

Chapter 5 Workshop

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Dataset Toxaemia

This dataset is from the `vcdExtra` package. Two signs of *toxaemia*, an abnormal condition during pregnancy characterized by high blood pressure (hypertension) and high levels of protein in the urine. If untreated, both the mother and baby are at risk of complications or death. The dataset **Toxaemia** represents 13384 expectant mothers in Bradford, England in their first pregnancy, who were also classified according to social class and the number of cigarettes smoked per day.

The dataset is a 5 x 3 x 2 x 2 contingency table, with 60 observations on the following 5 variables:

class - Social class of mother, a factor with levels: 1, 2, 3, 4, 5

smoke - Cigarettes smoked per day during pregnancy, a factor with levels: 0, 1-19, 20+

hyper - Hypertension level, a factor with levels: Low, High

urea - Protein urea level, a factor with levels: Low, High

Freq - frequency in each cell, a numeric vector

Exercise 5.1

Obtain relevant graphical displays for this dataset.

Bar charts-

```
library(tidyverse)

library(vcdExtra)
data(Toxaemia)

Toxaemia |>
  ggplot() +
  aes(x=smoke, y=Freq, fill=hyper) +
  geom_bar(stat='identity')

Toxaemia |>
  ggplot() +
  aes(x=smoke, y=Freq, fill=hyper) +
  geom_bar(stat='identity',
          position = "dodge"
          )

Toxaemia |>
  ggplot() +
  aes(x=smoke, y=Freq, fill=hyper) +
  geom_bar(stat = 'identity',
          position = "dodge") +
  facet_grid(urea ~ ., scales = "free")
```

Mosaic type charts

```
tab.data <- xtabs(Freq ~ smoke + hyper + urea, data=Toxaemia)

plot(tab.data)
```

```
mosaic(tab.data, shade=TRUE, legend=TRUE)
```

```
assoc(tab.data, shade=TRUE)
```

```
strucplot(tab.data)
```

```
sieve(tab.data)
```

The full dataset is a 5 x 3 x 2 x 2 contingency table, with 60 observations on the following 5 variables. For this question we will focus on two categorical variables from this dataset, **hyper** and **urea**. This forms a 2 x 2 contingency table since these variables each have two levels.

```
# subset the data
tox_2 <- Toxaemia |>
  dplyr::select(hyper, urea, Freq)

# the tidyverse way
tox_display <- tox_2 |>
  pivot_wider(names_from = urea,
              values_from = Freq,
              values_fn = sum) |>
  column_to_rownames( var = "hyper") # make values of hyper column row names

tox_display
```

	High	Low
High	665	2715
Low	589	9415

```
# xtabs()
```

Two signs of *toxaemia*, are high blood pressure (hypertension) and high levels of protein in the urine. We want to ask if in our sample of expectant mothers in Bradford, England, is high blood pressure related to high protein levels? If these two variables are associated this may indicate the presence of toxaemia in the sample, if they are independent toxaemia may not be present.

We can test this question using a Chi-squared test.

The null hypothesis of the chi-squared test is that the two variables are independent and the alternative hypothesis is that the two variables are not independent.

Our null hypothesis is that Hypertension level and the Protein urea level in expectant mothers in Bradford, England are independent.

Our alternative hypothesis that Hypertension level and the Protein urea level in expectant mothers in Bradford, England are *not* independent.

Set our $\alpha = 0.05$

```
chisq.test(tox_display)
```

Pearson's Chi-squared test with Yates' continuity correction

```
data:  tox_display
X-squared = 563.9, df = 1, p-value < 2.2e-16
```

Since our p-value is less than our alpha level we reject the null hypothesis and conclude that the two variables (hyper & urea) are not independent. We found evidence of an association between hypertension levels and protein in urine levels in our sample of expectant mothers in Bradford, England.

We can see the expected counts

```
chisq.test(tox_display)$expected
```

	High	Low
High	316.6856	3063.314
Low	937.3144	9066.686

```
# compared to our observed
tox_display
```

	High	Low
High	665	2715
Low	589	9415

```
# total counts 13384
```

Exercise 5.2

The genetic information of an organism is stored in its Deoxyribonucleic acid (DNA). DNA is a double stranded helix made up of four different nucleotides. These nucleotides differ in which of the four bases Adenine (A), Guanine (G), Cytosine (C), or Thymine (T) they contain. Nucleotides combine to form amino acids which are the building blocks of proteins. Simply put, three nucleotides form an amino acid and the specific order of a combination dictates what amino acid is formed. A simple pattern that we may want to detect in a DNA sequence is that of the nucleotide at position $i+1$ based on the nucleotide at position i . The nucleotide positional data collected by a researcher in a particular case is given in the following table:

$i \backslash (i+1)$	A	C	G	T
A	622	316	328	536
C	428	262	204	306
G	354	294	174	266
T	396	330	382	648

Perform a test of association and then obtain the symmetric plot.

```
tabledata <- data.frame(  
  A = c(622, 428, 354, 396),  
  C = c(316, 262, 294, 330),  
  G = c(328, 204, 174, 382),  
  T = c(536, 306, 266, 648),  
  row.names = c("A", "C", "G", "T")  
)
```

```
chisq.test(tabledata)$exp
```

	A	C	G	T
A	554.8409	370.5104	335.3705	541.2781
C	369.4834	246.7328	223.3322	360.4516
G	334.9983	223.7044	202.4879	326.8094
T	540.6774	361.0523	326.8094	527.4608

```
chisq.test(tabledata)
```

Pearson's Chi-squared test

```
data: tabledata
X-squared = 153.21, df = 9, p-value < 2.2e-16
```

```
chisq.test(tabledata, simulate.p.value = T)
```

Pearson's Chi-squared test with simulated p-value (based on 2000 replicates)

```
data: tabledata
X-squared = 153.21, df = NA, p-value = 0.0004998
```

```
# if there is an association we can examine patterns
library(MASS)
corresp(tabledata)
```

First canonical correlation(s): 0.1443355

```
Row scores:
      A      C      G      T
-0.1921802 -0.8894387 -1.0334109  1.4453224
```

```
Column scores:
      A      C      G      T
-1.1304512 -0.6952989  0.8139424  1.1304056
```

```
plot(corresp(tabledata, nf=2))
abline(v=0)
abline(h=0)
```

```
#or
library(FactoMineR)
CA(tabledata)
```


****Results of the Correspondence Analysis (CA)****

The row variable has 4 categories; the column variable has 4 categories

The chi square of independence between the two variables is equal to 153.2146 (p-value = 1.9e-05)

*The results are available in the following objects:

	name	description
1	"\$eig"	"eigenvalues"
2	"\$col"	"results for the columns"
3	"\$col\$coord"	"coord. for the columns"
4	"\$col\$cos2"	"cos2 for the columns"
5	"\$col\$contrib"	"contributions of the columns"
6	"\$row"	"results for the rows"
7	"\$row\$coord"	"coord. for the rows"
8	"\$row\$cos2"	"cos2 for the rows"
9	"\$row\$contrib"	"contributions of the rows"
10	"\$call"	"summary called parameters"
11	"\$call\$marge.col"	"weights of the columns"
12	"\$call\$marge.row"	"weights of the rows"

- More R code examples are [here](#)