B)$$

Consequently, the game is convex.

## 2. "if" direction:

Assume the game is convex. Thus, for all  $A,B\subset N$ , we have:

$$v(A) - v(A \cap B) \le v(A \cup B) - v(B)$$

By setting  $S \cup \{i\} = A$  and R = B where  $S \subseteq R$ :

$$v(S \cup \{i\}) - v((S \cup \{i\}) \cap T) \le v(T \cup (S \cup \{i\})) - v(T)$$

$$\to v(S \cup \{i\}) - v(S) \le v(T \cup \{i\}) - v(T)$$

As a direct consequence of this proposition, in order to keep the characteristic function convex, new web services should have more marginal contribution as the coalition size grows.

Our algorithm works as follows. We have an established community with a master and some member web services already residing in the community. A web service would send a join request to the community. The ideal solution would be analyzing the *core* or  $\epsilon$ -core stability of the group having this new member. As the normal core membership algorithm is computationally intractable, we exploit Proposition 1 and Equation 6 to check the convexity of our game having characteristic function where the new member is added. In the equation, we set C to be our community members (C) before having the new web service. We assign i to the new web service, and then verify the equation for S, setting S = T/W1 where W1 is the set of all possible subsets of the set N having the size 1. We can relax the equation a bit by adding a constant  $\epsilon$  to the left side of the equation. We call this method *Depth-1 Convex-Checker* algorithm. If the equation is satisfied for all W1, we let the new web service join our community, since the web service will contribute positively enough to make our new community stable. Since only subsets of size 1 are checked, the following Proposition holds.

**Proposition 2.** The run time complexity of Depth-1 Convex-Checker algorithm is O(n).

By this result, we obtain a significant reduction from  $O(2^n)$ , which is the complexity of checking all possible subsets of N. In our second method, we use the same algorithm, but this time we set W2 to be the set of all possible subsets of size two and one of the community C.

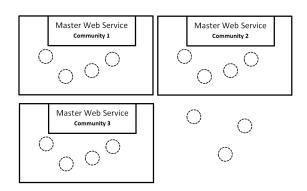


Figure 2. Web Services and Many Communities

We call this method *Depth-2 Convex-Checker* and its run time complexity is still linear:

**Proposition 3.** The run time complexity of Depth-2 Convex-Checker algorithm is  $O(n^2)$ .

It is possible to develop an anytime algorithm by continuing the verification of this condition against all subsets of size 3, 4, etc. until the algorithm gets interrupted.

## B. Web Services and Many Communities

In this scenario, we consider multiple communities managed by multiple master web services, each of which is providing independent request pools (see Figure 2). Identical to the first scenario, master web services form coalitions with web services. We use coalition structure formation methods to partition web services into non-empty disjoint coalition structures. As mentioned in Section II-C, the used algorithms [15], [14], [16] try to solve key fundamental problems of what coalitions to form, and how to divide the payoffs among the collaborators.

In coalition-formation games, formation of the coalitions is the most important aspect. The solutions focus on maximizing the social welfare. For any coalition structure  $\pi$ , let  $v_{cs}(\pi)$  denote the total worth  $\sum_{C \in \pi} v(C)$ , which represents the social welfare. The solution concepts in this area deal with finding the maximum value for the social welfare over all the possible coalition structures  $\pi$ . There are centralized algorithms for this end, but these approaches are generally NP-complete. The reason is that the number of all possible partitions of the set N grows exponentially with the number of players in N, and the centralized algorithms need to iterate through all these partitions. In our model, we propose using a distributed algorithm where each community master and web service can be a decision maker and decide for its own good. The aim is to find less complex and distributed algorithms for forming web services coalitions[17], [18], [19]. The distributed merge-and-split algorithm in [17] suits our application very well. It keeps splitting and merging coalitions to partitions which are preferred by all the players inside those coalitions.

This merge-and-split algorithm is designed to be adaptable to different applications. One major ingredient to use such an algorithm is a preference relation or well-defined orders proper for comparing collections of different coalition partitions of the same set of players. Having two partition sets of players, namely  $P=P_1,...,P_k$  and  $Q=Q_1,...Q_l$ , one example would be to use the social welfare comparison  $\sum_{i=1}^k v(P_i) > \sum_{j=1}^l v(Q_j)$ . For our scenario, we use *Pareto order* comparison, which is an individual-value order appropriate for our self-interest web services. In the Pareto order, an allocation or partition P is preferred over another Q if at least one player improves its payoff in the new allocation and all the other players still maintain their payoff  $(p_i \geq q_i)$  with at least one element  $p_i > q_i$ ).

The valuation function v(C) for this scenario is the same as "Web Services and One Community" scenario. However, in order to prevent master web services joining the same community, we set v(C)=0 when C has either none, or more than one master web service as member.

In this scenario, as new web services are discovered and get ready to join communities, our algorithm keeps merging and splitting partitions based on the preference function. The decision to merge or split is tied to the fact that all players must benefit. The new web services will merge with communities if *all* the players are able to improve their individual payoff, and some web services may split from old communities, if splitting does not decrease the payoff of any web service of the community. According to [20], this sequence of merging and splitting will converge to a final partition, where web services cannot improve their payoff. More details of this algorithm and analysis of generic solutions on coalition formation games are described in [17].

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## C. Web Services Collaborating Independently

In this scenario, we do not consider pre-defined communities and master web services. Here web services are interested in forming coalitions to perform better and share benefits. We do not consider concept of master web services providing requests for others, each web service comes with its own request load which in this scenario we call it market share. Therefore coalitions will form is web services working together can perform and gain more than working alone individually. The worth or value of coalitions of web services is different in this setting. We average the quality for all metrics of web service  $(Q^m)$ , multiply it by a weight where the importance or weight of each metric is dependent on type of users and requests web services are dealing with. For each web service we multiply this by web service's market share  $(MS_{ws})$  and the summation would be the characteristic or valuation of independent web service coalitions.

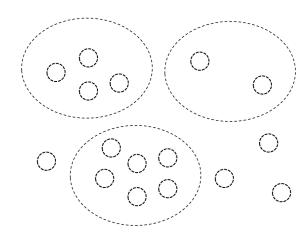


Figure 3. Web Services collaborating independently

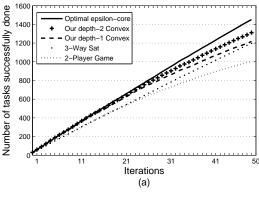
$$v(C) = \sum_{ws \in C} \left( \frac{\sum_{m=metrics} Q_{ws}^m \times w_m}{|metrics|} \right) \times MS_{ws} \quad (7)$$

 $w_m$  is the weight of important for a QoS metric, it gives the community the flexibility to emphasize or neglect a specific QoS parameter. Note that  $\sum_m w_m = 1$ . In this scenario we have no master web services, we assume they either dynamically vote for one, or collaborate and agree on decisions and distribute task in round robin or fair fashion. Here, we utilized the same merge-and-split algorithm which we applied for the "Web Services and Many Communities" scenario, to find stable coalitions of web services.

## IV. EXPERIMENTAL RESULTS

In this section, we discuss the experiments we performed for our scenarios to validate applicability and performance of our proposed methods in realistic environments. We created a pool of web services and populated most of their *QoS* parameters from a real world web service dataset [10]. We programmed the simulations using Java and executed the simulations on a Intel Xeon X3450 machine with 4GBs of memory. For other parameters missing from the dataset, we used normal random distribution with parameters that make most sense in real world examples.

We analyze the most important performance result the communities should perform, quality and quantity of tasks successfully performed by the communities. This is the most important criteria for user satisfaction. We initiate the community with few web services, then let rejecting and accepting of random web services go for a short number of iterations, after that we start task distribution for the communities and let them allocate tasks for web services. Then we measure the average output performance of tasks in communities following different methods.



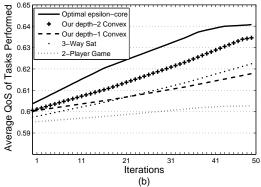


Figure 4. Part (a): Cumulative number of tasks successfully done. Part (b): Average QoS of tasks performed.

Figure 4 depicts the results of optimal  $\epsilon$ -core, by assigning  $\epsilon$  to 15% of total community worth,  $\epsilon=0.15\times v(C)$ , allowing subsets of coalition to gain maximum 15% of v(C), Depth-1 Convex-Checker, Depth-2 Convex-Checker, 3-Way Satisfactory[7] and 2 Player Non-Cooperative[8] methods in one grand community with many web services scenario. In the optimal  $\epsilon$ -core method we capped the coalition size to 25 web services, since anything more than that would require analysis with time complexity of  $O(2^{n-1})$ , making it impractical to run in our simulations. In other methods there were no cap on size of the community and we had communities of size 60 web services at some points. The results show depth-2 and 1 convex checker methods are performing better compared to other methods and their performance is close to optimal  $\epsilon$ -core method.

As mentioned in section II, the concept of *core*, assumes no coalition of players can gain anything by deviating which is a fairly strong requirement, that is why the notion of  $\epsilon$ -core was introduced. Least-Core e(G) of a game G, is the minimum amount of  $\epsilon$  in which the core is not empty. We evaluated the least-core value using our valuation function and our set of web services. We pick random number of web services from our dataset and formed around 10,000 random coalitions consisting of 3 to 26 web services. We choose 26 as maximum number of members in our grand

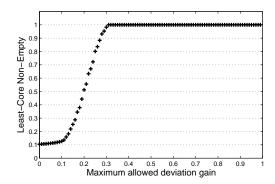


Figure 5. Analysis of  $\epsilon$ -core set non-emptiness, for different values of  $\epsilon$ 

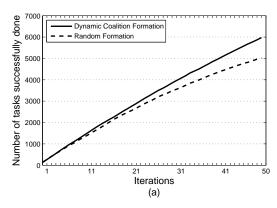
coalition since it is computationally very complex for bigger coalitions to compute  $\epsilon$ -core. We set  $\epsilon$  to a ratio of total payoff of coalition v(C) between 0 and 1. The results in figure 5 illustrates, almost 10% of our random web service coalitions have non-empty core solution and  $\epsilon$ -core solution is always non-empty when we let agents gain 30% (of v(C)) more, by deviating.

One of the properties of coalition structure formation algorithms in our scenario is that they partition web services with low throughput rate usually join coalitions with less request rate. Since the characteristic function v(C) and the fair payoff vector of Shapley value is proportional to web services' contribution, the web services with small contribution will get paid much less in communities having web services with high throughput. On the other hand, according to valuation function v(C) web services with high throughput will not contribute well to communities with low amount of user requests. The strong web services are much more likely to deviate weak coalitions, joining a stronger coalition, making the initial coalition unstable.

In figure 6 we compare our *Web Services and many Communities* scenario with a method which ignores QoS parameters and forms coalitions and allow web services to join only if they have enough requests for them in other words web services can join a community when request rate is less that throughput of all web services inside community ignoring QoS parameters. We name this method *Random Formation* and use it as our benchmark for our QoS aware coalition formation process. As results illustrate clearly, our QoS aware method, forms better coalitions of web services improving performance and satisfaction for both web service and coalitions.

## V. CONCLUSION

In this paper, we proposed a cooperative game theory based model for aggregation of web services within communities. The goal of our services is to maximize efficiency of performing tasks by collaborating and forming stable communities. Our method considers stability and fairness for



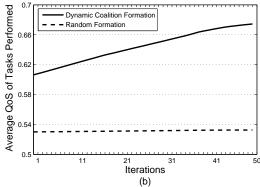


Figure 6. Part (a): Cumulative number of tasks succesfully done. Part (b): Average QoS of tasks performed.

all web services within a community and offers an applicable mechanism for membership requests and selection of web services. The goal is to increase revenue by improving user satisfaction, which comes from the ability to perform tasks with higher quality and quantity. Simulation results show that our, polynomial in complexity, approximation algorithms provide web services and community owners with applicable and near-optimal decision making mechanisms.

As future work, we would like to perform more analytical and theoretical work on the convexity condition for the characteristic function on web service applications. It is possible to work on compact or succinct representation of our service model (i.e. a graph representation) to reduce the input complexity and solution concepts of cooperative game and core membership checking algorithms. From web service aspect, the work can be extended to consider web service compositions where a group of web services having different set of skills cooperate to perform composite tasks. Also bargaining theory from cooperating game theory concepts can be used in our scenario. The web services would stay and join communities as they wish, however, they would resolve the instability and unfairness issues by side payments.

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